

$$\times \text{ Kcl @ } v_0: +\frac{dv_0}{dt} + \frac{v_0}{1} + \frac{3}{8} \int (v_0 - v) dt = 0$$

$$\text{Kcl @ } v: \frac{3}{8} \int (v - v_0) dt + \frac{v}{1} + \frac{dv}{dt} - i_s = 0$$

$$\Rightarrow \frac{d^2 v_0}{dt^2} + \frac{dv_0}{dt} + \frac{3}{8} v_0 - \frac{3}{8} v = 0 \Rightarrow v = \frac{8}{3} \frac{d^2 v_0}{dt^2} + \frac{8}{3} \frac{dv_0}{dt} + v_0$$

$$i_L = \frac{3}{8} \int (v_0 - v) dt$$

$$i_L + v + \frac{dv}{dt} = i_s$$

$$\frac{3}{8} v - \frac{3}{8} v_0 + \frac{dv}{dt} + \frac{d^2 v}{dt^2} - \frac{di_s}{dt} = 0$$

$$\Rightarrow \frac{d^2 v_0}{dt^2} + \frac{dv_0}{dt} + \frac{3}{8} v_0 - \frac{3}{8} v_0 + \frac{8}{3} \frac{d^3 v_0}{dt^3} + \frac{8}{3} \frac{d^2 v_0}{dt^2} + \frac{dv_0}{dt}$$

$$+ \frac{8}{3} \frac{d^4 v_0}{dt^4} + \frac{8}{3} \frac{d^3 v_0}{dt^3} + \frac{d^2 v_0}{dt^2} = \frac{di_s}{dt}$$

$$\frac{8}{3} \frac{d^4 v_0}{dt^4} + \frac{16}{3} \frac{d^3 v_0}{dt^3} + \frac{14}{3} \frac{d^2 v_0}{dt^2} + 2 \frac{dv_0}{dt} = \frac{di_s}{dt}$$

$$\Rightarrow \frac{8}{3} \frac{d^3 v_0}{dt^3} + \frac{16}{3} \frac{d^2 v_0}{dt^2} + \frac{14}{3} \frac{dv_0}{dt} + 2v_0 = i_s$$

$$\Rightarrow \frac{8}{3} \frac{d^3 v_0}{dt^3} + \frac{16}{3} \frac{d^2 v_0}{dt^2} + \frac{14}{3} \frac{dv_0}{dt} + 6v_0 = 3i_s \text{ (utt)}$$

$$8s^3 + 16s^2 + 14s + 6 = 0 \Rightarrow s_1 = -1, s_{2,3} = -\frac{1}{2} \pm \sqrt{2}j$$

$$v_{0p} = K \Rightarrow 8(0) + 16(0) + 14(0) + 6K = 3 \Rightarrow K = \frac{1}{2}$$

$$v_0(t) = K e^{-t} + e^{-\frac{1}{2}t} (K_2 \cos \sqrt{2}t + K_3 \sin \sqrt{2}t) + \frac{1}{2}$$

$$v_0(0+) = 0 \Rightarrow \frac{d^2 v_0}{dt^2}(0+) + \frac{dv_0}{dt}(0+) + \frac{3}{8} v_0(0+) - \frac{3}{8} v_0(0+) = 0 \Rightarrow \frac{d^2 v_0}{dt^2}(0+) = 0$$

$$v_0(0+) = 0 \Rightarrow K_1 + K_2 = -\frac{1}{2}$$

$$i_L(0+) = 0 \Rightarrow \frac{dv_0}{dt}(0+) + v_0(0+) + i_L(0+) = 0 \Rightarrow \frac{dv_0}{dt}(0+) = 0$$

$$\Rightarrow \begin{cases} K_1 + K_2 = -\frac{1}{2} \\ -K_1 - \frac{1}{2} K_2 + \sqrt{2} K_3 = 0 \\ K_1 - K_2 - \sqrt{2} K_3 = 0 \end{cases} \Rightarrow K_1 = -\frac{1}{2}, K_2 = 0, K_3 = -\frac{\sqrt{2}}{2}$$

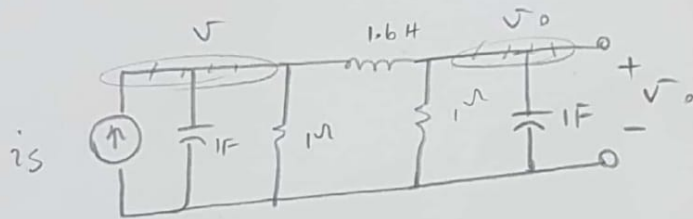
$$v_o(t) = \left(-\frac{1}{2}e^{-t} + e^{-\frac{1}{2}t} \left(-\frac{\sqrt{2}}{2} \sin \frac{\sqrt{2}}{2}t \right) + \frac{1}{2} \right) u(t) = s(t)$$

$$h(t) = \frac{ds(t)}{dt} = \left[\frac{1}{2}e^{-t} - \frac{1}{2}e^{-\frac{1}{2}t} \left(-\frac{\sqrt{2}}{2} \sin \frac{\sqrt{2}}{2}t \right) + e^{-\frac{1}{2}t} \left(-\frac{\sqrt{2}}{4} \cos \frac{\sqrt{2}}{2}t \right) \right] u(t) + \left(-\frac{1}{2}e^{-t} + e^{-\frac{1}{2}t} \left(-\frac{\sqrt{2}}{2} \sin \frac{\sqrt{2}}{2}t \right) + \frac{1}{2} \right) \delta(t)$$

$$\underbrace{-\frac{1}{2} + \frac{1}{2}}_{=0} \delta(t)$$

$$\Rightarrow h(t) = \left[\frac{1}{2}e^{-t} + \frac{\sqrt{2}}{2}e^{-\frac{1}{2}t} \left(\frac{1}{2} \sin \frac{\sqrt{2}}{2}t - \frac{\sqrt{2}}{2} \cos \frac{\sqrt{2}}{2}t \right) \right] u(t)$$

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$$i_s(t) = 2e^{-t}u(t)$$

$$\text{KCL @ } v: -i_s + \frac{dv}{dt} + v + \frac{1}{16} \int (v - v_o) dt = 0$$

$$\Rightarrow \frac{d^2v}{dt^2} + \frac{dv}{dt} + \frac{1}{16}v - \frac{1}{16}v_o = \frac{di_s}{dt}$$

$$\text{KCL @ } v_o: \frac{dv_o}{dt} + v_o + \frac{1}{16} \int (v_o - v) dt = 0$$

$$\Rightarrow \frac{d^2v_o}{dt^2} + \frac{dv_o}{dt} + \frac{1}{16}v_o = \frac{1}{16}v$$

$$\Rightarrow \frac{16}{1} \frac{d^4v_o}{dt^4} + \frac{16}{1} \frac{d^3v_o}{dt^3} + \frac{d^2v_o}{dt^2} + \frac{16}{1} \frac{d^3v_o}{dt^3} + \frac{16}{10} \frac{dv_o}{dt^2} + \frac{dv_o}{dt} + \frac{d^2v_o}{dt^2} + \frac{dv_o}{dt} + \frac{1}{16}v_o = -\frac{1}{16}v_o = \frac{di_s}{dt}$$

$$\frac{16}{8} \frac{d^3v_o}{dt^3} + \frac{32}{16} \frac{d^2v_o}{dt^2} + \frac{32}{18} \frac{dv_o}{dt} + \frac{2}{10}v_o = \frac{1}{5}2e^{-t} \rightarrow 2e^{-t}$$

$$\Rightarrow 8s^3 + 16s^2 + 18s + 10 = 0 \Rightarrow s_1 = -1, s_{2,3} = -\frac{1}{2} \pm j$$

$$v_{op} = Kte^{-t} \Rightarrow v_{op}' = ke^{-t} - kte^{-t}, v_{op}'' = -ke^{-t} + kte^{-t} - ke^{-t}$$

$$v_{op}''' = ke^{-t} + ke^{-t} - kte^{-t} + ke^{-t}$$

$$8(3ke^{-t} - kte^{-t}) + 16(-2ke^{-t} + kte^{-t}) + 18(ke^{-t} - kte^{-t}) + 10kte^{-t} = 10e^{-t}$$

$$\underbrace{(24 - 32 + 18)}_{10} ke^{-t} = 10e^{-t} \Rightarrow \underline{k=1}$$

$$v_o(t) = k_1 e^{-t} + e^{-\frac{1}{2}t} (k_2 \sin t + k_3 \cos t) + te^{-t}$$

$$v_o(0^+) = 0 \Rightarrow k_1 + k_2 = 0$$

$$\frac{dv_o}{dt}(0^+) = \dot{i}_R(0^+) + \underbrace{\dot{i}_L(0^+)}_0 = 0 \Rightarrow k_1 = \frac{4}{5}, k_2 = -\frac{4}{5}, k_3 = -\frac{3}{5}$$

$$\cancel{16} \frac{d^2 v_o}{dt^2}(0^+) + \cancel{16} \frac{dv_o}{dt}(0^+) + \cancel{v_o}(0^+) = \cancel{v_o}(0^+) \Rightarrow \underline{\frac{d^2 v_o}{dt^2}(0^+) = 0}$$

$$v_o(t) = \frac{4}{5} e^{-t} + e^{-\frac{1}{2}t} \left(-\frac{4}{5} \sin t - \frac{3}{5} \cos t \right) + te^{-t}$$

$$x(t) = e^{-t} u(t) \rightarrow y(t) = (-e^{-t} + 2e^{-2t}) u(t)$$

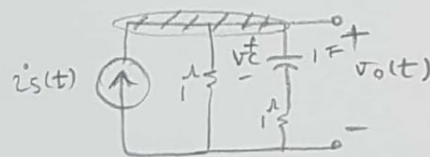
$$u(t) \rightarrow s(t) = ?$$

$$x'(t) = -e^{-t} u(t) + \underbrace{e^{-t} \delta(t)}_{\delta(t)} \Rightarrow x(t) + x'(t) = \delta(t)$$

$$\Rightarrow h(t) = y(t) + y'(t) \Rightarrow h(t) = (-e^{-t} + 2e^{-2t}) u(t) + (e^{-t} - 4e^{-2t}) u(t) + \underbrace{(-e^{-t} + 2e^{-2t}) \delta(t)}_1$$

$$\Rightarrow h(t) = -2e^{-2t} u(t) + \delta(t)$$

$$\Rightarrow s(t) = \int h(t) dt = \int_0^t -2e^{-2t} u(t) dt + \int_0^t \delta(t) dt = e^{-2t} - 1 + 1 = e^{-2t} \Big|_0^t = e^{-2t}$$



$$-i_s(t) + v_o + v_o - v_C = 0$$

$$v_o - v_C = \frac{dv_C}{dt} \Rightarrow (D+1)v_C = v_o \Rightarrow v_C = \frac{v_o}{D+1}$$

$$2v_o - \frac{v_o}{D+1} = i_s \Rightarrow 2(D+1)v_o - v_o = (D+1)i_s$$

$$\Rightarrow 2 \frac{dv_o}{dt} + 2v_o - v_o = \frac{di_s}{dt} + i_s \rightarrow \delta(t)$$

$$-e^{-t} u(t) + \underbrace{e^{-t} \delta(t)}_{\delta(t)} + e^{-t} u(t)$$

$$2s+1=0 \Rightarrow s = -\frac{1}{2}$$

$$\rightarrow v_o = K_1 e^{-\frac{1}{2}t} u(t)$$

$$\Rightarrow 2(-\frac{1}{2})K_1 e^{-\frac{1}{2}t} u(t) + 2K_1 e^{-\frac{1}{2}t} \delta(t) + K_1 e^{-\frac{1}{2}t} u(t) = \delta(t)$$

$$2K_1 \delta(t)$$

$$K_1 = \frac{1}{2}$$

$t=0^+ \rightarrow$ initial conditions

$$v_o(0^+) = \frac{1}{2} i_s = \frac{1}{2} e^{-t} u(t) = \frac{1}{2}$$

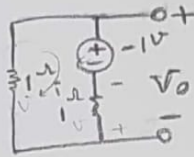
$$v_o(0^+) = K_1 = \frac{1}{2}$$

$$\Rightarrow v_o = \frac{1}{2} e^{-\frac{1}{2}t} u(t) \rightarrow \text{الخيار 4 صفر}$$

$$\frac{2dv_o}{dt} + v_o = \frac{di_s}{dt} + 15$$

$$v_o = K e^{-t} u(t)$$

$$v_o(0+) = -1^v \Rightarrow t=0+ \Rightarrow$$



$$v_{1,u} = -\frac{1}{2}^v \Rightarrow v_o^{(0+)} = -1 - (-\frac{1}{2}) = -\frac{1}{2}$$

$$\Rightarrow v_o(0+) = K = -\frac{1}{2}$$

$$\Rightarrow v_o(t) = -\frac{1}{2} e^{-t} u(t)$$

لے بائیں ورودی صفر

بایں کامل هم از مجموع بائیں ورودی صفر و حاصل تفاضل در دست می آید.

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$$h(t) = u(t) - 2u(t-1) + u(t-2)$$

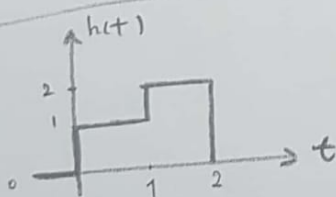
$$i_s(t) = u(t)$$

$$\Rightarrow s(t) = \int h(t) dt$$

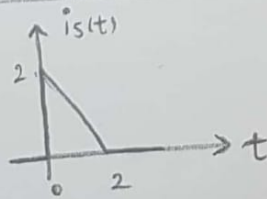
$$= \int u(t) dt - 2 \int u(t-1) dt + \int u(t-2) dt$$

$$\Rightarrow s(t) = r(t) - 2r(t-1) + r(t-2)$$

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$$i_s(t) =$$



$$i_s(t) = \begin{cases} 0 & t < 0 \\ -t+2 & 0 < t < 2 \\ 0 & t > 2 \end{cases}$$

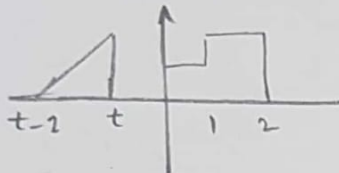
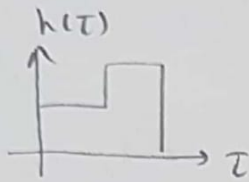
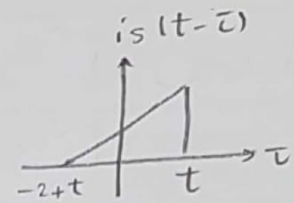
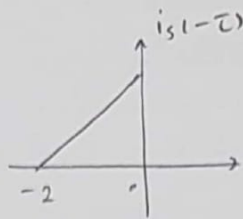
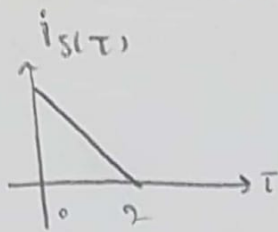
$$(0,2) \Rightarrow \frac{2-0}{0-2} = -1 \Rightarrow i_s - 0 = -(t-2)$$

$$h(t) = u(t) + u(t-1) - 2u(t-2) = (\delta(t) + \delta(t-1) - 2\delta(t-2)) * u(t)$$

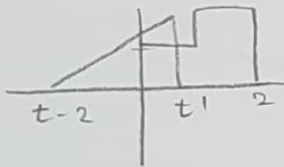
$$i_s(t) = 2u(t) - r(t) + r(t-2) = (2\delta(t) - u(t) + u(t-2)) * u(t)$$

$$r(t) = h(t) * i_s(t) = (\delta(t) + \delta(t-1) - 2\delta(t-2)) * u(t) * (2\delta(t) - u(t) + u(t-2))$$

$$\begin{aligned} & [2\delta(t) + 2\delta(t-1) - 4\delta(t-2) - u(t) - u(t-1) + 2u(t-2) + u(t-2) + u(t-3) - 2u(t-4)] \\ & * r(t) = 2r(t) + 2r(t-1) - 4r(t-2) - \frac{1}{2}t^2 u(t) - \frac{(t-1)^2}{2} u(t-1) + \frac{2(t-2)^2}{2} u(t-2) \\ & + \frac{(t-2)^2}{2} u(t-2) + \frac{(t-3)^2}{2} u(t-3) - 2 \frac{(t-4)^2}{2} u(t-4) \end{aligned}$$



$$\Rightarrow \int_0^t h(\tau) i_s(t-\tau) d\tau = 0 \Rightarrow \underline{t < 0}$$



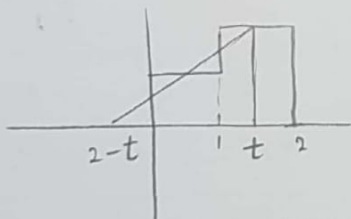
$$\Rightarrow \int_0^t (1)(-(t-\tau)+2) d\tau =$$

$$= -t\tau + \frac{1}{2}\tau^2 + 2\tau \Big|_0^t = -t^2 + \frac{1}{2}t^2 + 2t$$

$$\underline{0 < t < 1}$$

←

$$= -\frac{t^2}{2} + 2t$$



$$\int_1^t (2)(-t+\tau+2) d\tau + \int_0^1 (1)(-t+\tau+2) d\tau =$$

$$-2t\tau + \tau^2 + 4\tau \Big|_1^t = -2t^2 + t^2 + 4t + 2t - 1 - 4$$

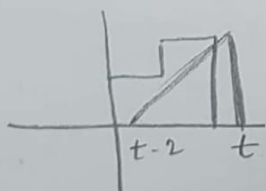
$$\underline{1 < t < 2}$$

←

$$= -t^2 + 6t - 5$$

$$= -t\tau + \frac{1}{2}\tau^2 + 2\tau \Big|_0^1 = -t + \frac{1}{2} + 2 = -t + \frac{5}{2}$$

$$\underline{-t^2 + 5t - \frac{5}{2}}$$



$$\int_{t-2}^1 (1)(-t+\tau+2) d\tau + \int_1^2 (2)(-t+\tau+2) d\tau$$

$$= -t\tau + \frac{1}{2}\tau^2 + 2\tau \Big|_{t-2}^1 = -t + \frac{1}{2} + 2 + t(t-2)$$

$$= -\frac{1}{2}(t-2)^2 - 2(t-2)$$

$$= -\frac{1}{2}(t^2 - 4t + 4) - 2t + 4$$

$$= -\frac{1}{2}t^2 + 2t - 2 - 2t + 4$$

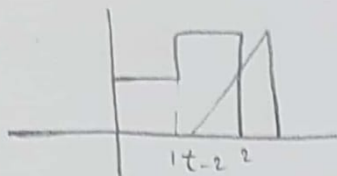
$$= -\frac{1}{2}t^2 + 2$$

$$= \frac{1}{2}t^2 - 3t + \frac{3}{2}$$

$$-2t\tau + \tau^2 + 4\tau \Big|_1^2 = -4t + 4 + 8 + 2t - 1 - 4 = -2t + 7$$

$$\Rightarrow = \frac{1}{2}t^2 - 5t + \frac{23}{2}$$

$$\Rightarrow 0 < t-2 < 1 \Rightarrow 2 < t < 3$$



$$\Rightarrow \int_{t-2}^2 (2)(1-t+\tau+2)d\tau$$

$$= -2t\tau + \tau^2 + 4\tau \Big|_{t-2}^2$$

$$= -\frac{4}{t} + 4 + 8 + 2t(t-2) - \frac{(t-2)^2}{2} - \frac{4(t-2)}{2}$$

$$= \frac{2t^2 - 4t}{2} - \frac{t^2 - 4t + 4}{2} - \frac{4t - 8}{2}$$

$$= \frac{t^2 - 8t + 16}{2}$$

$$1 < t-2 < 2 \Rightarrow \frac{3 < t < 4}{2}$$

$$\begin{cases} 0 & t < 0 \\ -\frac{t^2}{2} + 2t & 0 < t < 1 \\ -t^2 + 5t - \frac{5}{2} & 1 < t < 2 \\ \frac{1}{2}t^2 - 5t + \frac{23}{2} & 2 < t < 3 \\ t^2 - 8t + 16 & 3 < t < 4 \\ 0 & t > 4 \end{cases}$$

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$$\frac{d^2y}{dt^2} + 4\frac{dy}{dt} + 3y = 2\frac{dw}{dt} + w$$

$$2\delta' + \delta$$

$$w = \delta(t)$$

$$s^2 + 4s + 3 = 0$$

$$(s+1)(s+3) = 0 \Rightarrow s_1 = -1, s_2 = -3 \Rightarrow y(t) = (k_1 e^{-t} + k_2 e^{-3t}) u(t)$$

$$\frac{dy}{dt} = (-k_1 e^{-t} - 3k_2 e^{-3t}) u(t) + \underbrace{(k_1 e^{-t} + k_2 e^{-3t})}_{k_1 + k_2} \delta(t)$$

$$\frac{d^2y}{dt^2} = (k_1 e^{-t} + 9k_2 e^{-3t}) u(t) + \underbrace{(-k_1 e^{-t} - 3k_2 e^{-3t})}_{-k_1 - 3k_2} \delta(t) + (k_1 + k_2) \delta'(t)$$

$$+ (-4k_1 e^{-t} - 12k_2 e^{-3t}) u(t) + (4k_1 + 4k_2) \delta(t) + (3k_1 e^{-t} + 3k_2 e^{-3t}) u(t)$$

$$\begin{cases} k_1 + k_2 = 2 \\ -k_1 - 3k_2 + 4k_1 + 4k_2 = 1 \end{cases} \Rightarrow \begin{cases} k_1 + k_2 = 2 \\ 3k_1 + k_2 = 1 \end{cases}$$

$$-2k_1 = 1 \Rightarrow k_1 = -\frac{1}{2}$$

$$k_2 = 2 + \frac{1}{2} = \frac{5}{2}$$

$$\Rightarrow h(t) = \left(-\frac{1}{2}e^{-t} + \frac{5}{2}e^{-3t}\right) u(t)$$

$$\frac{d^2 y}{dt^2} + 2 \frac{dy}{dt} + 2y = \frac{dw}{dt} + 2w$$

$s'(t) + 2s(t)$

$$s^2 + 2s + 2 = 0 \Rightarrow s_{1,2} = -1 \pm j$$

$$\Delta = 4 - 4(1)(2) = -4$$

$$\hookrightarrow \frac{-2 \pm 2j}{2}$$

$$y(t) = e^{-t} (k_1 \cos t + k_2 \sin t) u(t)$$

$$\frac{dy}{dt} = -e^{-t} (k_1 \cos t + k_2 \sin t) u(t) + e^{-t} (-k_1 \sin t + k_2 \cos t) u(t)$$

$$+ \underbrace{e^{-t} (k_1 \cos t + k_2 \sin t)}_{k_2} \underbrace{s(t)}_{\substack{\hookrightarrow t=0 \\ t=0}}$$

$$\frac{d^2 y}{dt^2} = e^{-t} (k_1 \cos t + k_2 \sin t) u(t) - e^{-t} (-k_1 \sin t + k_2 \cos t) u(t)$$

$$- \underbrace{e^{-t} (k_1 \cos t + k_2 \sin t)}_{-k_1} s(t) + \underbrace{e^{-t} (-k_1 \sin t + k_2 \cos t)}_{k_2} s(t)$$

$$- e^{-t} (-k_1 \sin t + k_2 \cos t) u(t) + e^{-t} (-k_1 \cos t - k_2 \sin t) u(t)$$

$$+ k_2 s'(t)$$

$$- 2e^{-t} (k_1 \cos t + k_2 \sin t) u(t) + 2e^{-t} (-k_1 \sin t + k_2 \cos t) u(t) + 2k_2 s(t)$$

$$+ 2e^{-t} (k_1 \cos t + k_2 \sin t) u(t) = s'(t) + 2s(t)$$

$$k_2 = 1$$

$$-k_1 + k_2 + 2k_2 = 2 \Rightarrow 3k_2 - k_1 = 2 \Rightarrow \boxed{k_1 = 1}$$

$$h(t) = e^{-t} (\cos t + \sin t) u(t)$$

$$x(t) = (\cos t - \sin t) u(t) \rightarrow y = \begin{pmatrix} e^{-t} & -e^{-2t} \end{pmatrix} u(t)$$

↓

$$\hookrightarrow y' = (-e^{-t} + 2e^{-2t})u(t) + (e^{-t} - e^{-2t})\delta(t)$$

$$x'(t) = (-\sin t - \cos t)u(t) + (\cos t - \sin t)\delta(t)$$

↓

$$y'' = (e^{-t} - 4e^{-2t})u(t)$$

$$x''(t) = \underbrace{(-\cos t + \sin t)}_{-x(t)} u(t) + \underbrace{(-\sin t - \cos t)}_{-1} \delta(t) + \delta'(t)$$

$$S'(t) - S(t) = x''(t) + x(t)$$

$$\Rightarrow y''(t) + y(t) = h'(t) - h(t) \Rightarrow \frac{dh}{dt} - h = (2e^{-t} - 5e^{-2t})u(t) + \delta(t)$$

$$\lambda - 1 = 0 \Rightarrow \lambda = +1 \Rightarrow y_g = K e^t \Rightarrow K_1 \sin t + K_2 \cos t$$

$$y_p = k_1 e^{-t} + k_2 e^{-2t}$$

$$\Rightarrow -k_1 e^{-t} - 2k_2 e^{-2t} \quad -k_1 e^{-t} - k_2 e^{-2t} = 2e^{-t} - 5e^{-2t}$$

$$-2k_1 = 2 \Rightarrow k_1 = -1$$

$$-3K_2 = -5 \Rightarrow K_2 = \frac{5}{3}$$

$$y = y_g + y_p = \left(-e^{-t} + \frac{5}{3}e^{-2t} + ke^t \right) u(t) \quad -1 + \frac{5}{3} + k$$

$$\Rightarrow (e^{-t} - \frac{1}{3}e^{-2t} + ke^t)u(t) + (-e^{-t} + \frac{5}{3}e^{-2t} + ke^t)\delta(t)$$

$$+ (e^{-t} - \frac{5}{3}e^{-2t} - \cancel{ket})u(t) = (2e^{-t} - 5e^{-2t})u(t) + \delta(t)$$

$$k + \frac{2}{3} = 1 \Rightarrow \boxed{k = \frac{1}{3}}$$

$$d = (1 - e^{-t} + \frac{5}{3}e^{-2t} + \frac{1}{3}e^t) u(t) = h(t)$$

$$s(t) = \int h(t) dt = e^{-t} - \frac{5}{6}e^{-2t} + \frac{1}{3}e^t + C$$

$$S(0) = 0 \Rightarrow 1 - \frac{5}{6} + \frac{1}{3} + C = 0 \Rightarrow -\frac{1}{2}$$

$$\rightarrow s(t) = (e^{-t} - \frac{5}{6}e^{-2t} + \frac{1}{3}e^t - \frac{1}{2})u(t)$$