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```
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    Fall 2021 - Dr. Sameti  
%}
```

```
% Part 2: Z-Transform
```

```
syms x y t s  
assume(t, 'positive')
```

## 1.

```
f1 = t*heaviside(t - 1);  
f2 = sin(t)*exp(-4*t)*heaviside(t);  
f3 = 2*t*cos(3*t)*heaviside(t);
```

```
disp('1.')
```

```
fprintf('F1 = ')  
disp(laplace(f1))  
fprintf('F2 = ')  
disp(laplace(f2))  
fprintf('F3 = ')  
disp(laplace(f3))
```

```
1.  

$$F1 = \exp(-s)/s + \exp(-s)/s^2$$

```

```

$$F2 = 1/((s + 4)^2 + 1)$$

```

```

$$F3 = (4*s^2)/(s^2 + 9)^2 - 2/(s^2 + 9)$$

```

---

## 2.

```
F1 = exp(-3*s)/(s*(s + 1));  
F2 = 4/(s*(s^2 + 4));  
F3 = 1/(s^2 + 3*s + 1);
```

```
disp('2.')
```

$$\mathcal{L}\{F1\} = \frac{1}{s(s+1)} = \frac{1}{s} - \frac{1}{s+1}$$

```
fprintf('f1 = ')  
disp(ilaplace(F1))  
fprintf('f2 = ')  
disp(ilaplace(F2))  
fprintf('f1 = ')  
disp(ilaplace(F3))
```

```
2.  
f1 = -heaviside(t - 3)*(exp(3 - t) - 1)  
  
f2 = 1 - cos(2*t)  
  
f1 = (2*5^(1/2)*exp(-(3*t)/2)*sinh((5^(1/2)*t)/2))/5
```

## 3.

```
G = 8/(s^2 + s + 4);
```

---

```

g(t) = ilaplace(G);

G_unit = G/s;
g_unit(t) = ilaplace(G_unit);

disp('3.')
fprintf('Dirac response = ')
disp(g)
fprintf('Unit step response = ')
disp(g_unit)

subplot(2,1,1)
fplot(g)
title('Dirac response')
xlabel('t')

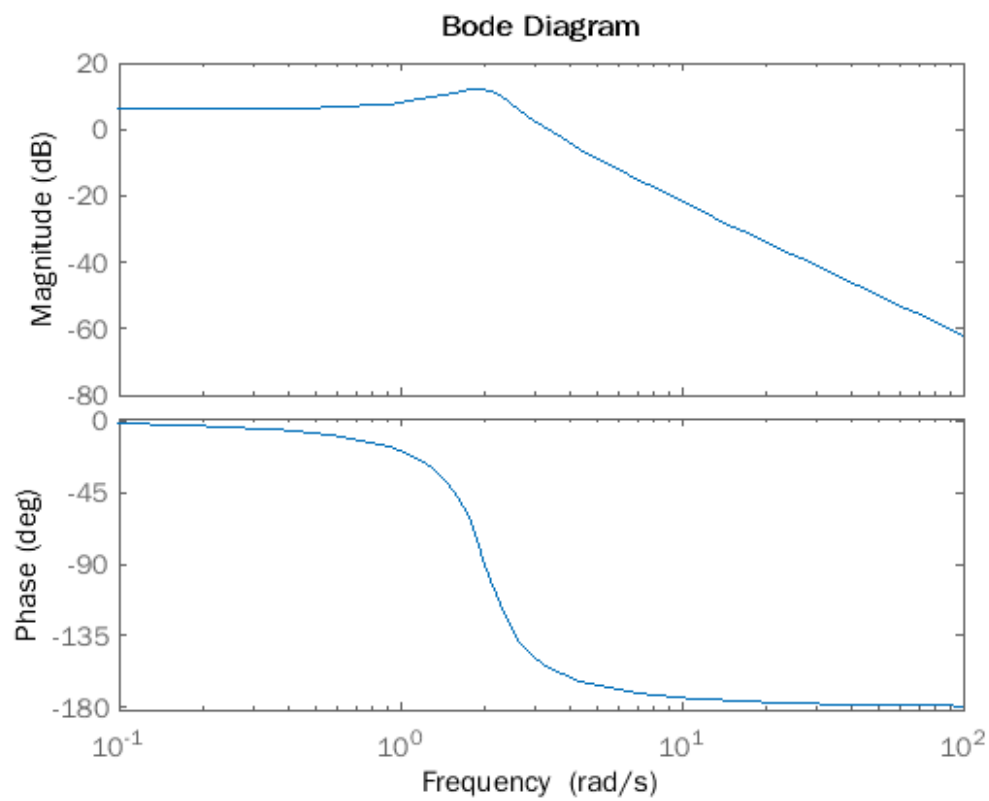
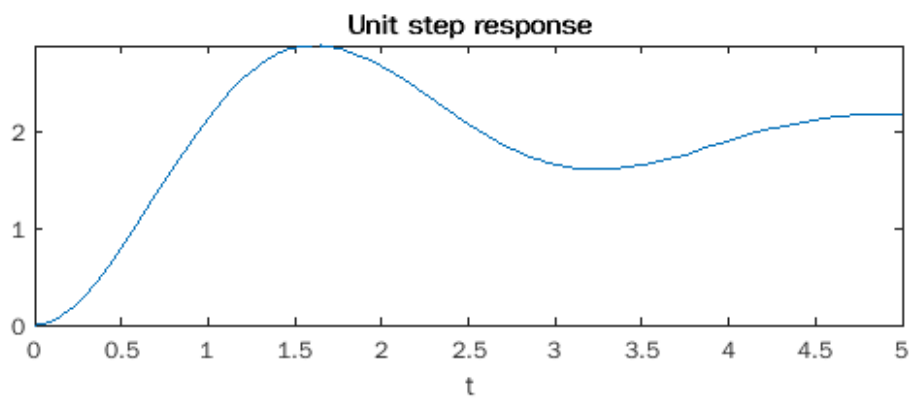
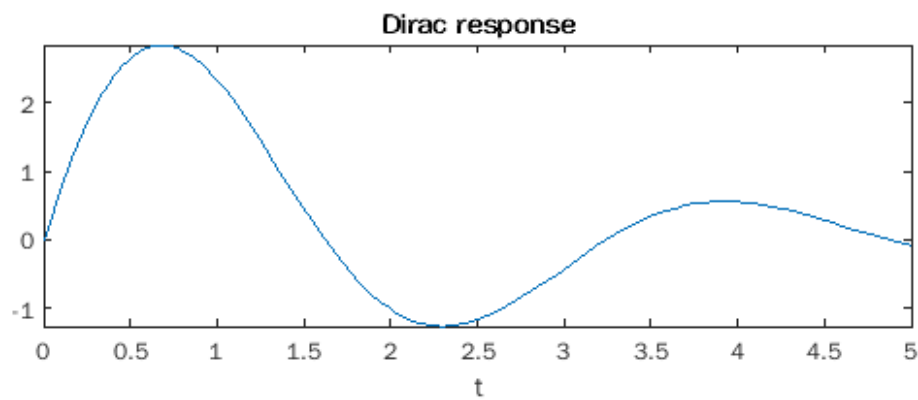
subplot(2,1,2)
fplot(g_unit)
title('Unit step response')
xlabel('t')

figure
H = tf([0 8],[1 1 4]);
bode(H)

3.
Dirac response = (16*15^(1/2)*exp(-t/2)*sin((15^(1/2)*t)/2))/15
symbolic function inputs: t

Unit step response = 2 - 2*exp(-t/2)*(cos((15^(1/2)*t)/2) +
(15^(1/2)*sin((15^(1/2)*t)/2))/15)
symbolic function inputs: t

```



---

## 4.

```
G1 = (2*s + 1)/(s^2 + 4*s + 7)/s;
G2 = (2*s + 1)/(s^2 + 6*s + 7)/s;

g1 = ilaplace(G1);
g2 = ilaplace(G2);

figure
a = 4;
subplot(2,1,1)
fplot(g1)
title('a = 4')

subplot(2,1,2)
fplot(g2)
title('a = 6')

disp('limit g(a=4)(t), t -> +inf =')
disp(limit(g1, t, sym(inf)))
disp('limit g(a=6)(t), t -> +inf =')
disp(limit(g2, t, sym(inf)))

t1 = vpasolve(diff(g1,t));
t2 = vpasolve(diff(g2,t));

disp('g1 maximum value =')
disp(double(subs(g1, t, t1)))
disp('g2 maximum value =')
disp(double(subs(g2, t, t2)))

disp('t1 where g1 is maximum = ')
disp(double(t1))
disp('t2 where g1 is maximum = ')
disp(double(t2))

limit g(a=4)(t), t -> +inf =
1/7

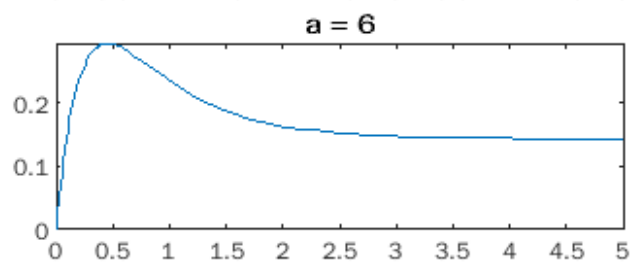
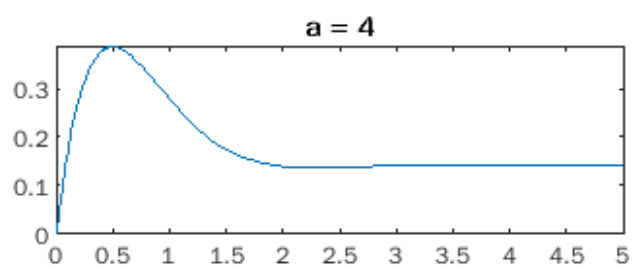
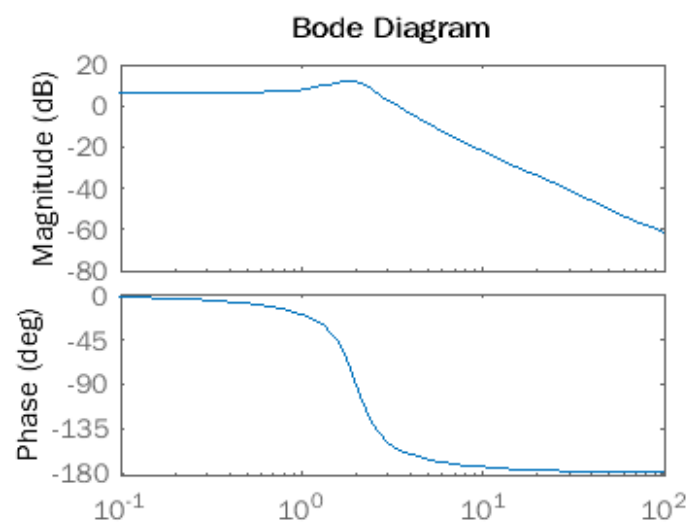
limit g(a=6)(t), t -> +inf =
1/7

g1 maximum value =
0.3862

g2 maximum value =
0.2940

t1 where g1 is maximum =
0.4948

t2 where g1 is maximum =
0.4534
```



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