



## Assignment 2

Deadline : 1401 / 01 / 10

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1. Discuss the causality and stability of the following discrete-time signals.

a)  $h[n] = 2^{-n}u[-n + 1],$

b)  $h[n] = (-1)^n e^{-n+1}u[-n + 1]$

c)  $h[n] = \sum_{k=-\infty}^{\infty} \delta(n - kN)$

2. Compute  $y[n]$  using the convolution sum  $y[n] = x[n] * h[n]$ .

a) 
$$\begin{cases} x[n] = \left(\frac{1}{3}\right)^{-n} u[-n - 1] \\ h[n] = u[n - 1] \end{cases}$$

b) 
$$\begin{cases} x[n] = \cos\left(\frac{\pi \cdot n}{6}\right) \\ h[n] = \left(\frac{1}{2}\right)^n u[n] \end{cases}$$

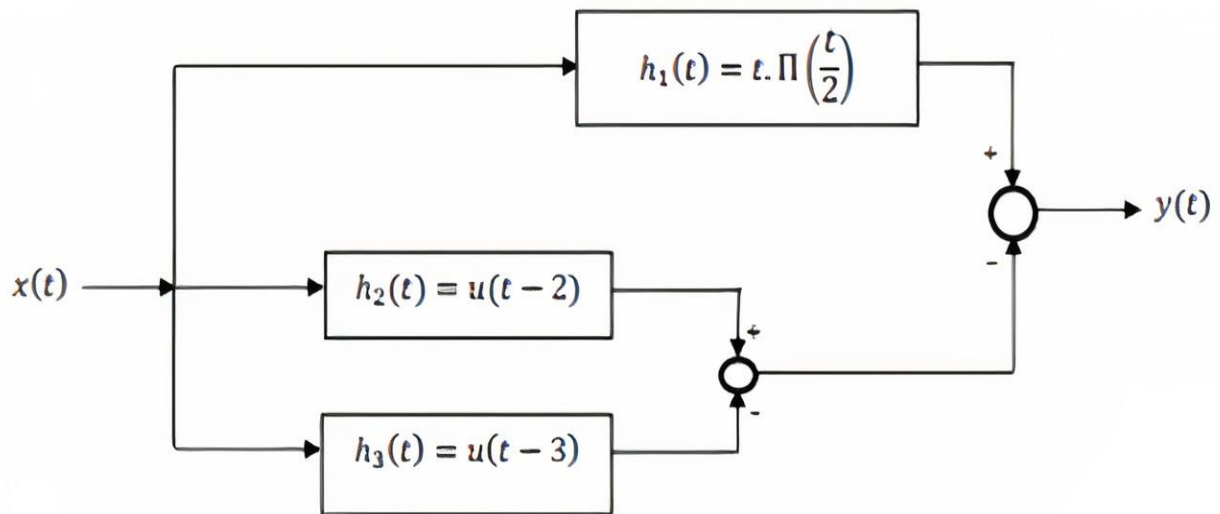
c) 
$$\begin{cases} X(t) = e^{-t}u(t) \\ h(t) = \cos(t) \cdot (u(t) - u(t - T)) \end{cases}$$

d) 
$$\begin{cases} x[n] = \sum_{k=-\infty}^{+\infty} \delta[n - kN] \\ h[n] = \left(\frac{1}{2}\right)^n u[n] \end{cases}$$

3. Prove that the following systems are inverse of each other.

$$h_1(t) = e^{-t}u(t), \quad h_2(t) = \delta(t) + \delta'(t)$$

4. Consider the following system. If the input signal of this system is  $x(t) = \Pi\left(\frac{t}{2}\right)$ . Find the output? ( $h_i(t)$  is an LTI system.)



$$\Pi(t) = \begin{cases} 0, & \text{if } |t| > \frac{1}{2} \\ \frac{1}{2}, & \text{if } |t| = \frac{1}{2} \\ 1, & \text{if } |t| < \frac{1}{2}. \end{cases}$$

5. Consider an LTI system with input and output related through the equation

$$y(t) = \int_{-\infty}^t e^{-(t-\tau)} x(\tau - 2) d\tau$$

- What is the impulse response  $h(t)$  for this problem?
- Determine the response of the system when the input  $x(t)$  is as shown in Fig 1.

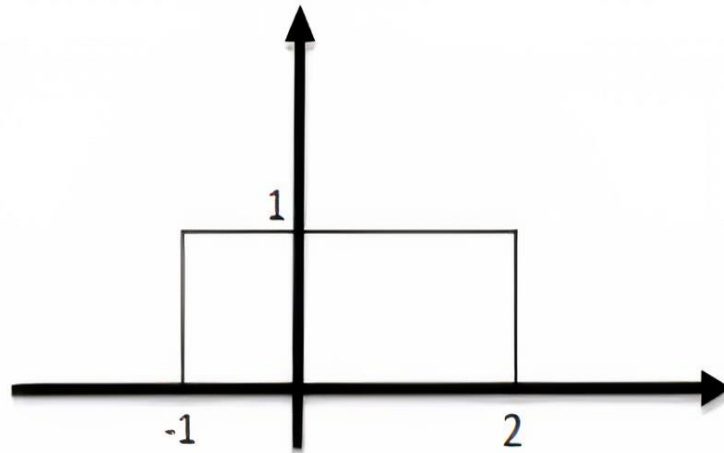


Figure 1

6. Consider an LTI system defined by the following difference equation

$$y[n] + \frac{1}{2}y[n-1] = x[n]$$

- Find the impulse response of the system.
- Given the output of the system,  $y[n] = \delta[n-1] + 2\delta[n-2] - \delta[n-3]$ , determine the input.

7. a) The input and output of a LTI system are given as :

$$x(t) = \sin(t)u(t)$$
$$y(t) = (e^{-t} - \cos t)u(t)$$

Find the impulse response of the system ( You should just use the convolution properties )

b) Consider a LTI system with impulse response of  $h(t) = e^{-5t}u(t)$ .

Find an input for this system in a way to obtain  $y(t) = \sin(t) + \cos(2t)$ .  
as output ( You should just use the convolution properties ).

8. For each of the following LTI systems determine whether the corresponding system is (i) Stable (ii) Causal.

(a)  $h_1(t) = \delta(t) + e^{-5t}u(t)$

(b)  $h_2(t) = e^{-5t}\sin(2\pi t)u(t)$

(c)  $h_3(t) = e^{-2|t|} + u(t+1) - u(t-1)$

(d)  $h_4(t) = t[u(t+4) - u(t-4)]$

(e)  $h_5(t) = \sin(10t)$

(f)  $h_6(t) = \cos(5t)u(t)$

(g)  $h_7(t) = 0.95^{|t|}$

(h)  $h_8(t) = \begin{cases} 1, & -1 \leq t < 0 \\ -1, & 0 \leq t \leq 1 \\ 0, & \text{otherwise} \end{cases}$