

# Artificial Bee Colony Algorithm

---

Alişan Köroğlu

# Optimization

$x = (x_1, x_2, \dots, x_i, \dots, x_n)$  Decision or design variables/parameters

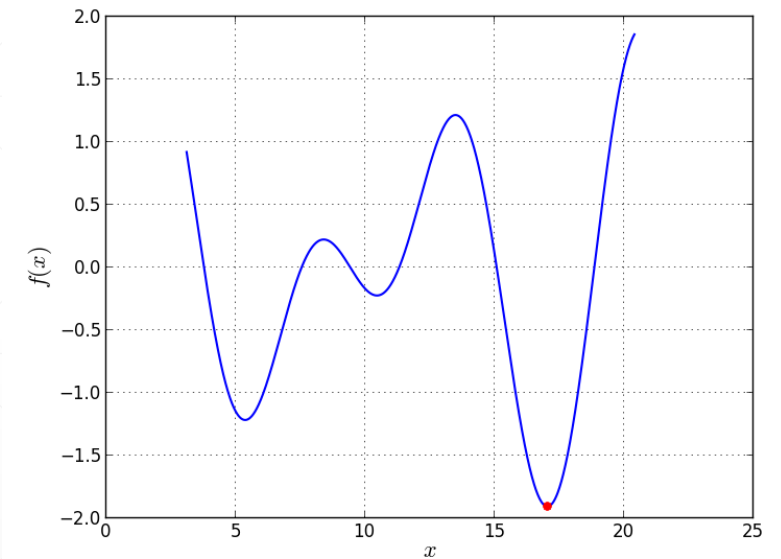
$f(x) = f(x_1, x_2, \dots, x_n)$  Objective Function

$h_j = h_j(x_1, x_2, \dots, x_n) = 0, \quad 1 \leq j \leq p$  Equality constraints

$g_i = g_i(x_1, x_2, \dots, x_n) \leq 0, \quad 1 \leq i \leq m$  Inequality constraints

$f(x^*) \leq f(x)$   $x^*$  represents optimum solution

Some problems may consist of more than one objective function.



# Classification of Optimization Techniques

## **Mathematical programming techniques**

(Based on the geometrical properties of the problem)

Simplex Algorithm, Interior point Algorithm

Steepest Decent, Newton's Method, Quasi-Newton

Branch and Bound, Cutting Planes

## **Other Techniques**

Nelder Mead/Simplex Search

Fibonacci Method

Golden Section Method

Hooke-Jeeves pattern search method

Powell's conjugate Direction Method

---

# Classification of Optimization Techniques

## Metaheuristic Techniques

- Genetic Algorithm(GA)
- Particle Swarm optimization
- Differential evolution(DE)
- Teaching learning Base optimization(TLBO)
- Grey Wolf Optimization
- Artificial Bee Colony Algorithm

Heuristic algorithms can not be proven to converge to the optimum solution in the solution space. They have the property of convergence but they can not guarantee the exact solution. They can only guarantee a solution close to the exact solution.

---

# Applications

Time tabling (limited runways)  
Production Planning and scheduling  
Civil engineering Structures  
Design of aircraft and aerospace  
Design electrical machinery  
Design of Pump, turbines and heat exchanger  
Machine learning and Data science  
Automobile Design  
Antenna Design

---

# Why nature-inspired optimization methods

Dimensionality

Multimodality

Complex Constraints

Interacting among parameters

Uncertainty in modeling

Dynamic Objectives

Multiple objectives

Computational cost

---

# Artificial Bee Colony Algorithm

AN IDEA BASED ON HONEY BEE SWARM FOR NUMERICAL OPTIMIZATION

(TECHNICAL REPORT-TR06, OCTOBER, 2005)

Dervis KARABOGA

[karaboga@erciyes.edu.tr](mailto:karaboga@erciyes.edu.tr)

Erciyes University, Engineering Faculty

Computer Engineering Department

Kayseri/Türkiye

## I. INTRODUCTION

Swarm intelligence has become a research interest to many research scientists of related fields in recent years. Bonabeau has defined the swarm intelligence as “any attempt to design

---

# Type of Bees

## **The Employed Bee**

These bees first collect the food from the source  
Share information about its location with onlookers  
Food is also called nectar.

## **The Onlooker Bee**

Receive the information of the food source from the employed bees  
and select one of the best food source to gather the food

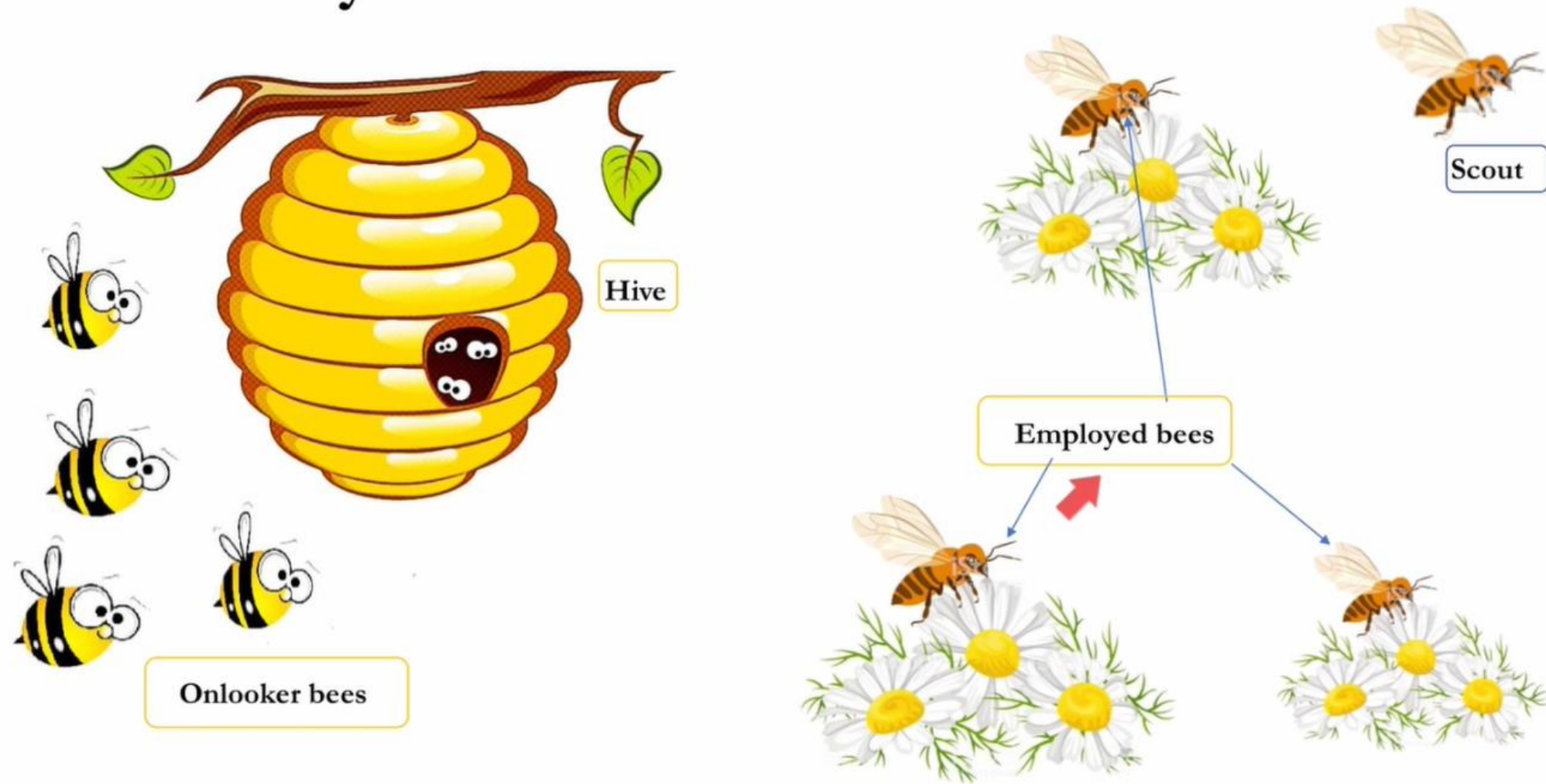
## **The Scout Bee**

Responsible for finding new food source whenever required

---



# Honey bee food Search Mechanism



Onlooker bees

Onlooker bees

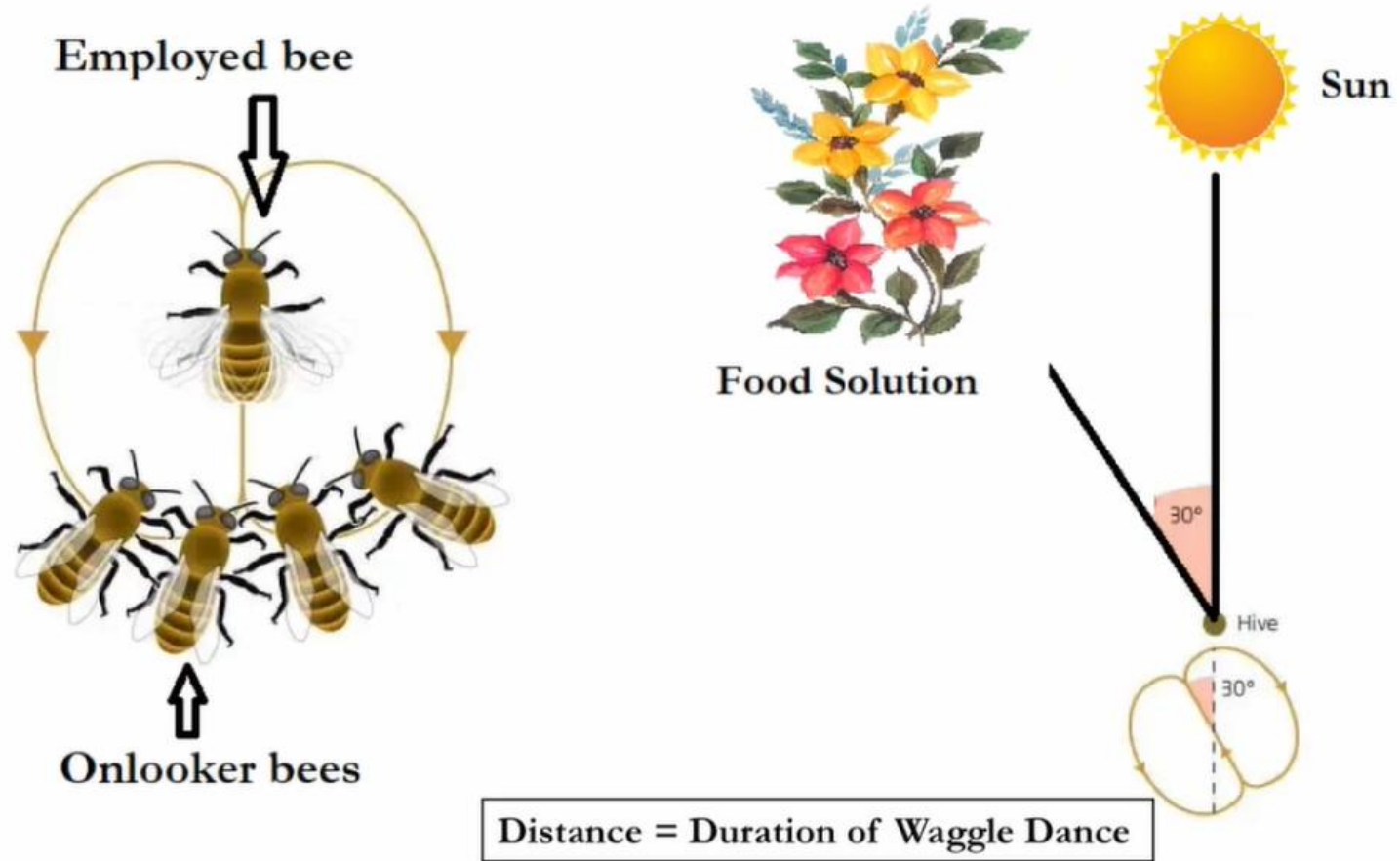
Unloading area

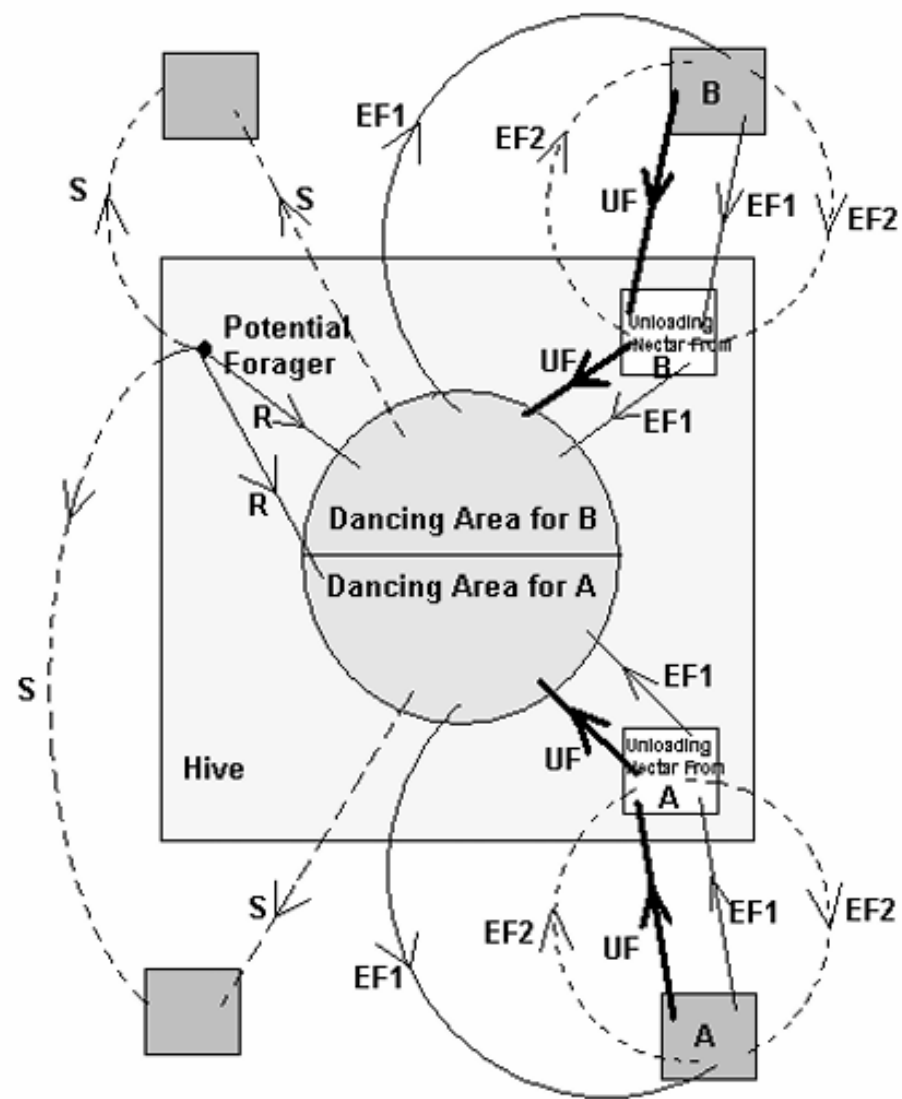


Dancing area



# Waggle Dance





# Self Organization

In the case of honey bees, the basic properties on which self organization relies are as follows:

- 1- **Positive feedback:** As the nectar amount of food sources increases, the number of onlookers visiting them increases, too.
  - 2- **Negative feedback:** The exploitation process of poor food sources is stopped by bees.
  - 3- **Fluctuations:** The scouts carry out a random search process for discovering new food sources.
  - 4- **Multiple interactions:** Bees share their information about food sources with their nest mates on the dance area.
-

# ABC Algorithm

The ABC Algorithm comprises four phases,

## **Initialization phase**

Common in all swarm intelligence methods

## **Employed bee Phase**

Bees Associated with specific food source

## **Onlooker bee phase**

Waiting in hive and watch the waggle dance

## **Scout bee phase**

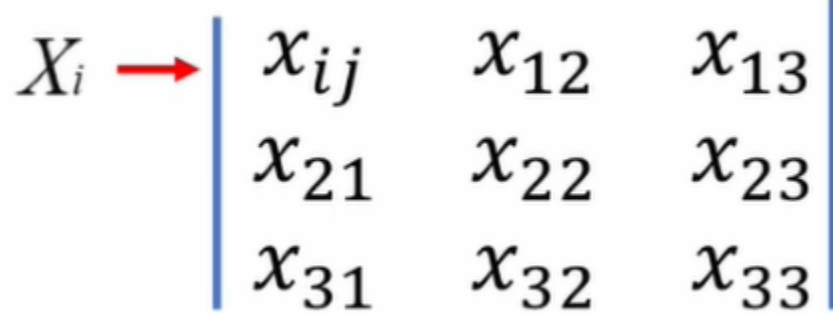
Bees with abandoned food source, start searching

---

# Initialization Phase

$$x_{ij} = x_{j,min} + rand(0,1) * (x_{j,max} - x_{j,min})$$

«i» be position of food source or set of possible solutions (randomly generated)



$X_i$	$\rightarrow$	$x_{ij}$	$x_{12}$	$x_{13}$
		$x_{21}$	$x_{22}$	$x_{23}$
		$x_{31}$	$x_{32}$	$x_{33}$

# Initialization Phase

Objective function values are obtained from the food source position  
The fitness value of solutions are calculated

$$fit_k = \begin{cases} \frac{1}{(1+f_k)} & \text{if } f_k \geq 0 \\ 1 + abs(f_k) & \text{if } f_k \leq 0 \end{cases}$$

At this stage trail encounter is set to zero

---



# Employed Bee Phase

Change in food position by employed bee

$$v_{ij} = x_{ij} + \phi_{ij} * (x_{ij} - x_{kj})$$

$\phi$  random number between  $[-1,1]$

$$X_i \rightarrow \begin{vmatrix} x_{ij} & x_{12} & x_{13} \\ x_{21} & x_{22} & x_{23} \\ x_{31} & x_{32} & x_{33} \end{vmatrix}$$

# Onlooker Bee Phase

Probability

$$P_i = \frac{Fit(X_i)}{\sum_{k=1}^S Fit(X_k)}$$

Calculation of the new position

$$v_{ij} = x_{ij} + \phi_{ij} * (x_{ij} - x_{kj})$$

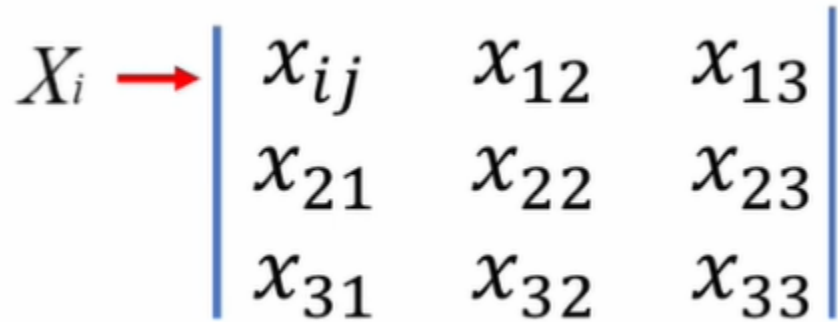
$\phi$  random number between  $[-1,1]$

$$X_i \rightarrow \begin{vmatrix} x_{ij} & x_{12} & x_{13} \\ x_{21} & x_{22} & x_{23} \\ x_{31} & x_{32} & x_{33} \end{vmatrix}$$

# Scout Bee Phase

If particular solution is not improved after predetermined trials, ignore it and create new solution randomly in the search space

$$x_{ij} = x_{j,min} + rand(0,1) * (x_{j,max} - x_{j,min})$$



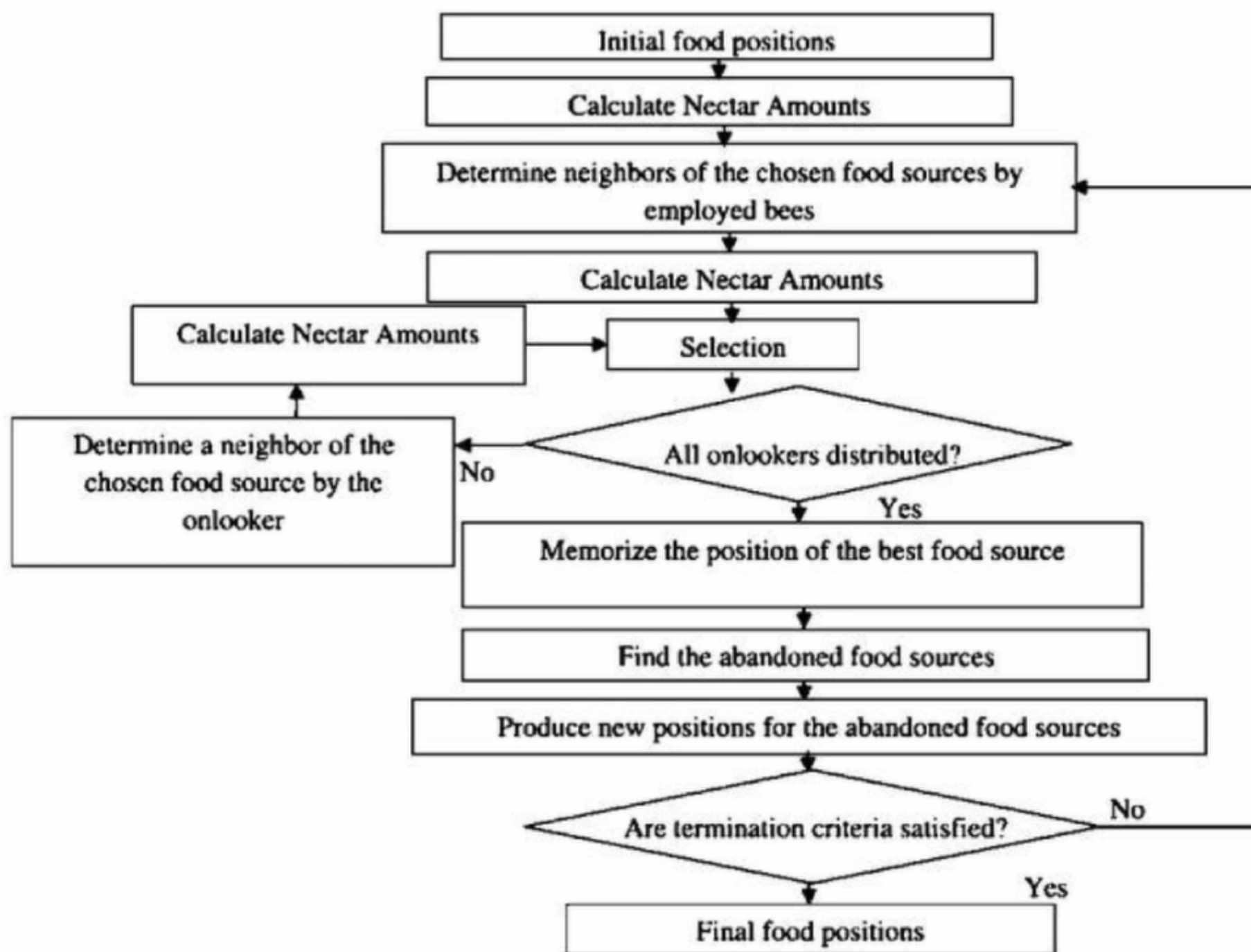
The diagram illustrates the Scout Bee Phase by showing a solution vector  $X_i$  pointing to a matrix of parameters  $x_{ij}$ . The vector  $X_i$  is on the left, followed by a red arrow pointing to a 3x3 matrix. The matrix is enclosed in a yellow box and has blue vertical lines on its left and right sides. The elements of the matrix are  $x_{ij}$ ,  $x_{12}$ ,  $x_{13}$  in the first row;  $x_{21}$ ,  $x_{22}$ ,  $x_{23}$  in the second row; and  $x_{31}$ ,  $x_{32}$ ,  $x_{33}$  in the third row.

$x_{ij}$	$x_{12}$	$x_{13}$
$x_{21}$	$x_{22}$	$x_{23}$
$x_{31}$	$x_{32}$	$x_{33}$

1. Initialize the population of solution  $x_{ij}$
2. Evaluate the population
3. Cycle=1
4. Repeat
5. Produce new solutions (food source positions)  $v_{ij}$  in the neighbourhood of  $x_{ij}$  for the employed bees using the formula  $v_{ij} = x_{ij} + \phi_{ij} * (x_{ij} - x_{kj})$  (k is the solution in the neighbourhood of i,  $\phi$  is the random number in the range of  $[-1,1]$ ) and evaluate them.
6. Apply greedy selection process between  $x_i$  and  $v_i$ .
7. Calculate the probability values  $P_i$  for the solution  $x_{ij}$  by means of their fitness values using the equation  $P_i = Fit_i / \sum Fit_i$ . In order to calculate fitness values of solutions we employed the following equation .

$$fit_k = \begin{cases} \frac{1}{(1+f_k)} & \text{if } f_k \geq 0 \\ 1 + abs(f_k) & \text{if } f_k \leq 0 \end{cases}$$

8. Produce the new solutions  $v_i$  for the onlookers from the solutions  $x_i$  selected depending on  $P_i$  and evaluate them.
9. Apply the greedy selection process for the onlookers between  $x_i$  and  $v_i$ .
10. Determine the abandoned solution, if exists, and replace it with a new randomly produced solution  $x_i$  for the scout using the equation  $x_{ij} = x_{j,min} + rand(0,1) * (x_{j,max} - x_{j,min})$
11. Memorize the best food source(solution) achieved so far.
12. Cycle =cycle + 1
13. Until cycle = maximum cycle number.



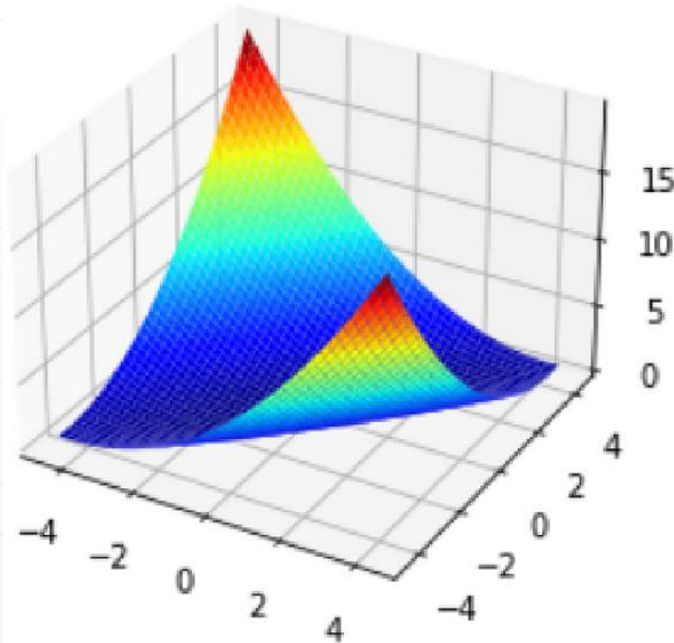
# Implementation

## Matyas Function

$$f(x, y) = 0.26(x^2 + y^2) - 0.48xy$$

$$f(0,0) = 0$$

$$-10 \leq x, y \leq 10$$



## Rosenbrock Function

$$f(x, y) = (1 - x)^2 + 100(y - x^2)^2,$$

subject to  $x^2 + y^2 \leq 2$

$$f(1,1) = 0 \quad -1.5 \leq x, y \leq 1.5$$

