

(191) Let's say  $\theta = \angle BAC$

$$\cos \theta = \frac{0,24}{\sqrt{0,24^2 + 0,18^2}} = 36,87^\circ$$

a.) take moment about C and apply the equilibrium condition  $\sum M_C = 0$   
taking sign conventions, anticlockwise moment is taken as positive and clockwise moment is taken as negative.

$$-(240N)(0,8m) - (240N)(0,4m) + (T_{AB} \cos \theta)(0,18m) = 0$$

$$T_{AB} (\cos 36,87^\circ)(0,18m) = 240(0,8 + 0,4)$$

$$\boxed{T_{AB} = 2000N}$$

b.)  $\sum F_x = 0 \quad \sum F_y = 0$

Take sum of all horizontal forces is equal to zero,

$$\sum F_x = 0$$

$$-2000N(\cos 36,87^\circ) + C_x = 0$$

$$C_x = 1600N$$

Take sum of all vertical forces is equal to zero,  $\sum F_y = 0$

$$C_y - 2000N(\sin 36,87^\circ) - 240N - 240N = 0$$

$$C_y = 1680N$$

The reaction at C is  $R_C = \sqrt{C_x^2 + C_y^2}$

$$R_C = \sqrt{(1600N)^2 + (1680N)^2}$$

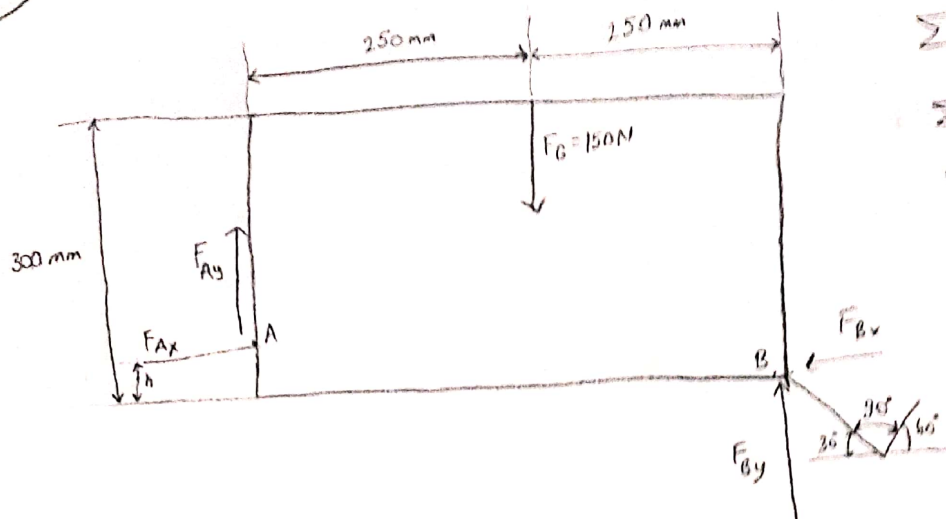
$$\boxed{R_C = 2320N}$$

the direction of  $R_C$  is  $\tan \theta = \frac{C_y}{C_x}$

$$\tan \theta = \frac{1680N}{1600N}$$

$$\boxed{\theta = 46,4^\circ}$$

Q2 Free body diagram



$$\begin{aligned}\sum F_x &= 0 \\ \sum F_y &= 0 \\ \sum M_A &= 0\end{aligned}$$

a.) distance of the point A from the base,  $h=0$

From  $\sum M_A = 0$

$$-(150\text{ N})(250\text{ mm}) - (F_{Bx} \cdot h) + F_{By}(500\text{ mm}) = 0$$

$$0 = (-37500 \text{ N}\cdot\text{mm}) + F_{By}(500\text{ mm})$$

$$F_{By}(500\text{ mm}) = (37500 \text{ N}\cdot\text{mm})$$

$$F_{By} = \frac{(37500 \text{ N}\cdot\text{mm})}{(500 \text{ mm})} = 75 \text{ N}$$

From the condition of equilibrium,  $\sum F_y = 0$

$$F_{Ay} - (150 \text{ N}) + F_{By} = 0$$

$$F_{Ay} - (150 \text{ N}) + (75 \text{ N}) = 0 \quad F_{Ay} = 75 \text{ N}$$

From the condition of equilibrium,  $\sum F_x = 0$

Assume the forces acting in the positive x-direction as positive

$$\sum F_x = F_{Ax} - F_{Bx} \quad \text{Apply condition of equilibrium}$$

$$0 = F_{Ax} - F_{Bx} \quad F_{Ax} = F_{Bx}$$

$$F_{By} = F_B \sin 30^\circ$$

$$75 \text{ N} = F_B \sin 30^\circ \quad F_B = \frac{75 \text{ N}}{\sin 30^\circ} = 150 \text{ N}$$

$$\boxed{F_B = 150 \text{ N}} \quad \boxed{\theta_B = 30^\circ}$$

$$F_{Bx} = F_B \cos 30^\circ$$

$$= 150 \cos 30^\circ$$

$$= 130 \text{ N}$$

Substituting in expression (1)

$$F_{Ax} = 130 \text{ N}$$

$$\theta_A = \arctan\left(\frac{F_{Ay}}{F_{Ax}}\right)$$

$$= \arctan\left(\frac{75}{130}\right)$$

$$\theta_A = 30^\circ$$

$$F_A = \sqrt{F_{Ax}^2 + F_{Ay}^2}$$

$$= \sqrt{(130 \text{ N})^2 + (75 \text{ N})^2}$$

$$F_A = 150 \text{ N}$$

$$b.) \sum M_A = 0$$

$$(-37500 \text{ N}\cdot\text{mm}) - F_B \cos 30^\circ (200 \text{ mm}) + F_B \sin 30^\circ (500 \text{ mm}) = 0$$

$$F_B (76,8 \text{ mm}) = (37500 \text{ N}\cdot\text{mm})$$

$$F_B = \frac{37500 \text{ N}\cdot\text{mm}}{76,8 \text{ mm}}$$

$$F_B = 488,28 \text{ N}$$

$$\theta_B = 30^\circ$$

$$F_{Bx} = F_B \cos \theta_B$$

$$F_{Bx} = 488,28 \cos 30^\circ$$

$$= 422,86 \text{ N}$$

$$F_{By} = F_B \sin \theta_B$$

$$= 488,28 \sin 30^\circ$$

$$= 244,14 \text{ N}$$

The angle of reaction  $F_A$ ,

$$\theta_A = \tan^{-1} \frac{F_{Ay}}{F_{Ax}}$$

$$= \tan^{-1} \left| \frac{(-94,14 \text{ N})}{(422,86 \text{ N})} \right|$$

$$\theta_A = 12,55^\circ$$

$$F_A = \sqrt{F_{Ax}^2 + F_{Ay}^2}$$

$$= \sqrt{(422,86 \text{ N})^2 + (-94,14 \text{ N})^2}$$

$$= 433,21 \text{ N}$$

$$F_A = 433,21 \text{ N}$$

$$\theta_A = 12,55^\circ$$

Q3

$$W = mg$$

$$W = 100 \times 9,81$$

$$= 981 \text{ N}$$

$$a.) \sum M_{AB} = 0$$

$$\lambda_{AB} \cdot [(\bar{AC} \times \bar{T}_{CD}) + (\bar{AC} \times \bar{T}_{CE}) + (\bar{AG} \times \bar{W})] = 0$$

$\downarrow$   
 unit vector                      weight force

the position vector of AB

$$\bar{AB} = \bar{OB} - \bar{OA}$$

$$= 0,87i - 0,09i$$

$$= 0,78i$$

$$\lambda_{AB} = \frac{\bar{AB}}{AB}$$

$$\lambda_{AB} = \frac{0,78i}{0,78} = i$$

$$AB = \sqrt{(0,78)^2}$$

$$= 0,78 \text{ m}$$

same for AC

$$\bar{AC} = \bar{OC} - \bar{OA}$$

$$= 0,69i + 0,45k - (0,09i)$$

$$= 0,6i + 0,45k$$

for AG

$$\bar{AG} = \bar{OG} - \bar{OA}$$

$$= \frac{(0,69 + 0,27)}{2}i + \frac{(0,45)}{2}k - 0,09i$$

$$= 0,48i + 0,225k - 0,09i$$

$$= 0,39i + 0,225k$$

$$\bar{T}_{CD} = \bar{T}_{CD} \cdot \lambda_{CD}$$

$$\lambda_{CD} = \frac{\bar{CD}}{CD}$$

position vector of CD

$$\bar{CD} = \bar{OD} - \bar{OC}$$

$$= 0,675j - (0,69i - 0,45k)$$

$$= -0,69i + 0,675j - 0,45k$$

$$CD = \sqrt{(-0,69)^2 + (0,675)^2 + (-0,45)^2}$$

$$= \sqrt{1,1336}$$

$$= 1,065 \text{ m}$$

$$\text{So } \lambda_{CD} = \frac{-0,69i + 0,675j - 0,45k}{1,065} = -0,65i + 0,634j - 0,423k$$



$$\vec{T}_{CD} = T \cdot \vec{\lambda}_{CD}$$

$$= T \cdot (-0,65i + 0,634j - 0,423k)$$

$$\vec{\lambda}_{CE} = \frac{\vec{CE}}{CE}$$

$$\vec{CE} = \vec{OE} - \vec{OC}$$

$$= 0,96i + 0,675j - (0,69i + 0,45k)$$

$$= 0,27i + 0,675j - 0,45k$$

$$CE = \sqrt{(0,27)^2 + (0,675)^2 + (-0,45)^2}$$

$$= \sqrt{0,0729 + 0,455 + 0,2025}$$

$$= \sqrt{0,7304}$$

$$= 0,855 \text{ m}$$

$$\vec{\lambda}_{CE} = \frac{0,27i + 0,675j - 0,45k}{0,855}$$

$$= 0,316i + 0,789j - 0,526k$$

$$\vec{T}_{CE} = T \cdot \vec{\lambda}_{CE}$$

$$\vec{T}_{CE} = T \cdot (0,316i + 0,789j - 0,526k)$$

$$\lambda_{AB} \cdot [(\vec{AC} \times \vec{T}_{CD}) + (\vec{AC} \times \vec{T}_{CE}) + (\vec{AG} \times \vec{W})] = 0$$

Substitute all values then we get

$$T = \frac{220,725}{0,6403} = \boxed{344,72 \text{ N}} \text{ tension in DCE}$$

$$b) \sum M_{B_z} = 0$$

$$-A_y(0,78) + (W)(0,39) - [T_{CD}j](0,18) - [T_{CE}j](0,18) = 0$$

$$-0,78A_y + 382,6 - 39 - 48,95 = 0$$

$$0,78A_y = 294,65$$

$$A_y = 377,75 \text{ N}$$

$$\sum M_{B_y} = 0$$

$$A_z(0,78) - [T(0,423)](0,18) - [T(0,65)](0,45) - [T(0,526)](0,18) + [T(0,316)](0,45) = 0$$

Substitute 344,72 N for T

$$0,78 A_z - 26,25 - 100,83 - 32,63 + 49,0 = 0$$

$$0,78 A_z = 110,71$$

$$A_z = 141,93 \text{ N}$$

$$\sum F_x = 0$$

$$A_x - T(0,65) + T(0,316) = 0$$

Substitute 344,72 N for T,

$$A_x = 115,14 \text{ N}$$

the reaction force vector at point A, is  $(115,14 \text{ N})i + (377,75 \text{ N})j + (141,93 \text{ N})k$

$$\sum F_y = 0$$

$$B_y - W + A_y + T(0,636) + T(0,789) = 0$$

Substitute 344,72 N for T

$$\boxed{B_y = 112,72 \text{ N}}$$

$$\sum F_z = 0$$

$$B_z - A_z - T(0,423) - T(0,526) = 0$$

$$T = 344,72 \text{ N} \quad 141,93 \text{ N} = A_z$$

$$B_z = 185,213 \text{ N}$$

the reaction force vector is  $(112,72 \text{ N})j + (185,213 \text{ N})k$