\mathbf{B}

Name, SURNAME \Rightarrow

Denia SAYIN

• Middle East Technical University Department of Computer Engineering

CENG 477

Fall '18

Instructors:

AHMET OGUZ AKYUZ, TOLGA CAN

Midterm Exam #1

Assistants:

ARIF GORKEM OZER, YUSUF MUCAHIT CETINKAYA, KADIR CENK ALPAY

- Duration: 120 minutes.
- Grading:
 - Each of the 15 TRUE-FALSE questions is worth 2 points.
 - points.

- 12.

- Each of the 10 Multiple-choice questions is worth 5 points.
 Each of the 2 Classical-type questions is worth 10 points.
- For TRUE-FALSE and multiple-choice questions 4 wrong points cancel out 1 correct point.
- Asking questions: is not allowed. If you decide that a question is wrong:
 - DO NOT ask the proctor about a clarification.
 - Indicate clearly your objection and your proposed answer on the first page of the question booklet.
- Mark your group ID (as A or B) on your answer sheet.
- Turn in your question booklet (this booklet) together with the answer sheet. Otherwise your answer sheet will not be evaluated, and you will receive a zero from this exam.
- GOOD LUCK!

I believe there is a problem with question 27. The question states a GOOX300 image, but illustrates a GOIX301 image due to zero-based indexing, showing the top-left pixel as (0,0) and botton-right pixel as (400,000); while it should be (399,299). This also means that the middle point is not in the middle of a pixel as in the illustration, but het ween for pixels => [] O.C.

while John the quarion, I dorego Led the illustration and took the bottom-right pixel as (399, 299) and the dimensions as 400×300 V

Also, for querion 15, I owne that ready who images can be saled ox.

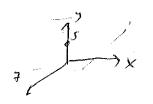
All that aside, coal ex. ...

· t ,

We start with TRUE-FALSE questions, mark A box for TRUE, B box for FALSE on your answer sheet In Blinn-Phong shading of a shiny sphere, when we increase the specular exponent (shininess), the specular highlight on the sphere will get larger. The specular (Blinn-Phong shading) component of the ray tracing illumination model depends on the viewer's position and the light position, but it does not depend on the normal vector of the surface. In bilinear interpolation for texture mapping, the nearest two pixels' colors are interpolated 3 to find the final color. In ray tracing, with everything else being constant, the image size of the objects become smaller if the image plane is brought closer to the camera. The surface color obtained by texture mapping can be used as an object's reflectance coefficient in ray tracing computations. In a k-D tree used to partition a 3D scene, each interior node has k = 3 children. No objects will be in shadow if there are three or more light sources that are separated by depended by 120° on an arbitrary place, I assume ... 120° in a scene. The surface of a unit sphere can be modeled by a parametric equation with two parameters. 8 In ray tracing, the color of a pixel is independent from the colors of neighboring pixels. 9 Vectors remain unchanged by all modeling transformations. The dot product of any two vectors gives the cosine of the angle between them. 11 The barycentric coordinates of a point inside a triangle will add up to 1 even if some of them may be negative. The running-time complexity of ray tracing grows quadratically with the number of pixels. 13 Diffuse shading components of a surface point are the same for cameras located at different points. A rectangular image cannot be used for texture mapping of a triangle. TRUE-FALSE questions END here.

2





Which of the following matrices can be used to draw the reflection of an object from a mirror with plane equation y=5?

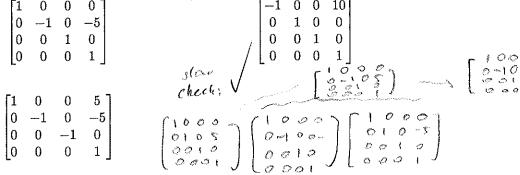


$$\begin{bmatrix} 1 & 0 & 0 & 0 \\ 0 & -1 & 0 & 10 \\ 0 & 0 & 1 & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}$$

$$\begin{bmatrix} 1 & 0 & 0 & -5 \\ 0 & -1 & 0 & 0 \\ 0 & 0 & -1 & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}$$

B)

$$\begin{bmatrix} 1 & 0 & 0 & 0 \\ 0 & -1 & 0 & -5 \\ 0 & 0 & 1 & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}$$



C)

$$\begin{bmatrix} 1 & 0 & 0 & 5 \\ 0 & -1 & 0 & -5 \\ 0 & 0 & -1 & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}$$

$$\begin{pmatrix}
1000 & & & \\
0105 & & & \\
0010 & & \\
0010 & & \\
0010 & & \\
0010 & & \\
0010 & & \\
0001 & & \\
0001
\end{pmatrix}$$

17 Assume that a 3×3 modeling transformation matrix is defined as follows:

$$M = \begin{bmatrix} 3 & 0 & 0 \\ 0 & 2 & 0 \\ 0 & 0 & 1 \end{bmatrix}$$

$$M = \begin{bmatrix} 3 & 0 & 0 \\ 0 & 2 & 0 \\ 0 & 0 & 1 \end{bmatrix} \qquad (M^{-1})^{\top} \qquad M^{-1} = \begin{bmatrix} 1/1 & 0 & 0 \\ 0 & 2/2 & 0 \\ 0 & 0 & 1 \end{bmatrix}$$

What is the correct transformation matrix to transform the normals?

 $\mathbf{A})$

$$\begin{bmatrix} 3 & 0 & 0 \\ 0 & 2 & 0 \\ 0 & 0 & 1 \end{bmatrix}$$

$$\begin{bmatrix} \frac{1}{2} & 0 & 0 \\ 0 & \frac{1}{3} & 0 \\ 0 & 0 & 1 \end{bmatrix}$$

B)

$$\begin{bmatrix} 1 & 0 & 0 \\ 0 & 2 & 0 \\ 0 & 0 & 3 \end{bmatrix}$$

$$\begin{bmatrix} \frac{1}{3} & 0 & 0 \\ 0 & \frac{1}{2} & 0 \\ 0 & 0 & 1 \end{bmatrix}$$

C)

$$\begin{bmatrix} 1 & 0 & 0 \\ 0 & 1 & 0 \\ 0 & 0 & 1 \end{bmatrix}$$

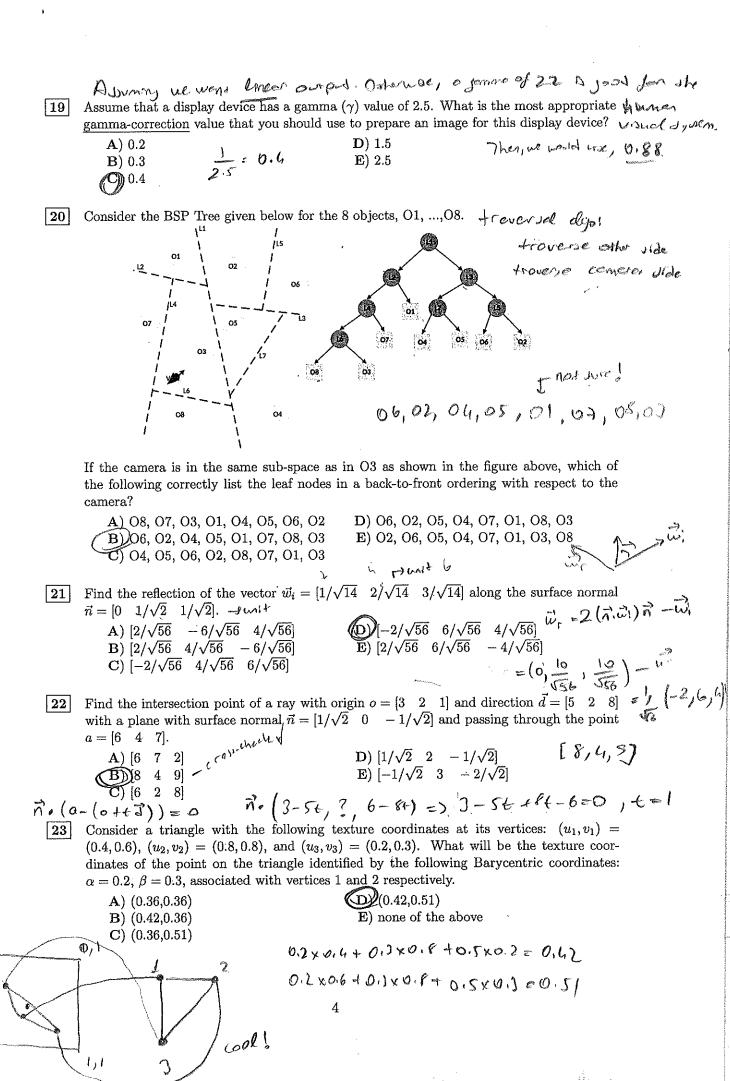
- Assume that we want to store 8 different vertices and a closed-mesh made up of 12 triangles to represent a shape. Each vertex is made up of 3 floating point numbers (assume one float occupies 4 bytes). Each index is represented using an integer value (assume one integer also occupies 4 bytes). If the only extra information that the file contains is the number of vertices (one integer) and number of triangular faces (another integer), how many total bytes will be used to represent this mesh using an Indexed-Face-Set representation that only supports triangles?
 - A) 216
 - B) 232 **(C))**248

- D) 256
- E) 282
- Fores 12 by to x 12 = 144 Vestion - 12 34 to, 50 8 = 96

extra, 8 bytes

248





00

1,0



Given the following transformation definitions: 24

- $R_x(\theta)$: Rotate a point around the x axis counter-clockwise by θ degrees
- $R_y(\theta)$: Rotate a point around the y axis counter-clockwise by θ degrees
- $R_z(\theta)$: Rotate a point around the z axis counter-clockwise by θ degrees

Which of the following transformations will rotate any given point along the line passing through $P_1 = (0,0,0)$ and $P_2 = (-2\sqrt{2},2,2)$ by an angle of θ degrees counter-clockwise?

- $\begin{array}{c} \textbf{(A)} \, R_x(-45^o) R_y(-45^o) R_z(\theta) R_y(45^o) R_x(45^o) \\ \textbf{(B)} \, R_x(-45^o) R_y(-45^o) R_y(\theta) R_y(45^o) R_x(45^o) \\ \textbf{(C)} \, R_x(-45^o) R_y(-45^o) R_x(\theta) R_y(45^o) R_x(45^o) \end{array}$

 - D) All of the above
 - E) None of the above

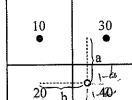


Assume that the uv coordinates of a texture point is indicated by the empty circle in the 25 diagram below. Its distance to the top pixel is given by a = 0.75 and the left pixel by b =0.60. The numbers above filled circles indicate the intensities of different pixels. Compute the final color that should be used for this texture point assuming bilinear interpolation.

D) 28.0

E) 30.0

- A) 28.5
- **B**) 29.0
- 129.5



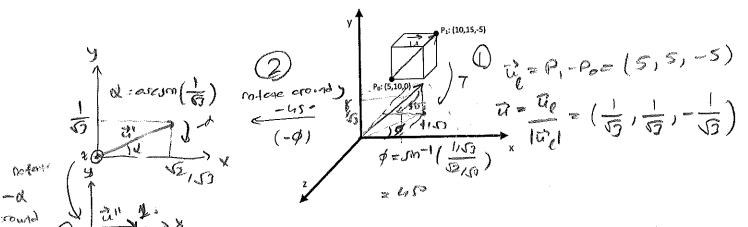
The Multiple-choice questions END here.





Classical questions BEGIN here. You must show your work with a clear writing. You can use the back of the page if needed.

- is CW for rotation. A CCLU and Consider the 3D cube shown below. 26



Derive the composite transformation matrix as a multiplication of basic transformation matrices to rotate the cube θ degrees around the axis defined from vertex P_0 to vertex P_1 . The direction of the rotation axis is from P_0 to P_1 . Write your solution as a sequence of basic transformations. In other words, you do not need to write or multiply any 4×4 matrices. You may indicate basic transformations as $R_*(\alpha)$: rotate around *-axis (* is either x, y, or z) α degrees and T(tx, ty, tz): translate tx, ty, and tz units. You may use the arccos, i.e., cos^{-1} and the arcsin, i.e., sin^{-1} functions to indicate angles in your rotations.

Honestly, I prefer the afternetive orthonormal few method. But 1841, 301 # Let the transformation matrix be M. First, we have to traval all writers to

that Po is at the origin: [M=T(5,10,0) Mo T(-5,-10,0)]

Then, we can bring the divector to the Xy place by rotatey to -450 dayrees

around the y-axis: [Mo = Ry (+450) m, Ry (-450) (see 2)

* Then, we can brity the new il vector to the x axr by contentry 17 - d

degrees around +, where d = arcsin (1/53): [M, = R, (d) M2 R, (-d)] (see 0) # Findley, now that our vector is aligned with X, we can perform the notation

around the x ax D: [m2 = Rx (0)]

& Since as how embedded the inverse operations as well, we can early write the full composite metrix of

M=T(5,10,0)Ry (+450)Rz (arcsm(+3)) Rx (0) Rz (-arcsm (+3))Ry(-450)T(-5,-10,0)



image plane is 401x301 (gen-malexed, lest a 400,700 instead of 335,235).

I will assume the illustration is wrong. (in passes between pixels, not from the handed world coordinate system:

[3, 4, 5]Eve position (e): View direction (g): [0,0,-1]p = (300, 200)[0, 1, 0]Up vector (v): 10 Near plane (NP) distance (d): -10NP left coordinate (1): 10 NP right coordinate (r): -7.5NP bottom coordinate (b): 7.5 NP top coordinate (t): 400 Image width (pixels): (400, 300) 300 Image height (pixels): 399,199 Image origin: top-left Q=qx7=(1,0,0)

Given the configuration above, find the world coordinate of pixel p(x = 300, y = 200).

Let m be the midpoint of the image plane, fin a vector advancing one pixel by height and fix a vector advancy ent pixel by which

in corresponds to the middle, which is between four pixels, as (199,5, 149,5) assuming then, we can formulate p=m+100.5 fw+50.5 fh (1)

Macyany

 $m = e + dg^2 = (3,4,-5), \hat{\rho}_w = \frac{r-l}{r_w}\vec{u} = \frac{1}{2}\vec{u} = (0.05,0,0), \hat{\rho}_h = \frac{t-b}{r_h}\vec{v} = -\frac{1}{2}\vec{v}$ = (0,-0.05,0)

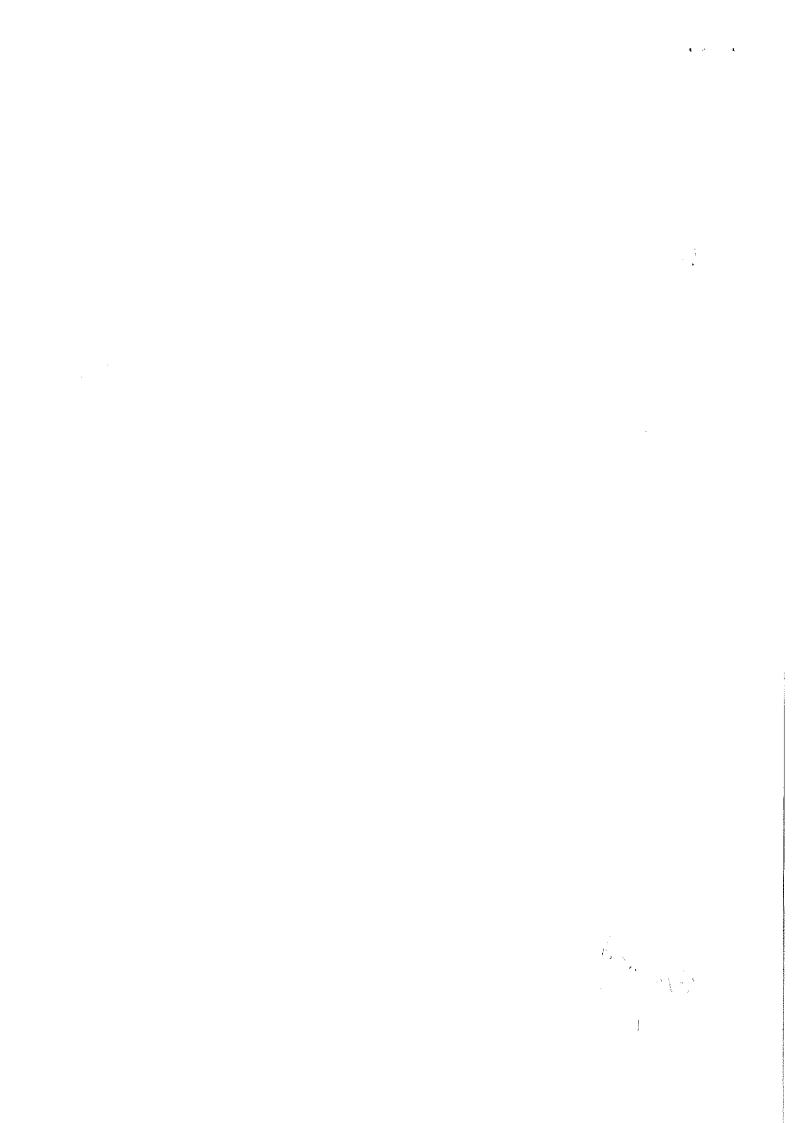
p = (3,4,-5) + 100,5(0,05,0,0) + 50.5(0,-0.05,0), ump (1) $= (8.025, 1.675, -5) \mu$

Compute the world coordinate of the primary ray passing through the same pixel p at ray parameter t=2. Assume that at t=1 the ray will be on the image plane.

r(t) = e + (p-e)t = r(1) = p, on the image plane $\sqrt{3}$

r(2) = e + 2(p-e) = 2p - e = (16.05, 2.95, -10) - (3,4,5)

Excellent







Name, SURNAME ⇒

Trfan Can Kaleli / 2035996

(Middle East Technical University Department of Computer Engineering

CENG 477



Fall '18

Instructors:

Midterm Exam #1

AHMET OGUZ AKYUZ, TOLGA CAN

Assistants:

ARIF GORKEM OZER, YUSUF MUCAHIT CETINKAYA, KADIR CENK ALPAY

- Duration: 120 minutes.
- Grading:

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50 26: 7/10

- Each of the 10 Multiple-choice questions is worth 5 points.

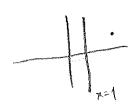
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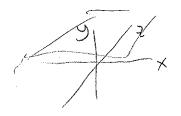
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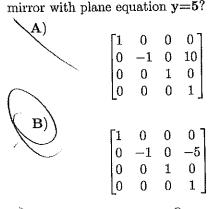
	We start with TRUE-FALSE questions, mark A box for TRUE, B box for SE on your answer sheet
1	In Blinn-Phong shading of a shiny sphere, when we increase the specular exponent (shininess), the specular highlight on the sphere will get larger.
2	The specular (Blinn-Phong shading) component of the ray tracing illumination model depends on the viewer's position and the light position, but it does not depend on the normal vector of the surface.
3	In bilinear interpolation for texture mapping, the nearest two pixels' colors are interpolated to find the final color.
4	In ray tracing, with everything else being constant, the <u>image size of the objects</u> become smaller if the image plane is brought closer to the camera.
5	The surface color obtained by texture mapping can be used as an object's reflectance coefficient in ray tracing computations.
6	In a k-D tree used to partition a 3D scene, each interior node has $k = 3$ children.
7	No objects will be in shadow if there are three or more light sources that are separated by 120° in a scene.
8	The surface of a unit sphere can be modeled by a parametric equation with two parameters.
9	In ray tracing, the color of a pixel is independent from the colors of neighboring pixels.
10	Vectors remain unchanged by all modeling transformations.
[11]	The dot product of any two vectors gives the cosine of the angle between them.
12	The barycentric coordinates of a point inside a triangle will add up to 1 even if some of them may be negative.
13	The running-time complexity of ray tracing grows quadratically with the number of pixels.
14	Diffuse shading components of a surface point are the same for cameras located at different points.
15	A rectangular image cannot be used for texture mapping of a triangle.

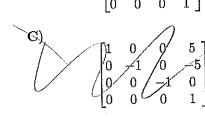
The TRUE-FALSE questions END here.

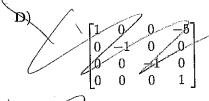


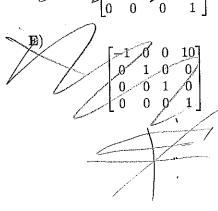


Which of the following matrices can be used to draw the reflection of an object from a









- Assume that a 3×3 modeling transformation matrix is defined as follows:

$\begin{bmatrix} 3 \\ 0 \\ 0 \end{bmatrix}$	0 2 0	$\begin{bmatrix} 0 \\ 0 \\ 1 \end{bmatrix}$	010	1/3
			C 13	1_9

What is the correct transformation matrix to transform the normals?

A)	$\begin{bmatrix} 3 & 0 & 0 \\ 0 & 2 & 0 \\ 0 & 0 & 1 \end{bmatrix}$	D)	$\begin{bmatrix} \frac{1}{2} & 0 & 0 \\ 0 & \frac{1}{3} & 0 \\ 0 & 0 & 1 \end{bmatrix}$	7-
В)	$\begin{bmatrix} 1 & 0 & 0 \\ 0 & 2 & 0 \\ 0 & 0 & 3 \end{bmatrix}$	(E)	$\begin{bmatrix} \frac{1}{3} & 0 & 0 \\ 0 & \frac{1}{2} & 0 \\ 0 & 0 & 1 \end{bmatrix}$	
36 Line Vint 1	$ \begin{array}{cccccccccccccccccccccccccccccccccccc$	3 1	vertice.	36 3 floor

12 T

Assume that we want to store 8 different vertices and a closed-mesh made up of 12 triangles to represent a shape. Each vertex is made up of 3 floating point numbers (assume one float occupies 4 bytes). Each index is represented using an integer value (assume one integer also occupies 4 bytes). If the only extra information that the file contains is the number of vertices (one integer) and number of triangular faces (another integer), how many total bytes will be used to represent this mesh using an Indexed-Face-Set representation that L only supports triangles?

3

A) 216 B) 232 C) 248

8 Köre - 3flot 96 bytes

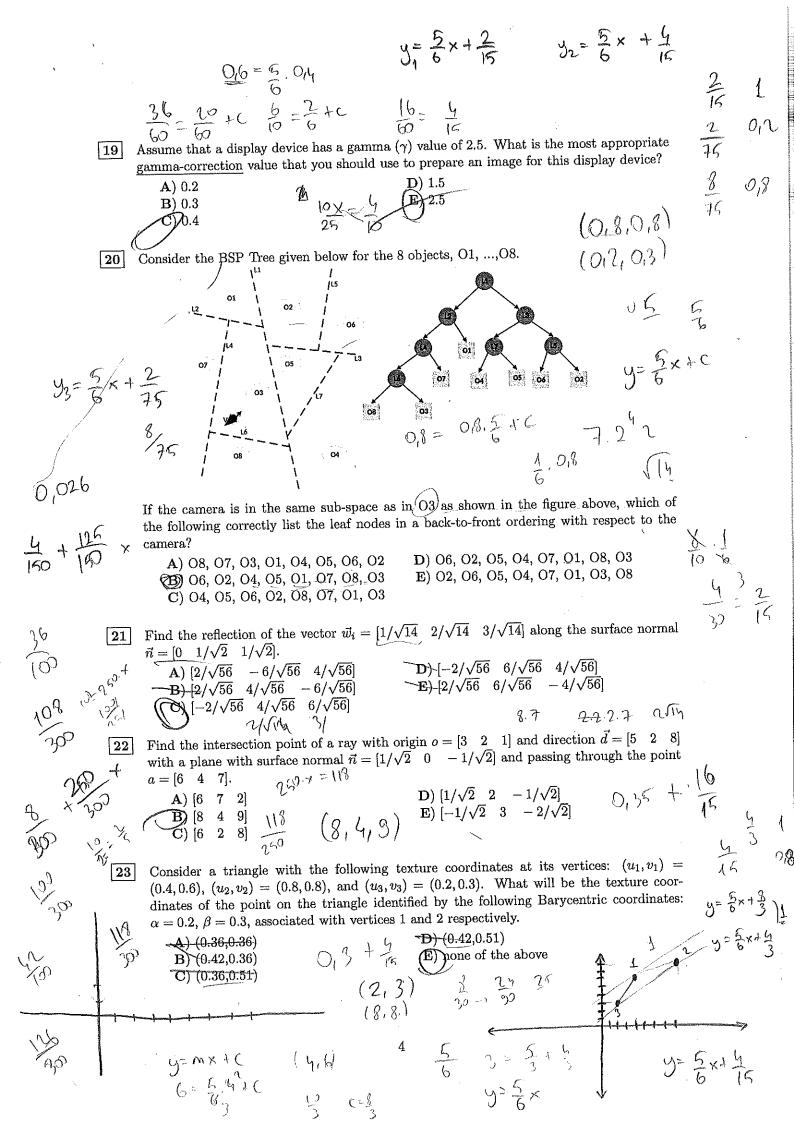
- **D**) 256 **E**) 282

- 160 43
- # Vertices -> 4 bytes

 8 Vertices -> B. 12 = 96 byes

 1 Index -> 316.4= 144

. •



Given the following transformation definitions: 24

- $R_x(\theta)$: Rotate a point around the x axis counter-clockwise by θ degrees
- $R_y(\theta)$: Rotate a point around the y axis counter-clockwise by θ degrees
- $R_z(\theta)$: Rotate a point around the z axis counter-clockwise by θ degrees

Which of the following transformations will rotate any given point along the line passing through $P_1=(0,0,0)$ and $P_2=(-2\sqrt{2},2,2)$ by an angle of θ degrees counter-clockwise?

- A) $R_x(-45^o)R_y(-45^o)R_z(\theta)R_y(45^o)R_x(45^o)$ B) $R_x(-45^o)R_y(-45^o)R_y(\theta)R_y(45^o)R_x(45^o)$ C) $R_x(-45^o)R_y(-45^o)R_x(\theta)R_y(45^o)R_x(45^o)$

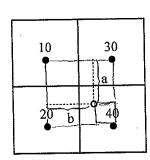
- D) All of the above
- E) None of the above



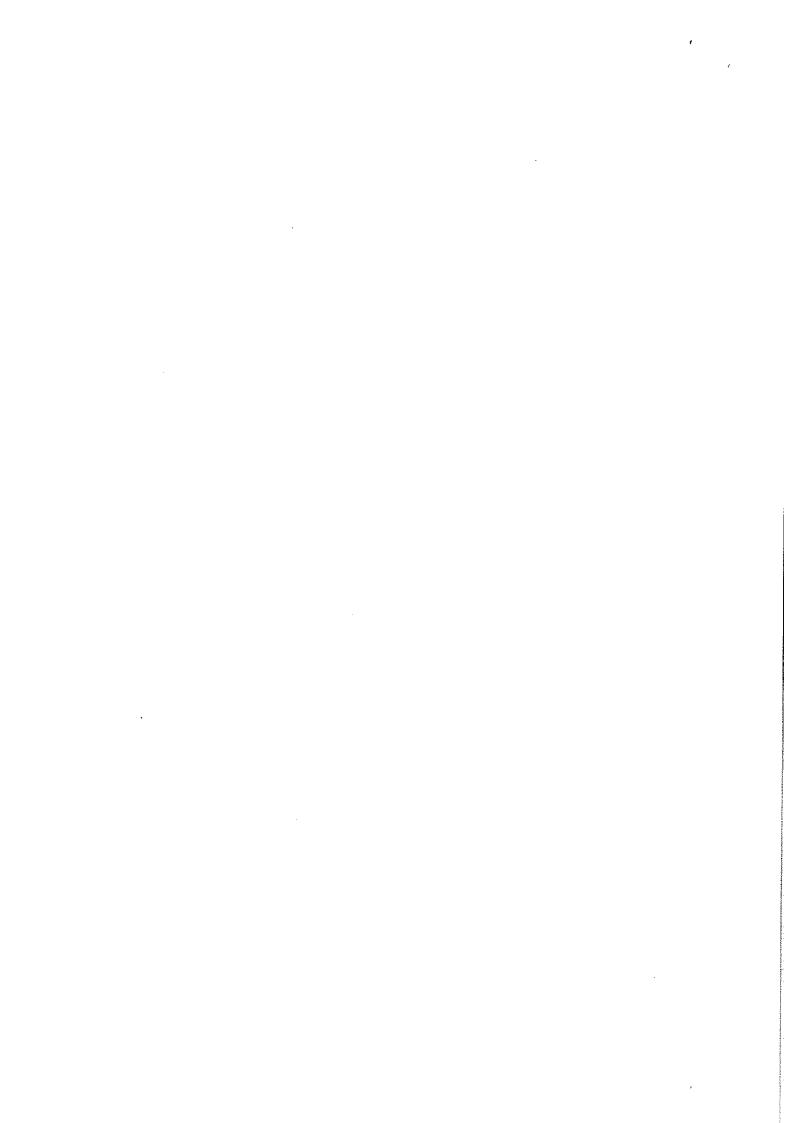
U.V Assume that the uv coordinates of a texture point is indicated by the empty circle in the 25 diagram below. Its distance to the top pixel is given by a=0.75 and the left pixel by b=0.750.60. The numbers above filled circles indicate the intensities of different pixels. Compute the final color that should be used for this texture point assuming bilinear interpolation.

- A) 28.5
- **B**) 29.0
- C) 29.5

- D) 28.0
- E) 30.0

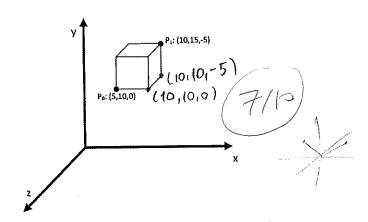


The Multiple-choice questions END here.



Classical questions BEGIN here. You must show your work with a clear writing. You can use the back of the page if needed.

26 Consider the 3D cube shown below.



Derive the composite transformation matrix as a multiplication of basic transformation matrices to rotate the cube θ degrees around the axis defined from vertex P_0 to vertex P_1 . The direction of the rotation axis is from P_0 to P_1 . Write your solution as a sequence of basic transformations. In other words, you do not need to write or multiply any 4×4 matrices. You may indicate basic transformations as $R_*(\alpha)$: rotate around *-axis (* is either x, y, or z) α degrees and T(tx, ty, tz): translate tx, ty, and tz units. You may use the arccos, i.e., cos^{-1} and the arcsin, i.e., sin^{-1} functions to indicate angles in your rotations

1) The vector $P_0P_1 = P_1 - P_0 = (5, 5, 0) \rightarrow Name this vector as <math>u$.

Take another vector v such that $u \cdot v = 0$ (Meaning that angle between them is 90°) V = (-5, 5, 0) satisfies this condition. Now lets find $u \times v$ in order to create a vector that is perpendicular to both u and v.

 $u \times v = w = (0,0,50)$ So lets write M¹ matrix by u,v,w

2) M= [5-500] Since Mis an orthonormal motrix M=MT.

So if we take transpose of both sides we obtain

M.

M= (5 5 0 0) 0 0 50 0 0 0 50 0 12 metros -3

[3] In order to rotate cube by O degrees:

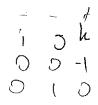
First we must translate it to the origin by vector, then multiply by M, after that rotate around X axis

by O (since new position of vector lies on x-axis),

then multiply by M-1, then retranslate back to first position which can be denoted by:

T(5,10,0), M-1. Rx(0), M. T(-5,-10,0). P

(P is any point on Cube)



Assume that you are given the following configuration for ray tracing defined in a righthanded world coordinate system:

Given the configuration above, find the world coordinate of pixel p(x = 300, y = 200).

$$q = m + l. u + t.v = [3,4,-5] + [10,0,0] + [0,7.5,0]$$

For t=2

$$S_{300,200} = [13,11.5,-5] + (15,025) \cdot [-1,0.0]$$

$$Q = \begin{bmatrix} 13, & 11.5, & -5 \end{bmatrix}$$

$$S_{1,3} = Q + S_{1}U - S_{2}V$$

$$S_{1,3} = (r-1). (i+0.5)/n_{x} = \frac{20.(300.5)}{400} = \frac{300.5}{20} = 15.025$$

$$S_{y} = (t-1). (j+0.5)/n_{y} = \frac{15.(200.5)}{300} = \frac{200.5}{20} = 10.025$$

$$S_{y} = \frac{15.(200.5)}{20} = \frac{200.5}{20} = 10.025$$
Compute the world coordinate of the primary ray passing through the same pixel p at ray $\frac{1}{2} = \frac{1}{2}$

Compute the world coordinate of the primary ray passing through the same pixel p at parameter t=2. Assume that at t=1 the ray will be on the image plane.





Name, SURNAME \Rightarrow

Amena Akten Nipa

Middle East Technical University Department of Computer Engineering **CENG 477**

Midterm Exam #1

Fall '18

Instructors:

Ahmet Oguz Akyuz, Tolga Can

Assistants:

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\$ c $\cdot\cdot$. .

We start with TRUE-FALSE questions, mark A box for TRUE, B box for FALSE on your answer sheet 1 In Blinn-Phong shading of a shiny sphere, when we increase the specular exponent (shininess), the specular highlight on the sphere will get larger. The specular (Blinn-Phong shading) component of the ray tracing illumination model depends on the viewer's position and the light position, but it does not depend on the normal vector of the surface. In bilinear interpolation for texture mapping, the nearest two pixels' colors are interpolated to find the final color. In ray tracing, with everything else being constant, the image size of the objects become smaller if the image plane is brought closer to the camera. The surface color obtained by texture mapping can be used as an object's reflectance coefficient in ray tracing computations. [6] In a k-D tree used to partition a 3D scene, each interior node has k=3 children. No objects will be in shadow if there are three or more light sources that are separated by 120° in a scene. The surface of a unit sphere can be modeled by a parametric equation with two parameters. In ray tracing, the color of a pixel is independent from the colors of neighboring pixels. Vectors remain unchanged by all modeling transformations. 10 The dot product of any two vectors gives the cosine of the angle between them. 11 The barycentric coordinates of a point inside a triangle will add up to 1 even if some of 12

them may be negative.

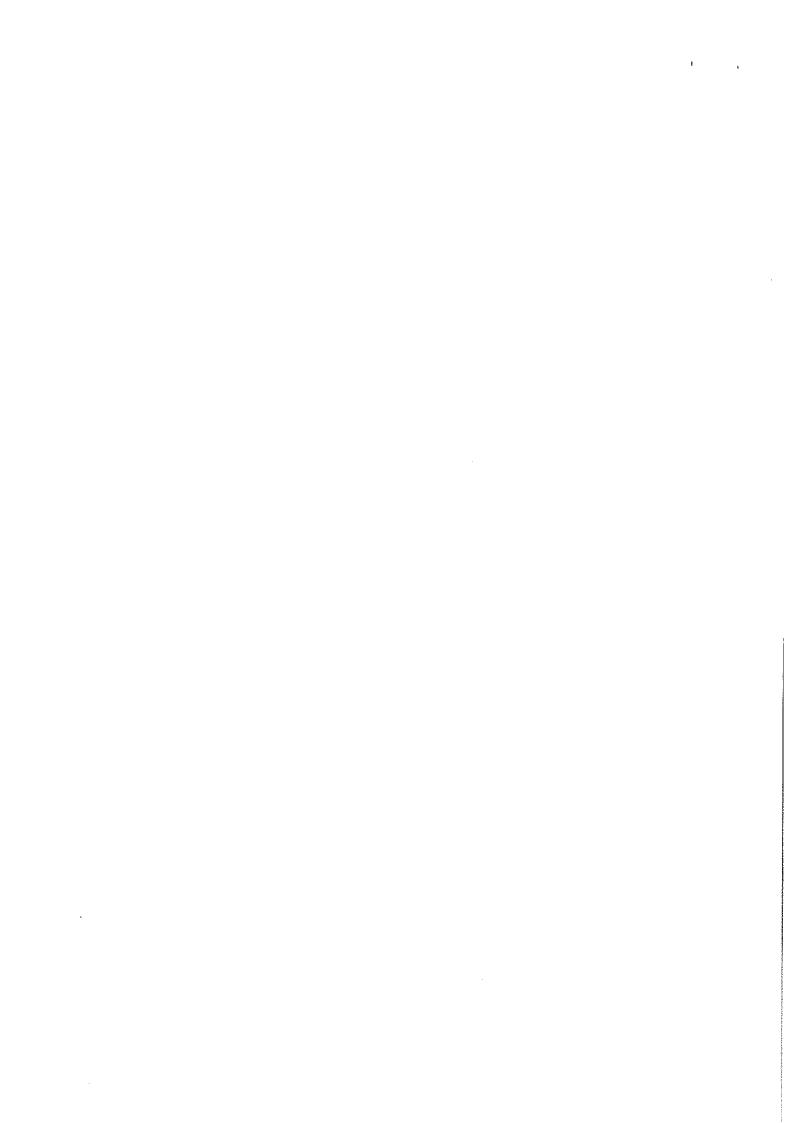
The running-time complexity of ray tracing grows quadratically with the number of pixels.

Diffuse shading components of a surface point are the same for cameras located at different 14 points.

A rectangular image cannot be used for texture mapping of a triangle. 15



The TRUE-FALSE questions END here.



Which of the following matrices can be used to draw the reflection of an object from a mirror with plane equation y=5?

 \mathbf{E})

$$\begin{bmatrix} 1 & 0 & 0 & 0 \\ 0 & -1 & 0 & 10 \\ 0 & 0 & 1 & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}$$

$$\begin{bmatrix} 1 & 0 & 0 & -5 \\ 0 & -1 & 0 & 0 \\ 0 & 0 & -1 & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}$$

$$\begin{bmatrix} 1 & 0 & 0 & 0 \\ 0 & -1 & 0 & -5 \\ 0 & 0 & 1 & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}$$

$$\begin{bmatrix} -1 & 0 & 0 & 10 \\ 0 & 1 & 0 & 0 \\ 0 & 0 & 1 & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}$$



C)
$$\begin{bmatrix} 1 & 0 & 0 & 5 \\ 0 & -1 & 0 & -5 \\ 0 & 0 & -1 & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}$$

Assume that a 3×3 modeling transformation matrix is defined as follows: 17

$$\begin{bmatrix} 3 & 0 & 0 \\ 0 & 2 & 0 \\ 0 & 0 & 1 \end{bmatrix}$$

What is the correct transformation matrix to transform the normals?

A)
$$\begin{bmatrix} 3 & 0 & 0 \\ 0 & 2 & 0 \\ 0 & 0 & 1 \end{bmatrix} \qquad \begin{bmatrix} \frac{1}{2} & 0 & 0 \\ 0 & \frac{1}{3} & 0 \\ 0 & 0 & 1 \end{bmatrix}$$

B)
$$\begin{bmatrix} 1 & 0 & 0 \\ 0 & 2 & 0 \\ 0 & 0 & 3 \end{bmatrix} \qquad \qquad \begin{bmatrix} \frac{1}{3} & 0 & 0 \\ 0 & \frac{1}{2} & 0 \\ 0 & 0 & 1 \end{bmatrix}$$

$$\begin{bmatrix} 1 & 0 & 0 \\ 0 & 1 & 0 \\ 0 & 0 & 1 \end{bmatrix}$$

Assume that we want to store 8 different vertices and a closed-mesh made up of 12 triangles to represent a shape. Each vertex is made up of 3 floating point numbers (assume one float occupies 4 bytes). Each index is represented using an integer value (assume one integer also occupies 4 bytes). If the only extra information that the file contains is the number of vertices (one integer) and number of triangular faces (another integer), how many total bytes will be used to represent this mesh using an Indexed-Face-Set representation that only supports triangles?

12thiangle

V=8
V=(3 flot
4 bytes

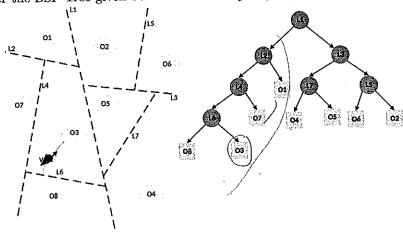
4 bytes

4 bytes + 4 byte (# of integen)

= 16 pen face

- Assume that a display device has a gamma (γ) value of 2.5. What is the most appropriate 19 gamma-correction value that you should use to prepare an image for this display device?
 - A) 0.2
 - **B**) 0.3 (C) 0.4

- with off 49 **D**) 1.5 E) 2.5
- Consider the BSP Tree given below for the 8 objects, O1, ...,O8:

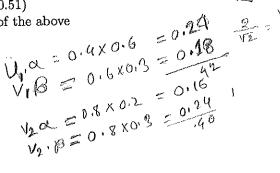


If the camera is in the same sub-space as in O3 as shown in the figure above, which of the following correctly list the leaf nodes in a back-to-front ordering with respect to the camera?

- A) Q8, O7, O3, O1, O4, O5, O6, Q2X
- D) O6, O2, O5, O4, O7, O1, O8, O3
- B) O6, O2, O4, O5, O1, O7, O8, O3
- E) O2, O6, O5, O4, O7, O1, O3, O8
- C) O4, O5, O6, O2, O8, O7, O1, O3
- Find the reflection of the vector $\vec{w_i} = [1/\sqrt{14} \quad 2/\sqrt{14} \quad 3/\sqrt{14}]$ along the surface normal $\vec{n} = [0 \quad 1/\sqrt{2} \quad 1/\sqrt{2}].$
 - **A)** $[2/\sqrt{56} 6/\sqrt{56} \ 4/\sqrt{56}]$
- D) $[-2/\sqrt{56} \quad 6/\sqrt{56} \quad 4/\sqrt{56}]$ E) $[2/\sqrt{56} \quad 6/\sqrt{56} \quad -4/\sqrt{56}]$
- B) $[2/\sqrt{56} \quad 4/\sqrt{56} \quad -6/\sqrt{56}]$
- C) $[-2/\sqrt{56} \quad 4/\sqrt{56} \quad 6/\sqrt{56}]$
- Find the intersection point of a ray with origin $o = \begin{bmatrix} 3 & 2 & 1 \end{bmatrix}$ and direction $\vec{d} = \begin{bmatrix} 5 & 2 & 8 \end{bmatrix}$ with a plane with surface normal $\vec{n} = [1/\sqrt{2} \quad 0 \quad -1/\sqrt{2}]$ and passing through the point $a = [6 \ 4 \ 7].$
 - **A**) $[6 \ 7 \ 2]$
 - **B**) [8 4 9]
 - C) [6 2

- D) $[1/\sqrt{2} \ 2 \ -1/\sqrt{2}]$ $(0+dt-a) \cdot n = 0$ E) $[-1/\sqrt{2} \ 3 \ -2/\sqrt{2}]$ $(0+dt-a) \cdot n = 0$
- Consider a triangle with the following texture coordinates at its vertices: (u_1, v_1) 23 $(0.4,0.6), (u_2,v_2) = (0.8,0.8), \text{ and } (u_3,v_3) = (0.2,0.3).$ What will be the texture coordinates of the point on the triangle identified by the following Barycentric coordinates: $\alpha = 0.2, \, \beta = 0.3$, associated with vertices 1 and 2 respectively.
 - **A**) (0.36,0.36)
 - **B**) (0.42,0.36)
 - C) (0.36,0.51)

- **D**) (0.42,0.51)
- E) none of the above



	•

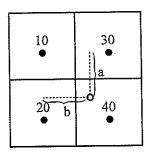
Given the following transformation definitions: 24

- $R_x(\theta)$: Rotate a point around the x axis counter-clockwise by θ degrees
- $R_y(\theta)$: Rotate a point around the y axis counter-clockwise by θ degrees
- $R_z(\theta)$: Rotate a point around the z axis counter-clockwise by θ degrees

Which of the following transformations will rotate any given point along the line passing through $P_1 = (0,0,0)$ and $P_2 = (-2\sqrt{2},2,2)$ by an angle of θ degrees counter-clockwise?

- A) $R_x(-45^o)R_y(-45^o)R_z(\theta)R_y(45^o)R_x(45^o)$ B) $R_x(-45^o)R_y(-45^o)R_y(\theta)R_y(45^o)R_x(45^o)$ C) $R_x(-45^o)R_y(-45^o)R_x(\theta)R_y(45^o)R_x(45^o)$
- D) All of the above
- E) None of the above
- Assume that the \underline{uv} coordinates of a texture point is indicated by the empty circle in the 25 diagram below. Its distance to the top pixel is given by a = 0.75 and the left pixel by b =0.60. The numbers above filled circles indicate the intensities of different pixels. Compute the final color that should be used for this texture point assuming bilinear interpolation.
 - A) 28.5
 - B) 29.0
 - C) 29.5

- $\mathbf{D}) 28.0$
- E) 30.0



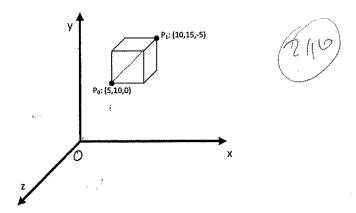
VI 301420 V000+400

The Multiple-choice questions END here.



Classical questions BEGIN here. You must show your work with a clear writing. You can use the back of the page if needed.

26 Consider the 3D cube shown below.



Derive the composite transformation matrix as a multiplication of basic transformation matrices to rotate the cube θ degrees around the axis defined from vertex P_0 to vertex P_1 . The direction of the rotation axis is from P_0 to P_1 . Write your solution as a sequence of basic transformations. In other words, you do not need to write or multiply any 4×4 matrices. You may indicate basic transformations as $R_*(\alpha)$: rotate around *-axis (* is either x, y, or z) α degrees and T(tx, ty, tz): translate tx, ty, and tz units. You may use the arccos, i.e., cos^{-1} and the arcsin, i.e., sin^{-1} functions to indicate angles in your rotations.

Translate the eabe's popoint to the origine O.

T (-tx,-ty,-tz) then Rotate along x axis Rx(0)

Again no tate along Yaxis Ry(0) Then translate back to the previous position

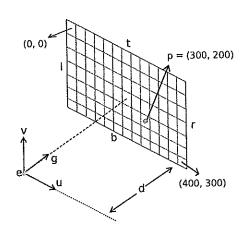
T(tx, ty, tz) Ry(0) R(0)T(-tx,-ty,-tz)

/



Assume that you are given the following configuration for ray tracing defined in a right-handed world coordinate system:

Eye position (e): View direction (g): Up vector (v): Near plane (NP) distance (d): NP left coordinate (l): NP right coordinate (r): NP bottom coordinate (b): NP top coordinate (t): Image width (pixels): Image height (pixels):	$ \begin{bmatrix} 3, 4, 5 \\ 0, 0, -1 \\ \hline{0, 1, 0} \\ \hline{10} \\ -10 \\ \hline{10} \\ -7.5 \\ \hline{7.5} \\ 400 \\ 300 $
Image neight (pixels). Image origin:	top-left



Given the configuration above, find the world coordinate of pixel p(x = 300, y = 200).

For Y:
$$\frac{300+0.5}{400} = \frac{\chi-(1)}{20} \Rightarrow \frac{300.5}{400} = \frac{\chi+10}{20} \Rightarrow \frac{300.5}{20} = \chi+10$$

$$56 \ \chi = \frac{300.5}{20} - 10 = \frac{300.5-200}{20} = \frac{100.5}{20} = \frac{5.995}{20} = \frac{5.995}{20} = \frac{100.5}{20} =$$



Compute the world coordinate of the primary ray passing through the same pixel p at ray parameter t=2. Assume that at t=1 the ray will be on the image plane.

$$p(t) = e + (p-e)t$$

$$= \begin{bmatrix} 3 \\ 4 \end{bmatrix} + \begin{bmatrix} 5.995 - 3 \\ 3.495 - 4 \end{bmatrix} t$$

$$= \begin{bmatrix} 3 \\ 4 \end{bmatrix} + \begin{bmatrix} 2.995 \\ -0.505 \end{bmatrix} t$$

$$= \begin{bmatrix} 3 \\ 4 \end{bmatrix} + \begin{bmatrix} 2.995 \\ -0.505 \end{bmatrix} t$$

$$\frac{1}{10} p(2) = \begin{bmatrix} 3 \\ 4 \\ 5 \end{bmatrix} + \begin{bmatrix} 2.93 \\ -0.505 \end{bmatrix} \cdot 2$$

z = -10

h . 9.

1 30/12

