CPSC 532W Assignment 2

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1 Evaluation Based Sampling

Write a FOPPL evaluator that evaluates the FOPPL as described in lecture and in the book (Alg. 6)

1.1 Code

Provide code snippets that document critical aspects of your implementation sufficient to allow us to quickly determine whether or not you individually completed the assignment.

1.1.1 primitives

```
baseprimitives = {
       '+': lambda x: x[0] + x[1],
       '-': lambda x: x[0] - x[1],
       '*': lambda x: x[0] * x[1],
      '/': lambda x: x[0] / x[1],
      '>': lambda x: x[0] > x[1],
      '>=': lambda x: x[0] >= x[1],
      '<': lambda x: x[0] < x[1],
      '<=': lambda x: x[0] <= x[1],
9
10
      '==': lambda x: x[0] == x[1],
      'sqrt': lambda x: torch.sqrt(x[0]),
11
      'exp': lambda x: torch.exp(x[0]),
12
      'log': lambda x: torch.log(x[0]),
       'vector': vector,
14
      'list': list,
15
       'get': get,
16
      'put': put,
17
18
      'hash-map': hash_map,
       'first': lambda x: x[0][0],
19
      'last': lambda x: x[0][-1],
20
      'nth': lambda x: x[0][int(x[1].item())],
21
      'second': lambda x: x[0][1],
22
      'rest': lambda x: x[0][1:],
23
       'append': append,
24
      'cons': lambda x: append([x[1],x[0]]),
25
      'conj': append,
26
      'mat-add': lambda x: x[0] + x[1],
      'mat-mul': lambda x: torch.matmul(x[0], x[1]),
28
       'mat-transpose': lambda x: x[0].T,
29
30
       'mat-tanh': lambda x: x[0].tanh(),
      \verb|`mat-repmat': lambda x: x[0].repeat((int(x[1].item()), int(x[2].item())))| \\
31
32 }
```

Listing 1: primitives.py - Base primitives

```
def vector(x):
2
          vector = torch.stack(x)
3
      except:
          vector = x
6
      return vector
  def list(x):
9
10
         list = torch.stack(x)
11
      except:
12
          list = x
13
      return list
14
def get(x):
     if type(x[0]) == dict:
16
          value = x[0][x[1].item()]
17
18
        value = x[0][x[1].long()]
19
     return value
21
22 def put(x):
      if type(x[0]) == dict:
23
          x[0][x[1].item()] = x[2]
24
25
          x[0][x[1].long()] = x[2]
26
27
      return x[0]
28
def hash_map(x):
30
     keys = x[::2]
      value = x[1::2]
31
32
      new_keys = []
      for key in keys:
33
34
          try:
              new_keys.append(key.item())
35
36
          except:
37
              new_keys.append(key)
      result = dict(zip(new_keys, value))
38
39
      return result
40
41 def append(x):
      first = x[0]
42
      second = x[1]
43
44
      if first == 'vector':
45
          first = torch.tensor([])
46
      elif first.dim() == 0:
47
          first = first.unsqueeze(0)
48
      if second == 'vector':
          second = torch.tensor([])
50
51
      if second.dim() == 0:
          second = second.unsqueeze(0)
52
      return torch.cat((first, second))
53
```

Listing 2: primitives.py - Functions

```
1 import torch
2 from torch import distributions
4 class Dist:
      def __init__(self, name, distribution, num_par, *par):
          self.name = name
          self.distribution = distribution
          self.num_par = num_par
          self.pars = []
9
10
          for i in range(num_par):
11
               self.pars.append(par[i])
12
13
      def sample(self):
          return self.distribution.sample()
14
15
16 class normal(Dist):
17
      def __init__(self, pars):
18
          mean = pars[0]
          var = pars[1]
19
          super().__init__('normal', distributions.Normal(mean, var), 2, mean, var)
21
22 class beta(Dist):
     def __init__(self, pars):
23
          alpha = pars[0]
24
          betta = pars[1]
25
          super().__init__('beta', distributions.Beta(alpha, betta), 2, alpha, betta)
26
27
28 class exponential(Dist):
      def __init__(self, par):
29
30
          lamda = par[0]
          super().__init__('exponential', distributions.Exponential(lamda), 1, lamda)
31
32
33 class uniform(Dist):
     def __init__(self, pars):
34
35
          a = pars[0]
          b = pars[1]
36
37
          super().__init__('uniform', distributions.Uniform(a, b), 2, a, b)
38
39 class discrete(Dist):
40
     def __init__(self, pars):
          prob = pars[0]
41
          super().__init__('discrete', distributions.Categorical(prob), 0)
42
43
44 class bernoulli(Dist):
      def __init__(self, pars):
45
46
          p = pars[0]
          super().__init__('bernoulli', distributions.Bernoulli(p), 1, p)
```

Listing 3: primitives.py - Distributions

```
distlist = {
    'normal' : normal,
    'beta' : beta,
    'exponential' : exponential,
    'uniform' : uniform,
    'discrete' : discrete,
    'bernoulli': bernoulli
}
```

Listing 4: primitives.py - distlist

1.1.2 evaluate program

```
1 from primitives import baseprimitives, distlist
3
  def evaluate_program(ast):
      """Evaluate a program as desugared by daphne, generate a sample from the prior
          ast: json FOPPL program
      Returns: sample from the prior of ast
8
9
      funcs = {}
10
11
      final_ast = ast
      if isinstance(ast, list):
12
          if isinstance(ast[0], list):
              if ast[0][0] == 'defn':
14
                   for statement in ast:
15
                       if statement[0] == 'defn':
16
                           funcs[statement[1]] = (statement[1], statement[2], statement[3])
17
18
                           final_ast = final_ast[1:]
19
                           result = eval(statement, {}, {}, funcs)
20
               if final_ast[0][0] != 'defn':
21
                   result = eval(final_ast[0], {}, {}, funcs)
22
23
          else:
               result = eval(ast, {}, {}, funcs)
24
25
          result = eval(ast, {}, {}, funcs)
26
      return result[0]
27
```

Listing 5: evaluation_based_sampling.py - evaluate_program

1.1.3 eval

```
def eval(x, sigma, 1, funcs):
2
       "Evaluate an expression in an environment."
       if isinstance(x, list) and len(x) == 1:
           x = x[0]
       if not isinstance(x, list):
           if isinstance(x, int) or isinstance(x, float):
6
                result = torch.tensor(x, dtype=float)
           elif x in baseprimitives or torch.is_tensor(x) or x in funcs or x in distlist:
                result = x
9
10
           else:
11
                result = l[x]
       elif x[0] == 'if':
12
            cond_result, sigma = eval(x[1], sigma, 1, funcs)
13
           if cond_result:
14
                result = x[2]
           else:
16
17
                result = x[3]
       elif x[0] == 'let':
18
           result_temp, sigma = eval(x[1][1], sigma, 1, funcs)
19
20
           for e in x[2:-1]:
           _, sigma = eval(e, sigma, \{**1, **\{x[1][0]: result_temp\}\}, funcs) result, sigma = eval(x[-1], sigma, \{**1, **\{x[1][0]: result_temp\}\}, funcs)
21
22
       elif x[0] == 'sample':
23
           dist, sigma = eval(x[1], sigma, 1, funcs)
24
           result = dist.sample()
25
       elif x[0] == 'observe':
26
27
           result = None
       else:
28
           statements = []
29
           for expression in x:
```

```
statement, sigma = eval(expression, sigma, 1, funcs)
31
32
               statements.append(statement)
33
34
          first_statemnt, other_statements = statements[0], statements[1:]
          if first_statemnt in baseprimitives:
35
              result = baseprimitives[first_statemnt](other_statements)
36
37
          elif first_statemnt in distlist:
              result = distlist[first_statemnt](other_statements)
38
39
          elif first_statemnt in funcs:
40
               _, variables, process = funcs[first_statemnt]
41
               assignment = {key:value for key, value in zip(variables, other_statements)}
42
              result, sigma = eval(process, sigma, {**1, **assignment}, funcs)
43
44
              result = torch.tensor(statements)
45
      return result, sigma
```

Listing 6: evaluation_based_sampling.py - evaluate_program

1.2 Results

Draw 1000 samples for each of the task programs.

1.2.1 Marginal Expectation

Report marginal expectations for all return value dimensions.

Definitely the result changes each time we draw the samples, and in the following I have provided the result of the only one run of the code.

1.2.1.1 Task 1

Marginal Expectation of mu is: 0.9896

1.2.1.2 Task 2

Marginal Expectation of slope is: -0.1806 Marginal Expectation of bias is: 0.0168

1.2.1.3 Task 3

Marginal Expectation of each step is these numbers by order: 1.8824, 1.6470, 1.7058, 1.6471, 1.7059, 0.9412, 1.1176, 1.2941, 1.2353, 1.7647, 1.5294, 1.11765, 1.11765, 1.3529, 1.3529, 1.5882

1.2.1.4 Task 4

Marginal Expectation of w_1 elements are:

-0.1264-0.36710.04190.07670.1846-0.12500.23400.2118-0.15310.6157-0.17880.12030.8325-0.18070.0838-0.2090-0.0974

Marginal Expectation of b_1 elements are:

0.21120.54170.0480.2376-0.0978-0.05860.3023-0.4403-0.5109-0.0517-0.1594-0.11850.72490.02140.0119-0.32930.0979

Marginal Expectation of w_2 elements are:

[-0.0354]	0.0195	-0.0046	-0.0041	-0.0542	0.028	-0.0106	0.0013	0.0318	0.0063
0.0385	-0.0414	-0.0328	-0.0524	0.0058	-0.0672	-0.0242	-0.0182	-0.0357	0.0026
-0.0005	0.0281	-0.0467	-0.0054	-0.0168	0.0125	-0.0054	0.0226	0.0022	-0.023
-0.0065	0.0267	0.03	0.0366	0.0354	0.046	0.0115	-0.0267	0.0344	-0.004
0.0507	-0.0629	0.0439	0.0585	0.0141	-0.0153	-0.0057	0.0291	-0.0244	0.0308
-0.0106	-0.0203	0.0332	0.0199	0.0279	-0.0208	0.0066	0.0153	0.0396	-0.0323
-0.0101	-0.0367	0.0427	0.0245	-0.0546	0.0185	0.0037	-0.0173	0.0014	0.0599
-0.0261	0.0029	-0.0164	-0.0138	0.0364	0.0285	0.0475	-0.0012	-0.0091	-0.052
-0.0146	-0.0539	-0.0297	-0.0349	0.0144	-0.0121	-0.0167	-0.0114	0.0126	0.0041
0.0027	-0.0295	-0.0509	0.0139	0.0441	0.0168	-0.0433	-0.0706	0.0254	0.0179

Marginal Expectation of b_2 elements are:

-0.3279
0.2553
0.4049
0.1395
0.1667
-0.3218
0.3551
0.1866
0.1888
0.0709
-0.0666
-0.0663
0.0215
0.3254
0.198
-0.1191
-0.1661

1.2.2 Histograms

1.2.2.1 Task 1

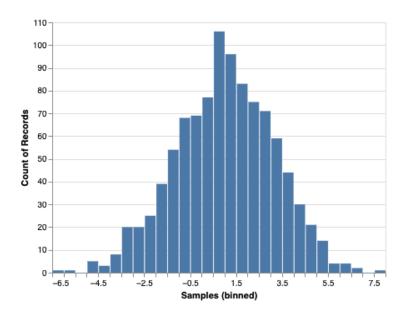


Figure 1: Histogram of mu

1.2.2.2 Task 2

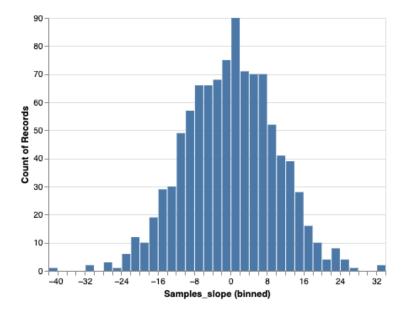


Figure 2: Histogram of slope

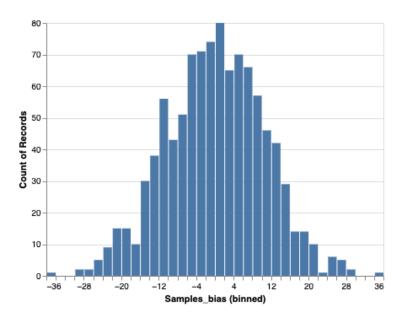


Figure 3: Histogram of bias

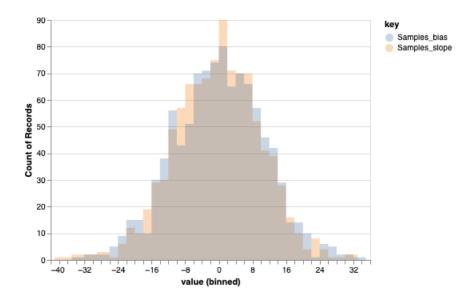


Figure 4: Histogram of slope and bias together

1.2.2.3 Task 3

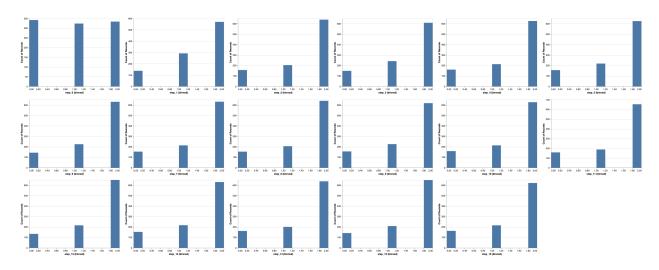


Figure 5: Histogram of states in each step

1.2.2.4 Task 4

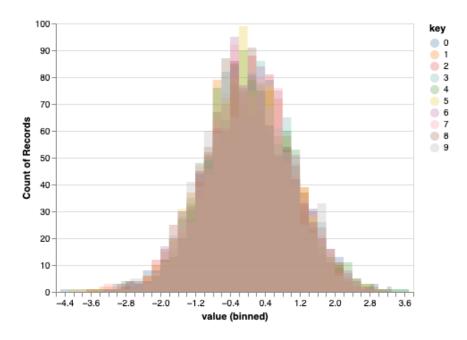


Figure 6: Histogram of W_1 elements together

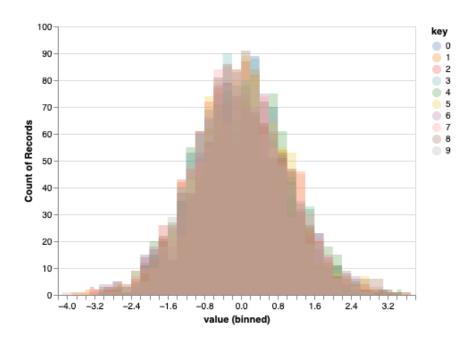


Figure 7: Histogram of b_1 elements together

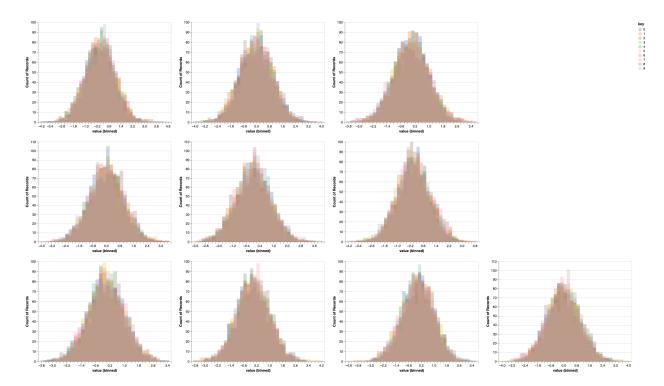


Figure 8: Histogram of W_2 elements together

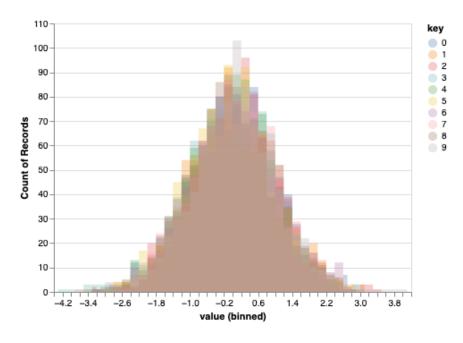


Figure 9: Histogram of b_2 elements together

2 Graph Based Sampling

Write a FOPPL evaluator that evaluates the FOPPL program via ancestral sampling in the graphical model.

2.1 Code

Provide code snippets that document critical aspects of your implementation sufficient to allow us to quickly determine whether or not you individually completed the assignment.

2.1.1 primitives

This part is exactly same as 1.1.1

2.1.2 topological sort

```
def topological_sort(graph):
      nodes = graph[1]['V']
      edges = graph[1]['A']
      is_visited = dict.fromkeys(nodes, False)
      node_stack = []
      node_order_reverse = []
      for node in nodes:
          if not is_visited[node]:
               node_stack.append((node, False))
          while len(node_stack) > 0:
               node, flag = node_stack.pop()
11
12
               if flag:
                   node_order_reverse.append(node)
13
                   continue
14
               is_visited[node] = True
15
               node_stack.append((node, True))
17
               if node not in edges:
                   continue
18
19
               children = edges[node]
               for child in children:
20
                   if not is_visited[child]:
21
                       node_stack.append((child, False))
22
      return node_order_reverse[::-1]
23
```

Listing 7: graph_based_sampling.py - topological_sort

2.1.3 environment

```
env = {**baseprimitives, **distlist}
```

Listing 8: graph_based_sampling.py - environment

2.1.4 deterministic eval

```
def deterministic_eval(exp):
    "Evaluation function for the deterministic target language of the graph based
    representation."

if isinstance(exp, list):
    if exp[0] == 'hash-map':
        exp = ['hash-map'] + [value for expression in exp[1:] for value in expression]
    return evaluate_program(exp)
```

Listing 9: graph_based_sampling.py - deterministic_eval

2.1.5 value substitution

```
def value_subs(expressions, variables):
    if isinstance(expressions, list):
        result = []
        for expression in expressions:
            result.append(value_subs(expression, variables))
    else:
        if expressions in variables:
            result = variables[expressions]
        else:
            result = expressions
        return result
```

Listing 10: graph_based_sampling.py - value_subs

2.1.6 sample from joint

```
def sample_from_joint(graph):
    "This function does ancestral sampling starting from the prior."
    node_order = topological_sort(graph)
    results = {}
    for node in node_order:
        first_statement, *other_statements = graph[1]['P'].get(node)
        if first_statement == 'sample*':
            dist = deterministic_eval(value_subs(other_statements, results))
            result = dist.sample()
        if first_statement == 'observe*':
            result = graph[1]['Y'].get(node)
        results[node] = result
    return deterministic_eval(value_subs(graph[2], results))
```

Listing 11: graph_based_sampling.py - sample_from_joint

2.2 Results

Draw 1000 samples for each of the task programs.

2.2.1 Marginal Expectation

Report marginal expectations for all return value dimensions. Definitely the result changes each time we draw the samples, and in the following I have provided the result of the only one run of the code.

2.2.1.1 Task 1

Marginal Expectation of mu is: 1.0183

2.2.1.2 Task 2

Marginal Expectation of slope is: -0.1693 Marginal Expectation of bias is: 0.1126

2.2.1.3 Task 3

Marginal Expectation of each step is these numbers by order: $1.2353\ 1.3529\ 1.5294\ 1.5882\ 0.8824\ 1.3529\ 1.9412\ 1.3529$ $1.4118\ 1.5294\ 1.6471\ 1.2353\ 1.2941\ 1.1176\ 1.2941\ 1.5294\ 1.2353$

2.2.1.4 Task 4

Marginal Expectation of w_1 elements are:

-0.0116-0.12540.3629-0.22370.2997-0.0427-0.0172-0.23220.0637-0.23890.172-0.11980.2513-0.3007-0.1563-0.0328-0.1635

Marginal Expectation of b_1 elements are:

-0.2130.1301-0.30420.1645-0.2951-0.08240.5833-0.16530.1151-0.13170.1903-0.1795-0.42520.7888-0.06380.3291-0.2595

Marginal Expectation of w_2 elements are:

```
-0.0142
         -0.0052
                   -0.0494
                              0.0185
                                        -0.0629
                                                  -0.0547
                                                             0.009
                                                                      -0.0188
                                                                                 0.0162
                                                                                           -0.004
                                                  -0.0126
                                                                                          -0.0516
-0.0064
          0.0193
                    -0.0407
                              0.0317
                                        0.0051
                                                            -0.0207
                                                                      -0.0025
                                                                                 0.0251
-0.057
          -0.0017
                    0.0374
                                        -0.0176
                                                  -0.0082
                                                                                -0.0085
                                                                                          -0.0243
                              0.0038
                                                             0.0151
                                                                      -0.0269
0.0122
          -0.0005
                    -0.0448
                              -0.0564
                                        0.0005
                                                   0.0345
                                                             0.0718
                                                                       0.0308
                                                                                 0.005
                                                                                          -0.0089
-0.0819
         -0.0145
                    -0.0286
                              -0.0325
                                        -0.0565
                                                   0.044
                                                             0.0178
                                                                      -0.0043
                                                                                 0.0271
                                                                                           0.0003
0.0219
          0.0345
                                        -0.0139
                                                   0.047
                                                                                 0.0469
                                                                                           0.0204
                    0.0251
                              0.0254
                                                             0.0051
                                                                       0.0255
0.0492
          -0.0257
                    -0.003
                              0.0182
                                        -0.035
                                                  -0.0264
                                                             0.0609
                                                                       0.0106
                                                                                 0.0003
                                                                                           -0.0122
-0.019
          0.0187
                    -0.0308
                              -0.0158
                                        0.0189
                                                  -0.0126
                                                                                -0.0088
                                                                                           0.0434
                                                             0.0241
                                                                      -0.0395
-0.0166
          -0.0015
                   -0.0674
                              0.0265
                                        -0.0046
                                                   0.0763
                                                            -0.0201
                                                                       0.0072
                                                                                 0.0231
                                                                                           -0.004
-0.0346
          -0.026
                    0.0248
                              -0.0126
                                        -0.0444
                                                   0.0066
                                                             0.0662
                                                                      -0.0013
                                                                                -0.0439
                                                                                           0.0088
```

Marginal Expectation of b_2 elements are:

0.0754-0.0440.1044-0.33830.115-0.0623-0.68440.2550.00210.30571.155 0.15890.0446-0.1136-1.0082-0.3659-0.0531

2.2.2 Histograms

2.2.2.1 Task 1

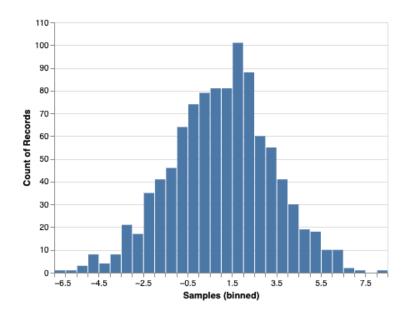


Figure 10: Histogram of mu

2.2.2.2 Task 2

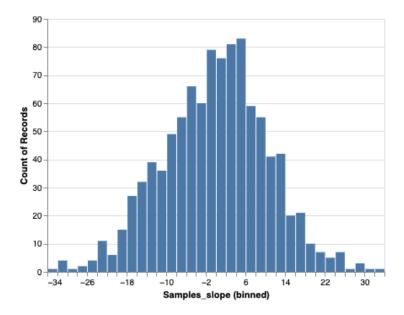


Figure 11: Histogram of slope

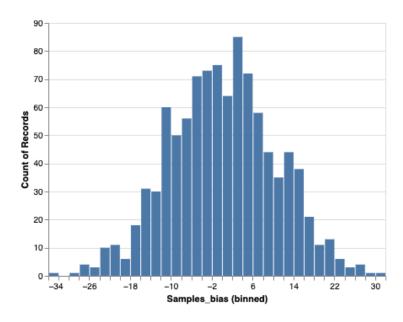


Figure 12: Histogram of bias

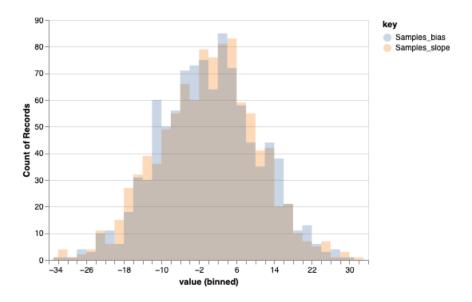


Figure 13: Histogram of slope and bias together

2.2.2.3 Task 3

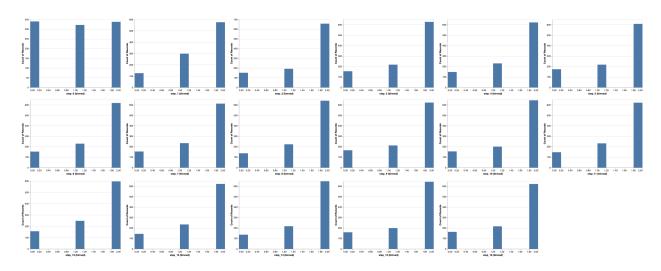


Figure 14: Histogram of states in each step

2.2.2.4 Task 4

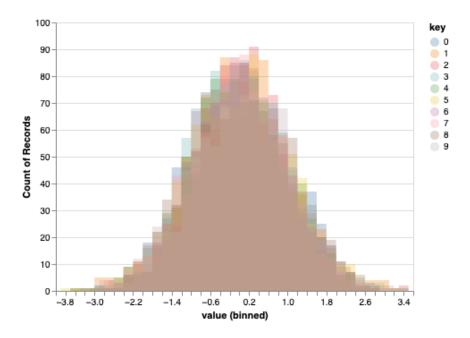


Figure 15: Histogram of W_1 elements together

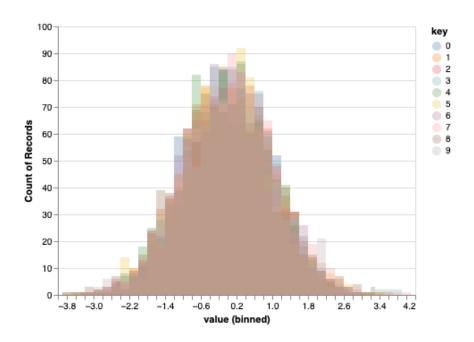


Figure 16: Histogram of b_1 elements together

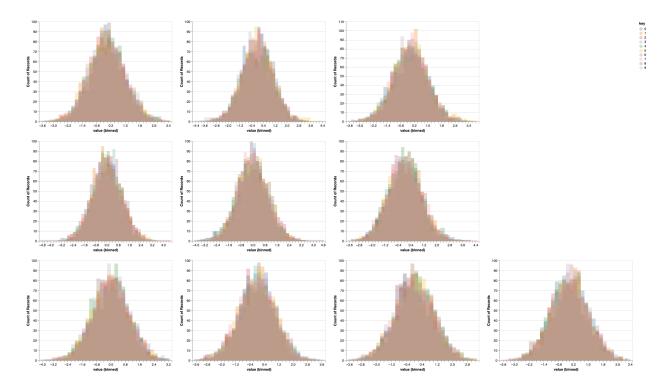


Figure 17: Histogram of W_2 elements together

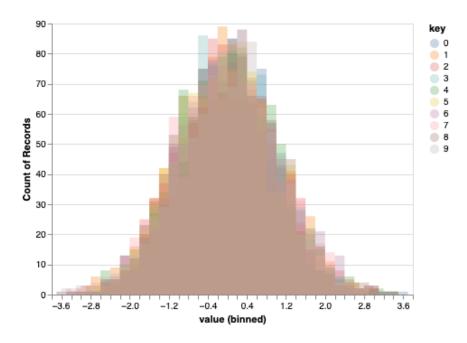


Figure 18: Histogram of b_2 elements together