# Overview

- 1. Introduction
- 2. Models definition
- 3. GANs Training
- 4. Types of GANs
- 5. GANs Applications

# Introduction

Two components, the **generator** and the **discriminator**:

- The **generator** G needs to capture the data distribution.
- The **discriminator** D estimates the probability that a sample comes from the training data rather than from G.

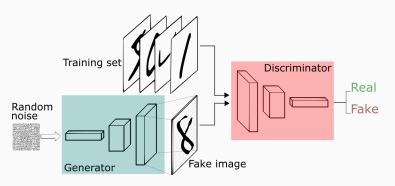


Figure 1: Credits: Silva

#### GANs game:

$$\min_{G} \max_{D} V_{GAN}(D, G) = \underset{x \sim p_{data}(x)}{\mathbb{E}} [\log D(x)] + \underset{z \sim p_{z}(z)}{\mathbb{E}} [\log (1 - D(G(z)))]$$

GANs game:

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#### **GANs** - Discriminator

- Discriminator needs to:
  - · Correctly classify real data:

$$\left[\max_{D} \underset{x \sim p_{data}(x)}{\mathbb{E}} [\log D(x)]\right] \qquad D(x) \to 1$$

Correctly classify wrong data:

$$\left(\max_{D} \underset{z \sim p_{z}(z)}{\mathbb{E}} \left[\log(1 - D(G(z)))\right]\right) \qquad D(G(z)) \to 0$$

• The discriminator is an adaptive loss function.

#### **GANs** - Generator

- **Generator** needs to **fool** the discriminator:
  - Generate samples similar to the real ones:

$$\min_{G} \mathbb{E}_{z \sim p_z(z)}[\log(1 - D(G(z)))] \qquad D(G(z)) \to 1$$

#### **GANs** - Generator

- **Generator** needs to **fool** the discriminator:
  - Generate samples similar to the real ones:

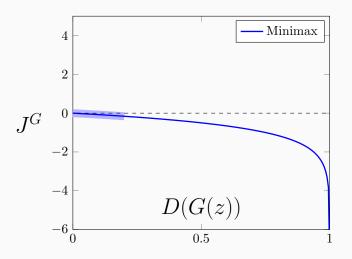
$$\left[ \min_{G} \underset{z \sim p_z(z)}{\mathbb{E}} \left[ \log(1 - D(G(z))) \right] \right] \qquad D(G(z)) o 1$$

• Non saturating objective (Goodfellow et al., 2014):

$$\min_{G} \mathbb{E}_{z \sim p_z(z)} \left[ -\log(D(G(z))) \right]$$

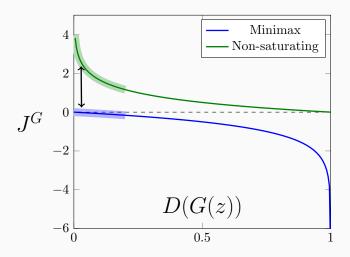
# **GANs - Generator Objectives**

• Minimax: log(1 - D(G(z)))



# **GANs - Generator Objectives**

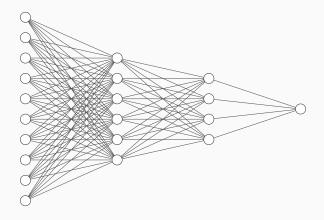
- Minimax: log(1 D(G(z)))
- Non-saturating:  $-\log(D(G(z)))$



**Models definition** 

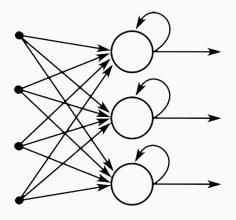
## **GANs** - Models definition

- Different architectures for different data types.
  - Tuple of numbers? Fully Connected Neural Networks



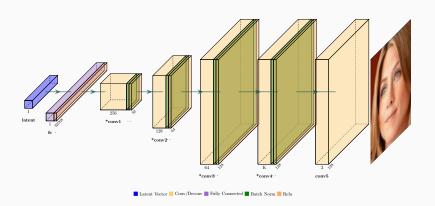
# **GANs** - Models definition

- Different architectures for different data types.
  - Text or sequences? Recurrent Neural Networks



#### **GANs - Models definition**

- Different architectures for different data types.
  - Images? Convolutional Neural Networks



# GANs Training

# **GANs** - Training

- D and G are **competing** against each other.
- Alternating execution of training steps.
- Use minibatch stochastic gradient descent/ascent.



# **GANs - Training - Discriminator**

How to **train** the **discriminator**?

Repeat from 1 to k:

1. Sample minibatch of m noise samples  $z^{(1)}, \ldots, z^{(m)}$  from  $p_z(z)$ 

# **GANs - Training - Discriminator**

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- 2. Sample minibatch of m examples  $x^{(1)}, \ldots, x^{(m)}$  from  $p_{data}(x)$

# **GANs** - Training - Discriminator

## How to **train** the **discriminator**?

#### Repeat from 1 to **k**:

- 1. Sample minibatch of *m* noise samples  $z^{(1)}, \ldots, z^{(m)}$  from  $p_z(z)$
- 2. Sample minibatch of *m* examples  $x^{(1)}, \ldots, x^{(m)}$  from  $p_{data}(x)$
- 3. Update D:

$$\mathbf{J} = \underbrace{\frac{1}{m} \sum_{i=1}^{m} \log \mathbf{D}(\mathbf{x}^{(i)}) + \log(1 - \mathbf{D}(\mathbf{G}(\mathbf{z}^{(i)})))}_{\text{D performance}}$$

$$\theta_{\mathbf{d}} = \theta_{\mathbf{d}} + \lambda \nabla_{\theta_{\mathbf{d}}} \mathbf{J}$$

# **GANs - Training - Generator**

How to **train** the **generator**?

Update executed **only once** after **D** updates:

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# **GANs - Training - Generator**

# How to **train** the **generator**?

Update executed **only once** after **D** updates:

- 1. Sample minibatch of *m* noise samples  $z^{(1)}, \ldots, z^{(m)}$  from  $p_z(z)$
- 2. Update G:

$$\mathbf{J} = \underbrace{\frac{1}{m} \sum_{i=1}^{m} \log(\mathbf{D}(\mathbf{G}(\mathbf{z}^{(i)})))}_{\text{G performance}}$$

$$\theta_{g} = \theta_{g} + \lambda \nabla_{\theta_{g}} \mathbf{J}$$

# **GANs - Training - Considerations**

- Optimizers: Adam, Momentum, RMSProp.
- Arbitrary number of steps or epochs.
- Training is completed when D is **completely fooled** by G.
- Goal: reach a Nash Equilibrium where the best D can do is random guessing.

# Types of GANs

# **Types of GANs**

# Two big families:

- Unconditional GANs (just described).
- Conditional GANs (Mirza and Osindero, 2014).

### **Conditional GANs**

- **Both** *G* and *D* are **conditioned** on some extra information **y**.
- In **practice**: perform conditioning by feeding **y** into D and G.

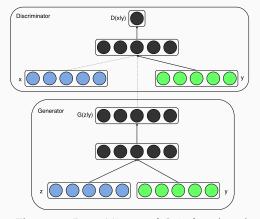


Figure 2: From Mirza and Osindero (2014)

#### **Conditional GANs**

# The GANs game becomes:

$$\min_{G} \max_{D} \underset{x \sim p_{data}(x|\mathbf{y})}{\mathbb{E}} [\log D(x, \mathbf{y})] + \underset{z \sim p_{z}(z)}{\mathbb{E}} [\log (1 - D(G(z|\mathbf{y}), \mathbf{y}))]$$

Notice: the same representation of the condition has to be presented to both network.

#### **Real-world GANs**

- Semi-Supervised Learning (Salimans et al., 2016)
- Image Generation (almost all GAN papers)
- Image Captioning
- Anomalies Detection (Zenati et al., 2018)
- Program Synthesis (Ganin et al., 2018)
- Genomics and Proteomics (Killoran et al., 2017) (De Cao and Kipf, 2018)
- Personalized GANufactoring (Hwang et al., 2018)
- Planning