# Week 10 - Modeling Data and More Shiny

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## Welcome!

Welcome to week 11!

**Record the meeting** 

#### Topics for today

#### **Record the meeting**

Modeling continued

- A. Recap from the buffet and further expansion
- B. Model outputs and summaries
- C. Model helpers tests, diagnostics, and model components
- D. Shiny continued

What a model is:

**model**: a simplified *representation* of your data that can be informative to you (and others) about your data - and, maybe, what your data represents.

From this broad definition, models can take many different forms:

- A sample statistic (e.g., a *mean* of a variable)
- A relationship describing how two variables co-vary (e.g., a bivariate *correlation*)
- A linear regression model

How do we represent model equations in R? Many R packages share a common modeling syntax, or interface: the formula syntax.

This code represents the regression of hp upon mpg:

```
mpg ~ hp
```

Then there are other formula operators:

```
# additional independent variables
mpg ~ hp + disp
# interactions with main effects
mpg ~ hp + disp + hp*disp
# interactions without main effects
mpg ~ hp + disp + hp:disp
# All remaining variables
mpg ~ .
```

There are a number of helper functions that work with lm and other models

And there's some more advanced formula tricks too

```
# Polynomial Regression
y ~ x + I(x^2) + I(x^3)

## y ~ x + I(x^2) + I(x^3)

# Factorial ANOVA
y ~ (a*b*c)^2

## y ~ (a * b * c)^2

# Variable transformations
Sepal.Width ~ Petal.Width + log(Petal.Length) + Species

## Sepal.Width ~ Petal.Width + log(Petal.Length) + Species
```

The lm() function is the base case of using these model formulas

Estimating a model; seeing the result:

```
lm(FinalGradeCEMS ~ TimeSpent_hours, data = d)

##
## Call:
## lm(formula = FinalGradeCEMS ~ TimeSpent_hours, data = d)
##
## Coefficients:
## (Intercept) TimeSpent_hours
## 65.8085 0.3648
```

The lm() function is the base case of using these model formulas

Saving the output to an *object* and printing a summary of the results

```
m1 <- lm(FinalGradeCEMS ~ TimeSpent hours, data = d)</pre>
summary(m1)
##
## Call:
## lm(formula = FinalGradeCEMS ~ TimeSpent hours, data = d)
##
## Residuals:
                10 Median
       Min
                                30
                                       Max
## -67.136 -7.805
                   4.723 14.471 30.317
##
## Coefficients:
                   Estimate Std. Error t value Pr(>|t|)
##
## (Intercept)
                  65.80851
                              1.49120
                                         44.13
                                                 <2e-16
## TimeSpent_hours 0.36484
                              0.03889
                                          9.38
                                                 <2e-16 ***
## ---
## Signif. codes:
## 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 20.71 on 571 degrees of freedom
## (30 observations deleted due to missingness)
## Multiple R-squared: 0.1335, Adjusted R-squared: 0.132
## F-statistic: 87.99 on 1 and 571 DF, p-value: < 2.2e-16
```

The lm() function is the base case of using these model formulas

Making the model more complex - a multiple regression

```
m2 <- lm(FinalGradeCEMS ~ TimeSpent_hours + int + Gender, data = d)
summary(m2)</pre>
```

```
##
## Call:
## lm(formula = FinalGradeCEMS ~ TimeSpent hours + int + Gender,
      data = d
##
##
## Residuals:
               1Q Median
      Min
                               30
                                      Max
## -66.593 -7.382
                    4.761 14.534 30.618
##
## Coefficients:
                  Estimate Std. Error t value Pr(>|t|)
##
                                        9.859
                                                <2e-16 ***
## (Intercept)
                  69.61325
                              7.06075
## TimeSpent hours 0.36962
                              0.04198 8.804
                                                <2e-16 ***
## int
                  -0.99359 1.58756 -0.626
                                               0.532
                            2.06489 -0.266
                                                0.790
## GenderM
                 -0.54962
## ---
## Signif. codes:
## 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 21.03 on 499 degrees of freedom
    (100 observations deleted due to missingness)
## Multiple R-squared: 0.1375, Adjusted R-squared: 0.1323
## F-statistic: 26.51 on 3 and 499 DF, p-value: 6.362e-16
```

But other functions and packages use this as well

t-test

```
m t test <- t.test(FinalGradeCEMS ~ Gender, data = d)</pre>
m t test
##
      Welch Two Sample t-test
##
##
## data: FinalGradeCEMS by Gender
## t = -0.30379, df = 327.71, p-value = 0.7615
## alternative hypothesis: true difference in means between group F and group M is not equal to 0
## 95 percent confidence interval:
## -4.579370 3.354211
## sample estimates:
## mean in group F mean in group M
                          77.63135
##
         77.01877
ANOVA
m anova <- aov(FinalGradeCEMS ~ subject, data = d)
m anova
## Call:
     aov(formula = FinalGradeCEMS ~ subject, data = d)
##
##
## Terms:
                     subject Residuals
##
## Sum of Squares
                    13484.46 269057.23
## Deg. of Freedom
                                   568
                           4
##
## Residual standard error: 21.76447
## Estimated effects may be unbalanced
## 30 observations deleted due to missingness
```

Some packages add to this syntax too -- Multi-level model

```
library(lme4)
m5 <- lmer(FinalGradeCEMS ~ TimeSpent hours + int*Gender + (1|course id), data = d)
summary(m5)
## Linear mixed model fit by REML ['lmerMod']
## Formula:
## FinalGradeCEMS ~ TimeSpent hours + int * Gender + (1 | course id)
##
     Data: d
##
## REML criterion at convergence: 4433.8
##
## Scaled residuals:
               10 Median
      Min
                               30
                                      Max
## -3.4970 -0.4169 0.2413 0.6507 2.3171
##
## Random effects:
## Groups
                         Variance Std.Dev.
             Name
## course id (Intercept) 46.47
                                   6.817
## Residual
                         384.21
                                  19.601
## Number of obs: 503, groups: course id, 26
##
## Fixed effects:
##
                   Estimate Std. Error t value
## (Intercept)
                   74.22969
                               8.45385
                                        8.781
## TimeSpent hours 0.43078 0.04128 10.435
                   -2.84129 1.89455 -1.500
## int
## GenderM
                  -26.55507
                            13.10001 -2.027
## int:GenderM
                             3.09236
                    6.39449
                                        2.068
##
## Correlation of Fixed Effects:
              (Intr) TmSpn_ int
                                   GendrM
## TimSpnt hrs -0.239
## int
              -0.963 0.091
## GenderM
              -0.595 0.021 0.611
## int:GenderM 0.583 -0.027 -0.609 -0.989
```

Weights using lm()

```
# Adding weights
wts1 <- rnorm(n = nrow(d), mean = 0, sd = 1)
wts2 <- rnorm(n = nrow(d), mean = 0, sd = 1)
wts <- abs(wts1/wts2)
m1 wt <- lm(FinalGradeCEMS ~ TimeSpent hours, data = d, weights = wts)
summary(m1_wt)
##
## Call:
## lm(formula = FinalGradeCEMS ~ TimeSpent hours, data = d, weights = wts)
##
## Weighted Residuals:
       Min
                 10
                      Median
                                   30
                                           Max
## -286.678 -8.548
                       3.008
                               12.598 182.823
##
## Coefficients:
                  Estimate Std. Error t value Pr(>|t|)
##
                  68.98517
                              1.19727 57.619 < 2e-16 ***
## (Intercept)
## TimeSpent hours 0.30513
                              0.03885 7.853 2.02e-14 ***
## ---
## Signif. codes:
## 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 36.64 on 571 degrees of freedom
   (30 observations deleted due to missingness)
## Multiple R-squared: 0.09748, Adjusted R-squared: 0.0959
## F-statistic: 61.67 on 1 and 571 DF, p-value: 2.021e-14
```

The glm() function - the way to fit other types of regression models

glm() lets you specify distribution families for different kinds of outcomes:

- "gaussian" = standard regression for continuous dependent variables (default)
- "binomial" = binary (0/1) outcome variables
- "poisson" = count outcome variables
- several others are available

The base case with default options will be same as lm()

```
glm1 <- glm(FinalGradeCEMS ~ TimeSpent hours, data = d)</pre>
summary(glm1)
##
## Call:
## qlm(formula = FinalGradeCEMS ~ TimeSpent hours, data = d)
##
## Deviance Residuals:
       Min
                 10
                      Median
                                    3Q
                                            Max
## -67.136
             -7.805
                       4.723
                               14.471
                                         30.317
##
## Coefficients:
                   Estimate Std. Error t value Pr(>|t|)
##
## (Intercept)
                   65.80851
                               1.49120
                                         44.13
                                                  <2e-16 ***
## TimeSpent hours 0.36484
                               0.03889
                                           9.38
                                                  <2e-16 ***
## ---
## Signif. codes:
## 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
##
## (Dispersion parameter for gaussian family taken to be 428.7479)
##
       Null deviance: 282542 on 572 degrees of freedom
##
## Residual deviance: 244815 on 571 degrees of freedom
     (30 observations deleted due to missingness)
## AIC: 5103
##
## Number of Fisher Scoring iterations: 2
```

The family argument to glm() helps you change the kind of model being estimated.

```
d <- d %>%
  mutate(Points Earned Bin = ifelse(dPoints Earned > mean(dPoints Earned, na.rm = T), 1, 0))
qlm1 <- qlm(Points Earned Bin ~ TimeSpent hours, data = d, family = "binomial")</pre>
summary(glm1)
##
## Call:
## qlm(formula = Points Earned Bin ~ TimeSpent hours, family = "binomial",
       data = d
##
## Deviance Residuals:
                 10 Median
       Min
                                   30
                                           Max
## -0.6393 -0.6166 -0.5992 -0.5624
                                        2.0446
##
## Coefficients:
                    Estimate Std. Error z value Pr(>|z|)
##
## (Intercept)
                   -1.484105
                             0.199288 -7.447 9.55e-14 ***
## TimeSpent hours -0.004482 0.005535 -0.810
                                                   0.418
## ---
## Signif. codes:
## 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
##
## (Dispersion parameter for binomial family taken to be 1)
##
       Null deviance: 455.26 on 506 degrees of freedom
## Residual deviance: 454.58 on 505 degrees of freedom
    (96 observations deleted due to missingness)
## AIC: 458.58
##
## Number of Fisher Scoring iterations: 4
```

We've previously discussed making better looking output tables in .Rmd documents

library(sjPlot)
tab\_model(m1)

	Final Grade CEMS		
Predictors	Estimates	CI	р
(Intercept)	65.81	62.88 - 68.74	<0.001
TimeSpent_hours	0.36	0.29 - 0.44	<0.001
Observations	573		
R <sup>2</sup> / R <sup>2</sup> adjusted	0.134 / 0.132		

Another package makes it easier to pull out model estimates in an easier format to use for further operations: broom

tidy() Makes lm() coefficient output into a tidy data frame format, which you can then use all of your tidyverse tools on

<code>glance()</code> works similarly but with the whole model diagnostic statistics such as  $R^2$ 

```
library(broom)
# Model coefficents
tidy(m1)
## # A tibble: 2 × 5
                    estimate std.error statistic
                                                    p.value
##
    term
    <chr>
##
                        <dbl>
                                  <dbl>
                                            <dbl>
                                                      <dbl>
## 1 (Intercept)
                      65.8
                                 1.49
                                           44.1 3.71e-186
## 2 TimeSpent hours
                                             9.38 1.53e- 19
                       0.365
                                 0.0389
# whole model stats
glance(m1)
## # A tibble: 1 × 12
    r.squared adj.r.squared sigma statistic p.value
                                                <dbl> <dbl>
##
         <dbl>
                       <dbl> <dbl>
                                       <dbl>
                      0.132 20.7
## 1
         0.134
                                        88.0 1.53e-19
                                                          1
## # ... with 6 more variables: logLik <dbl>, AIC <dbl>,
      BIC <dbl>, deviance <dbl>, df.residual <int>,
      nobs <int>
## #
```

broom can also help you grab other diagnostics from the model with augment()

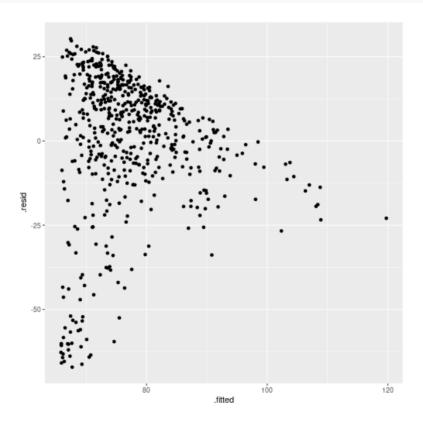
```
# Data level additional model generated values
head(augment(m1))
```

```
## # A tibble: 6 × 9
     .rownames FinalGradeCEMS TimeSpent_hours .fitted .resid
                                        <dbl>
##
     <chr>
                        <dbl>
                                                <dbl> <dbl>
                                         25.9
                         93.5
                                                 75.3 18.2
## 1 1
                         81.7
                                         23.0
## 2 2
                                                 74.2
                                                       7.49
## 3 3
                         88.5
                                         14.3
                                                 71.0 17.4
                                         26.6
                                                 75.5
                                                       6.32
## 4 4
                         81.9
## 5 5
                         84
                                         24.7
                                                 74.8
                                                       9.18
                         83.6
                                         22.0
                                                 73.8
## 6 7
                                                        9.74
## # ... with 4 more variables: .hat <dbl>, .sigma <dbl>,
       .cooksd <dbl>, .std.resid <dbl>
```

broom can also help you grab other diagnostics from the model

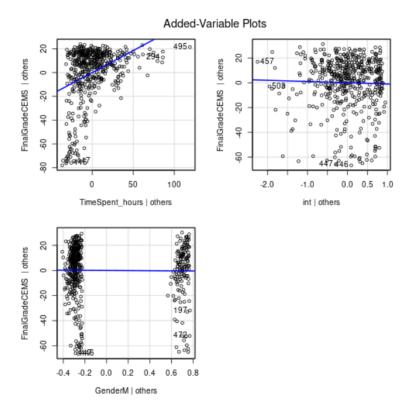
```
f <- augment(m1)

ggplot(f) +
  geom_point(aes(x=.fitted, y=.resid))</pre>
```



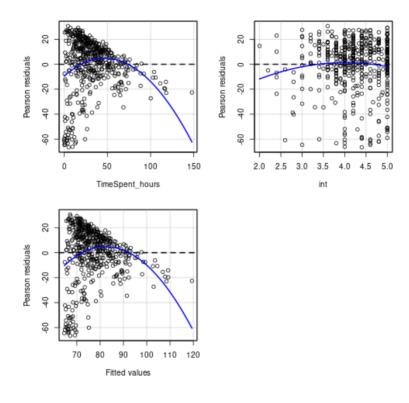
The car package has plotting and testing functions that can help you evaluate models

library(car)
avPlots(m2)



The car package has plotting and testing functions that can help you evaluate models

residualPlots(m2)



The report package can generate written summaries of the results of your models

```
#devtools::install_github("https://github.com/easystats/report")
library(report)
report(m1)

## We fitted a linear model (estimated using OLS) to predict FinalGradeCEMS with TimeSpent_hours (formula: Fin ##

## - The effect of TimeSpent_hours is statistically significant and positive (beta = 0.36, 95% CI [0.29, 0.4 ##

## Standardized parameters were obtained by fitting the model on a standardized version of the dataset.
```

Components of an lm() object, some of which you can get with helper functions

```
## (Intercept) TimeSpent_hours
## 65.8085094 0.3648365

head(m1$residuals)

## 1 2 3 4 5 7
## 18.188854 7.485674 17.447115 6.323524 9.181244 9.742307
```

There are a number of helper functions that work with lm and other models

```
# model coefficients
coef(m1)
       (Intercept) TimeSpent_hours
       65.8085094
##
                         0.3648365
# model residuals
head(residuals(m1))
##
## 18.188854 7.485674 17.447115 6.323524 9.181244 9.742307
# regression fitted values
head(fitted(m1))
##
## 75.26487 74.21617 71.04047 75.52907 74.81876 73.84596
# Get the data used to fit the model
head(model.frame(m1))
     FinalGradeCEMS TimeSpent hours
## 1
           93.45372
                           25.91944
## 2
           81.70184
                           23.04500
           88.48758
                           14.34056
## 3
           81.85260
## 4
                           26.64361
## 5
           84.00000
                           24.69667
## 7
           83.58827
                           22.03027
```

There are a number of helper functions that work with lm and other models - How do we know which ones?

```
library(sloop)
s3 methods class("lm")
## # A tibble: 86 × 4
                    class visible source
     generic
     <chr>
                    <chr> <lql>
##
                                  <chr>
   1 add1
                          FALSE
                                  registered S3method
                    lm
## 2 alias
                          FALSE
                                 registered S3method
                    lm
                          FALSE
                                 registered S3method
## 3 anova
                    lm
                          FALSE
## 4 Anova
                                  registered S3method
## 5 as.data.frame lm
                          FALSE
                                  registered S3method
                          FALSE
   6 augment
                                  registered S3method
                    lm
## 7 avPlot
                          FALSE
                                  registered S3method
                    lm
                          FALSE
                                  registered S3method
## 8 Boot
                    lm
## 9 bootCase
                          FALSE
                                  registered S3method
                    lm
                                  registered S3method
## 10 boxCox
                    lm
                          FALSE
## # ... with 76 more rows
confint(m1)
##
                        2.5 %
                                 97.5 %
## (Intercept)
                   62.8796038 68.737415
## TimeSpent hours 0.2884451 0.441228
vcov(m1)
                   (Intercept) TimeSpent hours
##
## (Intercept)
                    2.22367608
                                  -0.047242592
## TimeSpent hours -0.04724259
                                   0.001512691
```

The lmSupport package provides number of additional tools for regression models

```
library(lmSupport)
m1 <- lm(FinalGradeCEMS ~ TimeSpent hours, data = d)</pre>
m2 <- lm(FinalGradeCEMS ~ TimeSpent hours + int + Gender, data = d)
# A function to check regression model assumptions
modelAssumptions(m1)
## Descriptive Statistics for Studentized Residuals
##
## Call:
## lm(formula = FinalGradeCEMS ~ TimeSpent hours, data = d)
##
## Coefficients:
       (Intercept)
                    TimeSpent hours
##
           65.8085
                              0.3648
##
##
## ASSESSMENT OF THE LINEAR MODEL ASSUMPTIONS
## USING THE GLOBAL TEST ON 4 DEGREES-OF-FREEDOM:
## Level of Significance = 0.05
##
## Call:
## gvlma(x = Model)
##
                               p-value
##
                       Value
## Global Stat
                      313.26 0.000e+00
## Skewness
                      182.13 0.000e+00
## Kurtosis
                       69.89 1.110e-16
## Link Function
                       40.33 2.143e-10
## Heteroscedasticity 20.91 4.820e-06
##
                                         Decision
## Global Stat
                      Assumptions NOT satisfied!
## Skewness
                      Assumptions NOT satisfied!
## Kurtosis
                      Assumptions NOT satisfied!
                      Assumptions NOT satisfied!
## Link Function
## Heteroscedasticity Assumptions NOT satisfied!
```

The lmSupport package provides number of additional tools for regression models

```
m2 <- lm(FinalGradeCEMS ~ TimeSpent_hours + int + Gender, data = d)
m1 <- lm(FinalGradeCEMS ~ TimeSpent_hours, data = model.frame(m2$model))
# F Test difference between 2 models
modelCompare(m1, m2)

## SSE (Compact) = 220820.1
## SSE (Augmented) = 220624.9
## Delta R-Squared = 0.0007632935
## Partial Eta-Squared (PRE) = 0.0008841496
## F(2,499) = 0.2207905, p = 0.8019629</pre>
```

## D. Shiny Continued

#### Storms App Additional Features

Fixing the multiple hurricanes issue

Adding a zoom slider

Adding Color

Data table under plot

# Addendum: Other modeling packages to be aware of

- lme4 and nlme: hierarchical linear models (aka multilevel models)
- lavaan: structural equation models
- MASS: Robust regression
- caret: Lots of different classification and regression models for machine learning applications
- parsnip: (tidyverse) Unified interface to many different models, largely machine learning type
- Time series: <a href="https://cran.r-project.org/web/views/TimeSeries.html">https://cran.r-project.org/web/views/TimeSeries.html</a>

Other types of models that may be more applicable to your field can also be found in the CRAN task views: <a href="https://cran.r-project.org/web/views/">https://cran.r-project.org/web/views/</a>

Tutorials for many different varieties of Regression can be found here: <a href="https://stats.idre.ucla.edu/other/dae/">https://stats.idre.ucla.edu/other/dae/</a>

Other packages that can help you with your models <a href="https://easystats.github.io/easystats/">https://easystats.github.io/easystats/</a> e.g. the <a href="performance">performance</a> package does model assumption checking and model comparison

# Logistics

#### This week

- Homework 8: Available tomorrow, Due next Tuesday
- Reading: \* <a href="https://www.tmwr.org/base-r.html#formula">https://www.tmwr.org/base-r.html#formula</a>

# Assignment updates

- <u>Final project</u>
  - NEXT Thursday Give updated version of your idea

### Wrapping up

#### On Slack channel:

- What is one thing you learned today?What is something you want to learn more about?Share your feelings in GIF form!