

Let  $X_1, \dots, X_n$  iid r.v.'s  $\sim U(0, \theta)$  but actually  $\theta = 3$ .

i) Generate random numbers from true dist. i.e.  $U(0, 3)$ . ( $N=100000/n$  simulations)

ii) For  $n=10, 30, 50$  and  $100$  (may be  $200$  also)

Find the values of MLE estimator of  $\theta$ .

iii) check the dist. of MLE estimator  $\hat{\theta}$  of  $\theta$ , is it BAN?

iv) check unbiasedness and consistency properties of  $\hat{\theta}$ .