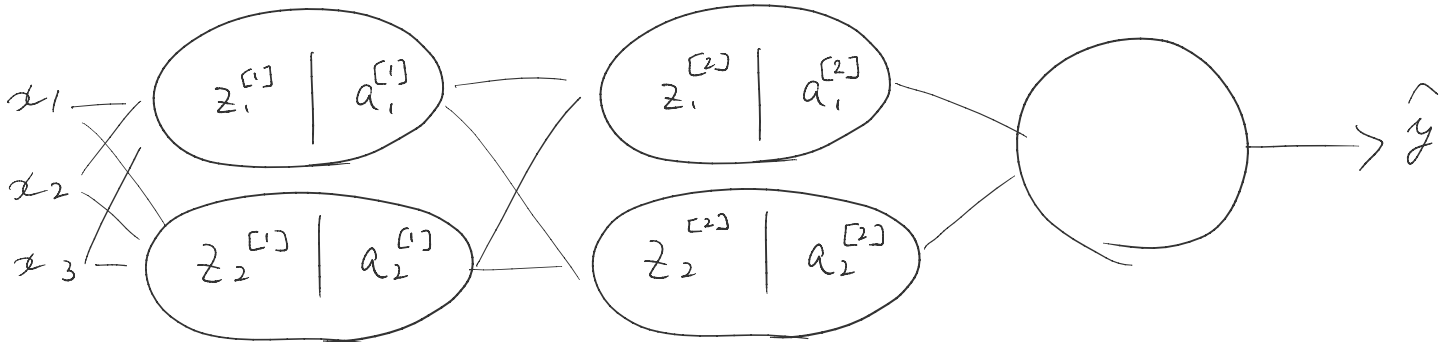


Batch Norm



$$X \xrightarrow{w^{[1]}, b^{[1]}} z^{[1]} \xrightarrow[\text{Batch Norm (BN)}]{\beta^{[1]}, \gamma^{[1]}} \tilde{z}^{[1]} \xrightarrow{a^{[1]} = g^{[1]}(\tilde{z}^{[1]})} z^{[2]} \dots$$

$$\text{Params} : \left. \begin{matrix} w^{[1]}, b^{[1]}, \dots, w^{[L]}, b^{[L]} \\ \beta^{[1]}, \gamma^{[1]}, \dots, \beta^{[L]}, \gamma^{[L]} \end{matrix} \right\} d\beta^{[L]} \quad \beta^{[L]} := \beta^{[L]} - \alpha d\beta^{[L]}$$

Softmax

$$\left\{ \begin{array}{l} x = e^{z^{[L]}} \\ a^{[L]} = \frac{e^{z^{[L]}}}{\sum_{i=1}^{n_L} x_i} \end{array} \right. \quad (n_L, 1)$$

Softmax.

$$\text{例 } z = \begin{bmatrix} 5 \\ 2 \\ -1 \\ 3 \end{bmatrix}$$

$$x = \begin{bmatrix} e^5 \\ e^2 \\ e^{-1} \\ e^3 \end{bmatrix} = \begin{bmatrix} 148.4 \\ 7.4 \\ 0.4 \\ 20.1 \end{bmatrix}$$

$$\sum_{i=1}^4 x_i = 176.3$$

$$a = \frac{x}{176.3} = \begin{bmatrix} 0.842 \\ 0.042 \\ 0.002 \\ 0.114 \end{bmatrix} \quad \left. \vphantom{\frac{x}{176.3}} \right\} 1$$