

**Experimental numerical results of the paper: A
Perry-type derivative-free algorithm for solving
convex constrained nonlinear monotone equations
and minimizing ℓ_1 regularized problem.
Submitted to Optimization**

The following tables contain the numerical experimental results of the paper titled "A Perry-type derivative-free algorithm for solving convex constrained nonlinear monotone equations and minimizing ℓ_1 regularized problem" by A. M. Awwal, P. Kumam, H. Mohammad, W. Watthayu and A. B. Abubakar.

Tables 1–4 contain the numerical results for general nonlinear equations 5.1.1–5.1.7 while tables 5–13 contain the numerical results for monotone nonlinear equations 5.2.1–5.2.10.

Table 1: Numerical results for problems 5.1.1 and 5.1.2

| Problem | DIM | DPP | | | | | MPD | | | | LSQNONLIN | | | |
|---------|------|-----|------|------|---------|----------|------|------|--------|----------|-----------|--------|----------|----------|
| | | IP | ITER | FVAL | TIME | NORM | ITER | FVAL | TIME | NORM | ITER | FVAL | TIME | NORM |
| 5.1.1 | 1000 | x1 | 422 | 845 | 0.6254 | 9.94E-07 | - | - | - | - | 13 | 140014 | 1.0406 | 1.30E-11 |
| | | x2 | 646 | 1293 | 1.9086 | 9.8E-07 | - | - | - | - | 15 | 16016 | 1.2815 | 9.61E-11 |
| | | x3 | 545 | 1091 | 0.5862 | 9.92E-07 | - | - | - | - | 15 | 16016 | 1.2442 | 1.62E-13 |
| | | x4 | 849 | 1699 | 2.3312 | 9.71E-07 | - | - | - | - | 18 | 19019 | 1.4558 | 4.42E-10 |
| | | x5 | 916 | 1833 | 1.8609 | 9.65E-07 | - | - | - | - | 10 | 11011 | 0.9140 | 1.72E-09 |
| | | x6 | 466 | 933 | 0.7681 | 9.94E-07 | - | - | - | - | 6 | 7007 | 0.5468 | 2.24E-11 |
| | | x7 | 520 | 1041 | 1.4007 | 9.14E-07 | - | - | - | - | 14 | 15015 | 1.2059 | 7.13E-10 |
| | | x9 | 458 | 917 | 1.0327 | 9.55E-07 | - | - | - | - | 7 | 8008 | 0.6124 | 1.30E-07 |
| | | x10 | 447 | 895 | 0.5158 | 9.88E-07 | - | - | - | - | 7 | 8008 | 1.4998 | 6.52E-08 |
| | | x11 | 385 | 771 | 0.4513 | 9.08E-07 | - | - | - | - | - | - | - | - |
| | | x12 | 536 | 1073 | 1.4636 | 9.28E-07 | - | - | - | - | - | - | - | - |
| | | x13 | 637 | 1275 | 0.6998 | 4.91E-07 | - | - | - | - | 9 | 10010 | 0.8008 | 1.09E-10 |
| | | x14 | 420 | 841 | 0.7197 | 5.94E-07 | - | - | - | - | 14 | 15015 | 1.1930 | 1.70E-09 |
| | | x15 | 488 | 977 | 0.55751 | 8.05E-07 | - | - | - | - | 26 | 27027 | 1.0801 | 1.56E-07 |
| | 5000 | x1 | 466 | 933 | 4.2844 | 6.52E-07 | - | - | - | - | 10 | 55011 | 20.0229 | 2.70E-10 |
| | | x2 | 531 | 1063 | 4.1997 | 9.76E-07 | - | - | - | - | 16 | 85017 | 32.2950 | 3.35E-10 |
| | | x3 | 759 | 1519 | 8.4600 | 9.94E-07 | - | - | - | - | 13 | 70014 | 28.3132 | 3.20E-09 |
| | | x4 | 712 | 1425 | 6.3864 | 9.37E-07 | - | - | - | - | 17 | 90018 | 33.2679 | 1.64E-09 |
| | | x5 | 516 | 1033 | 3.8582 | 9.83E-07 | - | - | - | - | 13 | 70014 | 25.4307 | 1.82E-12 |
| | | x6 | 440 | 881 | 3.2306 | 9.41E-07 | - | - | - | - | 6 | 35007 | 13.1260 | 2.64E-07 |
| | | x7 | 720 | 1441 | 6.6270 | 9.58E-07 | - | - | - | - | 15 | 80016 | 31.3672 | 1.20E-09 |
| | | x9 | 407 | 815 | 4.4749 | 9.96E-07 | - | - | - | - | 8 | 45009 | 14.8810 | 1.24E-09 |
| | | x10 | 333 | 667 | 3.2233 | 6.64E-07 | - | - | - | - | 6 | 35007 | 12.4793 | 2.14E-08 |
| | | x11 | 332 | 665 | 3.0836 | 8.77E-07 | - | - | - | - | - | - | - | - |
| | | x12 | 513 | 1027 | 5.1906 | 9.37E-07 | - | - | - | - | - | - | - | - |
| | | x13 | 498 | 997 | 4.0878 | 9.56E-07 | - | - | - | - | - | - | - | - |
| | | x14 | 392 | 785 | 3.0830 | 9.91E-07 | - | - | - | - | - | - | - | - |
| | | x15 | 404 | 809 | 2.1516 | 9.53E-07 | - | - | - | - | 41 | 210042 | 27.0551 | 6.03E-11 |
| 5.1.2 | 1000 | x1 | 475 | 951 | 1.5427 | 9.69E-07 | - | - | - | - | 8 | 9009 | 1.2899 | 4.15E-09 |
| | | x2 | 457 | 915 | 0.7763 | 8.1E-07 | - | - | - | - | 20 | 21021 | 2.1792 | 1.97E-11 |
| | | x3 | 556 | 1113 | 1.3289 | 8.42E-07 | 968 | 1937 | 1.2227 | 9.47E-07 | 18 | 19019 | 1.8844 | 1.40E-11 |
| | | x4 | 660 | 1321 | 1.5753 | 9.9E-07 | 970 | 1941 | 2.2063 | 6.9E-07 | 17 | 18018 | 1.8523 | 3.63E-08 |
| | | x5 | 638 | 1277 | 1.9164 | 9.85E-07 | - | - | - | - | 11 | 12012 | 1.2107 | 7.75E-10 |
| | | x6 | 529 | 1059 | 1.6887 | 9.83E-07 | 600 | 1201 | 0.7557 | 7.42E-07 | 6 | 7007 | 0.7255 | 8.02E-11 |
| | | x7 | 596 | 1193 | 1.5967 | 9.2E-07 | - | - | - | - | 25 | 26026 | 2.6066 | 1.64E-07 |
| | | x9 | 532 | 1065 | 1.4394 | 9.05E-07 | - | - | - | - | 8 | 7007 | 0.8060 | 5.29E-07 |
| | | x10 | 491 | 983 | 1.3261 | 9.56E-07 | 806 | 1613 | 1.0458 | 5.38E-07 | 7 | 8008 | 0.8046 | 7.73E-08 |
| | | x11 | 350 | 701 | 0.9660 | 9.53E-07 | - | - | - | - | - | - | - | - |
| | | x12 | 559 | 1119 | 1.1710 | 8.29E-07 | 824 | 1649 | 1.4994 | 6.2E-07 | 10 | 11011 | 1.1084 | 3.56E-07 |
| | | x13 | 412 | 825 | 1.6665 | 9.04E-07 | 815 | 1631 | 1.1767 | 9.94E-07 | 9 | 10010 | 1.0299 | 7.64E-10 |
| | | x14 | 512 | 1025 | 1.2701 | 8.41E-07 | 816 | 1633 | 1.9014 | 8.83E-07 | - | - | - | - |
| | | x15 | 507 | 1015 | 0.78963 | 8.99E-07 | - | - | - | - | 33 | 34034 | 1.2013 | 7.59E-13 |
| | 5000 | x1 | 476 | 953 | 7.2773 | 9.38E-07 | 865 | 1731 | 8.3414 | 5.22E-07 | 10 | 55011 | 36.1470 | 6.36E-09 |
| | | x2 | 586 | 1173 | 7.3841 | 8.11E-07 | - | - | - | - | 23 | 120024 | 74.8632 | 1.70E-10 |
| | | x3 | 596 | 1193 | 7.8625 | 9.65E-07 | - | - | - | - | 19 | 100020 | 60.7995 | 7.34E-09 |
| | | x4 | 702 | 1405 | 8.6168 | 9.65E-07 | 995 | 1991 | 7.8182 | 6.59E-07 | 15 | 80016 | 47.4654 | 2.97E-07 |
| | | x5 | 665 | 1331 | 8.0973 | 8.4E-07 | - | - | - | - | 16 | 85017 | 50.2866 | 4.76E-12 |
| | | x6 | 511 | 1023 | 5.6933 | 9.6E-07 | 624 | 1249 | 5.5355 | 5.75E-07 | 6 | 35007 | 16.5406 | 2.33E-07 |
| | | x7 | 586 | 1173 | 6.0457 | 9.57E-07 | - | - | - | - | - | - | - | - |
| | | x9 | 533 | 1067 | 6.8590 | 9.58E-07 | - | - | - | - | 8 | 45009 | 22.2349 | 1.85E-09 |
| | | x10 | 500 | 1001 | 5.2751 | 9.85E-07 | 790 | 1581 | 6.0865 | 5.75E-07 | 6 | 35007 | 16.5315 | 1.97E-07 |
| | | x11 | 362 | 725 | 3.9470 | 9.07E-07 | 650 | 1301 | 5.0070 | 7.82E-07 | 25 | 130026 | 72.2535 | 2.06E-09 |
| | | x12 | 485 | 971 | 5.1688 | 3.27E-07 | 803 | 1607 | 6.3100 | 6.97E-07 | 11 | 60012 | 31.6845 | 3.16E-08 |
| | | x13 | 499 | 999 | 4.7399 | 9.12E-07 | - | - | - | - | - | - | - | - |
| | | x14 | 529 | 1059 | 6.2710 | 9.27E-07 | 840 | 1681 | 6.3684 | 6.96E-07 | 37 | 190038 | 107.6571 | 2.02E-08 |
| | | x15 | 467 | 935 | 3.9788 | 9.28E-07 | 874 | 1749 | 5.3678 | 7.53E-07 | 14 | 75015 | 71.0122 | 2.05E+13 |

Table 2: Numerical results for problems 5.1.3 and 5.1.4

| DPP | | | | | | | | | | | | | | | MPD | | | | | LSQNONLIN | | | | |
|---------|------|-----|------|------|----------|----------|------|------|----------|----------|------|-------|----------|----------|-----|--|--|--|--|-----------|--|--|--|--|
| Problem | DIM | IP | ITER | FVAL | TIME | NORM | ITER | FVAL | TIME | NORM | ITER | FVAL | TIME | NORM | | | | | | | | | | |
| 5.1.3 | 1000 | x1 | 30 | 61 | 1.3230 | 5.42E-07 | 143 | 287 | 4.3716 | 9.06E-07 | 4 | 5005 | 10.3934 | 1.89E-12 | | | | | | | | | | |
| | | x2 | 46 | 93 | 3.4917 | 3.93E-07 | 116 | 233 | 3.6699 | 9.53E-07 | 14 | 15015 | 32.2641 | 2.91E-08 | | | | | | | | | | |
| | | x3 | 39 | 79 | 2.9297 | 6.4E-07 | 120 | 241 | 4.5149 | 8.29E-07 | 7 | 8008 | 15.9070 | 1.42E-08 | | | | | | | | | | |
| | | x4 | 34 | 69 | 1.3477 | 7.84E-07 | 169 | 339 | 7.1546 | 9.73E-07 | 7 | 10010 | 19.8610 | 1.21E-12 | | | | | | | | | | |
| | | x5 | 45 | 91 | 3.6360 | 3.34E-07 | 162 | 325 | 3.4402 | 9.49E-07 | 6 | 7007 | 12.9047 | 1.44E-13 | | | | | | | | | | |
| | | x6 | 49 | 99 | 3.9800 | 7.11E-07 | 104 | 209 | 2.9332 | 9.52E-07 | 7 | 8008 | 15.7993 | 5.27E-08 | | | | | | | | | | |
| | | x7 | 46 | 93 | 3.7980 | 8.1E-07 | 177 | 355 | 4.5541 | 9.56E-07 | 13 | 14014 | 27.2606 | 2.15E-07 | | | | | | | | | | |
| | | x8 | 32 | 65 | 4.6242 | 3.26E-07 | 183 | 367 | 4.0275 | 9.99E-07 | 6 | 7007 | 13.7751 | 6.09E-07 | | | | | | | | | | |
| | | x9 | 34 | 69 | 1.9857 | 5.34E-07 | 83 | 167 | 2.0925 | 9.08E-07 | 8 | 9009 | 17.8692 | 1.37E-08 | | | | | | | | | | |
| | | x10 | 28 | 57 | 1.7806 | 4.75E-07 | 168 | 337 | 6.8842 | 9.5E-07 | 5 | 6006 | 11.2337 | 5.64E-08 | | | | | | | | | | |
| | | x11 | 28 | 57 | 3.2888 | 3.99E-07 | 102 | 205 | 3.6440 | 6.44E-07 | 6 | 7007 | 12.7857 | 3.79E-10 | | | | | | | | | | |
| | | x12 | 57 | 115 | 3.8454 | 5.56E-07 | 196 | 393 | 5.2430 | 9.1E-07 | 10 | 11011 | 20.8603 | 2.53E-08 | | | | | | | | | | |
| | | x13 | 26 | 53 | 2.1978 | 2.61E-07 | 87 | 175 | 2.9585 | 6.75E-07 | 4 | 5005 | 9.1988 | 3.92E-10 | | | | | | | | | | |
| | | x14 | 23 | 47 | 1.6613 | 9.12E-07 | 83 | 167 | 2.8920 | 7.17E-07 | 7 | 8008 | 14.5198 | 7.07E-07 | | | | | | | | | | |
| | | x15 | 49 | 99 | 1.724 | 2.85E-07 | 118 | 237 | 2.4933 | 9.87E-07 | 7 | 8008 | 13.2411 | 3.81E-10 | | | | | | | | | | |
| | 5000 | x1 | 28 | 57 | 10.7954 | 4.83E-07 | 131 | 263 | 21.2707 | 9.39E-07 | 4 | 25005 | 228.2259 | 1.89E-12 | | | | | | | | | | |
| | | x2 | 94 | 189 | 36.5803 | 8.33E-07 | 153 | 307 | 25.8935 | 8.94E-07 | 15 | 80016 | 721.2084 | 1.44E-07 | | | | | | | | | | |
| | | x3 | 67 | 135 | 19.5590 | 2.58E-07 | 132 | 265 | 24.4659 | 7.94E-07 | 8 | 45009 | 407.8396 | 8.65E-10 | | | | | | | | | | |
| | | x4 | 30 | 61 | 6.7214 | 5.23E-07 | 151 | 303 | 27.1983 | 9.49E-07 | 10 | 55011 | 545.5740 | 2.37E-13 | | | | | | | | | | |
| | | x5 | 52 | 105 | 11.8423 | 3.55E-07 | 116 | 233 | 17.2172 | 9.66E-07 | 6 | 35007 | 347.4983 | 9.60E-08 | | | | | | | | | | |
| | | x6 | 85 | 171 | 26.7619 | 9.18E-07 | 187 | 375 | 24.1148 | 9.73E-07 | 8 | 45009 | 453.3148 | 5.35E-09 | | | | | | | | | | |
| | | x7 | 52 | 105 | 13.8590 | 7.62E-07 | 105 | 211 | 15.7544 | 8.76E-07 | 15 | 80016 | 920.7487 | 9.94E-14 | | | | | | | | | | |
| | | x8 | 32 | 65 | 6.8817 | 9.12E-07 | 169 | 339 | 20.3689 | 9.11E-07 | 7 | 40008 | 442.9817 | 5.56E-08 | | | | | | | | | | |
| | | x9 | 43 | 87 | 9.7835 | 3.65E-07 | 120 | 241 | 17.0023 | 7.55E-07 | 9 | 50010 | 541.5937 | 5.67E-09 | | | | | | | | | | |
| | | x10 | 31 | 63 | 8.5254 | 8.93E-07 | 165 | 331 | 20.0570 | 9.99E-07 | 6 | 35007 | 421.9235 | 3.67E-12 | | | | | | | | | | |
| | | x11 | 25 | 51 | 6.0765 | 8.06E-07 | 171 | 343 | 23.7837 | 9.83E-07 | 7 | 40008 | 434.6823 | 4.64E-13 | | | | | | | | | | |
| | | x12 | 119 | 239 | 43.6141 | 5.85E-07 | 117 | 235 | 20.8932 | 9.81E-07 | 11 | 60012 | 732.2555 | 1.63E-08 | | | | | | | | | | |
| | | x13 | 25 | 51 | 6.2327 | 5.57E-07 | 76 | 153 | 7.4901 | 8.54E-07 | 5 | 30006 | 332.2781 | 2.50E-14 | | | | | | | | | | |
| | | x14 | 27 | 55 | 6.4885 | 9.25E-07 | 169 | 339 | 24.2997 | 9.87E-07 | 8 | 45009 | 519.3971 | 2.70E-08 | | | | | | | | | | |
| | | x15 | 50 | 101 | 8.381 | 3.15E-07 | 118 | 237 | 12.4321 | 7.09E-07 | 8 | 45009 | 511.2201 | 2.71E-12 | | | | | | | | | | |
| 5.1.4 | 1000 | x1 | 12 | 25 | 0.0255 | 9.41E-07 | 27 | 55 | 0.0138 | 6.39E-07 | 5 | 6006 | 0.5721 | 5.37E-14 | | | | | | | | | | |
| | | x2 | 13 | 27 | 0.0517 | 9.55E-07 | 29 | 59 | 0.0155 | 5.46E-07 | 6 | 7007 | 0.6249 | 9.75E-12 | | | | | | | | | | |
| | | x3 | 13 | 27 | 0.0180 | 5.02E-07 | 28 | 57 | 0.0177 | 5.55E-07 | 5 | 6006 | 0.5204 | 1.99E-12 | | | | | | | | | | |
| | | x4 | 18 | 37 | 0.0295 | 3.24E-07 | 24 | 49 | 0.0150 | 5.35E-07 | 6 | 7007 | 0.6463 | 2.04E-13 | | | | | | | | | | |
| | | x5 | 13 | 27 | 0.0172 | 3.95E-07 | 27 | 55 | 0.0130 | 8.75E-07 | 5 | 6006 | 0.5336 | 7.11E-13 | | | | | | | | | | |
| | | x6 | 12 | 25 | 0.0719 | 4.2E-07 | 26 | 53 | 0.0132 | 5.73E-07 | 3 | 4004 | 0.3701 | 8.91E-07 | | | | | | | | | | |
| | | x7 | 13 | 27 | 0.0565 | 7.53E-07 | 28 | 57 | 0.0258 | 8.56E-07 | 6 | 7007 | 0.6183 | 3.38E-12 | | | | | | | | | | |
| | | x8 | 12 | 25 | 0.1002 | 5.93E-07 | 26 | 53 | 0.0308 | 8.08E-07 | 4 | 5005 | 0.4197 | 1.20E-13 | | | | | | | | | | |
| | | x9 | 11 | 23 | 0.0154 | 8.09E-07 | 25 | 51 | 0.0277 | 6.76E-07 | 3 | 4004 | 0.3425 | 3.55E-14 | | | | | | | | | | |
| | | x10 | 12 | 25 | 0.0140 | 7.67E-07 | 27 | 55 | 0.0149 | 5.22E-07 | 4 | 5005 | 0.4534 | 3.93E-13 | | | | | | | | | | |
| | | x11 | 12 | 25 | 0.0150 | 7.74E-07 | 27 | 55 | 0.0128 | 5.26E-07 | 4 | 5005 | 0.4346 | 1.34E-12 | | | | | | | | | | |
| | | x12 | 12 | 25 | 0.0147 | 4.39E-07 | 26 | 53 | 0.0160 | 6.03E-07 | 4 | 5005 | 0.4283 | 2.22E-14 | | | | | | | | | | |
| | | x13 | 12 | 25 | 0.0257 | 9.06E-07 | 27 | 55 | 0.0136 | 6.16E-07 | 5 | 6006 | 0.5375 | 3.29E-14 | | | | | | | | | | |
| | | x14 | 12 | 25 | 0.0163 | 5.65E-07 | 26 | 53 | 0.0138 | 7.69E-07 | 4 | 5005 | 0.4555 | 5.19E-13 | | | | | | | | | | |
| | | x15 | 13 | 27 | 0.009719 | 3.06E-07 | 27 | 55 | 0.011096 | 6.8E-07 | 5 | 6006 | 0.6521 | 2.66E-13 | | | | | | | | | | |
| | 5000 | x1 | 13 | 27 | 0.0655 | 6.46E-07 | 28 | 57 | 0.0791 | 7.16E-07 | 5 | 30006 | 10.5951 | 1.82E-07 | | | | | | | | | | |
| | | x2 | 14 | 29 | 0.1470 | 6.74E-07 | 30 | 61 | 0.0614 | 6.11E-07 | 7 | 40008 | 14.0736 | 1.30E-11 | | | | | | | | | | |
| | | x3 | 14 | 29 | 0.1568 | 3.43E-07 | 29 | 59 | 0.1371 | 6.21E-07 | 6 | 35007 | 12.4250 | 8.39E-14 | | | | | | | | | | |
| | | x4 | 18 | 37 | 0.1909 | 7.21E-07 | 24 | 49 | 0.1121 | 5.36E-07 | 6 | 35007 | 12.3974 | 9.59E-07 | | | | | | | | | | |
| | | x5 | 13 | 27 | 0.0859 | 8.84E-07 | 28 | 57 | 0.1447 | 9.79E-07 | 6 | 35007 | 11.6380 | 5.20E-14 | | | | | | | | | | |
| | | x6 | 12 | 25 | 0.0534 | 9.46E-07 | 27 | 55 | 0.0690 | 6.42E-07 | 4 | 25005 | 8.2832 | 3.30E-08 | | | | | | | | | | |
| | | x7 | 14 | 29 | 0.1798 | 5.29E-07 | 29 | 59 | 0.0678 | 9.59E-07 | 7 | 40008 | 13.2578 | 4.63E-12 | | | | | | | | | | |
| | | x8 | 13 | 27 | 0.0624 | 4.08E-07 | 27 | 55 | 0.0850 | 9.05E-07 | 4 | 25005 | 8.3649 | 2.71E-07 | | | | | | | | | | |
| | | x9 | 12 | 25 | 0.0540 | 5.58E-07 | 26 | 53 | 0.0507 | 7.57E-07 | 3 | 20004 | 6.5951 | 4.70E-08 | | | | | | | | | | |
| | | x10 | 13 | 27 | 0.1295 | 5.27E-07 | 28 | 57 | 0.0782 | 5.84E-07 | 5 | 30006 | 9.9280 | 6.66E-15 | | | | | | | | | | |
| | | x11 | 13 | 27 | 0.2050 | 5.32E-07 | 28 | 57 | 0.1010 | 5.89E-07 | 5 | 30006 | 9.7382 | 4.89E-14 | | | | | | | | | | |
| | | x12 | 12 | 25 | 0.1176 | 9.95E-07 | 27 | 55 | 0.1651 | 6.75E-07 | 4 | 25005 | 8.3623 | 8.60E-07 | | | | | | | | | | |
| | | x13 | 13 | 27 | 0.0597 | 6.22E-07 | 28 | 57 | 0.1289 | 6.9E-07 | 7 | 35006 | 11.5420 | 4.44E-15 | | | | | | | | | | |
| | | x14 | 13 | 27 | 0.1074 | 3.89E-07 | 27 | 55 | 0.1301 | 8.62E-07 | 4 | 25005 | 8.1616 | 6.63E-07 | | | | | | | | | | |
| | | x15 | 13 | 27 | 0.049022 | 6.88E-07 | 28 | 57 | 0.065137 | 7.63E-07 | 5 | 30006 | 10.2896 | 3.66E-07 | | | | | | | | | | |

Table 3: Numerical results for problems 5.1.5 and 5.1.6

| | | | | DPP | | | | MPD | | | | LSQNONLIN | | | | |
|---------|------|------|------|------|----------|----------|----------|------|----------|----------|----------|-----------|---------|----------|----------|----------|
| Problem | DIM | IP | ITER | FVAL | TIME | NORM | ITER | FVAL | TIME | NORM | ITER | FVAL | TIME | NORM | | |
| 5.1.5 | 1000 | x1 | 17 | 35 | 0.0146 | 8.09E-07 | 26 | 53 | 0.0126 | 8.91E-07 | 2 | 3003 | 0.2503 | 3.84E-10 | | |
| | | x2 | - | - | - | - | - | 93 | 187 | 0.8534 | 8.82E-07 | - | - | - | - | |
| | | x3 | 35 | 71 | 0.0662 | 9.86E-07 | 57 | 115 | 0.1719 | 6.63E-07 | 12 | 13013 | 1.1547 | 1.78E-15 | | |
| | | x4 | 35 | 71 | 0.0355 | 9.22E-07 | 71 | 143 | 0.2575 | 6.69E-07 | 22 | 23023 | 2.0100 | 1.72E-15 | | |
| | | x5 | 32 | 65 | 0.0279 | 5.54E-07 | 39 | 79 | 0.0314 | 7.49E-07 | 4 | 5005 | 0.4438 | 4.42E-14 | | |
| | | x6 | 43 | 87 | 0.0661 | 7.29E-07 | 144 | 289 | 0.2051 | 8.42E-07 | 7 | 8008 | 0.7162 | 6.30E-09 | | |
| | | x7 | 38 | 77 | 0.0863 | 9.39E-07 | 72 | 145 | 0.1630 | 8.8E-07 | 92 | 93093 | 8.1511 | 2.44E-09 | | |
| | | x8 | 32 | 65 | 0.0710 | 8.47E-07 | 39 | 79 | 0.0323 | 8.37E-07 | 4 | 5005 | 0.4116 | 1.21E-11 | | |
| | | x9 | 37 | 75 | 0.0516 | 9.5E-07 | 61 | 123 | 0.2147 | 7.45E-07 | 12 | 13013 | 1.1359 | 2.46E-09 | | |
| | | x10 | 30 | 61 | 0.0373 | 5.33E-07 | 39 | 79 | 0.0689 | 9.57E-07 | 3 | 4004 | 0.3614 | 4.24E-11 | | |
| | | x11 | 31 | 63 | 0.0654 | 8.08E-07 | 40 | 81 | 0.0688 | 7.53E-07 | 3 | 4004 | 0.3724 | 1.10E-07 | | |
| | | x12 | 33 | 67 | 0.1238 | 8.58E-07 | 61 | 123 | 0.1517 | 8.73E-07 | 32 | 33033 | 4.0013 | 2.44E-09 | | |
| | | x13 | 30 | 61 | 0.0719 | 7.1E-07 | 55 | 111 | 0.0345 | 7.15E-07 | 2 | 3003 | 0.2615 | 3.49E-10 | | |
| | | x14 | 94 | 189 | 0.6520 | 8.44E-07 | 102 | 205 | 0.2729 | 9.53E-07 | 16 | 17017 | 1.4661 | 3.47E-18 | | |
| | | x15 | 28 | 57 | 0.024471 | 9.45E-07 | 35 | 71 | 0.024564 | 7.52E-07 | 4 | 5005 | 1.2014 | 1.65E-14 | | |
| | 5000 | x1 | 17 | 35 | 0.0881 | 8.04E-07 | 26 | 53 | 0.0652 | 8.87E-07 | 2 | 15003 | 5.0671 | 3.34E-14 | | |
| | | x2 | 44 | 89 | 0.5841 | 6.14E-07 | 82 | 165 | 2.8911 | 7.32E-07 | - | - | - | - | | |
| | | x3 | 47 | 95 | 1.1229 | 8.28E-07 | 39 | 79 | 0.1397 | 8.64E-07 | 9 | 50010 | 19.9945 | 6.76E-12 | | |
| | | x4 | 54 | 109 | 0.3754 | 9.98E-07 | 65 | 131 | 0.6102 | 6.91E-07 | 19 | 100020 | 39.9828 | 5.49E-12 | | |
| | | x5 | 30 | 61 | 0.1402 | 7.11E-07 | 38 | 77 | 0.1185 | 8.12E-07 | 4 | 25005 | 9.2630 | 3.30E-10 | | |
| | | x6 | 35 | 71 | 0.1876 | 8.03E-07 | 40 | 81 | 0.1296 | 9.8E-07 | 6 | 35007 | 14.0282 | 6.60E-11 | | |
| | | x7 | - | - | - | - | - | 87 | 175 | 1.9213 | 8.12E-07 | 89 | 450090 | 180.9928 | 4.74E-11 | |
| | | x8 | 30 | 61 | 0.2498 | 6.34E-07 | 38 | 77 | 0.1016 | 9.03E-07 | 4 | 25005 | 9.7429 | 4.12E-10 | | |
| | | x9 | 36 | 73 | 0.7128 | 9.6E-07 | 570 | 1141 | 8.7491 | 6.51E-07 | 9 | 50010 | 18.1894 | 5.93E-11 | | |
| | | x10 | 34 | 69 | 0.3866 | 8.13E-07 | 38 | 77 | 0.1050 | 9.47E-07 | 4 | 25005 | 10.4435 | 3.75E-15 | | |
| | | x11 | 30 | 61 | 0.3215 | 5.79E-07 | 40 | 81 | 0.1215 | 8.43E-07 | 4 | 25005 | 9.0540 | 6.67E-14 | | |
| | | x12 | 53 | 107 | 1.0391 | 8.94E-07 | 97 | 195 | 2.7151 | 7.53E-07 | 29 | 150030 | 57.1945 | 4.71E-11 | | |
| | | x13 | 32 | 65 | 0.1479 | 5.47E-07 | 45 | 91 | 0.2618 | 8.75E-07 | 2 | 15003 | 4.6077 | 3.17E-14 | | |
| | | x14 | 113 | 227 | 4.0425 | 8.26E-07 | 112 | 225 | 1.7131 | 7.58E-07 | 12 | 65013 | 26.2234 | 1.17E-14 | | |
| | | x15 | 28 | 57 | 0.1085 | 6.81E-07 | 35 | 71 | 0.078578 | 7.24E-07 | 4 | 25005 | 5.1051 | 2.05E-10 | | |
| 5.1.6 | 1000 | x2 | - | - | - | - | - | - | - | - | 5 | 6006 | 0.3292 | 6.72E-08 | | |
| | | x3 | 15 | 31 | 0.0086 | 6.54E-07 | 26 | 53 | 0.0057 | 6.45E-07 | 5 | 6005 | 0.3188 | 6.71E-08 | | |
| | | x4 | 16 | 33 | 0.0065 | 3.44E-07 | 26 | 53 | 0.0059 | 8.07E-07 | 6 | 7007 | 0.3867 | 7.98E-09 | | |
| | | x5 | 14 | 29 | 0.0063 | 5.9E-07 | 25 | 51 | 0.0072 | 7.76E-07 | 4 | 5005 | 0.2662 | 2.82E-09 | | |
| | | x6 | - | - | - | - | - | 4 | 9 | 0.0034 | 2.08E-11 | 5 | 6006 | 0.3260 | 1.34E-09 | |
| | | x8 | 16 | 33 | 0.0090 | 5.69E-07 | 4 | 9 | 0.0021 | 3.16E-14 | 4 | 5005 | 0.2706 | 8.42E-09 | | |
| | | x9 | - | - | - | - | - | 4 | 9 | 0.0018 | 2.07E-09 | 5 | 6006 | 0.3197 | 3.63E-07 | |
| | | x10 | 15 | 31 | 0.0116 | 9.94E-07 | 3 | 7 | 0.0010 | 1.24E-08 | 4 | 5005 | 0.2655 | 1.53E-13 | | |
| | | x11 | 16 | 33 | 0.0095 | 3.64E-07 | 25 | 51 | 0.0144 | 5.16E-07 | 4 | 5005 | 0.2843 | 3.13E-10 | | |
| | | x12 | 16 | 33 | 0.0061 | 5.72E-07 | 5 | 11 | 0.0015 | 5.83E-11 | 7 | 8008 | 0.4293 | 2.51E-10 | | |
| | | x13 | 14 | 29 | 0.0128 | 6.5E-07 | 3 | 7 | 0.0013 | 3.16E-14 | 2 | 3003 | 0.1673 | 1.04E-07 | | |
| | | x14 | - | - | - | - | - | 25 | 51 | 0.0058 | 9.65E-07 | 5 | 6006 | 0.3316 | 1.84E-07 | |
| | | x15 | 13 | 27 | 0.005518 | 8.46E-07 | 38 | 77 | 0.00676 | 8.83E-07 | 4 | 5005 | 0.3289 | 5.03E-09 | | |
| | | 5000 | x2 | - | - | - | - | - | - | - | - | - | 6 | 35007 | 7.6255 | 5.02E-08 |
| | | | x3 | 16 | 33 | 0.0321 | 4.47E-07 | 27 | 55 | 0.0684 | 7.21E-07 | 6 | 35007 | 7.8077 | 5.02E-08 | |
| | x4 | | 16 | 33 | 0.0302 | 7.68E-07 | 27 | 55 | 0.0681 | 9.03E-07 | 7 | 40008 | 9.0358 | 1.81E-08 | | |
| | x5 | | 15 | 31 | 0.0368 | 4.04E-07 | 26 | 53 | 0.0718 | 8.68E-07 | 5 | 30006 | 6.7700 | 7.72E-10 | | |
| | x6 | | - | - | - | - | - | 4 | 9 | 0.0128 | 4.64E-11 | 6 | 35007 | 7.9447 | 6.96E-10 | |
| | x8 | | 17 | 35 | 0.0423 | 3.89E-07 | 4 | 9 | 0.0125 | 7.07E-14 | 5 | 30006 | 6.9963 | 1.94E-09 | | |
| | x9 | | - | - | - | - | - | 4 | 9 | 0.0096 | 4.63E-09 | 6 | 35007 | 8.2785 | 2.54E-07 | |
| | x10 | | 16 | 33 | 0.0297 | 6.8E-07 | 3 | 7 | 0.0161 | 2.76E-08 | 4 | 25005 | 5.7580 | 3.39E-08 | | |
| | x11 | | 16 | 33 | 0.0394 | 8.04E-07 | 25 | 51 | 0.0589 | 9.72E-07 | 5 | 30006 | 7.5145 | 4.08E-12 | | |
| | x12 | | 17 | 35 | 0.0362 | 3.91E-07 | 5 | 11 | 0.0104 | 1.3E-10 | 8 | 45009 | 10.4847 | 6.73E-10 | | |
| | x13 | | 15 | 31 | 0.0321 | 4.45E-07 | 3 | 7 | 0.0084 | 7.07E-14 | 2 | 15003 | 3.3157 | 1.04E-07 | | |
| | x14 | | - | - | - | - | - | 27 | 55 | 0.0829 | 5.33E-07 | 6 | 35007 | 8.3699 | 1.01E-07 | |
| | x15 | | 14 | 29 | 0.057251 | 5.91E-07 | 37 | 75 | 0.025964 | 9.99E-07 | 5 | 30006 | 6.7582 | 1.24E-09 | | |

Table 4: Numerical results for problems 5.1.7

| Problem | DIM | DPP | | | | | MPD | | | LSQNONLIN | | | | |
|---------|------|-----|------|------|----------|----------|------|------|----------|-----------|------|--------|---------|----------|
| | | IP | ITER | FVAL | TIME | NORM | ITER | FVAL | TIME | NORM | ITER | FVAL | TIME | NORM |
| 5.1.7 | 1000 | x1 | 16 | 33 | 0.0403 | 2.2E-07 | 53 | 107 | 0.0838 | 8.58E-07 | 1 | 1001 | 0.0694 | 0 |
| | | x2 | 78 | 157 | 0.1092 | 8.1E-07 | 102 | 205 | 0.1094 | 7.94E-07 | 15 | 16016 | 1.0620 | 2.69E-08 |
| | | x3 | 79 | 159 | 0.0561 | 9.47E-07 | 87 | 175 | 0.1028 | 8.5E-07 | 14 | 15015 | 0.9762 | 8.13E-10 |
| | | x4 | 62 | 125 | 0.0508 | 5.55E-07 | 115 | 231 | 0.1277 | 9.69E-07 | 14 | 15015 | 0.9578 | 2.69E-08 |
| | | x5 | 55 | 111 | 0.0728 | 6.84E-07 | 91 | 183 | 0.1025 | 8.95E-07 | 9 | 10010 | 0.6540 | 8.26E-08 |
| | | x6 | 100 | 201 | 0.0722 | 6.72E-07 | 96 | 193 | 0.0912 | 8.64E-07 | 7 | 8008 | 0.5226 | 8.44E-07 |
| | | x7 | 72 | 145 | 0.0827 | 9.67E-07 | 115 | 231 | 0.1095 | 7.74E-07 | 14 | 15015 | 0.9879 | 2.77E-08 |
| | | x8 | 82 | 165 | 0.0563 | 7.07E-07 | 98 | 197 | 0.0403 | 8.68E-07 | 6 | 7007 | 0.4713 | 2.34E-10 |
| | | x9 | 36 | 73 | 0.1009 | 9.51E-07 | 95 | 191 | 0.0507 | 9.57E-07 | 8 | 9009 | 0.5823 | 1.49E-07 |
| | | x10 | 79 | 159 | 0.1934 | 6.64E-07 | 90 | 181 | 0.0382 | 8.66E-07 | 5 | 6006 | 0.3974 | 1.27E-08 |
| | | x11 | 15 | 31 | 0.0256 | 5.23E-07 | 43 | 87 | 0.0190 | 6.56E-07 | 16 | 17017 | 1.1032 | 1.30E-09 |
| | | x12 | 86 | 173 | 0.0724 | 9.72E-07 | 111 | 223 | 0.0562 | 9.53E-07 | 11 | 12012 | 0.7930 | 3.78E-10 |
| | | x13 | 40 | 81 | 0.0342 | 9.84E-07 | 70 | 141 | 0.0751 | 8.44E-07 | 10 | 11011 | 0.7204 | 7.38E-13 |
| | | x14 | 47 | 95 | 0.0659 | 9.21E-07 | 72 | 145 | 0.0727 | 7.73E-07 | 13 | 14014 | 0.9028 | 1.22E-12 |
| | | x15 | 47 | 95 | 0.039078 | 7.16E-07 | 107 | 215 | 0.060134 | 8.5E-07 | 7 | 8008 | 0.8521 | 2.43E-07 |
| | 5000 | x1 | 17 | 35 | 0.0655 | 2.83E-07 | 63 | 127 | 0.2859 | 8.33E-07 | 1 | 5001 | 1.2046 | 0.00E+00 |
| | | x2 | 116 | 233 | 0.5070 | 7.08E-07 | 169 | 339 | 0.8942 | 9.87E-07 | 16 | 85017 | 24.8629 | 1.06E-07 |
| | | x3 | 72 | 145 | 0.6564 | 8.83E-07 | 95 | 191 | 0.6958 | 7.66E-07 | 14 | 75015 | 21.8448 | 7.10E-07 |
| | | x4 | 120 | 241 | 0.9315 | 7.52E-07 | 107 | 215 | 0.7671 | 8.35E-07 | 14 | 75015 | 24.2092 | 4.64E-13 |
| | | x5 | 47 | 95 | 0.1700 | 8.85E-07 | 99 | 199 | 0.5073 | 8.51E-07 | 9 | 50010 | 13.9868 | 7.51E-13 |
| | | x6 | 117 | 235 | 0.5739 | 6.85E-07 | 95 | 191 | 0.5010 | 9.49E-07 | 8 | 45009 | 12.9194 | 1.55E-07 |
| | | x7 | 127 | 255 | 1.5801 | 8.04E-07 | 132 | 265 | 0.9161 | 9.75E-07 | 15 | 80016 | 24.5737 | 3.54E-08 |
| | | x8 | 47 | 95 | 0.3584 | 6.12E-07 | 97 | 195 | 0.5110 | 9.98E-07 | 7 | 40008 | 11.2833 | 3.13E-12 |
| | | x9 | 38 | 77 | 0.3818 | 9.3E-07 | 96 | 193 | 0.2038 | 9.85E-07 | 9 | 50010 | 14.3557 | 4.65E-08 |
| | | x10 | 88 | 177 | 0.3205 | 9.28E-07 | 103 | 207 | 0.2142 | 9.89E-07 | 5 | 30006 | 8.3952 | 1.27E-08 |
| | | x11 | 17 | 35 | 0.0637 | 9.85E-08 | 39 | 79 | 0.0999 | 7.18E-07 | 19 | 100020 | 30.4028 | 6.98E-08 |
| | | x12 | 86 | 173 | 0.2797 | 8.71E-07 | 100 | 201 | 0.4045 | 9.96E-07 | 12 | 65013 | 18.2419 | 2.90E-10 |
| | | x13 | 69 | 139 | 0.4708 | 8.77E-07 | 72 | 145 | 0.3740 | 8.61E-07 | 9 | 50010 | 14.0725 | 8.74E-12 |
| | | x14 | 22 | 45 | 0.1985 | 7.04E-07 | 60 | 121 | 0.3506 | 9.6E-07 | 18 | 95019 | 25.7369 | 4.29E-08 |
| | | x15 | 75 | 151 | 0.266 | 9.67E-07 | 109 | 219 | 0.25697 | 8.39E-07 | 8 | 45009 | 7.2015 | 4.33E-09 |

Table 5: Numerical results for problems 5.2.1

| Problem | DIM | DPP | | | | | AFP | | | | | PDY | | | |
|---------|--------|-----|------|-------|----------|----------|------|-------|----------|----------|------|-------|----------|----------|--|
| | | IP | ITER | FEVAL | TIME | NORM | ITER | FEVAL | TIME | NORM | ITER | FEVAL | TIME | NORM | |
| 5.2.1 | 1000 | x1 | 2 | 5 | 0.0035 | 0 | 9 | 20 | 0.0947 | 5.72E-07 | 36 | 74 | 0.0536 | 3.49E-07 | |
| | | x2 | 4 | 9 | 0.0028 | 7.15E-08 | 11 | 23 | 0.0278 | 2.53E-07 | 42 | 85 | 0.0215 | 8.84E-07 | |
| | | x3 | 2 | 5 | 0.0016 | 0 | 11 | 24 | 0.0045 | 2.99E-07 | 46 | 94 | 0.0155 | 2.21E-08 | |
| | | x4 | 2 | 5 | 0.0015 | 0 | 9 | 20 | 0.0073 | 8.46E-07 | 40 | 82 | 0.0128 | 3.16E-07 | |
| | | x5 | 1 | 3 | 0.0009 | 0 | 11 | 24 | 0.0218 | 6.1E-07 | 51 | 104 | 0.0243 | 9.89E-07 | |
| | | x6 | 1 | 3 | 0.0010 | 0 | 11 | 24 | 0.0048 | 6.07E-07 | 54 | 110 | 0.0167 | 7.06E-07 | |
| | | x7 | 3 | 7 | 0.019563 | 1.96E-08 | 12 | 26 | 0.032634 | 2.27E-07 | 25 | 52 | 0.029216 | 6.13E-07 | |
| | 5000 | x1 | 2 | 5 | 0.0054 | 0 | 10 | 22 | 0.0141 | 2.54E-07 | 27 | 56 | 0.0303 | 1.3E-08 | |
| | | x2 | 4 | 9 | 0.0112 | 7.15E-08 | 11 | 23 | 0.0168 | 2.53E-07 | 42 | 85 | 0.0643 | 8.84E-07 | |
| | | x3 | 2 | 5 | 0.0070 | 0 | 11 | 24 | 0.0331 | 3.91E-07 | 28 | 58 | 0.0675 | 4.05E-07 | |
| | | x4 | 2 | 5 | 0.0068 | 0 | 9 | 20 | 0.0110 | 8.46E-07 | 36 | 74 | 0.0623 | 3.44E-07 | |
| | | x5 | 1 | 3 | 0.0027 | 0 | 12 | 26 | 0.0194 | 2.68E-07 | 51 | 104 | 0.1057 | 7.98E-07 | |
| | | x6 | 1 | 3 | 0.0030 | 0 | 12 | 26 | 0.0182 | 2.69E-07 | 50 | 102 | 0.0650 | 8.02E-07 | |
| | | x7 | 3 | 7 | 0.034749 | 9.53E-09 | 12 | 26 | 0.02115 | 3.63E-07 | 26 | 54 | 0.047353 | 6.93E-07 | |
| | 10000 | x1 | 2 | 5 | 0.0093 | 0 | 10 | 22 | 0.0296 | 3.59E-07 | 29 | 60 | 0.1036 | 2.14E-08 | |
| | | x2 | 4 | 9 | 0.0227 | 7.15E-08 | 11 | 23 | 0.0307 | 2.53E-07 | 42 | 85 | 0.1206 | 8.84E-07 | |
| | | x3 | 2 | 5 | 0.0111 | 0 | 11 | 24 | 0.0326 | 5.01E-07 | 31 | 64 | 0.1170 | 1.18E-07 | |
| | | x4 | 2 | 5 | 0.0093 | 0 | 9 | 20 | 0.0250 | 8.46E-07 | 41 | 84 | 0.1155 | 1.1E-07 | |
| | | x5 | 1 | 3 | 0.0049 | 0 | 12 | 26 | 0.0351 | 3.78E-07 | 47 | 95 | 0.1782 | 5.62E-07 | |
| | | x6 | 1 | 3 | 0.0094 | 0 | 12 | 26 | 0.0341 | 3.78E-07 | 46 | 94 | 0.1467 | 5.59E-07 | |
| | | x7 | 3 | 7 | 0.017296 | 6.83E-09 | 12 | 26 | 0.037283 | 4.77E-07 | 26 | 54 | 0.087295 | 9.82E-07 | |
| | 50000 | x1 | 2 | 5 | 0.0763 | 0 | 10 | 22 | 0.1361 | 8.03E-07 | 28 | 58 | 0.3599 | 8.48E-08 | |
| | | x2 | 4 | 9 | 0.1808 | 7.15E-08 | 11 | 23 | 0.2346 | 2.53E-07 | 42 | 85 | 0.5511 | 8.84E-07 | |
| | | x3 | 2 | 5 | 0.0825 | 0 | 12 | 26 | 0.1608 | 2.05E-07 | 44 | 90 | 1.0946 | 2.61E-07 | |
| | | x4 | 2 | 5 | 0.0413 | 0 | 9 | 20 | 0.1499 | 8.46E-07 | 45 | 92 | 0.7007 | 2.84E-07 | |
| | | x5 | 1 | 3 | 0.0141 | 0 | 12 | 26 | 0.1680 | 8.43E-07 | 51 | 104 | 0.6174 | 6.27E-07 | |
| | | x6 | 1 | 3 | 0.0196 | 0 | 12 | 26 | 0.1298 | 8.43E-07 | 49 | 100 | 0.6005 | 6.26E-07 | |
| | | x7 | 6 | 13 | 0.13314 | 2.99E-09 | 12 | 26 | 0.12438 | 9.91E-07 | 28 | 58 | 0.33771 | 6.43E-07 | |
| | 100000 | x1 | 2 | 5 | 0.0774 | 0 | 11 | 24 | 0.3029 | 2.27E-07 | 21 | 44 | 0.7041 | 7.7E-07 | |
| | | x2 | 4 | 9 | 0.2129 | 7.15E-08 | 11 | 23 | 0.2955 | 2.53E-07 | 42 | 85 | 1.5025 | 8.84E-07 | |
| | | x3 | 2 | 5 | 0.1169 | 0 | 12 | 26 | 0.3713 | 2.86E-07 | 37 | 76 | 1.1488 | 4.43E-08 | |
| | | x4 | 2 | 5 | 0.0957 | 0 | 9 | 20 | 0.2441 | 8.46E-07 | 32 | 66 | 0.6929 | 7.38E-07 | |
| | | x5 | 1 | 3 | 0.0681 | 0 | 13 | 28 | 0.4874 | 2.38E-07 | 51 | 104 | 1.6804 | 7.08E-07 | |
| | | x6 | 1 | 3 | 0.0500 | 0 | 13 | 28 | 0.5627 | 2.38E-07 | 49 | 100 | 1.4841 | 7.08E-07 | |
| | | x7 | 6 | 13 | 0.39183 | 4.23E-09 | 13 | 28 | 0.25888 | 2.77E-07 | 29 | 60 | 1.0541 | 6.43E-07 | |

Table 6: Numerical results for problems 5.2.2

| Problem | DIM | DPP | | | | | AFP | | | | | PDY | | | |
|---------|--------|-----|------|-------|----------|----------|------|-------|----------|----------|------|-------|----------|----------|--|
| | | IP | ITER | FEVAL | TIME | NORM | ITER | FEVAL | TIME | NORM | ITER | FEVAL | TIME | NORM | |
| 5.2.2 | 1000 | x1 | 13 | 28 | 0.0223 | 7.07E-07 | 3 | 8 | 0.0433 | 1.49E-07 | 2 | 6 | 0.0021 | 5.17E-07 | |
| | | x2 | 12 | 26 | 0.0115 | 4.65E-07 | 9 | 20 | 0.0108 | 4.62E-07 | 18 | 38 | 0.0071 | 4.14E-07 | |
| | | x3 | 14 | 30 | 0.0123 | 4.96E-07 | 6 | 14 | 0.0033 | 4.36E-09 | 5 | 12 | 0.0042 | 1.74E-08 | |
| | | x4 | 14 | 29 | 0.0290 | 9.32E-07 | 14 | 30 | 0.0090 | 4.75E-07 | 20 | 42 | 0.0085 | 8.06E-07 | |
| | | x5 | 29 | 60 | 0.0882 | 9.68E-07 | 8 | 18 | 0.0306 | 5.58E-08 | 27 | 56 | 0.0105 | 1.81E-07 | |
| | | x6 | 69 | 140 | 0.3084 | 3.91E-07 | 7 | 16 | 0.0147 | 1.41E-07 | 17 | 36 | 0.0077 | 1.1E-07 | |
| | | x7 | 15 | 32 | 0.016075 | 4.56E-07 | 12 | 26 | 0.062709 | 3.75E-07 | 24 | 50 | 0.013574 | 4.79E-07 | |
| | 5000 | x1 | 14 | 30 | 0.0483 | 5.03E-07 | 3 | 8 | 0.0085 | 3.89E-08 | 2 | 6 | 0.0051 | 1.75E-07 | |
| | | x2 | 12 | 26 | 0.0420 | 4.86E-07 | 10 | 22 | 0.0159 | 8.73E-08 | 30 | 62 | 0.0440 | 1.54E-07 | |
| | | x3 | 15 | 32 | 0.0929 | 3.61E-07 | 6 | 14 | 0.0135 | 3.39E-10 | 5 | 12 | 0.0125 | 2.36E-09 | |
| | | x4 | 14 | 30 | 0.0527 | 3.55E-07 | 12 | 26 | 0.0186 | 3.16E-07 | 18 | 38 | 0.0211 | 5.88E-08 | |
| | | x5 | 27 | 56 | 0.1085 | 7.95E-07 | 11 | 24 | 0.0272 | 5.09E-07 | 22 | 46 | 0.0464 | 8.16E-07 | |
| | | x6 | 45 | 92 | 0.1595 | 3.6E-07 | 9 | 20 | 0.0227 | 9.09E-07 | 29 | 60 | 0.0911 | 4.18E-07 | |
| | | x7 | 16 | 34 | 0.061952 | 4.23E-07 | 15 | 32 | 0.029267 | 9.02E-07 | 16 | 34 | 0.033741 | 4.93E-07 | |
| | 10000 | x1 | 14 | 30 | 0.2332 | 7.16E-07 | 3 | 8 | 0.0152 | 2.52E-08 | 2 | 6 | 0.0166 | 1.21E-07 | |
| | | x2 | 12 | 26 | 0.2246 | 4.88E-07 | 11 | 24 | 0.0343 | 3.07E-08 | 28 | 58 | 0.1648 | 1.05E-07 | |
| | | x3 | 16 | 34 | 0.1051 | 9.36E-07 | 6 | 14 | 0.0244 | 1.35E-10 | 5 | 12 | 0.0341 | 3.62E-09 | |
| | | x4 | 14 | 30 | 0.0871 | 3.6E-07 | 13 | 28 | 0.0438 | 1.12E-07 | 15 | 32 | 0.1042 | 5.56E-07 | |
| | | x5 | 17 | 36 | 0.1077 | 8.75E-07 | 11 | 24 | 0.0374 | 2.85E-07 | 25 | 52 | 0.0697 | 9E-07 | |
| | | x6 | 17 | 36 | 0.1610 | 8.75E-07 | 11 | 24 | 0.0853 | 2.81E-07 | 22 | 46 | 0.1037 | 2.8E-07 | |
| | | x7 | 16 | 34 | 0.15031 | 6.54E-07 | 19 | 40 | 0.087761 | 3.15E-07 | 14 | 30 | 0.056115 | 7.31E-07 | |
| | 50000 | x1 | 15 | 32 | 0.5547 | 4.92E-07 | 3 | 8 | 0.0609 | 1.09E-08 | 2 | 6 | 0.0294 | 6.32E-08 | |
| | | x2 | 12 | 26 | 0.5452 | 4.9E-07 | 15 | 32 | 0.1840 | 6.34E-10 | 21 | 44 | 0.3342 | 6.18E-10 | |
| | | x3 | 16 | 34 | 0.5829 | 5.32E-07 | 6 | 14 | 0.1117 | 2.58E-11 | 6 | 14 | 0.0781 | 9.31E-09 | |
| | | x4 | 14 | 30 | 0.3279 | 3.64E-07 | 16 | 34 | 0.2418 | 5.27E-09 | 15 | 32 | 0.3077 | 2.59E-07 | |
| | | x5 | 15 | 32 | 0.3538 | 5.79E-07 | 14 | 30 | 0.1818 | 3.16E-08 | 23 | 48 | 0.5426 | 1.82E-07 | |
| | | x6 | 15 | 32 | 0.8437 | 5.11E-07 | 14 | 30 | 0.4377 | 3.21E-08 | 24 | 50 | 0.4941 | 5.15E-07 | |
| | | x7 | 16 | 34 | 0.45146 | 9.4E-07 | 20 | 42 | 0.29844 | 7.54E-08 | 16 | 34 | 0.27335 | 9.16E-08 | |
| | 100000 | x1 | 15 | 32 | 0.7980 | 6.96E-07 | 3 | 8 | 0.1821 | 8.03E-09 | 2 | 6 | 0.0512 | 5.4E-08 | |
| | | x2 | 12 | 26 | 0.5381 | 4.91E-07 | 16 | 34 | 0.6858 | 2.03E-10 | 29 | 60 | 0.7758 | 6.52E-08 | |
| | | x3 | 16 | 34 | 1.4319 | 7.53E-07 | 6 | 14 | 0.1629 | 1.54E-11 | 7 | 16 | 0.4030 | 1.1E-09 | |
| | | x4 | 14 | 30 | 0.5969 | 3.65E-07 | 18 | 38 | 0.4598 | 7.16E-10 | 15 | 32 | 0.6093 | 2.34E-07 | |
| | | x5 | 15 | 32 | 1.2120 | 7.21E-07 | 15 | 32 | 0.5378 | 1.48E-08 | 20 | 42 | 0.6005 | 3.99E-07 | |
| | | x6 | 15 | 32 | 1.0270 | 7.21E-07 | 15 | 32 | 0.9451 | 1.58E-08 | 18 | 38 | 0.4942 | 7.66E-07 | |
| | | x7 | 17 | 36 | 0.89842 | 3.95E-07 | 22 | 46 | 0.64874 | 1.51E-08 | 17 | 36 | 0.73163 | 1.03E-07 | |

Table 7: Numerical results for problems 5.2.3

| Problem | DIM | DPP | | | | | AFP | | | | | PDY | | | |
|---------|--------|-----|------|-------|----------|----------|------|-------|----------|----------|------|-------|----------|----------|--|
| | | IP | ITER | FEVAL | TIME | NORM | ITER | FEVAL | TIME | NORM | ITER | FEVAL | TIME | NORM | |
| 5.2.3 | 1000 | x1 | 2 | 5 | 0.0017 | 0 | 29 | 60 | 0.0614 | 6.98E-07 | 21 | 44 | 0.0116 | 7.52E-07 | |
| | | x2 | 1 | 3 | 0.0011 | 0 | 25 | 52 | 0.0090 | 9.52E-07 | 19 | 40 | 0.0149 | 5.27E-07 | |
| | | x3 | 1 | 3 | 0.0024 | 0 | 34 | 70 | 0.0114 | 6.28E-07 | 24 | 50 | 0.0215 | 8.19E-07 | |
| | | x4 | 1 | 3 | 0.0032 | 0 | 27 | 56 | 0.0112 | 7.07E-07 | 20 | 42 | 0.0218 | 5.35E-07 | |
| | | x5 | 1 | 3 | 0.0041 | 0 | 32 | 66 | 0.0116 | 7.89E-07 | 23 | 48 | 0.0354 | 9.58E-07 | |
| | | x6 | 1 | 3 | 0.0024 | 0 | 32 | 66 | 0.0112 | 7.79E-07 | 23 | 48 | 0.0155 | 9.62E-07 | |
| | | x7 | 2 | 5 | 0.002736 | 0 | 33 | 68 | 0.011254 | 7.8E-07 | 24 | 50 | 0.009124 | 6.55E-07 | |
| | 5000 | x1 | 2 | 5 | 0.0058 | 0 | 30 | 62 | 0.0714 | 9.36E-07 | 22 | 46 | 0.0321 | 2.34E-22 | |
| | | x2 | 1 | 3 | 0.0033 | 0 | 25 | 52 | 0.0381 | 9.52E-07 | 19 | 40 | 0.0244 | 5.27E-07 | |
| | | x3 | 2 | 5 | 0.0054 | 0 | 35 | 72 | 0.1222 | 0 | 26 | 54 | 0.0512 | 9.45E-07 | |
| | | x4 | 1 | 3 | 0.0034 | 0 | 27 | 56 | 0.1080 | 7.08E-07 | 20 | 42 | 0.0194 | 5.35E-07 | |
| | | x5 | 1 | 3 | 0.0018 | 0 | 34 | 70 | 0.0987 | 6.36E-07 | 25 | 52 | 0.0340 | 5.36E-07 | |
| | | x6 | 1 | 3 | 0.0045 | 0 | 34 | 70 | 0.1021 | 6.38E-07 | 25 | 52 | 0.0403 | 5.31E-07 | |
| | | x7 | 2 | 5 | 0.005641 | 0 | 35 | 72 | 0.11423 | 0 | 25 | 52 | 0.043758 | 7.4E-07 | |
| | 10000 | x1 | 2 | 5 | 0.0090 | 0 | 31 | 64 | 0.1447 | 0 | 22 | 46 | 0.0500 | 3.31E-22 | |
| | | x2 | 1 | 3 | 0.0042 | 0 | 25 | 52 | 0.0617 | 9.52E-07 | 19 | 40 | 0.0491 | 5.27E-07 | |
| | | x3 | 2 | 5 | 0.0103 | 0 | 35 | 72 | 0.1617 | 0 | 27 | 56 | 0.2452 | 6.68E-07 | |
| | | x4 | 1 | 3 | 0.0039 | 0 | 27 | 56 | 0.0731 | 7.08E-07 | 20 | 42 | 0.1893 | 5.35E-07 | |
| | | x5 | 1 | 3 | 0.0047 | 0 | 34 | 70 | 0.1369 | 8.99E-07 | 25 | 52 | 0.1644 | 7.58E-07 | |
| | | x6 | 1 | 3 | 0.0090 | 0 | 34 | 70 | 0.0866 | 8.99E-07 | 25 | 52 | 0.0661 | 7.55E-07 | |
| | | x7 | 2 | 5 | 0.009806 | 0 | 35 | 72 | 0.09615 | 0 | 26 | 54 | 0.15627 | 9.33E-20 | |
| | 50000 | x1 | 2 | 5 | 0.0702 | 0 | 31 | 64 | 0.7288 | 0 | 24 | 50 | 0.2259 | 6.65E-07 | |
| | | x2 | 1 | 3 | 0.0277 | 0 | 25 | 52 | 0.5251 | 9.52E-07 | 19 | 40 | 0.1999 | 5.27E-07 | |
| | | x3 | 4 | 9 | 0.1842 | 0 | 35 | 72 | 0.4154 | 0 | 27 | 56 | 0.3348 | 2.37E-20 | |
| | | x4 | 1 | 3 | 0.0143 | 0 | 27 | 56 | 0.3102 | 7.08E-07 | 20 | 42 | 0.5169 | 5.35E-07 | |
| | | x5 | 1 | 3 | 0.0102 | 0 | 35 | 72 | 0.5859 | 0 | 26 | 54 | 0.5025 | 8.48E-07 | |
| | | x6 | 1 | 3 | 0.0389 | 0 | 35 | 72 | 0.8709 | 0 | 26 | 54 | 0.3384 | 8.47E-07 | |
| | | x7 | 6 | 13 | 0.10647 | 3.44E-07 | 35 | 72 | 0.5175 | 0 | 27 | 56 | 0.31698 | 9.01E-07 | |
| | 100000 | x1 | 2 | 5 | 0.0771 | 0 | 31 | 64 | 0.7165 | 0 | 19 | 40 | 0.4021 | 3.35E-20 | |
| | | x2 | 1 | 3 | 0.0305 | 0 | 25 | 52 | 0.7960 | 9.52E-07 | 19 | 40 | 0.3788 | 5.27E-07 | |
| | | x3 | 5 | 11 | 0.4825 | 0 | 35 | 72 | 1.0854 | 0 | 34 | 70 | 1.3969 | 5.62E-07 | |
| | | x4 | 1 | 3 | 0.0417 | 0 | 27 | 56 | 0.5418 | 7.08E-07 | 20 | 42 | 0.3753 | 5.35E-07 | |
| | | x5 | 2 | 5 | 0.1054 | 0 | 35 | 72 | 1.0416 | 0 | 27 | 56 | 0.5500 | 9.24E-07 | |
| | | x6 | 2 | 5 | 0.0998 | 0 | 35 | 72 | 1.0976 | 0 | 26 | 54 | 0.9390 | 3.53E-22 | |
| | | x7 | 3 | 7 | 0.13034 | 0 | 35 | 72 | 0.75288 | 0 | 28 | 58 | 0.6749 | 9.39E-07 | |

Table 8: Numerical results for problems 5.2.4

| Problem | DIM | IP | DPP | | | | AFP | | | | PDY | | | |
|---------|--------|----|------|-------|----------|----------|------|-------|----------|----------|------|-------|----------|----------|
| | | | ITER | FEVAL | TIME | NORM | ITER | FEVAL | TIME | NORM | ITER | FEVAL | TIME | NORM |
| 5.2.4 | 1000 | x1 | 1 | 3 | 0.0020 | 0 | 29 | 60 | 0.0111 | 6.43E-07 | 21 | 44 | 0.0151 | 6.82E-07 |
| | | x2 | 1 | 3 | 0.0024 | 2.22E-16 | 25 | 52 | 0.0093 | 6.83E-07 | 19 | 39 | 0.0070 | 7.03E-07 |
| | | x3 | 1 | 3 | 0.0017 | 0 | 33 | 68 | 0.0276 | 6.08E-07 | 23 | 48 | 0.0082 | 9.98E-07 |
| | | x4 | 2 | 5 | 0.0021 | 0 | 26 | 54 | 0.0063 | 6.75E-07 | 19 | 40 | 0.0069 | 8.45E-07 |
| | | x5 | 2 | 5 | 0.0024 | 0 | 31 | 64 | 0.0109 | 7.49E-07 | 23 | 48 | 0.0112 | 5.48E-07 |
| | | x6 | 2 | 5 | 0.0028 | 0 | 31 | 64 | 0.0164 | 7.61E-07 | 23 | 48 | 0.0105 | 5.46E-07 |
| | | x7 | 2 | 5 | 0.001954 | 0 | 32 | 66 | 0.009784 | 6.59E-07 | 24 | 50 | 0.009663 | 7.16E-07 |
| | 5000 | x1 | 1 | 3 | 0.0051 | 0 | 30 | 62 | 0.0319 | 8.63E-07 | 22 | 46 | 0.0180 | 7.62E-07 |
| | | x2 | 1 | 3 | 0.0042 | 2.22E-16 | 25 | 52 | 0.0750 | 6.83E-07 | 19 | 39 | 0.0223 | 7.03E-07 |
| | | x3 | 2 | 5 | 0.0119 | 0 | 34 | 70 | 0.0855 | 8.16E-07 | 23 | 48 | 0.0220 | 6.33E-07 |
| | | x4 | 2 | 5 | 0.0103 | 0 | 26 | 54 | 0.0736 | 6.75E-07 | 19 | 40 | 0.0235 | 8.45E-07 |
| | | x5 | 2 | 5 | 0.0101 | 0 | 33 | 68 | 0.1872 | 6.03E-07 | 24 | 50 | 0.0666 | 6.13E-07 |
| | | x6 | 2 | 5 | 0.0045 | 0 | 33 | 68 | 0.0410 | 6.02E-07 | 24 | 50 | 0.0724 | 6.14E-07 |
| | | x7 | 3 | 7 | 0.019657 | 0 | 33 | 68 | 0.037543 | 8.92E-07 | 25 | 52 | 0.034708 | 8.23E-07 |
| | 10000 | x1 | 1 | 3 | 0.0028 | 0 | 31 | 64 | 0.0639 | 7.32E-07 | 23 | 48 | 0.1033 | 5.39E-07 |
| | | x2 | 1 | 3 | 0.0034 | 2.22E-16 | 25 | 52 | 0.0482 | 6.83E-07 | 19 | 39 | 0.1043 | 7.03E-07 |
| | | x3 | 2 | 5 | 0.0095 | 0 | 35 | 72 | 0.0689 | 6.92E-07 | 26 | 54 | 0.0548 | 9.36E-07 |
| | | x4 | 2 | 5 | 0.0081 | 0 | 26 | 54 | 0.1097 | 6.76E-07 | 19 | 40 | 0.0448 | 8.45E-07 |
| | | x5 | 2 | 5 | 0.0090 | 0 | 33 | 68 | 0.0694 | 8.53E-07 | 24 | 50 | 0.0542 | 8.66E-07 |
| | | x6 | 2 | 5 | 0.0079 | 0 | 33 | 68 | 0.0908 | 8.55E-07 | 24 | 50 | 0.0822 | 8.72E-07 |
| | | x7 | 5 | 11 | 0.021961 | 1.59E-08 | 34 | 70 | 0.066519 | 7.58E-07 | 25 | 52 | 0.052607 | 7.67E-07 |
| | 50000 | x1 | 1 | 3 | 0.0174 | 0 | 32 | 66 | 0.5095 | 0 | 24 | 50 | 0.1716 | 0 |
| | | x2 | 1 | 3 | 0.0194 | 2.22E-16 | 25 | 52 | 0.5458 | 6.83E-07 | 19 | 39 | 0.1304 | 7.03E-07 |
| | | x3 | 3 | 7 | 0.1799 | 0 | 1000 | 2001 | 20.3478 | Inf | 29 | 60 | 0.4948 | 0 |
| | | x4 | 2 | 5 | 0.0665 | 0 | 26 | 54 | 0.3440 | 6.76E-07 | 19 | 40 | 0.3601 | 8.45E-07 |
| | | x5 | 2 | 5 | 0.0504 | 0 | 35 | 72 | 0.4293 | 6.86E-07 | 26 | 54 | 0.2362 | 7.4E-07 |
| | | x6 | 2 | 5 | 0.0834 | 0 | 35 | 72 | 0.3353 | 6.86E-07 | 26 | 54 | 0.2167 | 7.38E-07 |
| | | x7 | 5 | 11 | 0.099187 | 3.56E-08 | 36 | 74 | 0.36324 | 6.11E-07 | 26 | 54 | 0.33187 | 8.58E-07 |
| | 100000 | x1 | 1 | 3 | 0.0387 | 0 | 32 | 66 | 0.5790 | 0 | 24 | 50 | 0.3627 | 8.52E-07 |
| | | x2 | 1 | 3 | 0.0379 | 2.22E-16 | 25 | 52 | 0.6989 | 6.83E-07 | 19 | 39 | 0.4397 | 7.03E-07 |
| | | x3 | 5 | 11 | 0.2930 | 0 | 1000 | 2001 | 41.5945 | Inf | 33 | 68 | 0.8246 | 0 |
| | | x4 | 2 | 5 | 0.0576 | 0 | 26 | 54 | 0.3538 | 6.76E-07 | 19 | 40 | 0.3014 | 8.45E-07 |
| | | x5 | 2 | 5 | 0.0638 | 0 | 35 | 72 | 0.4950 | 9.71E-07 | 27 | 56 | 0.5657 | 5.23E-07 |
| | | x6 | 2 | 5 | 0.0739 | 0 | 35 | 72 | 0.7143 | 9.71E-07 | 27 | 56 | 0.7165 | 5.24E-07 |
| | | x7 | 3 | 7 | 0.10667 | 0 | 36 | 74 | 0.63267 | 8.64E-07 | 28 | 58 | 0.52477 | 5.01E-07 |

Table 9: Numerical results for problems 5.2.5

| Problem | DIM | DPP | | | | | AFP | | | | | PDY | | | |
|---------|--------|-----|------|-------|----------|----------|------|-------|----------|----------|------|-------|----------|----------|--|
| | | IP | ITER | FEVAL | TIME | NORM | ITER | FEVAL | TIME | NORM | ITER | FEVAL | TIME | NORM | |
| 5.2.5 | 1000 | x1 | 1 | 3 | 0.0019 | 0 | 10 | 22 | 0.0179 | 2.64E-07 | 16 | 34 | 0.0143 | 8.17E-07 | |
| | | x2 | 1 | 3 | 0.0030 | 2.22E-16 | 9 | 20 | 0.0146 | 3.85E-07 | 15 | 31 | 0.0070 | 7.97E-07 | |
| | | x3 | 1 | 3 | 0.0058 | 0 | 12 | 26 | 0.0232 | 4.88E-07 | 18 | 38 | 0.0154 | 8.51E-07 | |
| | | x4 | 2 | 5 | 0.0043 | 0 | 12 | 26 | 0.0167 | 3.8E-07 | 17 | 36 | 0.0108 | 4.98E-07 | |
| | | x5 | 4 | 9 | 0.0111 | 0 | 13 | 28 | 0.0322 | 2.71E-07 | 19 | 40 | 0.0305 | 4.77E-07 | |
| | | x6 | 4 | 9 | 0.0190 | 0 | 13 | 28 | 0.0114 | 2.41E-07 | 19 | 40 | 0.0113 | 4.89E-07 | |
| | | x7 | 6 | 13 | 0.026131 | 7.78E-07 | 96 | 193 | 0.19369 | 0 | 19 | 40 | 0.012275 | 8.26E-07 | |
| | 5000 | x1 | 1 | 3 | 0.0130 | 0 | 10 | 22 | 0.0230 | 5.91E-07 | 17 | 36 | 0.0429 | 6.85E-07 | |
| | | x2 | 1 | 3 | 0.0111 | 2.22E-16 | 9 | 20 | 0.0216 | 3.85E-07 | 15 | 31 | 0.0238 | 7.97E-07 | |
| | | x3 | 2 | 5 | 0.0118 | 0 | 13 | 28 | 0.0304 | 2.18E-07 | 20 | 42 | 0.0681 | 8.59E-07 | |
| | | x4 | 2 | 5 | 0.0075 | 0 | 12 | 26 | 0.0261 | 3.81E-07 | 17 | 36 | 0.0397 | 4.99E-07 | |
| | | x5 | 4 | 9 | 0.0163 | 0 | 13 | 28 | 0.0318 | 6.14E-07 | 20 | 42 | 0.0819 | 4.02E-07 | |
| | | x6 | 4 | 9 | 0.0141 | 0 | 13 | 28 | 0.0279 | 6.71E-07 | 20 | 42 | 0.0566 | 4.04E-07 | |
| | | x7 | 12 | 25 | 0.070389 | 5.52E-07 | 128 | 257 | 0.79955 | 0 | 19 | 40 | 0.049302 | 8.36E-07 | |
| | 10000 | x1 | 1 | 3 | 0.0052 | 0 | 10 | 22 | 0.0434 | 8.36E-07 | 17 | 36 | 0.2357 | 9.69E-07 | |
| | | x2 | 1 | 3 | 0.0061 | 2.22E-16 | 9 | 20 | 0.0627 | 3.85E-07 | 15 | 31 | 0.1445 | 7.97E-07 | |
| | | x3 | 2 | 5 | 0.0183 | 0 | 13 | 28 | 0.1303 | 3.09E-07 | 21 | 44 | 0.2196 | 4.56E-07 | |
| | | x4 | 2 | 5 | 0.0153 | 0 | 12 | 26 | 0.1123 | 3.82E-07 | 17 | 36 | 0.0756 | 4.99E-07 | |
| | | x5 | 4 | 9 | 0.0333 | 0 | 13 | 28 | 0.1147 | 8.7E-07 | 20 | 42 | 0.0929 | 5.69E-07 | |
| | | x6 | 4 | 9 | 0.1308 | 0 | 13 | 28 | 0.1170 | 9.18E-07 | 20 | 42 | 0.1012 | 5.68E-07 | |
| | | x7 | 12 | 25 | 0.10803 | 7.76E-07 | 128 | 257 | 2.0163 | 0 | 20 | 42 | 0.10385 | 4.43E-07 | |
| | 50000 | x1 | 1 | 3 | 0.0422 | 0 | 11 | 24 | 0.3925 | 3.74E-07 | 18 | 38 | 0.3618 | 8.13E-07 | |
| | | x2 | 1 | 3 | 0.0448 | 2.22E-16 | 9 | 20 | 0.2972 | 3.85E-07 | 15 | 31 | 0.4860 | 7.97E-07 | |
| | | x3 | 3 | 7 | 0.2694 | 0 | 13 | 28 | 0.3579 | 6.91E-07 | 23 | 48 | 0.8131 | 9.93E-07 | |
| | | x4 | 2 | 5 | 0.1500 | 0 | 12 | 26 | 0.2054 | 3.82E-07 | 17 | 36 | 0.2629 | 4.99E-07 | |
| | | x5 | 3 | 7 | 0.1946 | 0 | 14 | 30 | 0.3102 | 3.9E-07 | 20 | 42 | 0.3717 | 7.76E-07 | |
| | | x6 | 3 | 7 | 0.1571 | 0 | 14 | 30 | 0.4382 | 3.88E-07 | 20 | 42 | 0.4595 | 7.75E-07 | |
| | | x7 | 13 | 27 | 0.65044 | 8.93E-08 | 1000 | 2001 | 53.6336 | 226216.3 | 20 | 42 | 0.4938 | 9.89E-07 | |
| | 100000 | x1 | 1 | 3 | 0.0871 | 0 | 11 | 24 | 0.6166 | 5.29E-07 | 19 | 40 | 1.1031 | 4.31E-07 | |
| | | x2 | 1 | 3 | 0.0988 | 2.22E-16 | 9 | 20 | 0.4358 | 3.85E-07 | 15 | 31 | 0.5085 | 7.97E-07 | |
| | | x3 | 6 | 13 | 1.1322 | 0 | 13 | 28 | 0.4762 | 9.77E-07 | 27 | 56 | 1.5973 | 4.72E-07 | |
| | | x4 | 2 | 5 | 0.2506 | 0 | 12 | 26 | 0.4179 | 3.82E-07 | 17 | 36 | 0.6561 | 4.99E-07 | |
| | | x5 | 3 | 7 | 0.3017 | 0 | 14 | 30 | 0.8434 | 5.51E-07 | 21 | 44 | 0.8204 | 4.11E-07 | |
| | | x6 | 3 | 7 | 0.1887 | 0 | 14 | 30 | 0.7843 | 5.5E-07 | 21 | 44 | 1.4167 | 4.11E-07 | |
| | | x7 | 3 | 7 | 0.24567 | 0 | 1000 | 2001 | 118.0797 | 2630442 | 22 | 46 | 1.0335 | 3.78E-07 | |

Table 10: Numerical results for problems 5.2.6

| Problem | DIM | DPP | | | | | AFP | | | | | PDY | | | |
|---------|--------|-----|------|-------|----------|----------|------|-------|----------|----------|------|-------|----------|----------|--|
| | | IP | ITER | FEVAL | TIME | NORM | ITER | FEVAL | TIME | NORM | ITER | FEVAL | TIME | NORM | |
| 5.2.6 | 1000 | x1 | 11 | 24 | 0.0095 | 9.96E-07 | 12 | 26 | 0.0287 | 4.58E-07 | 6 | 14 | 0.0029 | 2.09E-07 | |
| | | x2 | 12 | 25 | 0.0099 | 6.25E-07 | 12 | 26 | 0.0120 | 6.16E-07 | 34 | 70 | 0.0129 | 6.1E-07 | |
| | | x3 | 11 | 24 | 0.0100 | 5.26E-07 | 13 | 28 | 0.0094 | 2.82E-07 | 6 | 14 | 0.0029 | 6.55E-07 | |
| | | x4 | 12 | 25 | 0.0188 | 6.2E-07 | 12 | 26 | 0.0068 | 6.07E-07 | 33 | 68 | 0.0109 | 5.47E-07 | |
| | | x5 | 11 | 24 | 0.0109 | 5.52E-07 | 12 | 26 | 0.0045 | 2.97E-07 | 48 | 98 | 0.0199 | 8.73E-07 | |
| | | x6 | 11 | 24 | 0.0093 | 5.7E-07 | 12 | 26 | 0.0142 | 2.98E-07 | 48 | 98 | 0.0207 | 5.83E-07 | |
| | | x7 | 12 | 25 | 0.010243 | 7.46E-07 | 13 | 28 | 0.005048 | 7.18E-07 | 43 | 88 | 0.016828 | 9.57E-07 | |
| | 5000 | x1 | 12 | 26 | 0.0841 | 4.56E-07 | 13 | 28 | 0.0184 | 2.57E-07 | 6 | 14 | 0.0103 | 4.68E-07 | |
| | | x2 | 12 | 26 | 0.0841 | 5.52E-07 | 13 | 28 | 0.0179 | 3.46E-07 | 35 | 72 | 0.0824 | 5.59E-07 | |
| | | x3 | 12 | 25 | 0.0856 | 6.1E-07 | 13 | 28 | 0.0287 | 6.31E-07 | 7 | 16 | 0.0273 | 9.35E-08 | |
| | | x4 | 12 | 26 | 0.0877 | 5.51E-07 | 13 | 28 | 0.0250 | 3.45E-07 | 36 | 74 | 0.1255 | 6.96E-07 | |
| | | x5 | 12 | 25 | 0.0362 | 6.41E-07 | 12 | 26 | 0.0449 | 6.65E-07 | 34 | 70 | 0.1201 | 7.37E-07 | |
| | | x6 | 12 | 25 | 0.0887 | 6.44E-07 | 12 | 26 | 0.0518 | 6.72E-07 | 41 | 84 | 0.1007 | 5.78E-07 | |
| | | x7 | 12 | 26 | 0.048016 | 6.62E-07 | 14 | 30 | 0.028524 | 4.09E-07 | 51 | 104 | 0.08635 | 6.69E-07 | |
| | 10000 | x1 | 12 | 26 | 0.0789 | 6.45E-07 | 13 | 28 | 0.1385 | 3.64E-07 | 6 | 14 | 0.0176 | 6.62E-07 | |
| | | x2 | 12 | 26 | 0.0835 | 7.8E-07 | 13 | 28 | 0.1101 | 4.9E-07 | 16 | 34 | 0.0809 | 8.16E-07 | |
| | | x3 | 12 | 26 | 0.0843 | 9.31E-07 | 13 | 28 | 0.0380 | 8.93E-07 | 7 | 16 | 0.0285 | 1.36E-07 | |
| | | x4 | 12 | 26 | 0.1742 | 7.79E-07 | 13 | 28 | 0.0385 | 4.89E-07 | 35 | 72 | 0.1107 | 5.62E-07 | |
| | | x5 | 12 | 25 | 0.1700 | 9.06E-07 | 12 | 26 | 0.0484 | 9.4E-07 | 40 | 82 | 0.1919 | 6.2E-07 | |
| | | x6 | 12 | 25 | 0.3153 | 9.05E-07 | 12 | 26 | 0.0468 | 9.47E-07 | 48 | 98 | 0.1891 | 8.04E-07 | |
| | | x7 | 12 | 26 | 0.12039 | 9.38E-07 | 14 | 30 | 0.044984 | 5.81E-07 | 49 | 100 | 0.15458 | 8.86E-07 | |
| | 50000 | x1 | 13 | 27 | 0.6376 | 7.49E-07 | 13 | 28 | 0.1757 | 8.14E-07 | 7 | 16 | 0.1551 | 9.46E-08 | |
| | | x2 | 13 | 27 | 0.6450 | 9.06E-07 | 14 | 30 | 0.1603 | 2.75E-07 | 28 | 58 | 0.6275 | 7.57E-07 | |
| | | x3 | 13 | 28 | 0.8244 | 6.34E-07 | 14 | 30 | 0.3179 | 5.01E-07 | 8 | 18 | 0.1290 | 2.69E-07 | |
| | | x4 | 13 | 27 | 0.5837 | 9.06E-07 | 14 | 30 | 0.4268 | 2.75E-07 | 26 | 54 | 0.2961 | 1.44E-07 | |
| | | x5 | 12 | 26 | 0.4919 | 7.99E-07 | 13 | 28 | 0.2059 | 5.28E-07 | 37 | 76 | 0.4636 | 7.23E-07 | |
| | | x6 | 12 | 26 | 0.3301 | 8.01E-07 | 13 | 28 | 0.1691 | 5.28E-07 | 18 | 38 | 0.5021 | 4.52E-07 | |
| | | x7 | 13 | 27 | 0.33846 | 5.84E-07 | 15 | 32 | 0.16313 | 3.27E-07 | 32 | 66 | 0.41821 | 8.94E-07 | |
| | 100000 | x1 | 12 | 25 | 0.6815 | 7.57E-07 | 14 | 30 | 0.4714 | 2.89E-07 | 7 | 16 | 0.3316 | 8.58E-07 | |
| | | x2 | 12 | 26 | 1.0329 | 4.23E-07 | 14 | 30 | 0.4583 | 3.89E-07 | 35 | 72 | 0.8718 | 7.61E-07 | |
| | | x3 | 14 | 29 | 1.2016 | 6.05E-07 | 14 | 30 | 0.7840 | 7.09E-07 | 8 | 18 | 0.2379 | 3.81E-07 | |
| | | x4 | 12 | 26 | 1.0873 | 4.23E-07 | 14 | 30 | 0.5282 | 3.89E-07 | 29 | 60 | 1.2511 | 5.25E-07 | |
| | | x5 | 11 | 24 | 0.5025 | 6.89E-07 | 13 | 28 | 0.3541 | 7.46E-07 | 35 | 72 | 0.9400 | 4.43E-07 | |
| | | x6 | 11 | 24 | 0.7048 | 6.88E-07 | 13 | 28 | 0.5373 | 7.48E-07 | 45 | 92 | 1.7498 | 4.58E-07 | |
| | | x7 | 14 | 29 | 0.71678 | 7.31E-07 | 15 | 32 | 0.36039 | 4.62E-07 | 54 | 110 | 1.4312 | 5.69E-07 | |

Table 11: Numerical results for problems 5.2.7

| Problem | DIM | DPP | | | | | AFP | | | | | PDY | | |
|---------|--------|-----|------|-------|---------|----------|------|-------|---------|----------|------|-------|---------|----------|
| | | IP | ITER | FEVAL | TIME | NORM | ITER | FEVAL | TIME | NORM | ITER | FEVAL | TIME | NORM |
| 5.2.7 | 1000 | x1 | 22 | 45 | 0.0899 | 7.3E-07 | 137 | 276 | 0.2295 | 8.32E-07 | 139 | 280 | 0.1880 | 9.73E-07 |
| | | x2 | 23 | 47 | 0.0910 | 9.24E-07 | 89 | 180 | 0.1382 | 9.65E-07 | 187 | 376 | 0.1067 | 8.84E-07 |
| | | x3 | 37 | 75 | 0.1226 | 7.56E-07 | 148 | 298 | 0.0873 | 9.51E-07 | 227 | 456 | 0.1466 | 9.23E-07 |
| | | x4 | 23 | 48 | 0.0776 | 9.85E-07 | 98 | 198 | 0.0547 | 9.06E-07 | 218 | 438 | 0.2131 | 9.53E-07 |
| | | x5 | 35 | 71 | 0.1615 | 8.3E-07 | 151 | 304 | 0.0737 | 8.57E-07 | 233 | 468 | 0.1410 | 9.99E-07 |
| | | x6 | 39 | 80 | 0.1485 | 6.3E-07 | 116 | 234 | 0.0625 | 9.92E-07 | 198 | 398 | 0.1130 | 9.95E-07 |
| | | x7 | 17 | 36 | 0.13858 | 7.49E-07 | 85 | 172 | 0.04465 | 8.79E-07 | 181 | 364 | 0.1429 | 9.44E-07 |
| | 5000 | x1 | 21 | 44 | 0.1854 | 9.88E-07 | 142 | 286 | 0.3425 | 8.88E-07 | 188 | 378 | 1.1044 | 8.86E-07 |
| | | x2 | 23 | 47 | 0.1221 | 9.24E-07 | 89 | 180 | 0.5726 | 9.65E-07 | 187 | 376 | 0.5214 | 8.84E-07 |
| | | x3 | 28 | 58 | 0.1489 | 9.74E-07 | 152 | 306 | 0.8365 | 8.24E-07 | 277 | 556 | 0.7370 | 9.68E-07 |
| | | x4 | 23 | 48 | 0.1341 | 9.79E-07 | 96 | 194 | 0.5640 | 9.06E-07 | 218 | 438 | 1.4423 | 9.56E-07 |
| | | x5 | 39 | 79 | 0.1993 | 9.45E-07 | 110 | 222 | 0.5565 | 9.23E-07 | 181 | 364 | 1.0790 | 9.64E-07 |
| | | x6 | 41 | 84 | 0.5347 | 6.48E-07 | 124 | 250 | 0.4367 | 9.9E-07 | 199 | 400 | 0.5867 | 9.65E-07 |
| | | x7 | 15 | 32 | 0.18016 | 7.55E-07 | 90 | 182 | 0.25183 | 8.87E-07 | 189 | 380 | 0.52808 | 9.27E-07 |
| | 10000 | x1 | 21 | 44 | 0.4809 | 9.82E-07 | 144 | 290 | 0.8974 | 8.97E-07 | 193 | 388 | 1.5689 | 9.37E-07 |
| | | x2 | 23 | 47 | 0.5728 | 9.24E-07 | 89 | 180 | 1.0957 | 9.65E-07 | 187 | 376 | 1.3250 | 8.84E-07 |
| | | x3 | 28 | 57 | 0.6823 | 9.07E-07 | 165 | 332 | 0.8094 | 9.26E-07 | 220 | 442 | 2.3128 | 9.39E-07 |
| | | x4 | 23 | 48 | 0.4984 | 9.78E-07 | 96 | 194 | 0.9647 | 9.06E-07 | 218 | 438 | 1.7953 | 9.56E-07 |
| | | x5 | 40 | 81 | 0.9096 | 8.75E-07 | 154 | 310 | 1.7712 | 8.76E-07 | 232 | 466 | 2.2043 | 9.66E-07 |
| | | x6 | 42 | 85 | 0.6842 | 9.55E-07 | 130 | 262 | 0.7624 | 9.31E-07 | 204 | 410 | 1.1191 | 8.87E-07 |
| | | x7 | 13 | 28 | 0.15034 | 6.79E-07 | 94 | 190 | 0.46607 | 9.58E-07 | 182 | 366 | 1.1317 | 8.96E-07 |
| | 50000 | x1 | 21 | 44 | 0.8866 | 9.78E-07 | 148 | 298 | 3.5497 | 9.81E-07 | 190 | 382 | 5.2578 | 9.44E-07 |
| | | x2 | 23 | 47 | 1.7829 | 9.24E-07 | 89 | 180 | 2.3515 | 9.65E-07 | 187 | 376 | 4.6154 | 8.84E-07 |
| | | x3 | 28 | 58 | 1.6125 | 7.12E-07 | 195 | 392 | 5.6937 | 8.16E-07 | 233 | 468 | 5.8264 | 9.9E-07 |
| | | x4 | 23 | 48 | 1.2361 | 9.77E-07 | 96 | 194 | 2.3908 | 9.08E-07 | 218 | 438 | 4.6981 | 9.56E-07 |
| | | x5 | 30 | 62 | 2.2800 | 7.75E-07 | 177 | 356 | 4.3043 | 9.44E-07 | 238 | 478 | 5.6543 | 9.93E-07 |
| | | x6 | 43 | 87 | 1.9442 | 9.27E-07 | 135 | 272 | 3.3122 | 9.1E-07 | 208 | 418 | 4.7476 | 9.21E-07 |
| | | x7 | 12 | 25 | 0.6081 | 8.89E-07 | 98 | 198 | 2.6726 | 9.58E-07 | 197 | 396 | 5.5294 | 9.21E-07 |
| | 100000 | x1 | 21 | 44 | 2.7656 | 9.77E-07 | 153 | 308 | 7.4650 | 8.22E-07 | 197 | 396 | 9.0268 | 9.98E-07 |
| | | x2 | 23 | 47 | 2.5507 | 9.24E-07 | 89 | 180 | 4.2575 | 9.65E-07 | 187 | 376 | 8.5329 | 8.84E-07 |
| | | x3 | 31 | 64 | 3.5532 | 8.28E-07 | 199 | 400 | 11.4463 | 9.61E-07 | 184 | 370 | 8.4835 | 9.73E-07 |
| | | x4 | 23 | 48 | 2.3358 | 9.77E-07 | 99 | 200 | 4.4454 | 9.07E-07 | 218 | 438 | 10.3529 | 9.56E-07 |
| | | x5 | 29 | 60 | 3.4820 | 9.53E-07 | 185 | 372 | 9.0108 | 8.44E-07 | 257 | 516 | 12.4792 | 9.96E-07 |
| | | x6 | 44 | 90 | 4.6596 | 6.74E-07 | 136 | 274 | 5.6578 | 8.58E-07 | 206 | 414 | 9.6959 | 9.11E-07 |
| | | x7 | 47 | 95 | 4.3416 | 9.07E-07 | 100 | 202 | 5.3252 | 9.78E-07 | 201 | 404 | 9.2578 | 9.48E-07 |

Table 12: Numerical results for problems 5.2.8

| Problem | DIM | DPP | | | | | AFP | | | | | PDY | | | |
|---------|--------|-----|------|-------|----------|----------|------|-------|----------|----------|------|-------|---------|----------|--|
| | | IP | ITER | FEVAL | TIME | NORM | ITER | FEVAL | TIME | NORM | ITER | FEVAL | TIME | NORM | |
| 5.2.8 | 1000 | x1 | 19 | 39 | 0.0275 | 9.57E-07 | 124 | 250 | 0.0864 | 9.68E-07 | 225 | 452 | 0.0776 | 9.68E-07 | |
| | | x2 | 22 | 45 | 0.0309 | 8.02E-07 | 119 | 240 | 0.0790 | 9.99E-07 | 205 | 412 | 0.0708 | 9.84E-07 | |
| | | x3 | 19 | 39 | 0.0264 | 9.17E-07 | 79 | 160 | 0.0567 | 9.62E-07 | 152 | 306 | 0.0526 | 9.82E-07 | |
| | | x4 | 22 | 46 | 0.0308 | 8.42E-07 | 117 | 236 | 0.0378 | 9.12E-07 | 226 | 454 | 0.0784 | 9.59E-07 | |
| | | x5 | 24 | 50 | 0.0588 | 9.5E-07 | 115 | 232 | 0.0519 | 9.91E-07 | 204 | 410 | 0.0725 | 9.77E-07 | |
| | | x6 | 45 | 92 | 0.0393 | 8.13E-07 | 205 | 412 | 0.0667 | 9.36E-07 | 333 | 668 | 0.1911 | 9.79E-07 | |
| | | x7 | 45 | 92 | 0.044892 | 8.98E-07 | 243 | 488 | 0.082021 | 9.57E-07 | 397 | 796 | 0.14266 | 9.69E-07 | |
| | 5000 | x1 | 23 | 48 | 0.0689 | 9.63E-07 | 122 | 246 | 0.1891 | 9.19E-07 | 208 | 418 | 0.3759 | 9.98E-07 | |
| | | x2 | 20 | 41 | 0.0509 | 6.83E-07 | 115 | 232 | 0.1999 | 9.7E-07 | 208 | 418 | 0.4748 | 9.66E-07 | |
| | | x3 | 16 | 33 | 0.0514 | 9.92E-07 | 75 | 152 | 0.1784 | 9.29E-07 | 157 | 316 | 0.6156 | 9.77E-07 | |
| | | x4 | 20 | 42 | 0.0477 | 8.33E-07 | 113 | 228 | 0.5794 | 9.88E-07 | 202 | 406 | 0.4927 | 9.74E-07 | |
| | | x5 | 20 | 41 | 0.0773 | 7.68E-07 | 112 | 226 | 0.3357 | 9.44E-07 | 205 | 412 | 0.3757 | 9.48E-07 | |
| | | x6 | 49 | 100 | 0.2380 | 7.72E-07 | 217 | 436 | 0.3386 | 9.3E-07 | 353 | 708 | 0.7150 | 9.7E-07 | |
| | | x7 | 49 | 99 | 0.16122 | 7.74E-07 | 257 | 516 | 0.37349 | 8.9E-07 | 417 | 836 | 0.66291 | 9.82E-07 | |
| | 10000 | x1 | 19 | 40 | 0.3933 | 8.84E-07 | 119 | 240 | 0.4528 | 9.72E-07 | 219 | 440 | 1.5934 | 9.71E-07 | |
| | | x2 | 17 | 36 | 0.3484 | 5.52E-07 | 114 | 230 | 1.1297 | 8.95E-07 | 200 | 402 | 0.8693 | 9.98E-07 | |
| | | x3 | 16 | 34 | 0.3345 | 9.03E-07 | 72 | 146 | 0.2537 | 9.78E-07 | 148 | 298 | 1.3977 | 9.58E-07 | |
| | | x4 | 21 | 44 | 0.4899 | 7.68E-07 | 112 | 226 | 0.4053 | 9.11E-07 | 222 | 446 | 0.9129 | 9.6E-07 | |
| | | x5 | 20 | 41 | 0.1616 | 6.72E-07 | 111 | 224 | 0.7957 | 9.82E-07 | 197 | 396 | 1.6538 | 9.86E-07 | |
| | | x6 | 45 | 92 | 0.3350 | 6.6E-07 | 223 | 448 | 1.2007 | 9.28E-07 | 347 | 696 | 1.7237 | 9.98E-07 | |
| | | x7 | 44 | 90 | 0.34925 | 8.48E-07 | 261 | 524 | 1.8976 | 9.78E-07 | 414 | 830 | 2.6929 | 9.85E-07 | |
| | 50000 | x1 | 18 | 37 | 0.7895 | 8.1E-07 | 116 | 234 | 2.4448 | 9.25E-07 | 204 | 410 | 4.4595 | 9.76E-07 | |
| | | x2 | 17 | 35 | 1.1681 | 8.62E-07 | 110 | 222 | 1.9797 | 9.8E-07 | 201 | 404 | 3.8075 | 9.87E-07 | |
| | | x3 | 19 | 40 | 1.0530 | 4.46E-07 | 69 | 140 | 1.3805 | 9.06E-07 | 152 | 306 | 3.2491 | 9.9E-07 | |
| | | x4 | 18 | 38 | 0.7011 | 9.3E-07 | 107 | 216 | 2.3680 | 9.93E-07 | 198 | 398 | 3.8811 | 9.96E-07 | |
| | | x5 | 17 | 35 | 0.8687 | 7.37E-07 | 107 | 216 | 2.0567 | 9.57E-07 | 196 | 394 | 3.4828 | 9.62E-07 | |
| | | x6 | 33 | 68 | 1.9300 | 5.95E-07 | 235 | 472 | 4.1514 | 9.7E-07 | 364 | 730 | 6.3473 | 9.6E-07 | |
| | | x7 | 47 | 96 | 1.5811 | 7.87E-07 | 275 | 552 | 4.8473 | 9.01E-07 | 423 | 848 | 9.2912 | 9.73E-07 | |
| | 100000 | x1 | 17 | 35 | 1.8459 | 8.2E-07 | 114 | 230 | 5.6932 | 9.81E-07 | 210 | 422 | 8.2434 | 9.9E-07 | |
| | | x2 | 16 | 34 | 1.5101 | 6.25E-07 | 109 | 220 | 4.4860 | 9.08E-07 | 215 | 432 | 8.1169 | 1E-06 | |
| | | x3 | 18 | 38 | 1.6902 | 5.94E-07 | 67 | 136 | 2.0429 | 9.6E-07 | 155 | 312 | 6.2953 | 9.74E-07 | |
| | | x4 | 18 | 38 | 2.0344 | 7.9E-07 | 107 | 216 | 4.8187 | 9.19E-07 | 211 | 424 | 8.0925 | 9.6E-07 | |
| | | x5 | 16 | 34 | 1.6648 | 7.31E-07 | 106 | 214 | 4.4812 | 9.95E-07 | 212 | 426 | 8.0163 | 9.92E-07 | |
| | | x6 | 37 | 76 | 3.1285 | 9.6E-07 | 241 | 484 | 8.8279 | 9.16E-07 | 373 | 748 | 14.4183 | 9.48E-07 | |
| | | x7 | 51 | 104 | 3.5354 | 9.71E-07 | 279 | 560 | 10.8699 | 9.89E-07 | 427 | 856 | 15.0399 | 9.67E-07 | |

Table 13: Numerical results for problems 5.2.9–5.2.10

| Problem | DIM | DPP | | | | | AFP | | | | | PDY | | | |
|---------|--------|-----|------|-------|----------|----------|------|-------|----------|----------|------|-------|----------|----------|--|
| | | IP | ITER | FEVAL | TIME | NORM | ITER | FEVAL | TIME | NORM | ITER | FEVAL | TIME | NORM | |
| 5.2.9 | 1000 | x1 | 13 | 28 | 0.0101 | 7.99E-07 | 34 | 70 | 0.0239 | 6.42E-07 | 29 | 60 | 0.0063 | 7.81E-09 | |
| | | x2 | 13 | 28 | 0.0096 | 5.78E-07 | 33 | 68 | 0.0202 | 7.6E-07 | 26 | 54 | 0.0068 | 6.89E-07 | |
| | | x3 | 17 | 35 | 0.0110 | 4.29E-07 | 34 | 70 | 0.0208 | 9.25E-07 | 25 | 52 | 0.0089 | 7.61E-07 | |
| | | x4 | 13 | 28 | 0.0089 | 6.17E-07 | 32 | 66 | 0.0226 | 9.26E-07 | 27 | 56 | 0.0067 | 7.55E-07 | |
| | | x5 | 13 | 28 | 0.0105 | 7.94E-07 | 31 | 64 | 0.0178 | 7.55E-07 | 31 | 64 | 0.0089 | 6.25E-07 | |
| | | x6 | 16 | 34 | 0.0234 | 4.18E-07 | 44 | 90 | 0.0233 | 6.47E-07 | 28 | 58 | 0.0107 | 2.59E-07 | |
| | | x7 | 16 | 34 | 0.04833 | 9.78E-07 | 47 | 96 | 0.011614 | 9.75E-07 | 36 | 74 | 0.008849 | 6.02E-08 | |
| | 5000 | x1 | 15 | 32 | 0.1164 | 5.81E-07 | 34 | 70 | 0.0393 | 6.4E-07 | 34 | 70 | 0.0775 | 8.16E-07 | |
| | | x2 | 14 | 30 | 0.0727 | 7.51E-07 | 33 | 68 | 0.0559 | 7.9E-07 | 27 | 56 | 0.0281 | 8.45E-08 | |
| | | x3 | 17 | 35 | 0.0382 | 6.07E-07 | 39 | 80 | 0.0409 | 8.14E-07 | 30 | 62 | 0.0259 | 5.33E-07 | |
| | | x4 | 14 | 29 | 0.0344 | 6.97E-07 | 35 | 72 | 0.0372 | 9.67E-07 | 41 | 84 | 0.0322 | 7.52E-07 | |
| | | x5 | 15 | 32 | 0.0349 | 3.93E-07 | 36 | 74 | 0.0483 | 6.8E-07 | 27 | 56 | 0.0289 | 5.59E-07 | |
| | | x6 | 17 | 36 | 0.0465 | 4E-07 | 43 | 88 | 0.0493 | 6.29E-07 | 41 | 84 | 0.1155 | 5.04E-07 | |
| | | x7 | 18 | 37 | 0.050259 | 9.32E-07 | 47 | 96 | 0.046382 | 8.35E-07 | 35 | 72 | 0.031912 | 4.88E-07 | |
| | 10000 | x1 | 16 | 34 | 0.0653 | 3.45E-07 | 34 | 70 | 0.1837 | 7.33E-07 | 28 | 58 | 0.1479 | 6.94E-07 | |
| | | x2 | 15 | 32 | 0.1453 | 9.55E-07 | 33 | 68 | 0.1782 | 9.39E-07 | 28 | 58 | 0.1326 | 6.64E-07 | |
| | | x3 | 22 | 46 | 0.1089 | 4.59E-07 | 44 | 90 | 0.2739 | 7.04E-07 | 42 | 86 | 0.1028 | 7.31E-11 | |
| | | x4 | 16 | 33 | 0.2414 | 5.89E-07 | 34 | 70 | 0.0946 | 7.36E-07 | 25 | 52 | 0.0468 | 3.29E-07 | |
| | | x5 | 14 | 30 | 0.1310 | 9.23E-07 | 34 | 70 | 0.0732 | 9.24E-07 | 27 | 56 | 0.0544 | 6.74E-07 | |
| | | x6 | 18 | 38 | 0.1740 | 4.4E-07 | 48 | 98 | 0.1138 | 6.16E-07 | 33 | 68 | 0.0626 | 5.81E-08 | |
| | | x7 | 18 | 38 | 0.17212 | 7.63E-07 | 57 | 116 | 0.099218 | 7.2E-07 | 29 | 60 | 0.054973 | 4.88E-08 | |
| | 50000 | x1 | 16 | 34 | 0.5530 | 6.76E-07 | 63 | 128 | 1.1209 | 8.37E-07 | 32 | 66 | 0.3713 | 9.69E-07 | |
| | | x2 | 16 | 34 | 0.6400 | 3.73E-07 | 61 | 124 | 1.5469 | 9.64E-07 | 33 | 68 | 0.5687 | 7.92E-07 | |
| | | x3 | 16 | 34 | 0.5715 | 9.1E-07 | 53 | 108 | 0.6618 | 9.68E-07 | 35 | 72 | 0.8102 | 7.55E-07 | |
| | | x4 | 17 | 35 | 0.4514 | 5.86E-07 | 57 | 116 | 0.7697 | 8.04E-07 | 33 | 68 | 0.3161 | 5.82E-07 | |
| | | x5 | 15 | 32 | 0.3028 | 3.93E-07 | 36 | 74 | 0.3289 | 9.24E-07 | 29 | 60 | 0.2352 | 7.67E-07 | |
| | | x6 | 17 | 36 | 0.3408 | 4.53E-07 | 49 | 100 | 0.9080 | 6.18E-07 | 36 | 74 | 0.3400 | 9.24E-07 | |
| | | x7 | 17 | 36 | 0.35098 | 6.45E-07 | 54 | 110 | 0.34574 | 9.89E-07 | 41 | 84 | 0.30195 | 5.43E-07 | |
| | 100000 | x1 | 17 | 36 | 1.0030 | 5.13E-07 | 81 | 164 | 2.8790 | 7.04E-07 | 34 | 70 | 0.9616 | 6.98E-07 | |
| | | x2 | 17 | 36 | 1.0670 | 6.53E-07 | 79 | 160 | 2.7210 | 7.76E-07 | 34 | 70 | 0.7890 | 8.9E-07 | |
| | | x3 | 19 | 39 | 0.9326 | 3.62E-07 | 46 | 94 | 1.3439 | 8.26E-07 | 62 | 126 | 1.1449 | 7.39E-07 | |
| | | x4 | 16 | 34 | 0.5609 | 5.9E-07 | 99 | 200 | 3.8309 | 7.68E-07 | 35 | 72 | 1.0334 | 7.19E-07 | |
| | | x5 | 16 | 34 | 0.9415 | 4.72E-07 | 37 | 76 | 0.7650 | 7.97E-07 | 33 | 68 | 0.8900 | 5.29E-07 | |
| | | x6 | 17 | 36 | 1.0918 | 3.48E-07 | 56 | 114 | 1.7541 | 7.62E-07 | 43 | 88 | 0.7226 | 2.59E-07 | |
| | | x7 | 18 | 38 | 0.7502 | 7.1E-07 | 56 | 114 | 1.0845 | 8.44E-07 | 43 | 88 | 0.91235 | 6.08E-07 | |
| 5.2.10 | 4 | x1 | 39 | 79 | 0.0170 | 8.05E-07 | 52 | 105 | 0.0245 | 8.64E-07 | 57 | 115 | 0.0126 | 8.4E-07 | |
| | | x2 | 37 | 75 | 0.0109 | 9.03E-07 | 56 | 113 | 0.0096 | 9.06E-07 | 52 | 105 | 0.0109 | 8.24E-07 | |
| | | x3 | 50 | 101 | 0.0145 | 9.75E-07 | 56 | 113 | 0.0095 | 8.89E-07 | 59 | 119 | 0.0113 | 8.08E-07 | |
| | | x4 | 38 | 77 | 0.0116 | 7.84E-07 | 54 | 109 | 0.0090 | 9.46E-07 | 57 | 115 | 0.0119 | 8.21E-07 | |
| | | x5 | 40 | 81 | 0.0114 | 8.7E-07 | 40 | 81 | 0.0074 | 7.51E-07 | 39 | 79 | 0.0082 | 9.28E-07 | |
| | | x6 | 28 | 57 | 0.0079 | 9.94E-07 | 57 | 115 | 0.0099 | 9.86E-07 | 58 | 117 | 0.0112 | 9.95E-07 | |
| | | x7 | 46 | 93 | 0.029779 | 5.97E-07 | 57 | 115 | 0.017793 | 9.32E-07 | 62 | 125 | 0.047396 | 7.65E-07 | |