

Show using truth tables or expansion on why $!(P \& Q)$ is logically equal to $(!P \vee !Q)$ * 4 points

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By expansion:

$$!(P \& Q) = (!P \vee !Q)$$

let $P = \text{true}$, $Q = \text{false}$

$$!(\text{true} \& \text{false}) = (!\text{true} \vee !\text{false})$$

$$!(\text{false}) = (\text{false} \vee \text{true})$$

$$\text{true} = \text{true}$$

By Truth Table:

$!(P \& Q)$				$(!P \vee !Q)$				
P	Q	$P \& Q$	$!(P \& Q)$	P	Q	$!P$	$!Q$	$!P \vee !Q$
T	T	T	F	T	T	F	F	F
T	F	F	T	T	F	F	T	T
F	T	F	T	F	T	T	F	T
F	F	F	T	F	F	T	T	T

The truth table covers all possible values and proves $!(P \& Q)$ is equal to $(!P \vee !Q)$.
It is always better to prove using truth table.

Make a truth table for the following logical expression: *

4 points

$(A \ \&\& \ B) \ || \ (! (A \ \&\& \ C) \ \&\& \ (B \ || \ C))$

Values of A, B, C are boolean

Simplify each expression as much as possible

e.g. Make separate columns for A, B, $(A \ \&\& \ B)$, $(A \ \&\& \ C)$, $!(A \ \&\& \ C)$, $!(A \ \&\& \ C) \ \&\& \ (B \ || \ C)$, $(A \ \&\& \ B) \ || \ (! (A \ \&\& \ C) \ \&\& \ (B \ || \ C))$

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A	B	C	$A \ \&\& \ B$	$A \ \&\& \ C$	$!(A \ \&\& \ C)$	$B \ \ C$	$!(A \ \&\& \ C) \ \&\& \ (B \ \ C)$	$(A \ \&\& \ B) \ \ (! (A \ \&\& \ C) \ \&\& \ (B \ \ C))$
T	T	T	T	T	F	T	F	T
T	T	F	T	F	T	T	T	T
T	F	T	F	T	F	T	F	F
T	F	F	F	F	T	F	F	F
F	T	T	F	F	T	T	T	T
F	T	F	F	F	T	T	T	T
F	F	T	F	F	T	T	T	T
F	F	F	F	F	T	F	F	F

Simplifying the expression is important when creating a truth table.