An Introduction to Counting

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Introduction

Note that

i. first point
ii. second point
iii. third point

1 Binomial Theorem

Definition 1 (Factorial n!)**.** The count of all ways to permute a set of n distinct objects

$$n! = \prod_{i=1}^{n} i$$

Definition 2 (Binomial Coefficient)**.** $\binom{n}{k} = \frac{n!}{k!(n-k)!}$

Proof. □

2 Multinomial Theorem

Lemma 1. *We have*

$$\int_0^{\pi} \sin(3x)\,\mathrm{d}x = \frac{2}{3}.$$

Proof. A direct computation yields

$$\begin{aligned}\int_0^{\pi} \sin(3x)\,\mathrm{d}x &= \frac{1}{3}\int_0^{3\pi} \sin u\,\mathrm{d}u, \qquad u = 3x,\\ &= \frac{1}{3}\big[-\cos u\big]_0^{3\pi}\\ &= \frac{1}{3}\big[1-(-1)\big]\\ &= \frac{2}{3}.\end{aligned}$$

□

Remark 1. This is interesting since...

3 Possible Outcomes to Equations