

## Exercise Internet Users Logged in a Server Data- Solution

There is no evidence of existence of seasonal unit root --  $D=0$ .

There is evidence of existence of unit root so difference --  $d=1$

Better results if we difference one more so  $d=2$  because of the unit root test (more significant if  $d=2$ ).

If in first (needed) and seasonally differenced data (not needed) there is a peak in the seasonal lag in the PACF then the  $P=1$ . If there is a second peak in the  $2 \times$  seasonal lag then  $P=2$ .

If in first (needed) and seasonally differenced data (not needed) there is a peak in the seasonal lag in the ACF then the  $Q=1$ . If there is a second peak in the  $2 \times$  seasonal lag then  $Q=2$ .

Since  $D=0$  no need to check the above two.

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Process	ACF	PACF
AR(1)	Exponential decay: on positive side if $\phi_1 > 0$ and alternating in sign starting on negative side if $\phi_1 < 0$ .	Spike at lag 1, then cuts off to zero: spike positive if $\phi_1 > 0$ , negative if $\phi_1 < 0$ .
AR(p)	Exponential decay or damped sine-wave. The exact pattern depends on the signs and sizes of $\phi_1, \dots, \phi_p$ .	Spikes at lags 1 to $p$ , then cuts off to zero.
MA(1)	Spike at lag 1 then cuts off to zero: spike positive if $\theta_1 < 0$ , negative if $\theta_1 > 0$ .	Exponential decay: on negative side if $\theta_1 > 0$ and alternating in sign starting on positive side if $\theta_1 < 0$ .
MA(q)	Spikes at lags 1 to $q$ , then cuts off to zero.	Exponential decay or damped sine-wave. The exact pattern depends on the signs and sizes of $\theta_1, \dots, \theta_q$ .

Table 7-2: Expected patterns in the ACF and PACF for simple AR and MA models

ACF --  $\rightarrow$  AR(p) because we have damped sign wave

PACF --  $\rightarrow$  Spikes at lag 1, 2

From the two above  $p=2$  and  $d=2$

So our model is ARIMA (2,2,0) (0,0,0)