Contents

1 Setting

1.1 vimrc

```
set nocp ai si nu et bs=2 mouse=a
set ts=2 sts=2 sw=2 hls showmatch
set ruler rulerformat=%17.(%l:%c%)
set noswapfile autoread wildmenu wildmode=list:longest
syntax on | colorscheme evening

map <F5> <ESC>:w<CR>:!g++ -g -Wall --std=c++0x -O2 %:r.cpp -o %:r && %:r < %:r.in > %:r.out<CR>
map <F6> <ESC>:w<CR>:!g++ -g -Wall --std=c++0x -O2 %:r.cpp -o %:r && %:r < %:r.in<CR>

map k gk
map j gj

map <C-h> <C-w>h
map <C-j> <C-w>j
map <C-k> <C-w>k
map <C-l> <C-w>l
```

```
map <C-t> :tabnew<CR>

command -nargs=1 PS :cd d:/ | :vi <args>.cpp | vs <args>.in | sp <args>.out
```

2 Math

2.1 Basic Arithmetic

```
typedef long long ll;
typedef unsigned long long ull;

// calculate lg2(a)
inline int lg2(ll a)
{
    return 63 - __builtin_clzll(a);
}

// calculate the number of 1-bits
inline int bitcount(ll a)
{
    return __builtin_popcountll(a);
}

// calculate ceil(a/b)
// |a|, |b| <= (2^63)-1 (does not dover -2^63)
ll ceildiv(ll a, ll b) {
    if (b < 0) return ceildiv(-a, -b);
    if (a < 0) return (-a) / b;
    return ((ull)a + (ull)b - 1ull) / b;
}

// calculate floor(a/b)
// |a|, |b| <= (2^63)-1 (does not cover -2^63)
ll floordiv(ll a, ll b) {
    if (b < 0) return floordiv(-a, -b);
    if (a >= 0) return a / b;
    return -(ll)(((ull)(-a) + b - 1) / b);
}

// calculate a*b % m
// x86-64 only
ll large_mod_mul(ll a, ll b, ll m)
{
    return ll((__int128)a*(__int128)b%m);
}

// calculate a*b % m
// |m| < 2^62, x86 available
// O(logb)
ll large_mod_mul(ll a, ll b, ll m)
{
    a %= m; b %= m; ll r = 0, v = a;
    while (b) {
        if (b&1) r = (r + v) % m;
        b >>= 1;
        v = (v << 1) % m;
    }
    return r;
}

// calculate n^k % m
ll modpow(ll n, ll k, ll m) {
    ll ret = 1;
    n %= m;
    while (k) {
        if (k & 1) ret = large_mod_mul(ret, n, m);
        n = large_mod_mul(n, n, m);
        k /= 2;
    }
    return ret;
}

// calculate gcd(a, b)
ll gcd(ll a, ll b) {
    return b == 0 ? a : gcd(b, a % b);
}

// find a pair (c, d) s.t. ac + bd = gcd(a, b)
pair<ll, ll> extended_gcd(ll a, ll b) {
    if (b == 0) return { 1, 0 };
    auto t = extended_gcd(b, a % b);
    return { t.second, t.first - t.second * (a / b) };
}

// find x in [0,m) s.t. ax === gcd(a, m) (mod m)
ll modinverse(ll a, ll m) {
    return (extended_gcd(a, m).first % m + m) % m;
}

// calculate modular inverse for 1 ~ n
void calc_range_modinv(int n, int mod, int ret[]) {
    ret[1] = 1;
    for (int i = 2; i <= n; ++i)
        ret[i] = (ll)(mod - mod/i) * ret[mod%i] % mod;
}
```

2.2 Sieve Methods : Prime, Divisor, Euler phi

```
// find prime numbers in 1 ~ n
// ret[x] = false  ->  x is prime
// O(n*loglogn)
void sieve(int n, bool ret[]) {
    for (int i = 2; i * i <= n; ++i)
        if (!ret[i])
            for (int j = i * i; j <= n; j += i)
                ret[i] = true;
```

```
}

// calculate number of divisors for 1 ~ n
// when you need to calculate sum, change += 1 to += i
// O(n*logn)
void num_of_divisors(int n, int ret[]) {
    for (int i = 1; i <= n; ++i)
        for (int j = i; j <= n; j += i)
            ret[j] += 1;
}

// calculate euler totient function for 1 ~ n
// phi(n) = number of x s.t. 0 < x < n && gcd(n, x) = 1
// O(n*loglogn)
void euler_phi(int n, int ret[]) {
    for (int i = 1; i <= n; ++i) ret[i] = i;
    for (int i = 2; i <= n; ++i)
        if (ret[i] == i)
            for (int j = i; j <= n; j += i)
                ret[j] -= ret[j] / i;
}
```

2.3 Primality Test

```
bool test_witness(ull a, ull n, ull s) {
    if (a >= n) a %= n;
    if (a <= 1) return true;
    ull d = n >> s;
    ull x = modpow(a, d, n);
    if (x == 1 || x == n-1) return true;
    while (s-- > 1) {
        x = large_mod_mul(x, x, n);
        if (x == 1) return false;
        if (x == n-1) return true;
    }
    return false;
}

// test whether n is prime
// based on miller-rabin test
// O(logn*logn)
bool is_prime(ull n) {
    if (n == 2) return true;
    if (n < 2 || n % 2 == 0) return false;

    ull d = n >> 1, s = 1;
    for(; (d&1) == 0; s++) d >>= 1;

#define T(a) test_witness(a##ull, n, s)
    if (n < 4759123141ull) return T(2) && T(7) && T(61);
    return T(2) && T(325) && T(9375) && T(28178)
        && T(450775) && T(9780504) && T(1795265022);
#undef T
}
```

2.4 Chinese Remainder Theorem

```
// find x s.t.  x === a[0] (mod n[0])
//              === a[1] (mod n[1])
//              ...
// assumption: gcd(n[i], n[j]) = 1
ll chinese_remainder(ll* a, ll* n, int size) {
    if (size == 1) return *a;
    ll tmp = modinverse(n[0], n[1]);
    ll tmp2 = (tmp * (a[1] - a[0]) % n[1] + n[1]) % n[1];
    ll ora = a[1];
    ll tgcd = gcd(n[0], n[1]);
    a[1] = a[0] + n[0] / tgcd * tmp2;
    n[1] *= n[0] / tgcd;
    ll ret = chinese_remainder(a + 1, n + 1, size - 1);
    n[1] /= n[0] / tgcd;
    a[1] = ora;
    return ret;
}
```

2.5 Modular Equation

$x \equiv a \pmod m$, $x \equiv b \pmod n$을 만족시키는 x를 구하는 방법.

m과 n을 소인수분해한 후 소수의 제곱꼴의 합동식들로 각각 쪼갠다. 이 때 특정 소수에 대하여 모순이 생기면 불가능한 경우고, 모든 소수에 대해서 모순이 생기지 않으면 전체 식을 CRT로 합치면 된다. 이제 $x \equiv x_1 \pmod{p^{k_1}}$과 $x \equiv x_2 \pmod{p^{k_2}}$가 모순이 생길 조건은 $k_1 \le k_2$라고 했을 때, $x_1 \not\equiv x_2 \pmod{p^{k_1}}$인 경우이다. 모순이 생기지 않았을 때 답을 구하려면 CRT로 합칠 때 $x \equiv x_2 \pmod{p^{k_2}}$만을 남기고 합쳐주면 된다.

2.6 Rational Number Class

```
struct rational {
    long long p, q;

    void red() {
        if (q < 0) {
            p = -p;
            q = -q;
        }
        ll t = gcd((p >= 0 ? p : -p), q);
        p /= t;
        q /= t;
    }

    rational(): p(0), q(1) {}
    rational(long long p_): p(p_), q(1) {}
    rational(long long p_, long long q_): p(p_), q(q_) { red(); }

    bool operator==(const rational& rhs) const {
        return p == rhs.p && q == rhs.q;
```

```
    }
    bool operator!=(const rational& rhs) const {
        return p != rhs.p || q != rhs.q;
    }
    bool operator<(const rational& rhs) const {
        return p * rhs.q < rhs.p * q;
    }
    rational operator+(const rational& rhs) const {
        ll g = gcd(q, rhs.q);
        return rational(p * (rhs.q / g) + rhs.p * (q / g), (q / g) * rhs.q);
    }
    rational operator-(const rational& rhs) const {
        ll g = gcd(q, rhs.q);
        return rational(p * (rhs.q / g) - rhs.p * (q / g), (q / g) * rhs.q);
    }
    rational operator*(const rational& rhs) const {
        return rational(p * rhs.p, q * rhs.q);
    }
    rational operator/(const rational& rhs) const {
        return rational(p * rhs.q, q * rhs.p);
    }
};
```

2.7 Burnside's Lemma

경우의 수를 세는데, 특정 transform operation(회전, 반사, ..) 해서 같은 경우들은 하나로 친다. 전체 경우의 수는?

- 각 operation마다 이 operation을 했을 때 변하지 않는 경우의 수를 센다 (단, "아무것도 하지 않는다"라는 operation도 있어야 함!)

- 전체 경우의 수를 더한 후, operation의 수로 나눈다. (답이 맞다면 항상 나누어 떨어져야 한다)

2.8 Kirchoff's Theorem

그래프의 스패닝 트리의 개수를 구하는 정리.

무향 그래프의 Laplacian matrix L를 만든다. 이것은 (정점의 차수 대각 행렬) - (인접행렬)이다. L에서 행과 열을 하나씩 제거한 것을 L'라 하자. 어느 행/열이든 관계 없다. 그래프의 스패닝 트리의 개수는 $det(L')$이다.

2.9 Lucas Theorem

```
// calculate nCm % p  when p is prime
int lucas_theorem(const char *n, const char *m, int p) {
    vector<int> np, mp;
    int i;
    for (i = 0; n[i]; i++) {
        if (n[i] == '0' && np.empty()) continue;
        np.push_back(n[i] - '0');
    }
    for (i = 0; m[i]; i++) {
        if (m[i] == '0' && mp.empty()) continue;
        mp.push_back(m[i] - '0');
    }

    int ret = 1;
    int ni = 0, mi = 0;
    while (ni < np.size() || mi < mp.size()) {
        int nmod = 0, mmod = 0;
        for (i = ni; i < np.size(); i++) {
            if (i + 1 < np.size())
                np[i + 1] += (np[i] % p) * 10;
            else
                nmod = np[i] % p;
            np[i] /= p;
        }
        for (i = mi; i < mp.size(); i++) {
            if (i + 1 < mp.size())
                mp[i + 1] += (mp[i] % p) * 10;
            else
                mmod = mp[i] % p;
            mp[i] /= p;
        }
        while (ni < np.size() && np[ni] == 0) ni++;
        while (mi < mp.size() && mp[mi] == 0) mi++;
        // implement binomial. binomial(m,n) = 0 if m < n
        ret = (ret * binomial(nmod, mmod)) % p;
    }
    return ret;
}
```

2.10 Fast Fourier Transform

```
void fft(int sign, int n, double *real, double *imag) {
    double theta = sign * 2 * pi / n;
    for (int m = n; m >= 2; m >>= 1, theta *= 2) {
        double wr = 1, wi = 0, c = cos(theta), s = sin(theta);
        for (int i = 0, mh = m >> 1; i < mh; ++i) {
            for (int j = i; j < n; j += m) {
                int k = j + mh;
                double xr = real[j] - real[k], xi = imag[j] - imag[k];
                real[j] += real[k], imag[j] += imag[k];
                real[k] = wr * xr - wi * xi, imag[k] = wr * xi + wi * xr;
            }
            double _wr = wr * c - wi * s, _wi = wr * s + wi * c;
            wr = _wr, wi = _wi;
        }
    }
    for (int i = 1, j = 0; i < n; ++i) {
        for (int k = n >> 1; k > (j ^= k); k >>= 1);
        if (j < i) swap(real[i], real[j]), swap(imag[i], imag[j]);
```

```
    }
}
// Compute Poly(a)*Poly(b), write to r; Indexed from 0
// O(n*logn)
int mult(int *a, int n, int *b, int m, int *r) {
    const int maxn = 100;
    static double ra[maxn], rb[maxn], ia[maxn], ib[maxn];
    int fn = 1;
    while (fn < n + m) fn <<= 1; // n + m: interested length
    for (int i = 0; i < n; ++i) ra[i] = a[i], ia[i] = 0;
    for (int i = n; i < fn; ++i) ra[i] = ia[i] = 0;
    for (int i = 0; i < m; ++i) rb[i] = b[i], ib[i] = 0;
    for (int i = m; i < fn; ++i) rb[i] = ib[i] = 0;
    fft(1, fn, ra, ia);
    fft(1, fn, rb, ib);
    for (int i = 0; i < fn; ++i) {
        double real = ra[i] * rb[i] - ia[i] * ib[i];
        double imag = ra[i] * ib[i] + rb[i] * ia[i];
        ra[i] = real, ia[i] = imag;
    }
    fft(-1, fn, ra, ia);
    for (int i = 0; i < fn; ++i) r[i] = (int)floor(ra[i] / fn + 0.5);
    return fn;
}
```

2.11 Matrix Operations

```
const int MATSZ = 100;

inline bool is_zero(double a) { return fabs(a) < 1e-9; }

// out = A^(-1), returns det(A)
// A becomes invalid after call this
// O(n^3)
double inverse_and_det(int n, double A[][MATSZ], double out[][MATSZ]) {
    double det = 1;
    for (int i = 0; i < n; i++) {
        for (int j = 0; j < n; j++) out[i][j] = 0;
        out[i][i] = 1;
    }
    for (int i = 0; i < n; i++) {
        if (is_zero(A[i][i])) {
            double maxv = 0;
            int maxid = -1;
            for (int j = i + 1; j < n; j++) {
                auto cur = fabs(A[j][i]);
                if (maxv < cur) {
                    maxv = cur;
                    maxid = j;
                }
            }
            if (maxid == -1 || is_zero(A[maxid][i])) return 0;
            for (int k = 0; k < n; k++) {
                A[i][k] += A[maxid][k];
                out[i][k] += out[maxid][k];
            }
        }
        det *= A[i][i];
        double coeff = 1.0 / A[i][i];
        for (int j = 0; j < n; j++) A[i][j] *= coeff;
        for (int j = 0; j < n; j++) out[i][j] *= coeff;
        for (int j = 0; j < n; j++) if (j != i) {
            double mp = A[j][i];
            for (int k = 0; k < n; k++) A[j][k] -= A[i][k] * mp;
            for (int k = 0; k < n; k++) out[j][k] -= out[i][k] * mp;
        }
    }
    return det;
}
```

2.12 Gaussian Elimination

```
const double EPS = 1e-10;
typedef vector<vector<double>> VVD;

// Gauss-Jordan elimination with full pivoting.
// solving systems of linear equations (AX=B)
// INPUT:    a[][] = an n*n matrix
//           b[][] = an n*m matrix
// OUTPUT:   X      = an n*m matrix (stored in b[][])
//           A^{-1} = an n*n matrix (stored in a[][])
// O(n^3)
bool gauss_jordan(VVD& a, VVD& b) {
    const int n = a.size();
    const int m = b[0].size();
    vector<int> irow(n), icol(n), ipiv(n);

    for (int i = 0; i < n; i++) {
        int pj = -1, pk = -1;
        for (int j = 0; j < n; j++) if (!ipiv[j])
            for (int k = 0; k < n; k++) if (!ipiv[k])
                if (pj == -1 || fabs(a[j][k]) > fabs(a[pj][pk])) { pj = j; pk =
                    k; }
        if (fabs(a[pj][pk]) < EPS) return false; // matrix is singular
        ipiv[pk]++;
        swap(a[pj], a[pk]);
        swap(b[pj], b[pk]);
        irow[i] = pj;
        icol[i] = pk;

        double c = 1.0 / a[pk][pk];
        a[pk][pk] = 1.0;
        for (int p = 0; p < n; p++) a[pk][p] *= c;
        for (int p = 0; p < m; p++) b[pk][p] *= c;
        for (int p = 0; p < n; p++) if (p != pk) {
            c = a[p][pk];
            a[p][pk] = 0;
            for (int q = 0; q < n; q++) a[p][q] -= a[pk][q] * c;
```

```
            for (int q = 0; q < m; q++) b[p][q] -= b[pk][q] * c;
        }
    }
    for (int p = n - 1; p >= 0; p--) if (irow[p] != icol[p]) {
        for (int k = 0; k < n; k++) swap(a[k][irow[p]], a[k][icol[p]]);
    }
    return true;
}
```

2.13 Simplex Algorithm

```
// Two-phase simplex algorithm for solving linear programs of the form
//     maximize     c^T x
//     subject to   Ax <= b
//                   x >= 0
// INPUT: A -- an m x n matrix
//        b -- an m-dimensional vector
//        c -- an n-dimensional vector
//        x -- a vector where the optimal solution will be stored
// OUTPUT: value of the optimal solution (infinity if unbounded
//         above, nan if infeasible)
// To use this code, create an LPSolver object with A, b, and c as
// arguments.  Then, call Solve(x).
typedef vector<double> VD;
typedef vector<VD> VVD;
typedef vector<int> VI;
const double EPS = 1e-9;

struct LPSolver {
    int m, n;
    VI B, N;
    VVD D;

    LPSolver(const VVD& A, const VD& b, const VD& c) :
        m(b.size()), n(c.size()), N(n + 1), B(m), D(m + 2, VD(n + 2)) {
        for (int i = 0; i < m; i++) for (int j = 0; j < n; j++) D[i][j] = A[i][j
          ];
        for (int i = 0; i < m; i++) { B[i] = n + i; D[i][n] = -1; D[i][n + 1] =
          b[i]; }
        for (int j = 0; j < n; j++) { N[j] = j; D[m][j] = -c[j]; }
        N[n] = -1; D[m + 1][n] = 1;
    }

    void pivot(int r, int s) {
        double inv = 1.0 / D[r][s];
        for (int i = 0; i < m + 2; i++) if (i != r)
            for (int j = 0; j < n + 2; j++) if (j != s)
                D[i][j] -= D[r][j] * D[i][s] * inv;
        for (int j = 0; j < n + 2; j++) if (j != s) D[r][j] *= inv;
        for (int i = 0; i < m + 2; i++) if (i != r) D[i][s] *= -inv;
        D[r][s] = inv;
        swap(B[r], N[s]);
    }

    bool simplex(int phase) {
        int x = phase == 1 ? m + 1 : m;
        while (true) {
            int s = -1;
            for (int j = 0; j <= n; j++) {
                if (phase == 2 && N[j] == -1) continue;
                if (s == -1 || D[x][j] < D[x][s] || D[x][j] == D[x][s] && N[j] <
                   N[s]) s = j;
            }
            if (D[x][s] > -EPS) return true;
            int r = -1;
            for (int i = 0; i < m; i++) {
                if (D[i][s] < EPS) continue;
                if (r == -1 || D[i][n + 1] / D[i][s] < D[r][n + 1] / D[r][s] ||
                    (D[i][n + 1] / D[i][s]) == (D[r][n + 1] / D[r][s]) && B[i] <
                      B[r]) r = i;
            }
            if (r == -1) return false;
            pivot(r, s);
        }
    }

    double solve(VD& x) {
        int r = 0;
        for (int i = 1; i < m; i++) if (D[i][n + 1] < D[r][n + 1]) r = i;
        if (D[r][n + 1] < -EPS) {
            pivot(r, n);
            if (!simplex(1) || D[m + 1][n + 1] < -EPS)
                return -numeric_limits<double>::infinity();
            for (int i = 0; i < m; i++) if (B[i] == -1) {
                int s = -1;
                for (int j = 0; j <= n; j++)
                    if (s == -1 || D[i][j] < D[i][s] || D[i][j] == D[i][s] && N[
                      j] < N[s]) s = j;
                pivot(i, s);
            }
        }
        if (!simplex(2))
            return numeric_limits<double>::infinity();
        x = VD(n);
        for (int i = 0; i < m; i++) if (B[i] < n) x[B[i]] = D[i][n + 1];
        return D[m][n + 1];
    }
};
```

3 Data Structure

3.1 Order statistic tree

```
#include <ext/pb_ds/assoc_container.hpp>
#include <ext/pb_ds/tree_policy.hpp>
#include <ext/pb_ds/detail/standard_policies.hpp>
#include <functional>
```

```cpp
#include <iostream>
using namespace __gnu_pbds;
using namespace std;

// tree<key_type, value_type(set if null), comparator, ...>
using ordered_set = tree<int, null_type, less<int>, rb_tree_tag,
    tree_order_statistics_node_update>;

int main()
{
    ordered_set X;
    for (int i = 1; i < 10; i += 2) X.insert(i); // 1 3 5 7 9
    cout << boolalpha;
    cout << *X.find_by_order(2) << endl; // 5
    cout << *X.find_by_order(4) << endl; // 9
    cout << (X.end() == X.find_by_order(5)) << endl; // true

    cout << X.order_of_key(-1) << endl; // 0
    cout << X.order_of_key(1) << endl; // 0
    cout << X.order_of_key(4) << endl; // 2
    X.erase(3);
    cout << X.order_of_key(4) << endl; // 1
    for (int t : X) printf("%d␣", t); // 1 5 7 9
}
```

3.2 Fenwick Tree

```cpp
const int TSIZE = 100000;
int tree[TSIZE + 1];

// Returns the sum from index 1 to p, inclusive
int query(int p) {
    int ret = 0;
    for (; p > 0; p -= p & -p) ret += tree[p];
    return ret;
}

// Adds val to element with index pos
void add(int p, int val) {
    for (; p <= TSIZE; p += p & -p) tree[p] += val;
}
```

3.3 Segment Tree with Lazy Propagation

```cpp
// example implementation of sum tree
const int TSIZE = 131072; // always 2^k form && n <= TSIZE
int segtree[TSIZE * 2], prop[TSIZE * 2];
void seg_init(int nod, int l, int r) {
    if (l == r) segtree[nod] = dat[l];
    else {
        int m = (l + r) >> 1;
        seg_init(nod << 1, l, m);
        seg_init(nod << 1 | 1, m + 1, r);
        segtree[nod] = segtree[nod << 1] + segtree[nod << 1 | 1];
    }
}
void seg_relax(int nod, int l, int r) {
    if (prop[nod] == 0) return;
    if (l < r) {
        int m = (l + r) >> 1;
        segtree[nod << 1] += (m - l + 1) * prop[nod];
        prop[nod << 1] += prop[nod];
        segtree[nod << 1 | 1] += (r - m) * prop[nod];
        prop[nod << 1 | 1] += prop[nod];
    }
    prop[nod] = 0;
}
int seg_query(int nod, int l, int r, int s, int e) {
    if (r < s || e < l) return 0;
    if (s <= l && r <= e) return segtree[nod];
    seg_relax(nod, l, r);
    int m = (l + r) >> 1;
    return seg_query(nod << 1, l, m, s, e) + seg_query(nod << 1 | 1, m + 1, r, s
      , e);
}
void seg_update(int nod, int l, int r, int s, int e, int val) {
    if (r < s || e < l) return;
    if (s <= l && r <= e) {
        segtree[nod] += (r - l + 1) * val;
        prop[nod] += val;
        return;
    }
    seg_relax(nod, l, r);
    int m = (l + r) >> 1;
    seg_update(nod << 1, l, m, s, e, val);
    seg_update(nod << 1 | 1, m + 1, r, s, e, val);
    segtree[nod] = segtree[nod << 1] + segtree[nod << 1 | 1];
}
// usage:
// seg_update(1, 0, n - 1, qs, qe, val);
// seg_query(1, 0, n - 1, qs, qe);
```

3.4 Persistent Segment Tree

```cpp
// persistent segment tree impl: sum tree
namespace pstree {
    typedef int val_t;
    const int DEPTH = 18;
    const int TSIZE = 1 << 18;
    const int MAX_QUERY = 262144;

    struct node {
        val_t v;
        node *l, *r;
    } npoll[TSIZE * 2 + MAX_QUERY * (DEPTH + 1)];

    int pptr, last_q;
```

```

    node *head[MAX_QUERY + 1];
    int q[MAX_QUERY + 1];
    int lqidx;

    void init() {
        // zero-initialize, can be changed freely
        memset(&npoll[TSIZE - 1], 0, sizeof(node) * TSIZE);

        for (int i = TSIZE - 2; i >= 0; i--) {
            npoll[i].v = 0;
            npoll[i].l = &npoll[i*2+1];
            npoll[i].r = &npoll[i*2+2];
        }

        head[0] = &npoll[0];
        last_q = 0;
        pptr = 2 * TSIZE - 1;
        q[0] = 0;
        lqidx = 0;
    }

    // update val to pos at time t
    // 0 <= t <= MAX_QUERY, 0 <= pos < TSIZE
    void update(int pos, int val, int t, int prev) {
        head[++last_q] = &npoll[pptr++];
        node *old = head[q[prev]], *now = head[last_q];
        while (lqidx < t) q[lqidx++] = q[prev];
        q[t] = last_q;

        int flag = 1 << DEPTH;
        for (;;) {
            now->v = old->v + val;
            flag >>= 1;
            if (flag==0) {
                now->l = now->r = nullptr; break;
            }
            if (flag & pos) {
                now->l = old->l;
                now->r = &npoll[pptr++];
                now = now->r, old = old->r;
            } else {
                now->r = old->r;
                now->l = &npoll[pptr++];
                now = now->l, old = old->l;
            }
        }
    }

    val_t query(int s, int e, int l, int r, node *n) {
        if (s == l && e == r) return n->v;
        int m = (l + r) / 2;
        if (m >= e) return query(s, e, l, m, n->l);
        else if (m < s) return query(s, e, m + 1, r, n->r);
        else return query(s, m, l, m, n->l) + query(m + 1, e, m + 1, r, n->r);
    }

```

```

    }

    // query summation of [s, e] at time t
    val_t query(int s, int e, int t) {
        s = max(0, s); e = min(TSIZE - 1, e);
        if (s > e) return 0;
        return query(s, e, 0, TSIZE - 1, head[q[t]]);
    }
}
```

3.5 Splay Tree

```
// example : https://www.acmicpc.net/problem/13159
struct node {
    node* l, * r, * p;
    int cnt, min, max, val;
    long long sum;
    bool inv;
    node(int _val) :
        cnt(1), sum(_val), min(_val), max(_val), val(_val), inv(false),
        l(nullptr), r(nullptr), p(nullptr) {
    }
};
node* root;

void update(node* x) {
    x->cnt = 1;
    x->sum = x->min = x->max = x->val;
    if (x->l) {
        x->cnt += x->l->cnt;
        x->sum += x->l->sum;
        x->min = min(x->min, x->l->min);
        x->max = max(x->max, x->l->max);
    }
    if (x->r) {
        x->cnt += x->r->cnt;
        x->sum += x->r->sum;
        x->min = min(x->min, x->r->min);
        x->max = max(x->max, x->r->max);
    }
}

void rotate(node* x) {
    node* p = x->p;
    node* b = nullptr;
    if (x == p->l) {
        p->l = b = x->r;
        x->r = p;
    }
    else {
        p->r = b = x->l;
        x->l = p;
    }
    x->p = p->p;
```

```
    p->p = x;
    if (b) b->p = p;
    x->p ? (p == x->p->l ? x->p->l : x->p->r) = x : (root = x);
    update(p);
    update(x);
}

// make x into root
void splay(node* x) {
    while (x->p) {
        node* p = x->p;
        node* g = p->p;
        if (g) rotate((x == p->l) == (p == g->l) ? p : x);
        rotate(x);
    }
}

void relax_lazy(node* x) {
    if (!x->inv) return;
    swap(x->l, x->r);
    x->inv = false;
    if (x->l) x->l->inv = !x->l->inv;
    if (x->r) x->r->inv = !x->r->inv;
}

// find kth node in splay tree
void find_kth(int k) {
    node* x = root;
    relax_lazy(x);
    while (true) {
        while (x->l && x->l->cnt > k) {
            x = x->l;
            relax_lazy(x);
        }
        if (x->l) k -= x->l->cnt;
        if (!k--) break;
        x = x->r;
        relax_lazy(x);
    }
    splay(x);
}

// collect [l, r] nodes into one subtree and return its root
node* interval(int l, int r) {
    find_kth(l - 1);
    node* x = root;
    root = x->r;
    root->p = nullptr;
    find_kth(r - l + 1);
    x->r = root;
    root->p = x;
    root = x;
    return root->r->l;
}

```

```
void traverse(node* x) {
    relax_lazy(x);
    if (x->l) {
        traverse(x->l);
    }
    // do something
    if (x->r) {
        traverse(x->r);
    }
}

void uptree(node* x) {
    if (x->p) {
        uptree(x->p);
    }
    relax_lazy(x);
}
```

3.6 Link/Cut Tree

4 DP

4.1 Convex Hull Optimization

4.1.1 requirement

$O(n^2) \rightarrow O(n \log n)$

조건 1) DP 점화식 꼴

$D[i] = \min_{j<i}(D[j] + b[j] * a[i])$

조건 2) $b[j] \leq b[j+1]$

특수조건) $a[i] \leq a[i+1]$ 도 만족하는 경우, 마지막 쿼리의 위치를 저장해두면 이분검색이 필요없어지기 때문에 amortized $O(n)$ 에 해결할 수 있음

4.1.2 Source Code

```
//O(n^3) -> O(n^2)

#define sz 100001
long long s[sz];
long long dp[2][sz];
//deque {index, x pos }
int dqi[sz];
long long dqm[sz];
//pointer to deque
int ql,qr;
//dp[i][j] = max(dp[i][k] + s[j]*s[k] - s[k]^2)
```

```
//Let y = dp[i][j], x = s[j] -> y = max(s[k]*x + dp[i][k] - s[k]^2);

//push new value to deque
//i = index, x = current x pos
void setq(int i, int x)
{
    //a1,b1 = prv line, a2,b2 = new line
    int a1, a2 = s[i];
    long long b1, b2 = dp[0][i] - s[i] * s[i], r;
    //renew deque
    while (qr>=ql)
    {
        //last line enqueued
        a1 = s[dqi[qr]];
        b1 = dp[0][dqi[qr]] - s[dqi[qr]] * s[dqi[qr]];
        //tie breaking to newer one
        if (a1 == a2)
        {
            dqi[qr] = i;
            return;
        }
        // x intersection between last line and new line
        r = (b1 - b2) / (a2 - a1);
        if ((b1 - b2) % (a2 - a1)) r++;
        //last line is not needed
        if (r <= dqm[qr])
        {
            qr--;
        }
        else break;
    }
    if (r < 0) r = 0;
    //push back new line
    if (dqm[qr] < s[n - 1] && r <= s[n - 1])
    {
        dqi[++qr] = i;
        dqm[qr] = r;
    }
    //discard old lines
    while (qr-ql && dqm[ql+1] <= x)
    {
        ql++;
    }
}

int main()
{
    for (int j = 0; j < k; j++)
    {
        ql = 0;
        qr = 1;
        dqi[0] = dqm[0] = 0;
        for (int i = 1; i < n; i++)
        {
            //get line used by current x pos
            setq(i, s[i]);
            //line index to use
            int g = dqi[ql];
            //set dp value
            dp[1][i] = dp[0][g] + s[g] * (s[i] - s[g]);
        }
        for (int i = 0; i < n; i++)
        {
            dp[0][i] = dp[1][i];
            dp[1][i] = 0;
        }
    }
}
```

4.2 Divide & Conquer Optimization

$O(kn^2) \rightarrow O(kn \log n)$

조건 1) DP 점화식 꼴

$D[t][i] = \min_{j<i}(D[t-1][j] + C[j][i])$

조건 2) $A[t][i]$는 $D[t][i]$의 답이 되는 최소의 j라 할 때, 아래의 부등식을 만족해야 함

$A[t][i] \le A[t][i+1]$

조건 2-1) 비용C가 다음의 사각부등식을 만족하는 경우도 조건 2)를 만족하게 됨

$C[a][c] + C[b][d] \le C[a][d] + C[b][c] \ \ (a \le b \le c \le d)$

4.3 Knuth Optimization

$O(n^3) \rightarrow O(n^2)$

조건 1) DP 점화식 꼴

$D[i][j] = \min_{i<k<j}(D[i][k] + D[k][j]) + C[i][j]$

조건 2) 사각 부등식

$C[a][c] + C[b][d] \le C[a][d] + C[b][c] \ \ (a \le b \le c \le d)$

조건 3) 단조성

$C[b][c] \le C[a][d] \ \ (a \le b \le c \le d)$

결론) 조건 2, 3을 만족한다면 $A[i][j]$를 $D[i][j]$의 답이 되는 최소의 k라 할 때, 아래의 부등식을 만족하게 됨

$A[i][j-1] \le A[i][j] \le A[i+1][j]$

3중 루프를 돌릴 때 위 조건을 이용하면 최종적으로 시간복잡도가 $O(n^2)$ 이 됨

5 Graph

5.1 SCC (Tarjan)

```cpp
const int MAXN = 100;
vector<int> graph[MAXN];
int up[MAXN], visit[MAXN], vtime;
vector<int> stk;
int scc_idx[MAXN], scc_cnt;

void dfs(int nod) {
    up[nod] = visit[nod] = ++vtime;
    stk.push_back(nod);
    for (int next : graph[nod]) {
        if (visit[next] == 0) {
            dfs(next);
            up[nod] = min(up[nod], up[next]);
        }
        else if (scc_idx[next] == 0)
            up[nod] = min(up[nod], visit[next]);
    }
    if (up[nod] == visit[nod]) {
        ++scc_cnt;
        int t;
        do {
            t = stk.back();
            stk.pop_back();
            scc_idx[t] = scc_cnt;
        } while (!stk.empty() && t != nod);
    }
}

// find SCCs in given directed graph
// O(V+E)
void get_scc() {
    vtime = 0;
    memset(visit, 0, sizeof(visit));
    scc_cnt = 0;
    memset(scc_idx, 0, sizeof(scc_idx));
    for (int i = 0; i < n; ++i)
        if (visit[i] == 0) dfs(i);
}
```

5.2 SCC (Kosaraju)

```cpp
const int MAXN = 100;
vector<int> graph[MAXN], grev[MAXN];
int visit[MAXN], vcnt;
int scc_idx[MAXN], scc_cnt;
vector<int> emit;

void dfs(int nod, vector<int> graph[]) {
    visit[nod] = vcnt;
    for (int next : graph[nod]) {
        if (visit[next] == vcnt) continue;
        dfs(next, graph);
    }
    emit.push_back(nod);
}

// find SCCs in given graph
// O(V+E)
void get_scc() {
    scc_cnt = 0;
    vcnt = 1;
    emit.clear();
    memset(visit, 0, sizeof(visit));

    for (int i = 0; i < n; i++) {
        if (visit[i] == vcnt) continue;
        dfs(i, graph);
    }

    ++vcnt;
    for (auto st : vector<int>(emit.rbegin(), emit.rend())) {
        if (visit[st] == vcnt) continue;
        emit.clear();
        dfs(st, grev);
        ++scc_cnt;
        for (auto node : emit)
            scc_idx[node] = scc_cnt;
    }
}
```

5.3 2-SAT

$(b_x \vee b_y) \wedge (\neg b_x \vee b_z) \wedge (b_z \vee \neg b_x) \wedge \cdots$ 같은 form을 2-CNF라고 함. 주어진 2-CNF 식을 참으로 하는 $\{b_1, b_2, \cdots\}$ 가 존재하는지, 존재한다면 그 값은 무엇인지 구하는 문제를 2-SAT이라 함.

boolean variable b_i 마다 b_i를 나타내는 정점, $\neg b_i$를 나타내는 정점 2개를 만듦. 각 clause $b_i \vee b_j$ 마다 $\neg b_i \to b_j$, $\neg b_j \to b_i$ 이렇게 edge를 이어줌. 그렇게 만든 그래프에서 SCC를 다 구함. 어떤 SCC 안에 b_i 와 $\neg b_i$가 같이 포함되어있다면 해가 존재하지 않음. 아니라면 해가 존재함.

해가 존재할 때 구체적인 해를 구하는 방법. 위에서 SCC를 구하면서 SCC DAG를 만들어 준다. 거기서 위상정렬을 한 후, 앞에서부터 SCC를 하나씩 봐준다. 현재 보고있는 SCC에 b_i가 속해있는데 얘가 $\neg b_i$보다 먼저 등장했다면 $b_i = \text{false}$, 반대의 경우라면 $b_i = \text{true}$, 이미 값이 assign되었다면 pass.

5.4 BCC, Cut vertex, Bridge

```cpp
const int MAXN = 100;
vector<pair<int, int>> graph[MAXN];  // { next vertex id, edge id }
int up[MAXN], visit[MAXN], vtime;
vector<pair<int, int>> stk;

int is_cut[MAXN];           // v is cut vertex if  is_cut[v] > 0
vector<int> bridge;         // list of edge ids
vector<int> bcc_idx[MAXN];  // list of bccids for vertex i
int bcc_cnt;

void dfs(int nod, int par_edge) {
    up[nod] = visit[nod] = ++vtime;
    int child = 0;
    for (const auto& e : graph[nod]) {
        int next = e.first, edge_id = e.second;
        if (edge_id == par_edge) continue;
        if (visit[next] == 0) {
            stk.push_back({ nod, next });
            ++child;
            dfs(next, edge_id);
            if (up[next] == visit[next]) bridge.push_back(edge_id);
            if (up[next] >= visit[nod]) {
                ++bcc_cnt;
                do {
                    auto last = stk.back();
                    stk.pop_back();
                    bcc_idx[last.second].push_back(bcc_cnt);
                    if (last == pair<int, int>{ nod, next }) break;
                } while (!stk.empty());
                bcc_idx[nod].push_back(bcc_cnt);
                is_cut[nod]++;
            }
            up[nod] = min(up[nod], up[next]);
        }
        else
            up[nod] = min(up[nod], visit[next]);
    }
    if (par_edge == -1 && is_cut[nod] == 1)
        is_cut[nod] = 0;
}

// find BCCs & cut vertexs & bridges in undirected graph
// O(V+E)
void get_bcc() {
    vtime = 0;
    memset(visit, 0, sizeof(visit));
    memset(is_cut, 0, sizeof(is_cut));
    bridge.clear();
    for (int i = 0; i < n; ++i) bcc_idx[i].clear();
    bcc_cnt = 0;
    for (int i = 0; i < n; ++i) {
        if (visit[i] == 0)
            dfs(i, -1);
    }
}
```

5.5 Shortest Path Faster Algorithm

```cpp
// shortest path faster algorithm
// average for random graph : O(E) , worst : O(VE)

const int MAXN = 20001;
const int INF = 100000000;
int n, m;
vector<pair<int, int>> graph[MAXN];
bool inqueue[MAXN];
int dist[MAXN];

void spfa(int st) {
    for (int i = 0; i < n; ++i) {
        dist[i] = INF;
    }
    dist[st] = 0;

    queue<int> q;
    q.push(st);
    inqueue[st] = true;
    while (!q.empty()) {
        int u = q.front();
        q.pop();
        inqueue[u] = false;
        for (auto& e : graph[u]) {
            if (dist[u] + e.second < dist[e.first]) {
                dist[e.first] = dist[u] + e.second;
                if (!inqueue[e.first]) {
                    q.push(e.first);
                    inqueue[e.first] = true;
                }
            }
        }
    }
}
```

5.6 Lowest Common Ancestor

```cpp
const int MAXN = 100;
const int MAXLN = 9;
vector<int> tree[MAXN];
int depth[MAXN];
int par[MAXLN][MAXN];

void dfs(int nod, int parent) {
    for (int next : tree[nod]) {
        if (next == parent) continue;
        depth[next] = depth[nod] + 1;
        par[0][next] = nod;
        dfs(next, nod);
    }
}

```

```cpp
void prepare_lca() {
    const int root = 0;
    dfs(root, -1);
    par[0][root] = root;
    for (int i = 1; i < MAXLN; ++i)
        for (int j = 0; j < n; ++j)
            par[i][j] = par[i - 1][par[i - 1][j]];
}

// find lowest common ancestor in tree between u & v
// assumption : must call 'prepare_lca' once before call this
// O(logV)
int lca(int u, int v) {
    if (depth[u] < depth[v]) swap(u, v);
    if (depth[u] > depth[v]) {
        for (int i = MAXLN - 1; i >= 0; --i)
            if (depth[u] - (1 << i) >= depth[v])
                u = par[i][u];
    }
    if (u == v) return u;
    for (int i = MAXLN - 1; i >= 0; --i) {
        if (par[i][u] != par[i][v]) {
            u = par[i][u];
            v = par[i][v];
        }
    }
    return par[0][u];
}
```

5.7 Heavy-Light Decomposition

```cpp
// heavy-light decomposition
//
// hld h;
// insert edges to tree[0~n-1];
// h.init(n);
// h.decompose(root);
// h.hldquery(u, v); // edges from u to v
struct hld {
    static const int MAXLN = 18;
    static const int MAXN = 1 << (MAXLN - 1);
    vector<int> tree[MAXN];
    int subsize[MAXN], depth[MAXN], pa[MAXLN][MAXN];

    int chead[MAXN], cidx[MAXN];
    int lchain;
    int flatpos[MAXN + 1], fptr;

    void dfs(int u, int par) {
        pa[0][u] = par;
        subsize[u] = 1;
        for (int v : tree[u]) {
            if (v == pa[0][u]) continue;
            depth[v] = depth[u] + 1;
            dfs(v, u);
            subsize[u] += subsize[v];
        }
    }

    void init(int size)
    {
        lchain = fptr = 0;
        dfs(0, -1);
        memset(chead, -1, sizeof(chead));

        for (int i = 1; i < MAXLN; i++) {
            for (int j = 0; j < size; j++) {
                if (pa[i - 1][j] != -1) {
                    pa[i][j] = pa[i - 1][pa[i - 1][j]];
                }
            }
        }
    }

    void decompose(int u) {
        if (chead[lchain] == -1) chead[lchain] = u;
        cidx[u] = lchain;
        flatpos[u] = ++fptr;

        int maxchd = -1;
        for (int v : tree[u]) {
            if (v == pa[0][u]) continue;
            if (maxchd == -1 || subsize[maxchd] < subsize[v]) maxchd = v;
        }
        if (maxchd != -1) decompose(maxchd);

        for (int v : tree[u]) {
            if (v == pa[0][u] || v == maxchd) continue;
            ++lchain; decompose(v);
        }
    }

    int lca(int u, int v) {
        if (depth[u] < depth[v]) swap(u, v);

        int logu;
        for (logu = 1; 1 << logu <= depth[u]; logu++);
        logu--;

        int diff = depth[u] - depth[v];
        for (int i = logu; i >= 0; --i) {
            if ((diff >> i) & 1) u = pa[i][u];
        }
        if (u == v) return u;

        for (int i = logu; i >= 0; --i) {
            if (pa[i][u] != pa[i][v]) {
                u = pa[i][u];
                v = pa[i][v];
```

```
            }
        }
        return pa[0][u];
    }

    // TODO: implement query functions
    inline int query(int s, int e) {
        return 0;
    }

    int subquery(int u, int v, int t) {
        int uchain, vchain = cidx[v];
        int ret = 0;
        for (;;) {
            uchain = cidx[u];
            if (uchain == vchain) {
                ret += query(flatpos[v], flatpos[u]);
                break;
            }

            ret += query(flatpos[chead[uchain]], flatpos[u]);
            u = pa[0][chead[uchain]];
        }
        return ret;
    }

    inline int hldquery(int u, int v) {
        int p = lca(u, v);
        return subquery(u, p) + subquery(v, p) - query(flatpos[p], flatpos[p]);
    }
};
```

5.8 Bipartite Matching (Hopcroft-Karp)

```
// in: n, m, graph
// out: match, matched
// vertex cover: (reached[0][left_node] == 0) || (reached[1][right_node] == 1)
// O(E*sqrt(V))
struct BipartiteMatching {
    int n, m;
    vector<vector<int>> graph;
    vector<int> matched, match, edgeview, level;
    vector<int> reached[2];
    BipartiteMatching(int n, int m) : n(n), m(m), graph(n), matched(m, -1),
      match(n, -1) {}

    bool assignLevel() {
        bool reachable = false;
        level.assign(n, -1);
        reached[0].assign(n, 0);
        reached[1].assign(m, 0);
        queue<int> q;
        for (int i = 0; i < n; i++) {
            if (match[i] == -1) {
                level[i] = 0;
                reached[0][i] = 1;
                q.push(i);
            }
        }
        while (!q.empty()) {
            auto cur = q.front(); q.pop();
            for (auto adj : graph[cur]) {
                reached[1][adj] = 1;
                auto next = matched[adj];
                if (next == -1) {
                    reachable = true;
                }
                else if (level[next] == -1) {
                    level[next] = level[cur] + 1;
                    reached[0][next] = 1;
                    q.push(next);
                }
            }
        }
        return reachable;
    }

    int findpath(int nod) {
        for (int &i = edgeview[nod]; i < graph[nod].size(); i++) {
            int adj = graph[nod][i];
            int next = matched[adj];
            if (next >= 0 && level[next] != level[nod] + 1) continue;
            if (next == -1 || findpath(next)) {
                match[nod] = adj;
                matched[adj] = nod;
                return 1;
            }
        }
        return 0;
    }

    int solve() {
        int ans = 0;
        while (assignLevel()) {
            edgeview.assign(n, 0);
            for (int i = 0; i < n; i++)
                if (match[i] == -1)
                    ans += findpath(i);
        }
        return ans;
    }
};
```

5.9 Maximum Flow (Dinic)

```
// usage:
// MaxFlowDinic::init(n);
// MaxFlowDinic::add_edge(0, 1, 100, 100); // for bidirectional edge
```

```cpp
// MaxFlowDinic::add_edge(1, 2, 100); // directional edge
// result = MaxFlowDinic::solve(0, 2); // source -> sink
// graph[i][edgeIndex].res -> residual
//
// in order to find out the minimum cut, use `l'.
// if l[i] == 0, i is unrechable.
//
// O(V*V*E)
// with unit capacities, O(min(V^(2/3), E^(1/2)) * E)
struct MaxFlowDinic {
    typedef int flow_t;
    struct Edge {
        int next;
        int inv; /* inverse edge index */
        flow_t res; /* residual */
    };
    int n;
    vector<vector<Edge>> graph;
    vector<int> q, l, start;

    void init(int _n) {
        n = _n;
        graph.resize(n);
        for (int i = 0; i < n; i++) graph[i].clear();
    }
    void add_edge(int s, int e, flow_t cap, flow_t caprev = 0) {
        Edge forward{ e, graph[e].size(), cap };
        Edge reverse{ s, graph[s].size(), caprev };
        graph[s].push_back(forward);
        graph[e].push_back(reverse);
    }
    bool assign_level(int source, int sink) {
        int t = 0;
        memset(&l[0], 0, sizeof(l[0]) * l.size());
        l[source] = 1;
        q[t++] = source;
        for (int h = 0; h < t && !l[sink]; h++) {
            int cur = q[h];
            for (const auto& e : graph[cur]) {
                if (l[e.next] || e.res == 0) continue;
                l[e.next] = l[cur] + 1;
                q[t++] = e.next;
            }
        }
        return l[sink] != 0;
    }
    flow_t block_flow(int cur, int sink, flow_t current) {
        if (cur == sink) return current;
        for (int& i = start[cur]; i < graph[cur].size(); i++) {
            auto& e = graph[cur][i];
            if (e.res == 0 || l[e.next] != l[cur] + 1) continue;
            if (flow_t res = block_flow(e.next, sink, min(e.res, current))) {
                e.res -= res;
                graph[e.next][e.inv].res += res;
                return res;
            }
        }
        return 0;
    }
    flow_t solve(int source, int sink) {
        q.resize(n);
        l.resize(n);
        start.resize(n);
        flow_t ans = 0;
        while (assign_level(source, sink)) {
            memset(&start[0], 0, sizeof(start[0]) * n);
            while (flow_t flow = block_flow(source, sink, numeric_limits<flow_t
              >::max()))
                ans += flow;
        }
        return ans;
    }
};
```

5.10 Min-cost Maximum Flow

```cpp
// precondition: there is no negative cycle.
// usage:
//  MinCostFlow mcf(n);
//  for(each edges) mcf.addEdge(from, to, cost, capacity);
//  mcf.solve(source, sink); // min cost max flow
//  mcf.solve(source, sink, 0); // min cost flow
//  mcf.solve(source, sink, goal_flow); // min cost flow with total_flow >=
  goal_flow if possible
struct MinCostFlow
{
    typedef int cap_t;
    typedef int cost_t;

    bool iszerocap(cap_t cap) { return cap == 0; }

    struct edge {
        int target;
        cost_t cost;
        cap_t residual_capacity;
        cap_t orig_capacity;
        size_t revid;
    };

    int n;
    vector<vector<edge>> graph;
    vector<cost_t> pi;
    bool needNormalize, ranbefore;
    int lastStart;

    MinCostFlow(int n) : graph(n), n(n), pi(n, 0), needNormalize(false),
      ranbefore(false) {}
    void addEdge(int s, int e, cost_t cost, cap_t cap)
    {
```

```
        if (s == e) return;
        edge forward={e, cost, cap, cap, graph[e].size()};
        edge backward={s, -cost, 0, 0, graph[s].size()};
        if (cost < 0 || ranbefore) needNormalize = true;
        graph[s].emplace_back(forward);
        graph[e].emplace_back(backward);
    }
    bool normalize(int s) {
        auto infinite_cost = numeric_limits<cost_t>::max();
        vector<cost_t> dist(n, infinite_cost);
        dist[s] = 0;
        queue<int> q;
        vector<int> v(n), relax_count(n);
        v[s] = 1; q.push(s);
        while(!q.empty()) {
            int cur = q.front();
            v[cur] = 0; q.pop();
            if (++relax_count[cur] >= n) return false;
            for (const auto &e : graph[cur]) {
                if (iszerocap(e.residual_capacity)) continue;
                auto next = e.target;
                auto ncost = dist[cur] + e.cost;
                if (dist[next] > ncost) {
                    dist[next] = ncost;
                    if (v[next]) continue;
                    v[next] = 1; q.push(next);
                }
            }
        }
        for (int i = 0; i < n; i++) pi[i] = dist[i];
        return true;
    }

    pair<cost_t, cap_t> AugmentShortest(int s, int e, cap_t flow_limit) {
        auto infinite_cost = numeric_limits<cost_t>::max();
        auto infinite_flow = numeric_limits<cap_t>::max();
        typedef pair<cost_t, int> pq_t;
        priority_queue<pq_t, vector<pq_t>, greater<pq_t>> pq;
        vector<pair<cost_t, cap_t>> dist(n, make_pair(infinite_cost, 0));
        vector<int> from(n, -1), v(n);

        if (needNormalize || (ranbefore && lastStart != s))
            normalize(s);
        ranbefore = true;
        lastStart = s;

        dist[s] = pair<cost_t, cap_t>(0, infinite_flow);
        pq.emplace(dist[s].first, s);
        while(!pq.empty()) {
            auto cur = pq.top().second; pq.pop();
            if (v[cur]) continue;
            v[cur] = 1;
            if (cur == e) continue;
            for (const auto &e : graph[cur]) {
                auto next = e.target;
                if (v[next]) continue;
                if (iszerocap(e.residual_capacity)) continue;
                auto ncost = dist[cur].first + e.cost - pi[next] + pi[cur];
                auto nflow = min(dist[cur].second, e.residual_capacity);
                if (dist[next].first <= ncost) continue;
                dist[next] = make_pair(ncost, nflow);
                from[next] = e.revid;
                pq.emplace(dist[next].first, next);
            }
        }
        /** augment the shortest path **/
        auto p = e;
        auto pathcost = dist[p].first + pi[p] - pi[s];
        auto flow = dist[p].second;
        if (iszerocap(flow)|| (flow_limit <= 0 && pathcost >= 0)) return pair<
          cost_t, cap_t>(0, 0);
        if (flow_limit > 0) flow = min(flow, flow_limit);
        /* update potential */
        for (int i = 0; i < n; i++) {
            if (iszerocap(dist[i].second)) continue;
            pi[i] += dist[i].first;
        }
        while (from[p] != -1) {
            auto nedge = from[p];
            auto np = graph[p][nedge].target;
            auto fedge = graph[p][nedge].revid;
            graph[p][nedge].residual_capacity += flow;
            graph[np][fedge].residual_capacity -= flow;
            p = np;
        }
        return make_pair(pathcost * flow, flow);
    }

    pair<cost_t,cap_t> solve(int s, int e, cap_t flow_minimum = numeric_limits<
      cap_t>::max()) {
        cost_t total_cost = 0;
        cap_t total_flow = 0;
        for(;;) {
            auto res = AugmentShortest(s, e, flow_minimum - total_flow);
            if (res.second <= 0) break;
            total_cost += res.first;
            total_flow += res.second;
        }
        return make_pair(total_cost, total_flow);
    }
};
```

5.11 General Min-cut (Stoer-Wagner)

```
// implementation of Stoer-Wagner algorithm
// O(V^3)
//usage
// MinCut mc;
// mc.init(n);
```

```
// for (each edge) mc.addEdge(a,b,weight);
// mincut = mc.solve();
// mc.cut = {0,1}^n describing which side the vertex belongs to.
struct MinCutMatrix
{
    typedef int cap_t;
    int n;
    vector<vector<cap_t>> graph;

    void init(int _n) {
        n = _n;
        graph = vector<vector<cap_t>>(n, vector<cap_t>(n, 0));
    }
    void addEdge(int a, int b, cap_t w) {
        if (a == b) return;
        graph[a][b] += w;
        graph[b][a] += w;
    }

    pair<cap_t, pair<int, int>> stMinCut(vector<int> &active) {
        vector<cap_t> key(n);
        vector<int> v(n);
        int s = -1, t = -1;
        for (int i = 0; i < active.size(); i++) {
            cap_t maxv = -1;
            int cur = -1;
            for (auto j : active) {
                if (v[j] == 0 && maxv < key[j]) {
                    maxv = key[j];
                    cur = j;
                }
            }
            t = s; s = cur;
            v[cur] = 1;
            for (auto j : active) key[j] += graph[cur][j];
        }
        return make_pair(key[s], make_pair(s, t));
    }

    vector<int> cut;

    cap_t solve() {
        cap_t res = numeric_limits<cap_t>::max();
        vector<vector<int>> grps;
        vector<int> active;
        cut.resize(n);
        for (int i = 0; i < n; i++) grps.emplace_back(1, i);
        for (int i = 0; i < n; i++) active.push_back(i);
        while (active.size() >= 2) {
            auto stcut = stMinCut(active);
            if (stcut.first < res) {
                res = stcut.first;
                fill(cut.begin(), cut.end(), 0);
                for (auto v : grps[stcut.second.first]) cut[v] = 1;
            }

            int s = stcut.second.first, t = stcut.second.second;
            if (grps[s].size() < grps[t].size()) swap(s, t);

            active.erase(find(active.begin(), active.end(), t));
            grps[s].insert(grps[s].end(), grps[t].begin(), grps[t].end());
            for (int i = 0; i < n; i++) { graph[i][s] += graph[i][t]; graph[i][t] = 0; }
            for (int i = 0; i < n; i++) { graph[s][i] += graph[t][i]; graph[t][i] = 0; }
            graph[s][s] = 0;
        }
        return res;
    }
};
```

5.12 Hungarian Algorithm

```
namespace hung {
    /*
    * alternative cost_t example
    *
    typedef pair<int,int> cost_t;
    cost_t MAX_COST = make_pair(2,0);
    pair<int,int> &operator += (pair<int,int> &a, const pair<int,int> &b) {
        a.first += b.first; a.second += b.second;
        return a;
    }
    pair<int,int> &operator -= (pair<int,int> &a, const pair<int,int> &b) {
        a.first -= b.first; a.second -= b.second;
        return a;
    }
    */
    typedef int cost_t;
    cost_t MAX_COST = numeric_limits<cost_t>::max() / 2;
    // input: n, dat(which is NOT const)
    // output: call solve(), match, matched
    // minimum matching 계산이다.
    const int MAX_N = 500;

    int n, match[MAX_N], matched[MAX_N];
    cost_t dat[MAX_N][MAX_N];
    int q[MAX_N], v[MAX_N], vcnt;
    int f[MAX_N], reach[MAX_N], reach2[MAX_N], rcnt;

    int augment(int r) {
        int h, t = 0;
        v[r] = ++vcnt;
        q[t++] = r;
        for (h = 0; h<t; h++) {
            int qh = q[h];
            for (int j = 0; j<n; j++) {
                if (dat[qh][j] != 0) continue;
                int next = matched[j];
```

```
                if (next == -1) {
                    for (;;) {
                        int org = match[qh];
                        match[qh] = j; matched[j] = qh;
                        if (qh == r) return 1;
                        qh = f[qh]; j = org;
                    }
                }
                else if (v[next] != vcnt) {
                    v[next] = vcnt, f[next] = qh, q[t++] = next;
                }
            }
        }
        for (int i = 0; i<n; i++)
            if (v[i] == vcnt) {
                reach[i] = rcnt;
                if (i != r) reach2[match[i]] = rcnt;
            }
        return 0;
    }

    cost_t solve() {
        cost_t ans = 0;
        for (int i = 0; i<n; i++) match[i] = matched[i] = -1;
        for (int i = 0; i<n; i++) {
            cost_t minv = *min_element(dat[i], dat[i] + n);
            for (int j = 0; j < n; j++) dat[i][j] -= minv;
            ans += minv;
            minv = dat[0][i];
            for (int j = 1; j<n; j++) minv = min(minv, dat[j][i]);
            for (int j = 0; j<n; j++) dat[j][i] -= minv;
            ans += minv;
        }
        for (;;) {
            ++rcnt;
            bool needMore = false;
            for (int i = 0; i<n; i++) {
                if (match[i] >= 0) continue;
                if (!augment(i)) needMore = true;
            }
            if (!needMore) break;
            cost_t minv = MAX_COST;
            for (int i = 0; i<n; i++) {
                if (reach[i] != rcnt) continue;
                for (int j = 0; j<n; j++) {
                    if (reach2[j] == rcnt) continue;
                    minv = min(minv, dat[i][j]);
                }
            }
            for (int i = 0; i<n; i++) {
                if (match[i]<0) ans += minv;
                for (int j = 0; j<n; j++) {
                    if (reach[i] != rcnt) dat[i][j] += minv;
                    if (reach2[j] != rcnt) dat[i][j] -= minv;
                }
            }
        }
        return ans;
    }
}
```

6 Geometry

6.1 Basic Operations

```
const double eps = 1e-9;

inline int diff(double lhs, double rhs) {
    if (lhs - eps < rhs && rhs < lhs + eps) return 0;
    return (lhs < rhs) ? -1 : 1;
}

inline bool is_between(double check, double a, double b) {
    if (a < b)
        return (a - eps < check && check < b + eps);
    else
        return (b - eps < check && check < a + eps);
}

struct Point {
    double x, y;
    bool operator==(const Point& rhs) const {
        return diff(x, rhs.x) == 0 && diff(y, rhs.y) == 0;
    }
    Point operator+(const Point& rhs) const {
        return Point{ x + rhs.x, y + rhs.y };
    }
    Point operator-(const Point& rhs) const {
        return Point{ x - rhs.x, y - rhs.y };
    }
    Point operator*(double t) const {
        return Point{ x * t, y * t };
    }
};

struct Circle {
    Point center;
    double r;
};

struct Line {
    Point pos, dir;
};

inline double inner(const Point& a, const Point& b) {
    return a.x * b.x + a.y * b.y;
}

```

```
inline double outer(const Point& a, const Point& b) {
    return a.x * b.y - a.y * b.x;
}

inline int ccw_line(const Line& line, const Point& point) {
    return diff(outer(line.dir, point - line.pos), 0);
}

inline int ccw(const Point& a, const Point& b, const Point& c) {
    return diff(outer(b - a, c - a), 0);
}

inline double dist(const Point& a, const Point& b) {
    return sqrt(inner(a - b, a - b));
}

inline double dist2(const Point &a, const Point &b) {
    return inner(a - b, a - b);
}

inline double dist(const Line& line, const Point& point, bool segment = false) {
    double c1 = inner(point - line.pos, line.dir);
    if (segment && diff(c1, 0) <= 0) return dist(line.pos, point);
    double c2 = inner(line.dir, line.dir);
    if (segment && diff(c2, c1) <= 0) return dist(line.pos + line.dir, point);
    return dist(line.pos + line.dir * (c1 / c2), point);
}

bool get_cross(const Line& a, const Line& b, Point& ret) {
    double mdet = outer(b.dir, a.dir);
    if (diff(mdet, 0) == 0) return false;
    double t2 = outer(a.dir, b.pos - a.pos) / mdet;
    ret = b.pos + b.dir * t2;
    return true;
}

bool get_segment_cross(const Line& a, const Line& b, Point& ret) {
    double mdet = outer(b.dir, a.dir);
    if (diff(mdet, 0) == 0) return false;
    double t1 = -outer(b.pos - a.pos, b.dir) / mdet;
    double t2 = outer(a.dir, b.pos - a.pos) / mdet;
    if (!is_between(t1, 0, 1) || !is_between(t2, 0, 1)) return false;
    ret = b.pos + b.dir * t2;
    return true;
}

Point inner_center(const Point &a, const Point &b, const Point &c) {
    double wa = dist(b, c), wb = dist(c, a), wc = dist(a, b);
    double w = wa + wb + wc;
    return Point{ (wa * a.x + wb * b.x + wc * c.x) / w, (wa * a.y + wb * b.y +
      wc * c.y) / w };
}

Point outer_center(const Point &a, const Point &b, const Point &c) {
    Point d1 = b - a, d2 = c - a;
    double area = outer(d1, d2);
    double dx = d1.x * d1.x * d2.y - d2.x * d2.x * d1.y
        + d1.y * d2.y * (d1.y - d2.y);
    double dy = d1.y * d1.y * d2.x - d2.y * d2.y * d1.x
        + d1.x * d2.x * (d1.x - d2.y);
    return Point{ a.x + dx / area / 2.0, a.y - dy / area / 2.0 };
}

vector<Point> circle_line(const Circle& circle, const Line& line) {
    vector<Point> result;
    double a = 2 * inner(line.dir, line.dir);
    double b = 2 * (line.dir.x * (line.pos.x - circle.center.x)
        + line.dir.y * (line.pos.y - circle.center.y));
    double c = inner(line.pos - circle.center, line.pos - circle.center)
        - circle.r * circle.r;
    double det = b * b - 2 * a * c;
    int pred = diff(det, 0);
    if (pred == 0)
        result.push_back(line.pos + line.dir * (-b / a));
    else if (pred > 0) {
        det = sqrt(det);
        result.push_back(line.pos + line.dir * ((-b + det) / a));
        result.push_back(line.pos + line.dir * ((-b - det) / a));
    }
    return result;
}

vector<Point> circle_circle(const Circle& a, const Circle& b) {
    vector<Point> result;
    int pred = diff(dist(a.center, b.center), a.r + b.r);
    if (pred > 0) return result;
    if (pred == 0) {
        result.push_back((a.center * b.r + b.center * a.r) * (1 / (a.r + b.r)));
        return result;
    }
    double aa = a.center.x * a.center.x + a.center.y * a.center.y - a.r * a.r;
    double bb = b.center.x * b.center.x + b.center.y * b.center.y - b.r * b.r;
    double tmp = (bb - aa) / 2.0;
    Point cdiff = b.center - a.center;
    if (diff(cdiff.x, 0) == 0) {
        if (diff(cdiff.y, 0) == 0)
            return result; // if (diff(a.r, b.r) == 0): same circle
        return circle_line(a, Line{ Point{ 0, tmp / cdiff.y }, Point{ 1, 0 } });
    }
    return circle_line(a,
        Line{ Point{ tmp / cdiff.x, 0 }, Point{ -cdiff.y, cdiff.x } });
}

Circle circle_from_3pts(const Point& a, const Point& b, const Point& c) {
    Point ba = b - a, cb = c - b;
    Line p{ (a + b) * 0.5, Point{ ba.y, -ba.x } };
    Line q{ (b + c) * 0.5, Point{ cb.y, -cb.x } };
    Circle circle;
    if (!get_cross(p, q, circle.center))
        circle.r = -1;
```

```
    else
        circle.r = dist(circle.center, a);
    return circle;
}

Circle circle_from_2pts_rad(const Point& a, const Point& b, double r) {
    double det = r * r / dist2(a, b) - 0.25;
    Circle circle;
    if (det < 0)
        circle.r = -1;
    else {
        double h = sqrt(det);
        // center is to the left of a->b
        circle.center = (a + b) * 0.5 + Point{ a.y - b.y, b.x - a.x } * h;
        circle.r = r;
    }
    return circle;
}
```

6.2 Compare angles

6.3 Convex Hull

```
// find convex hull
// O(n*logn)
vector<Point> convex_hull(vector<Point>& dat) {
    if (dat.size() <= 3) return dat;
    vector<Point> upper, lower;
    sort(dat.begin(), dat.end(), [](const Point& a, const Point& b) {
        return (a.x == b.x) ? a.y < b.y : a.x < b.x;
    });
    for (const auto& p : dat) {
        while (upper.size() >= 2 && ccw(*++upper.rbegin(), *upper.rbegin(), p)
          >= 0) upper.pop_back();
        while (lower.size() >= 2 && ccw(*++lower.rbegin(), *lower.rbegin(), p)
          <= 0) lower.pop_back();
        upper.emplace_back(p);
        lower.emplace_back(p);
    }
    upper.insert(upper.end(), ++lower.rbegin(), --lower.rend());
    return upper;
}
```

6.4 Polygon Cut

```
// left side of a->b
vector<Point> cut_polygon(const vector<Point>& polygon, Line line) {
    if (!polygon.size()) return polygon;
    typedef vector<Point>::const_iterator piter;
    piter la, lan, fi, fip, i, j;
    la = lan = fi = fip = polygon.end();
    i = polygon.end() - 1;
    bool lastin = diff(ccw_line(line, polygon[polygon.size() - 1]), 0) > 0;
    for (j = polygon.begin() ; j != polygon.end() ; j++) {
        bool thisin = diff(ccw_line(line, *j), 0) > 0;
        if (lastin && !thisin) {
            la = i;
            lan = j;
        }
        if (!lastin && thisin) {
            fi = j;
            fip = i;
        }
        i = j;
        lastin = thisin;
    }
    if (fi == polygon.end()) {
        if (!lastin) return vector<Point>();
        return polygon;
    }
    vector<Point> result;
    for (i = fi ; i != lan ; i++) {
        if (i == polygon.end()) {
            i = polygon.begin();
            if (i == lan) break;
        }
        result.push_back(*i);
    }
    Point lc, fc;
    get_cross(Line{ *la, *lan - *la }, line, lc);
    get_cross(Line{ *fip, *fi - *fip }, line, fc);
    result.push_back(lc);
    if (diff(dist2(lc, fc), 0) != 0) result.push_back(fc);
    return result;
}
```

6.5 Pick's theorem

격자점으로 구성된 simple polygon이 주어짐. i는 polygon 내부의 격자점 수, b는 polygon 선분 위 격자점 수, A는 polygon의 넓이라고 할 때, 다음과 같은 식이 성립한다.

$A = i + \frac{b}{2} - 1$

7 String

7.1 KMP

```
typedef vector<int> seq_t;

void calculate_pi(vector<int>& pi, const seq_t& str) {
    pi[0] = -1;
    for (int i = 1, j = -1; i < str.size(); i++) {
        while (j >= 0 && str[i] != str[j + 1]) j = pi[j];
```

```
        if (str[i] == str[j + 1])
            pi[i] = ++j;
        else
            pi[i] = -1;
    }
}

// returns all positions matched
// O(|text|+|pattern|)
vector<int> kmp(const seq_t& text, const seq_t& pattern) {
    vector<int> pi(pattern.size()), ans;
    if (pattern.size() == 0) return ans;
    calculate_pi(pi, pattern);
    for (int i = 0, j = -1; i < text.size(); i++) {
        while (j >= 0 && text[i] != pattern[j + 1]) j = pi[j];
        if (text[i] == pattern[j + 1]) {
            j++;
            if (j + 1 == pattern.size()) {
                ans.push_back(i - j);
                j = pi[j];
            }
        }
    }
    return ans;
}
```

7.2 Aho-Corasick

```
#include <algorithm>
#include <vector>
#include <queue>
using namespace std;

struct AhoCorasick
{
    const int alphabet;
    struct node {
        node() {}
        explicit node(int alphabet) : next(alphabet) {}
        vector<int> next, report;
        int back = 0, output_link = 0;
    };
    int maxid = 0;
    vector<node> dfa;
    explicit AhoCorasick(int alphabet) : alphabet(alphabet), dfa(1, node(
      alphabet)) { }
    template<typename InIt, typename Fn> void add(int id, InIt first, InIt last,
       Fn func) {
        int cur = 0;
        for ( ; first != last; ++first) {
            auto s = func(*first);
            if (auto next = dfa[cur].next[s]) cur = next;
            else {
                cur = dfa[cur].next[s] = (int)dfa.size();
                dfa.emplace_back(alphabet);
            }
        }
        dfa[cur].report.push_back(id);
        maxid = max(maxid, id);
    }
    void build() {
        queue<int> q;
        vector<char> visit(dfa.size());
        visit[0] = 1;
        q.push(0);
        while(!q.empty()) {
            auto cur = q.front(); q.pop();
            dfa[cur].output_link = dfa[cur].back;
            if (dfa[dfa[cur].back].report.empty())
                dfa[cur].output_link = dfa[dfa[cur].back].output_link;
            for (int s = 0; s < alphabet; s++) {
                auto &next = dfa[cur].next[s];
                if (next == 0) next = dfa[dfa[cur].back].next[s];
                if (visit[next]) continue;
                if (cur) dfa[next].back = dfa[dfa[cur].back].next[s];
                visit[next] = 1;
                q.push(next);
            }
        }
    }
    template<typename InIt, typename Fn> vector<int> countMatch(InIt first, InIt
       last, Fn func) {
        int cur = 0;
        vector<int> ret(maxid+1);
        for (; first != last; ++first) {
            cur = dfa[cur].next[func(*first)];
            for (int p = cur; p; p = dfa[p].output_link)
                for (auto id : dfa[p].report) ret[id]++;
        }
        return ret;
    }
};
```

7.3 Suffix Array with LCP

```
typedef char T;

// calculates suffix array.
// O(n*logn)
vector<int> suffix_array(const vector<T>& in) {
    int n = (int)in.size(), c = 0;
    vector<int> temp(n), pos2bckt(n), bckt(n), bpos(n), out(n);
    for (int i = 0; i < n; i++) out[i] = i;
    sort(out.begin(), out.end(), [&](int a, int b) { return in[a] < in[b]; });
    for (int i = 0; i < n; i++) {
        bckt[i] = c;
        if (i + 1 == n || in[out[i]] != in[out[i + 1]]) c++;
    }
```

```
    for (int h = 1; h < n && c < n; h <<= 1) {
        for (int i = 0; i < n; i++) pos2bckt[out[i]] = bckt[i];
        for (int i = n - 1; i >= 0; i--) bpos[bckt[i]] = i;
        for (int i = 0; i < n; i++)
            if (out[i] >= n - h) temp[bpos[bckt[i]]++] = out[i];
        for (int i = 0; i < n; i++)
            if (out[i] >= h) temp[bpos[pos2bckt[out[i] - h]]++] = out[i] - h;
        c = 0;
        for (int i = 0; i + 1 < n; i++) {
            int a = (bckt[i] != bckt[i + 1]) || (temp[i] >= n - h)
                    || (pos2bckt[temp[i + 1] + h] != pos2bckt[temp[i] + h]);
            bckt[i] = c;
            c += a;
        }
        bckt[n - 1] = c++;
        temp.swap(out);
    }
    return out;
}

// calculates lcp array. it needs suffix array & original sequence.
// O(n)
vector<int> lcp(const vector<T>& in, const vector<int>& sa) {
    int n = (int)in.size();
    if (n == 0) return vector<int>();
    vector<int> rank(n), height(n - 1);
    for (int i = 0; i < n; i++) rank[sa[i]] = i;
    for (int i = 0, h = 0; i < n; i++) {
        if (rank[i] == 0) continue;
        int j = sa[rank[i] - 1];
        while (i + h < n && j + h < n && in[i + h] == in[j + h]) h++;
        height[rank[i] - 1] = h;
        if (h > 0) h--;
    }
    return height;
}
```

7.4 Suffix Tree

7.5 Manacher's Algorithm

```
// find longest palindromic span for each element in str
// O(|str|)
void manacher(const string& str, int plen[]) {
    int r = -1, p = -1;
    for (int i = 0; i < str.length(); ++i) {
        if (i <= r)
            plen[i] = min((2 * p - i >= 0) ? plen[2 * p - i] : 0, r - i);
        else
            plen[i] = 0;
        while (i - plen[i] - 1 >= 0 && i + plen[i] + 1 < str.length()
                && str[i - plen[i] - 1] == str[i + plen[i] + 1]) {
            plen[i] += 1;
        }
        if (i + plen[i] > r) {
            r = i + plen[i];
            p = i;
        }
    }
}
```

8 Miscellaneous

8.1 Fast I/O

```
namespace fio {
    const int BSIZE = 524288;
    char buffer[BSIZE];
    int p = BSIZE;
    inline char readChar() {
        if(p == BSIZE) {
            fread(buffer, 1, BSIZE, stdin);
            p = 0;
        }
        return buffer[p++];
    }
    int readInt() {
        char c = readChar();
        while ((c < '0' || c > '9') && c != '-') {
            c = readChar();
        }
        int ret = 0; bool neg = c == '-';
        if (neg) c = readChar();
        while (c >= '0' && c <= '9') {
            ret = ret * 10 + c - '0';
            c = readChar();
        }
        return neg ? -ret : ret;
    }
}
```

8.2 Magic Numbers

소수 : 10 007 , 10 009 , 10 111 , 31 567 , 70 001 , 1 000 003 , 1 000 033 , 4 000 037 , 1 000 000 007 , 1 000 000 009

8.3 Java Examples

```
import java.util.Scanner;

public class example
{
```

```
5     public static void main(String[] args)
6     {
7         Scanner in = new Scanner(System.in);
8         int T = in.nextInt();
9         while (T --> 0)
10        {
11            String str = in.next();
12            if (str.matches("[A-F]?A+F+C+[A-F]?"))
13                System.out.println("Infected!");
14            else
15                System.out.println("Good");
16        }
17    }
18 }
```