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## 2 Math

### 2.1 Basic Arithmetic

```
1 typedef long long ll;
2 typedef unsigned long long ull;
3
4 // calculate lg2(a)
5 inline int lg2(ll a)
6 {
7     return 63 - __builtin_clzll(a);
8 }
9
10 // calculate the number of 1-bits
11 inline int bitcount(ll a)
12 {
13     return __builtin_popcountll(a);
14 }
15
16 // calculate ceil(a/b)
17 // |a|, |b| <= (2^63)-1 (does not cover -2^63)
18 ll ceildiv(ll a, ll b) {
19     if (b < 0) return ceildiv(-a, -b);
20     if (a < 0) return (-a) / b;
21     return ((ull)a + (ull)b - 1ull) / b;
22 }
23
24 // calculate floor(a/b)
25 // |a|, |b| <= (2^63)-1 (does not cover -2^63)
26 ll floordiv(ll a, ll b) {
27     if (b < 0) return floordiv(-a, -b);
28     if (a >= 0) return a / b;
29     return -(ll)((ull)(-a) + b - 1) / b;
30 }
31
32 // calculate a*b % m
33 // x86-64 only
34 ll large_mod_mul(ll a, ll b, ll m)
35 {
36     return ll((__int128)a*(__int128)b%m);
37 }
38
39 // calculate a*b % m
40 // |m| < 2^62, x86 available
41 // O(logb)
42 ll large_mod_mul(ll a, ll b, ll m)
43 {
44     a %= m; b %= m; ll r = 0, v = a;
45     while (b) {
46         if (b&1) r = (r + v) % m;
47         b >>= 1;
48         v = (v << 1) % m;
49     }
50     return r;
```

```
51 }
52
53 // calculate n^k % m
54 ll modpow(ll n, ll k, ll m) {
55     ll ret = 1;
56     n %= m;
57     while (k) {
58         if (k & 1) ret = large_mod_mul(ret, n, m);
59         n = large_mod_mul(n, n, m);
60         k /= 2;
61     }
62     return ret;
63 }
64
65 // calculate gcd(a, b)
66 ll gcd(ll a, ll b) {
67     return b == 0 ? a : gcd(b, a % b);
68 }
69
70 // find a pair (c, d) s.t. ac + bd = gcd(a, b)
71 pair<ll, ll> extended_gcd(ll a, ll b) {
72     if (b == 0) return { 1, 0 };
73     auto t = extended_gcd(b, a % b);
74     return { t.second, t.first - t.second * (a / b) };
75 }
76
77 // find x in [0, m) s.t. ax === gcd(a, m) (mod m)
78 ll modinverse(ll a, ll m) {
79     return (extended_gcd(a, m).first % m + m) % m;
80 }
81
82 // calculate modular inverse for 1 ~ n
83 void calc_range_modinv(int n, int mod, int ret[]) {
84     ret[1] = 1;
85     for (int i = 2; i <= n; ++i)
86         ret[i] = (ll)(mod - mod/i) * ret[mod%i] % mod;
87 }
```

### 2.2 Sieve Methods : Prime, Divisor, Euler phi

```
1 // find prime numbers in 1 ~ n
2 // ret[x] = false -> x is prime
3 // O(n*loglogn)
4 void sieve(int n, bool ret[]) {
5     for (int i = 2; i * i <= n; ++i)
6         if (!ret[i])
7             for (int j = i * i; j <= n; j += i)
8                 ret[j] = true;
9 }
10
11 // calculate number of divisors for 1 ~ n
12 // when you need to calculate sum, change += 1 to += i
13 // O(n*logn)
14 void num_of_divisors(int n, int ret[]) {
15     for (int i = 1; i <= n; ++i)
```

```

16     for (int j = i; j <= n; j += i)
17         ret[j] += 1;
18 }
19
20 // calculate euler totient function for 1 ~ n
21 // phi(n) = number of x s.t. 0 < x < n && gcd(n, x) = 1
22 // O(n*loglogn)
23 void euler_phi(int n, int ret[]) {
24     for (int i = 1; i <= n; ++i) ret[i] = i;
25     for (int i = 2; i <= n; ++i)
26         if (ret[i] == i)
27             for (int j = i; j <= n; j += i)
28                 ret[j] -= ret[j] / i;
29 }

```

## 2.3 Primality Test

```

1 bool test_witness(ull a, ull n, ull s) {
2     if (a >= n) a %= n;
3     if (a <= 1) return true;
4     ull d = n >> s;
5     ull x = modpow(a, d, n);
6     if (x == 1 || x == n-1) return true;
7     while (s-- > 1) {
8         x = large_mod_mul(x, x, n);
9         x = x * x % n;
10        if (x == 1) return false;
11        if (x == n-1) return true;
12    }
13    return false;
14 }
15
16 // test whether n is prime
17 // based on miller-rabin test
18 // O(logn*logn)
19 bool is_prime(ull n) {
20     if (n == 2) return true;
21     if (n < 2 || n % 2 == 0) return false;
22
23     ull d = n >> 1, s = 1;
24     for(; (d&1) == 0; s++) d >>= 1;
25
26 #define T(a) test_witness(a##ull, n, s)
27     if (n < 4759123141ull) return T(2) && T(7) && T(61);
28     return T(2) && T(325) && T(9375) && T(28178)
29         && T(450775) && T(9780504) && T(1795265022);
30 #undef T
31 }

```

## 2.4 Chinese Remainder Theorem

```

1 // find x s.t.  x == a[0] (mod n[0])
2 //              == a[1] (mod n[1])
3 //              ...

```

```

4 // assumption: gcd(n[i], n[j]) = 1
5 ll chinese_remainder(ll* a, ll* n, int size) {
6     if (size == 1) return *a;
7     ll tmp = modinverse(n[0], n[1]);
8     ll tmp2 = (tmp * (a[1] - a[0]) % n[1] + n[1]) % n[1];
9     ll ora = a[1];
10    ll tgcd = gcd(n[0], n[1]);
11    a[1] = a[0] + n[0] / tgcd * tmp2;
12    n[1] *= n[0] / tgcd;
13    ll ret = chinese_remainder(a + 1, n + 1, size - 1);
14    n[1] /= n[0] / tgcd;
15    a[1] = ora;
16    return ret;
17 }

```

## 2.5 Rational Number Class

```

1 struct rational {
2     long long p, q;
3
4     void red() {
5         if (q < 0) {
6             p = -p;
7             q = -q;
8         }
9         ll t = gcd((p >= 0 ? p : -p), q);
10        p /= t;
11        q /= t;
12    }
13
14    rational(): p(0), q(1) {}
15    rational(long long p_): p(p_), q(1) {}
16    rational(long long p_, long long q_): p(p_), q(q_) { red(); }
17
18    bool operator==(const rational& rhs) const {
19        return p == rhs.p && q == rhs.q;
20    }
21    bool operator!=(const rational& rhs) const {
22        return p != rhs.p || q != rhs.q;
23    }
24    bool operator<(const rational& rhs) const {
25        return p * rhs.q < rhs.p * q;
26    }
27    rational operator+(const rational& rhs) const {
28        ll g = gcd(q, rhs.q);
29        return rational(p * (rhs.q / g) + rhs.p * (q / g), (q / g) * rhs.q);
30    }
31    rational operator-(const rational& rhs) const {
32        ll g = gcd(q, rhs.q);
33        return rational(p * (rhs.q / g) - rhs.p * (q / g), (q / g) * rhs.q);
34    }
35    rational operator*(const rational& rhs) const {
36        return rational(p * rhs.p, q * rhs.q);
37    }
38    rational operator/(const rational& rhs) const {

```

```

39     return rational(p * rhs.q, q * rhs.p);
40 }
41 };

```

## 2.6 Burnside's Lemma

경우의 수를 세는데, 특정 transform operation(회전, 반사, ...) 해서 같은 경우들은 하나로 친다. 전체 경우의 수는?

- 각 operation마다 이 operation을 했을 때 변하지 않는 경우의 수를 센다 (단, “아무것도 하지 않는다”라는 operation도 있어야 함!)

- 전체 경우의 수를 더한 후, operation의 수로 나눈다. (답이 맞다면 항상 나누어 떨어져야 한다)

## 2.7 Kirchoff's Theorem

그래프의 스패닝 트리의 개수를 구하는 정리.

무향 그래프의 Laplacian matrix  $L$ 를 만든다. 이것은 (정점의 차수 대각 행렬) - (인접행렬)이다.  $L$ 에서 행과 열을 하나씩 제거한 것을  $L'$ 라 하자. 어느 행/열이든 관계 없다. 그래프의 스패닝 트리의 개수는  $\det(L')$ 이다.

## 2.8 Fast Fourier Transform

```

1 void fft(int sign, int n, double *real, double *imag) {
2     double theta = sign * 2 * pi / n;
3     for (int m = n; m >= 2; m >>= 1, theta *= 2) {
4         double wr = 1, wi = 0, c = cos(theta), s = sin(theta);
5         for (int i = 0, mh = m >> 1; i < mh; ++i) {
6             for (int j = i; j < n; j += m) {
7                 int k = j + mh;
8                 double xr = real[j] - real[k], xi = imag[j] - imag[k];
9                 real[j] += real[k], imag[j] += imag[k];
10                real[k] = wr * xr - wi * xi, imag[k] = wr * xi + wi * xr;
11            }
12            double _wr = wr * c - wi * s, _wi = wr * s + wi * c;
13            wr = _wr, wi = _wi;
14        }
15    }
16    for (int i = 1, j = 0; i < n; ++i) {
17        for (int k = n >> 1; k > (j ^ k); k >>= 1);
18        if (j < i) swap(real[i], real[j]), swap(imag[i], imag[j]);
19    }
20 }
21 // Compute Poly(a)*Poly(b), write to r; Indexed from 0
22 // O(n*logn)
23 int mult(int *a, int n, int *b, int m, int *r) {
24     const int maxn = 100;
25     static double ra[maxn], rb[maxn], ia[maxn], ib[maxn];

```

```

26     int fn = 1;
27     while (fn < n + m) fn <= 1; // n + m: interested length
28     for (int i = 0; i < n; ++i) ra[i] = a[i], ia[i] = 0;
29     for (int i = n; i < fn; ++i) ra[i] = ia[i] = 0;
30     for (int i = 0; i < m; ++i) rb[i] = b[i], ib[i] = 0;
31     for (int i = m; i < fn; ++i) rb[i] = ib[i] = 0;
32     fft(1, fn, ra, ia);
33     fft(1, fn, rb, ib);
34     for (int i = 0; i < fn; ++i) {
35         double real = ra[i] * rb[i] - ia[i] * ib[i];
36         double imag = ra[i] * ib[i] + rb[i] * ia[i];
37         ra[i] = real, ia[i] = imag;
38     }
39     fft(-1, fn, ra, ia);
40     for (int i = 0; i < fn; ++i) r[i] = (int)floor(ra[i] / fn + 0.5);
41     return fn;
42 }

```

## 2.9 Matrix Operations

```

1 const int MATSZ = 100;
2
3 inline bool is_zero(double a) { return fabs(a) < 1e-9; }
4
5 // out = A^(-1), returns det(A)
6 // A becomes invalid after call this
7 // O(n^3)
8 double inverse_and_det(int n, double A[][MATSZ], double out[][MATSZ]) {
9     double det = 1;
10    for (int i = 0; i < n; i++) {
11        for (int j = 0; j < n; j++) out[i][j] = 0;
12        out[i][i] = 1;
13    }
14    for (int i = 0; i < n; i++) {
15        if (is_zero(A[i][i])) {
16            double maxv = 0;
17            int maxid = -1;
18            for (int j = i + 1; j < n; j++) {
19                auto cur = fabs(A[j][i]);
20                if (maxv < cur) {
21                    maxv = cur;
22                    maxid = j;
23                }
24            }
25            if (maxid == -1 || is_zero(A[maxid][i])) return 0;
26            for (int k = 0; k < n; k++) {
27                A[i][k] += A[maxid][k];
28                out[i][k] += out[maxid][k];
29            }
30        }
31        det *= A[i][i];
32        double coeff = 1.0 / A[i][i];
33        for (int j = 0; j < n; j++) A[i][j] *= coeff;
34        for (int j = 0; j < n; j++) out[i][j] *= coeff;
35        for (int j = 0; j < n; j++) if (j != i) {

```

```

36     double mp = A[j][i];
37     for (int k = 0; k < n; k++) A[j][k] -= A[i][k] * mp;
38     for (int k = 0; k < n; k++) out[j][k] -= out[i][k] * mp;
39 }
40 }
41 return det;
42 }

```

## 2.10 Gaussian Elimination

```

1 const double EPS = 1e-10;
2 typedef vector<vector<double>> VVD;
3
4 // Gauss-Jordan elimination with full pivoting.
5 // solving systems of linear equations (AX=B)
6 // INPUT:  a[][] = an n*n matrix
7 //         b[][] = an n*m matrix
8 // OUTPUT: X      = an n*m matrix (stored in b[][])
9 //         A^{-1} = an n*n matrix (stored in a[][])
10 // O(n^3)
11 bool gauss_jordan(VVD& a, VVD& b) {
12     const int n = a.size();
13     const int m = b[0].size();
14     vector<int> irow(n), icol(n), ipiv(n);
15
16     for (int i = 0; i < n; i++) {
17         int pj = -1, pk = -1;
18         for (int j = 0; j < n; j++) if (!ipiv[j])
19             for (int k = 0; k < n; k++) if (!ipiv[k])
20                 if (pj == -1 || fabs(a[j][k]) > fabs(a[pj][pk])) { pj = j; pk
21                     = k; }
22         if (fabs(a[pj][pk]) < EPS) return false; // matrix is singular
23         ipiv[pk]++;
24         swap(a[pj], a[pk]);
25         swap(b[pj], b[pk]);
26         irow[i] = pj;
27         icol[i] = pk;
28
29         double c = 1.0 / a[pk][pk];
30         a[pk][pk] = 1.0;
31         for (int p = 0; p < n; p++) a[pk][p] *= c;
32         for (int p = 0; p < m; p++) b[pk][p] *= c;
33         for (int p = 0; p < n; p++) if (p != pk) {
34             c = a[p][pk];
35             a[p][pk] = 0;
36             for (int q = 0; q < n; q++) a[p][q] -= a[pk][q] * c;
37             for (int q = 0; q < m; q++) b[p][q] -= b[pk][q] * c;
38         }
39     }
40     for (int p = n - 1; p >= 0; p--) if (irow[p] != icol[p]) {
41         for (int k = 0; k < n; k++) swap(a[k][irow[p]], a[k][icol[p]]);
42     }
43     return true;
44 }

```

## 2.11 Simplex Algorithm

```

1 // Two-phase simplex algorithm for solving linear programs of the form
2 //      maximize    c^T x
3 //      subject to  Ax <= b
4 //                  x >= 0
5 // INPUT: A -- an m x n matrix
6 //        b -- an m-dimensional vector
7 //        c -- an n-dimensional vector
8 //        x -- a vector where the optimal solution will be stored
9 // OUTPUT: value of the optimal solution (infinity if unbounded
10 //        above, nan if infeasible)
11 // To use this code, create an LPSolver object with A, b, and c as
12 // arguments. Then, call Solve(x).
13 typedef vector<double> VD;
14 typedef vector<VD> VVD;
15 typedef vector<int> VI;
16 const double EPS = 1e-9;
17
18 struct LPSolver {
19     int m, n;
20     VI B, N;
21     VVD D;
22
23     LPSolver(const VVD& A, const VD& b, const VD& c) :
24         m(b.size()), n(c.size()), N(n + 1), B(m), D(m + 2, VD(n + 2)) {
25         for (int i = 0; i < m; i++) for (int j = 0; j < n; j++) D[i][j] = A[i
26             ][j];
27         for (int i = 0; i < m; i++) { B[i] = n + i; D[i][n] = -1; D[i][n + 1]
28             = b[i]; }
29         for (int j = 0; j < n; j++) { N[j] = j; D[m][j] = -c[j]; }
30         N[n] = -1; D[m + 1][n] = 1;
31     }
32
33     void pivot(int r, int s) {
34         double inv = 1.0 / D[r][s];
35         for (int i = 0; i < m + 2; i++) if (i != r)
36             for (int j = 0; j < n + 2; j++) if (j != s)
37                 D[i][j] -= D[r][j] * D[i][s] * inv;
38         for (int j = 0; j < n + 2; j++) if (j != s) D[r][j] *= inv;
39         D[r][s] = inv;
40         swap(B[r], N[s]);
41     }
42
43     bool simplex(int phase) {
44         int x = phase == 1 ? m + 1 : m;
45         while (true) {
46             int s = -1;
47             for (int j = 0; j <= n; j++) {
48                 if (phase == 2 && N[j] == -1) continue;
49                 if (s == -1 || D[x][j] < D[x][s] || D[x][j] == D[x][s] && N[j]
50                     < N[s]) s = j;
51             }
52             if (D[x][s] > -EPS) return true;
53         }
54     }
55 }

```

```

51     int r = -1;
52     for (int i = 0; i < m; i++) {
53         if (D[i][s] < EPS) continue;
54         if (r == -1 || D[i][n + 1] / D[i][s] < D[r][n + 1] / D[r][s]
55             || (D[i][n + 1] / D[i][s]) == (D[r][n + 1] / D[r][s]) && B[i]
56                 < B[r]) r = i;
57     }
58     if (r == -1) return false;
59     pivot(r, s);
60 }
61
62 double solve(VD& x) {
63     int r = 0;
64     for (int i = 1; i < m; i++) if (D[i][n + 1] < D[r][n + 1]) r = i;
65     if (D[r][n + 1] < -EPS) {
66         pivot(r, n);
67         if (!simplex(1) || D[m + 1][n + 1] < -EPS)
68             return -numeric_limits<double>::infinity();
69         for (int i = 0; i < m; i++) if (B[i] == -1) {
70             int s = -1;
71             for (int j = 0; j <= n; j++)
72                 if (s == -1 || D[i][j] < D[i][s] || D[i][j] == D[i][s] &&
73                     N[j] < N[s]) s = j;
74             pivot(i, s);
75         }
76         if (!simplex(2))
77             return numeric_limits<double>::infinity();
78         x = VD(n);
79         for (int i = 0; i < m; i++) if (B[i] < n) x[B[i]] = D[i][n + 1];
80         return D[m][n + 1];
81     }
82 };

```

## 3 Data Structure

### 3.1 Order statistic tree

```

1 #include <ext/pb_ds/assoc_container.hpp>
2 #include <ext/pb_ds/tree_policy.hpp>
3 #include <ext/pb_ds/detail/standard_policies.hpp>
4 #include <functional>
5 #include <iostream>
6 using namespace __gnu_pbds;
7 using namespace std;
8
9 // tree<key_type, value_type(set if null), comparator, ...>
10 using ordered_set = tree<int, null_type, less<int>, rb_tree_tag,
11     tree_order_statistics_node_update>;
12
13 int main()

```

```

14 {
15     ordered_set X;
16     for (int i = 1; i < 10; i += 2) X.insert(i); // 1 3 5 7 9
17     cout << boolalpha;
18     cout << *X.find_by_order(2) << endl; // 5
19     cout << *X.find_by_order(4) << endl; // 9
20     cout << (X.end() == X.find_by_order(5)) << endl; // true
21
22     cout << X.order_of_key(-1) << endl; // 0
23     cout << X.order_of_key(1) << endl; // 0
24     cout << X.order_of_key(4) << endl; // 2
25     X.erase(3);
26     cout << X.order_of_key(4) << endl; // 1
27     for (int t : X) printf("%d ", t); // 1 5 7 9
28 }

```

### 3.2 Fenwick Tree

```

1 const int TSIZE = 100000;
2 int tree[TSIZE + 1];
3
4 // Returns the sum from index 1 to p, inclusive
5 int query(int p) {
6     int ret = 0;
7     for (; p > 0; p -= p & -p) ret += tree[p];
8     return ret;
9 }
10
11 // Adds val to element with index pos
12 void add(int p, int val) {
13     for (; p <= TSIZE; p += p & -p) tree[p] += val;
14 }

```

### 3.3 Segment Tree with Lazy Propagation

```

1 // example implementation of sum tree
2 const int TSIZE = 131072; // always 2^k form && n <= TSIZE
3 int segtree[TSIZE * 2], prop[TSIZE * 2];
4 void seg_init(int nod, int l, int r) {
5     if (l == r) segtree[nod] = dat[l];
6     else {
7         int m = (l + r) >> 1;
8         seg_init(nod << 1, l, m);
9         seg_init(nod << 1 | 1, m + 1, r);
10        segtree[nod] = segtree[nod << 1] + segtree[nod << 1 | 1];
11    }
12 }
13 void seg_relax(int nod, int l, int r) {
14     if (prop[nod] == 0) return;
15     if (l < r) {
16         int m = (l + r) >> 1;
17         segtree[nod << 1] += (m - l + 1) * prop[nod];
18         prop[nod << 1] += prop[nod];
19         segtree[nod << 1 | 1] += (r - m) * prop[nod];

```

```

20     prop[nod << 1 | 1] += prop[nod];
21 }
22 prop[nod] = 0;
23 }
24 int seg_query(int nod, int l, int r, int s, int e) {
25     if (r < s || e < l) return 0;
26     if (s <= l && r <= e) return segtree[nod];
27     seg_relax(nod, l, r);
28     int m = (l + r) >> 1;
29     return seg_query(nod << 1, l, m, s, e) + seg_query(nod << 1 | 1, m + 1, r,
30         s, e);
31 }
32 void seg_update(int nod, int l, int r, int s, int e, int val) {
33     if (r < s || e < l) return;
34     if (s <= l && r <= e) {
35         segtree[nod] += (r - l + 1) * val;
36         prop[nod] += val;
37         return;
38     }
39     seg_relax(nod, l, r);
40     int m = (l + r) >> 1;
41     seg_update(nod << 1, l, m, s, e, val);
42     seg_update(nod << 1 | 1, m + 1, r, s, e, val);
43     segtree[nod] = segtree[nod << 1] + segtree[nod << 1 | 1];
44 }
45 // usage:
46 // seg_update(1, 0, n - 1, qs, qe, val);
47 // seg_query(1, 0, n - 1, qs, qe);

```

### 3.4 Persistent Segment Tree

```

1 // persistent segment tree impl: sum tree
2 namespace pstree {
3     typedef int val_t;
4     const int DEPTH = 18;
5     const int TSIZE = 1 << 18;
6     const int MAX_QUERY = 262144;
7
8     struct node {
9         val_t v;
10         node *l, *r;
11     } npoll[TSIZE * 2 + MAX_QUERY * (DEPTH + 1)];
12
13     int pptr, last_q;
14
15     node *head[MAX_QUERY + 1];
16     int q[MAX_QUERY + 1];
17     int lqidx;
18
19     void init() {
20         // zero-initialize, can be changed freely
21         memset(&npoll[TSIZE - 1], 0, sizeof(node) * TSIZE);
22
23         for (int i = TSIZE - 2; i >= 0; i--) {
24             npoll[i].v = 0;

```

```

25             npoll[i].l = &npoll[i*2+1];
26             npoll[i].r = &npoll[i*2+2];
27         }
28
29         head[0] = &npoll[0];
30         last_q = 0;
31         pptr = 2 * TSIZE - 1;
32         q[0] = 0;
33         lqidx = 0;
34     }
35
36     // update val to pos at time t
37     // 0 <= t <= MAX_QUERY, 0 <= pos < TSIZE
38     void update(int pos, int val, int t, int prev) {
39         head[++last_q] = &npoll[pptr++];
40         node *old = head[q[prev]], *now = head[last_q];
41         while (lqidx < t) q[lqidx++] = q[prev];
42         q[t] = last_q;
43
44         int flag = 1 << DEPTH;
45         for (;;) {
46             now->v = old->v + val;
47             flag >>= 1;
48             if (flag==0) {
49                 now->l = now->r = nullptr; break;
50             }
51             if (flag & pos) {
52                 now->l = old->l;
53                 now->r = &npoll[pptr++];
54                 now = now->r, old = old->r;
55             } else {
56                 now->r = old->r;
57                 now->l = &npoll[pptr++];
58                 now = now->l, old = old->l;
59             }
60         }
61     }
62
63     val_t query(int s, int e, int l, int r, node *n) {
64         if (s == l && e == r) return n->v;
65         int m = (l + r) / 2;
66         if (m >= e) return query(s, e, l, m, n->l);
67         else if (m < s) return query(s, e, m + 1, r, n->r);
68         else return query(s, m, l, m, n->l) + query(m + 1, e, m + 1, r, n->r);
69     }
70
71     // query summation of [s, e] at time t
72     val_t query(int s, int e, int t) {
73         s = max(0, s); e = min(TSIZE - 1, e);
74         if (s > e) return 0;
75         return query(s, e, 0, TSIZE - 1, head[q[t]]);
76     }
77 }

```

### 3.5 Splay Tree

```

1 // example : https://www.acmicpc.net/problem/13159
2 struct node {
3     node* l, * r, * p;
4     int cnt, min, max, val;
5     long long sum;
6     bool inv;
7     node(int _val) :
8         cnt(1), sum(_val), min(_val), max(_val), val(_val), inv(false),
9         l(nullptr), r(nullptr), p(nullptr) {}
10 }
11 };
12 node* root;
13
14 void update(node* x) {
15     x->cnt = 1;
16     x->sum = x->min = x->max = x->val;
17     if (x->l) {
18         x->cnt += x->l->cnt;
19         x->sum += x->l->sum;
20         x->min = min(x->min, x->l->min);
21         x->max = max(x->max, x->l->max);
22     }
23     if (x->r) {
24         x->cnt += x->r->cnt;
25         x->sum += x->r->sum;
26         x->min = min(x->min, x->r->min);
27         x->max = max(x->max, x->r->max);
28     }
29 }
30
31 void rotate(node* x) {
32     node* p = x->p;
33     node* b = nullptr;
34     if (x == p->l) {
35         p->l = b = x->r;
36         x->r = p;
37     }
38     else {
39         p->r = b = x->l;
40         x->l = p;
41     }
42     x->p = p->p;
43     p->p = x;
44     if (b) b->p = p;
45     x->p ? (p == x->p->l ? x->p->l : x->p->r) = x : (root = x);
46     update(p);
47     update(x);
48 }
49
50 // make x into root
51 void splay(node* x) {
52     while (x->p) {
53         node* p = x->p;

```

```

54         node* g = p->p;
55         if (g) rotate((x == p->l) == (p == g->l) ? p : x);
56         rotate(x);
57     }
58 }
59
60 void relax_lazy(node* x) {
61     if (!x->inv) return;
62     swap(x->l, x->r);
63     x->inv = false;
64     if (x->l) x->l->inv = !x->l->inv;
65     if (x->r) x->r->inv = !x->r->inv;
66 }
67
68 // find kth node in splay tree
69 void find_kth(int k) {
70     node* x = root;
71     relax_lazy(x);
72     while (true) {
73         while (x->l && x->l->cnt > k) {
74             x = x->l;
75             relax_lazy(x);
76         }
77         if (x->l) k -= x->l->cnt;
78         if (!k--) break;
79         x = x->r;
80         relax_lazy(x);
81     }
82     splay(x);
83 }
84
85 // collect [l, r] nodes into one subtree and return its root
86 node* interval(int l, int r) {
87     find_kth(l - 1);
88     node* x = root;
89     root = x->r;
90     root->p = nullptr;
91     find_kth(r - l + 1);
92     x->r = root;
93     root->p = x;
94     root = x;
95     return root->r->l;
96 }
97
98 void traverse(node* x) {
99     relax_lazy(x);
100     if (x->l) {
101         traverse(x->l);
102     }
103     // do something
104     if (x->r) {
105         traverse(x->r);
106     }
107 }
108

```



```

109 void uptree(node* x) {
110     if (x->p) {
111         uptree(x->p);
112     }
113     relax_lazy(x);
114 }

```

### 3.6 Link/Cut Tree

## 4 DP

### 4.1 Convex Hull Optimization

#### 4.1.1 requirement

$O(n^2) \rightarrow O(n \log n)$

조건 1) DP 점화식 꼴

$D[i] = \min_{j < i} (D[j] + b[j] * a[i])$

조건 2)  $b[j] \leq b[j + 1]$

특수조건)  $a[i] \leq a[i + 1]$  도 만족하는 경우, 마지막 쿼리의 위치를 저장해두면 이분검색이 필요없어지기 때문에 amortized  $O(n)$  에 해결할 수 있음

#### 4.1.2 Source Code

```

1 //O(n^3) -> O(n^2)
2
3 #define sz 100001
4 long long s[sz];
5 long long dp[2][sz];
6 //deque {index, x pos }
7 int dqi[sz];
8 long long dqm[sz];
9 //pointer to deque
10 int ql,qr;
11 //dp[i][j] = max(dp[i][k] + s[j]*s[k] - s[k]^2)
12 //let y = dp[i][j], x = s[j] -> y = max(s[k]*x + dp[i][k] - s[k]^2);
13
14 //push new value to deque
15 //i = index, x = current x pos
16 void setq(int i, int x)
17 {
18     //a1,b1 = prv line, a2,b2 = new line
19     int a1, a2 = s[i];
20     long long b1, b2 = dp[0][i] - s[i] * s[i], r;
21     //renew deque
22     while (qr >= ql)

```

```

23 {
24     //last line enqueued
25     a1 = s[dqi[qr]];
26     b1 = dp[0][dqi[qr]] - s[dqi[qr]] * s[dqi[qr]];
27     //tie breaking to newer one
28     if (a1 == a2)
29     {
30         dqi[qr] = i;
31         return;
32     }
33     // x intersection between last line and new line
34     r = (b1 - b2) / (a2 - a1);
35     if ((b1 - b2) % (a2 - a1)) r++;
36     //last line is not needed
37     if (r <= dqm[qr])
38     {
39         qr--;
40     }
41     else break;
42 }
43 if (r < 0) r = 0;
44 //push back new line
45 if (dqm[qr] < s[n - 1] && r <= s[n - 1])
46 {
47     dqi[++qr] = i;
48     dqm[qr] = r;
49 }
50 //discard old lines
51 while (qr - ql && dqm[ql + 1] <= x)
52 {
53     ql++;
54 }
55 }
56
57 int main()
58 {
59     for (int j = 0; j < k; j++)
60     {
61         ql = 0;
62         qr = 1;
63         dqi[0] = dqm[0] = 0;
64         for (int i = 1; i < n; i++)
65         {
66             //get line used by current x pos
67             setq(i, s[i]);
68             //line index to use
69             int g = dqi[ql];
70             //set dp value
71             dp[1][i] = dp[0][g] + s[g] * (s[i] - s[g]);
72         }
73         for (int i = 0; i < n; i++)
74         {
75             dp[0][i] = dp[1][i];
76             dp[1][i] = 0;
77         }

```

```

78     }
79 }

```

## 4.2 Divide & Conquer Optimization

$O(kn^2) \rightarrow O(kn \log n)$

조건 1) DP 점화식 꼴

$D[t][i] = \min_{j < i} (D[t-1][j] + C[j][i])$

조건 2)  $A[t][i]$ 는  $D[t][i]$ 의 답이 되는 최소의  $j$ 라 할 때, 아래의 부등식을 만족해야 함

$A[t][i] \leq A[t][i+1]$

조건 2-1) 비용  $C$ 가 다음의 사각부등식을 만족하는 경우도 조건 2)를 만족하게 됨

$C[a][c] + C[b][d] \leq C[a][d] + C[b][c] \quad (a \leq b \leq c \leq d)$

## 4.3 Knuth Optimization

$O(n^3) \rightarrow O(n^2)$

조건 1) DP 점화식 꼴

$D[i][j] = \min_{i < k < j} (D[i][k] + D[k][j]) + C[i][j]$

조건 2) 사각 부등식

$C[a][c] + C[b][d] \leq C[a][d] + C[b][c] \quad (a \leq b \leq c \leq d)$

조건 3) 단조성

$C[b][c] \leq C[a][d] \quad (a \leq b \leq c \leq d)$

결론) 조건 2, 3을 만족한다면  $A[i][j]$ 를  $D[i][j]$ 의 답이 되는 최소의  $k$ 라 할 때, 아래의 부등식을 만족하게 됨

$A[i][j-1] \leq A[i][j] \leq A[i+1][j]$

3중 루프를 돌릴 때 위 조건을 이용하면 최종적으로 시간복잡도가  $O(n^2)$  이 됨

## 5 Graph

### 5.1 SCC (Tarjan)

```

1 const int MAXN = 100;
2 vector<int> graph[MAXN];
3 int up[MAXN], visit[MAXN], vtime;
4 vector<int> stk;
5 int scc_idx[MAXN], scc_cnt;

```

```

6
7 void dfs(int nod) {
8     up[nod] = visit[nod] = ++vtime;
9     stk.push_back(nod);
10    for (int next : graph[nod]) {
11        if (visit[next] == 0) {
12            dfs(next);
13            up[nod] = min(up[nod], up[next]);
14        }
15        else if (scc_idx[next] == 0)
16            up[nod] = min(up[nod], visit[next]);
17    }
18    if (up[nod] == visit[nod]) {
19        ++scc_cnt;
20        int t;
21        do {
22            t = stk.back();
23            stk.pop_back();
24            scc_idx[t] = scc_cnt;
25        } while (!stk.empty() && t != nod);
26    }
27 }
28
29 // find SCCs in given directed graph
30 // O(V+E)
31 void get_scc() {
32     vtime = 0;
33     memset(visit, 0, sizeof(visit));
34     scc_cnt = 0;
35     memset(scc_idx, 0, sizeof(scc_idx));
36     for (int i = 0; i < n; ++i)
37         if (visit[i] == 0) dfs(i);
38 }

```

### 5.2 SCC (Kosaraju)

```

1 const int MAXN = 100;
2 vector<int> graph[MAXN], grev[MAXN];
3 int visit[MAXN], vcnt;
4 int scc_idx[MAXN], scc_cnt;
5 vector<int> emit;
6
7 void dfs(int nod, vector<int> graph[]) {
8     visit[nod] = vcnt;
9     for (int next : graph[nod]) {
10         if (visit[next] == vcnt) continue;
11         dfs(next, graph);
12     }
13     emit.push_back(nod);
14 }
15
16 // find SCCs in given graph
17 // O(V+E)
18 void get_scc() {
19     scc_cnt = 0;

```

```

20 vcnt = 1;
21 emit.clear();
22 memset(visit, 0, sizeof(visit));
23
24 for (int i = 0; i < n; i++) {
25     if (visit[i] == vcnt) continue;
26     dfs(i, graph);
27 }
28
29 ++vcnt;
30 for (auto st : vector<int>(emit.rbegin(), emit.rend())) {
31     if (visit[st] == vcnt) continue;
32     emit.clear();
33     dfs(st, grev);
34     ++scc_cnt;
35     for (auto node : emit)
36         scc_idx[node] = scc_cnt;
37 }
38 }

```

### 5.3 2-SAT

$(b_x \vee b_y) \wedge (\neg b_x \vee b_z) \wedge (b_z \vee \neg b_x) \wedge \dots$  같은 form을 2-CNF라고 함. 주어진 2-CNF 식을 참으로 하는  $\{b_1, b_2, \dots\}$  가 존재하는지, 존재한다면 그 값은 무엇인지 구하는 문제를 2-SAT 이라 함.

boolean variable  $b_i$  마다  $b_i$  를 나타내는 정점,  $\neg b_i$  를 나타내는 정점 2개를 만들. 각 clause  $b_i \vee b_j$  마다  $\neg b_i \rightarrow b_j, \neg b_j \rightarrow b_i$  이렇게 edge를 이어줌. 그렇게 만든 그래프에서 SCC를 다 구함. 어떤 SCC 안에  $b_i$  와  $\neg b_i$  가 같이 포함되어있다면 해가 존재하지 않음. 아니라면 해가 존재함.

해가 존재할 때 구체적인 해를 구하는 방법. 위에서 SCC를 구하면서 SCC DAG를 만들어 준다. 거기서 위상정렬을 한 후, 앞에서부터 SCC를 하나씩 봐준다. 현재 보고있는 SCC 에  $b_i$  가 속해있는데 애가  $\neg b_i$  보다 먼저 등장했다면  $b_i = \text{false}$ , 반대의 경우라면  $b_i = \text{true}$ , 이미 값이 assign되었다면 pass.

### 5.4 BCC, Cut vertex, Bridge

```

1 const int MAXN = 100;
2 vector<pair<int, int>> graph[MAXN]; // { next vertex id, edge id }
3 int up[MAXN], visit[MAXN], vtime;
4 vector<pair<int, int>> stk;
5
6 int is_cut[MAXN]; // v is cut vertex if is_cut[v] > 0
7 vector<int> bridge; // list of edge ids
8 vector<int> bcc_idx[MAXN]; // list of bccids for vertex i
9 int bcc_cnt;
10
11 void dfs(int nod, int par_edge) {
12     up[nod] = visit[nod] = ++vtime;
13     int child = 0;

```

```

14     for (const auto& e : graph[nod]) {
15         int next = e.first, edge_id = e.second;
16         if (edge_id == par_edge) continue;
17         if (visit[next] == 0) {
18             stk.push_back({ nod, next });
19             ++child;
20             dfs(next, edge_id);
21             if (up[next] == visit[next]) bridge.push_back(edge_id);
22             if (up[next] >= visit[nod]) {
23                 ++bcc_cnt;
24                 do {
25                     auto last = stk.back();
26                     stk.pop_back();
27                     bcc_idx[last.second].push_back(bcc_cnt);
28                     if (last == pair<int, int>{ nod, next }) break;
29                 } while (!stk.empty());
30                 bcc_idx[nod].push_back(bcc_cnt);
31                 is_cut[nod]++;
32             }
33             up[nod] = min(up[nod], up[next]);
34         }
35         else
36             up[nod] = min(up[nod], visit[next]);
37     }
38     if (par_edge == -1 && is_cut[nod] == 1)
39         is_cut[nod] = 0;
40 }
41
42 // find BCCs & cut vertexs & bridges in undirected graph
43 // O(V+E)
44 void get_bcc() {
45     vtime = 0;
46     memset(visit, 0, sizeof(visit));
47     memset(is_cut, 0, sizeof(is_cut));
48     bridge.clear();
49     for (int i = 0; i < n; ++i) bcc_idx[i].clear();
50     bcc_cnt = 0;
51     for (int i = 0; i < n; ++i) {
52         if (visit[i] == 0)
53             dfs(i, -1);
54     }
55 }

```

### 5.5 Shortest Path Faster Algorithm

```

1 // shortest path faster algorithm
2 // average for random graph : O(E) , worst : O(VE)
3
4 const int MAXN = 20001;
5 const int INF = 100000000;
6 int n, m;
7 vector<pair<int, int>> graph[MAXN];
8 bool inqueue[MAXN];
9 int dist[MAXN];
10

```

```

11 void spfa(int st) {
12     for (int i = 0; i < n; ++i) {
13         dist[i] = INF;
14     }
15     dist[st] = 0;
16
17     queue<int> q;
18     q.push(st);
19     inqueue[st] = true;
20     while (!q.empty()) {
21         int u = q.front();
22         q.pop();
23         inqueue[u] = false;
24         for (auto& e : graph[u]) {
25             if (dist[u] + e.second < dist[e.first]) {
26                 dist[e.first] = dist[u] + e.second;
27                 if (!inqueue[e.first]) {
28                     q.push(e.first);
29                     inqueue[e.first] = true;
30                 }
31             }
32         }
33     }
34 }

```

## 5.6 Lowest Common Ancestor

```

1 const int MAXN = 100;
2 const int MAXLN = 9;
3 vector<int> tree[MAXN];
4 int depth[MAXN];
5 int par[MAXLN][MAXN];
6
7 void dfs(int nod, int parent) {
8     for (int next : tree[nod]) {
9         if (next == parent) continue;
10        depth[next] = depth[nod] + 1;
11        par[0][next] = nod;
12        dfs(next, nod);
13    }
14 }
15
16 void prepare_lca() {
17     const int root = 0;
18     dfs(root, -1);
19     par[0][root] = root;
20     for (int i = 1; i < MAXLN; ++i)
21         for (int j = 0; j < n; ++j)
22             par[i][j] = par[i - 1][par[i - 1][j]];
23 }
24
25 // find lowest common ancestor in tree between u & v
26 // assumption : must call 'prepare_lca' once before call this
27 // O(logV)
28 int lca(int u, int v) {

```

```

29     if (depth[u] < depth[v]) swap(u, v);
30     if (depth[u] > depth[v]) {
31         for (int i = MAXLN - 1; i >= 0; --i)
32             if (depth[u] - (1 << i) >= depth[v])
33                 u = par[i][u];
34     }
35     if (u == v) return u;
36     for (int i = MAXLN - 1; i >= 0; --i) {
37         if (par[i][u] != par[i][v]) {
38             u = par[i][u];
39             v = par[i][v];
40         }
41     }
42     return par[0][u];
43 }

```

## 5.7 Heavy-Light Decomposition

```

1 // heavy-light decomposition
2 //
3 // hld h;
4 // insert edges to tree[0~n-1];
5 // h.init(n);
6 // h.decompose(root);
7 // h.hldquery(u, v); // edges from u to v
8 struct hld {
9     static const int MAXLN = 18;
10    static const int MAXN = 1 << (MAXLN - 1);
11    vector<int> tree[MAXN];
12    int subsize[MAXN], depth[MAXN], pa[MAXLN][MAXN];
13
14    int chead[MAXN], cidx[MAXN];
15    int lchain;
16    int flatpos[MAXN + 1], fptr;
17
18    void dfs(int u, int par) {
19        pa[0][u] = par;
20        subsize[u] = 1;
21        for (int v : tree[u]) {
22            if (v == pa[0][u]) continue;
23            depth[v] = depth[u] + 1;
24            dfs(v, u);
25            subsize[u] += subsize[v];
26        }
27    }
28
29    void init(int size)
30    {
31        lchain = fptr = 0;
32        dfs(0, -1);
33        memset(chead, -1, sizeof(chead));
34
35        for (int i = 1; i < MAXLN; i++) {
36            for (int j = 0; j < size; j++) {
37                if (pa[i - 1][j] != -1) {

```

```

38         pa[i][j] = pa[i - 1][pa[i - 1][j]];
39     }
40 }
41 }
42 }
43
44 void decompose(int u) {
45     if (chead[lchain] == -1) chead[lchain] = u;
46     cidx[u] = lchain;
47     flatpos[u] = ++fptr;
48
49     int maxchd = -1;
50     for (int v : tree[u]) {
51         if (v == pa[0][u]) continue;
52         if (maxchd == -1 || subsize[maxchd] < subsize[v]) maxchd = v;
53     }
54     if (maxchd != -1) decompose(maxchd);
55
56     for (int v : tree[u]) {
57         if (v == pa[0][u] || v == maxchd) continue;
58         ++lchain; decompose(v);
59     }
60 }
61
62 int lca(int u, int v) {
63     if (depth[u] < depth[v]) swap(u, v);
64
65     int logu;
66     for (logu = 1; 1 << logu <= depth[u]; logu++);
67     logu--;
68
69     int diff = depth[u] - depth[v];
70     for (int i = logu; i >= 0; --i) {
71         if ((diff >> i) & 1) u = pa[i][u];
72     }
73     if (u == v) return u;
74
75     for (int i = logu; i >= 0; --i) {
76         if (pa[i][u] != pa[i][v]) {
77             u = pa[i][u];
78             v = pa[i][v];
79         }
80     }
81     return pa[0][u];
82 }
83
84 // TODO: implement query functions
85 inline int query(int s, int e) {
86     return 0;
87 }
88
89 int subquery(int u, int v, int t) {
90     int uchain, vchain = cidx[v];
91     int ret = 0;
92     for (;;) {

```

```

93         uchain = cidx[u];
94         if (uchain == vchain) {
95             ret += query(flatpos[v], flatpos[u]);
96             break;
97         }
98
99         ret += query(flatpos[chead[uchain]], flatpos[u]);
100        u = pa[0][chead[uchain]];
101    }
102    return ret;
103 }
104
105 inline int hldquery(int u, int v) {
106     int p = lca(u, v);
107     return subquery(u, p) + subquery(v, p) - query(flatpos[p], flatpos[p])
        ;
108 }
109 };

```

## 5.8 Bipartite Matching (Hopcroft-Karp)

```

1 // in: n, m, graph
2 // out: match, matched
3 // vertex cover: (reached[0][left_node] == 0) || (reached[1][right_node] == 1)
4 // O(E*sqrt(V))
5 struct BipartiteMatching {
6     int n, m;
7     vector<vector<int>> graph;
8     vector<int> matched, match, edgeview, level;
9     vector<int> reached[2];
10    BipartiteMatching(int n, int m) : n(n), m(m), graph(n), matched(m, -1),
        match(n, -1) {}
11
12    bool assignLevel() {
13        bool reachable = false;
14        level.assign(n, -1);
15        reached[0].assign(n, 0);
16        reached[1].assign(m, 0);
17        queue<int> q;
18        for (int i = 0; i < n; i++) {
19            if (match[i] == -1) {
20                level[i] = 0;
21                reached[0][i] = 1;
22                q.push(i);
23            }
24        }
25        while (!q.empty()) {
26            auto cur = q.front(); q.pop();
27            for (auto adj : graph[cur]) {
28                reached[1][adj] = 1;
29                auto next = matched[adj];
30                if (next == -1) {
31                    reachable = true;
32                }
33                else if (level[next] == -1) {

```

```

34         level[next] = level[cur] + 1;
35         reached[0][next] = 1;
36         q.push(next);
37     }
38 }
39 }
40 return reachable;
41 }
42
43 int findpath(int nod) {
44     for (int &i = edgeview[nod]; i < graph[nod].size(); i++) {
45         int adj = graph[nod][i];
46         int next = matched[adj];
47         if (next >= 0 && level[next] != level[nod] + 1) continue;
48         if (next == -1 || findpath(next)) {
49             match[nod] = adj;
50             matched[adj] = nod;
51             return 1;
52         }
53     }
54     return 0;
55 }
56
57 int solve() {
58     int ans = 0;
59     while (assignLevel()) {
60         edgeview.assign(n, 0);
61         for (int i = 0; i < n; i++)
62             if (match[i] == -1)
63                 ans += findpath(i);
64     }
65     return ans;
66 }
67 };

```

## 5.9 Maximum Flow (Dinic)

```

1 // usage:
2 // MaxFlowDinic::init(n);
3 // MaxFlowDinic::add_edge(0, 1, 100, 100); // for bidirectional edge
4 // MaxFlowDinic::add_edge(1, 2, 100); // directional edge
5 // result = MaxFlowDinic::solve(0, 2); // source -> sink
6 // graph[i][edgeIndex].res -> residual
7 //
8 // in order to find out the minimum cut, use `l`.
9 // if l[i] == 0, i is unrechable.
10 //
11 // O(V*V*E)
12 // with unit capacities, O(min(V^(2/3), E^(1/2)) * E)
13 struct MaxFlowDinic {
14     typedef int flow_t;
15     struct Edge {
16         int next;
17         int inv; /* inverse edge index */
18         flow_t res; /* residual */

```

```

19     };
20     int n;
21     vector<vector<Edge>> graph;
22     vector<int> q, l, start;
23
24     void init(int _n) {
25         n = _n;
26         graph.resize(n);
27         for (int i = 0; i < n; i++) graph[i].clear();
28     }
29     void add_edge(int s, int e, flow_t cap, flow_t caprev = 0) {
30         Edge forward{ e, graph[e].size(), cap };
31         Edge reverse{ s, graph[s].size(), caprev };
32         graph[s].push_back(forward);
33         graph[e].push_back(reverse);
34     }
35     bool assign_level(int source, int sink) {
36         int t = 0;
37         memset(&l[0], 0, sizeof(l[0]) * l.size());
38         l[source] = 1;
39         q[t++] = source;
40         for (int h = 0; h < t && !l[sink]; h++) {
41             int cur = q[h];
42             for (const auto& e : graph[cur]) {
43                 if (l[e.next] || e.res == 0) continue;
44                 l[e.next] = l[cur] + 1;
45                 q[t++] = e.next;
46             }
47         }
48         return l[sink] != 0;
49     }
50     flow_t block_flow(int cur, int sink, flow_t current) {
51         if (cur == sink) return current;
52         for (int& i = start[cur]; i < graph[cur].size(); i++) {
53             auto& e = graph[cur][i];
54             if (e.res == 0 || l[e.next] != l[cur] + 1) continue;
55             if (flow_t res = block_flow(e.next, sink, min(e.res, current))) {
56                 e.res -= res;
57                 graph[e.next][e.inv].res += res;
58                 return res;
59             }
60         }
61         return 0;
62     }
63     flow_t solve(int source, int sink) {
64         q.resize(n);
65         l.resize(n);
66         start.resize(n);
67         flow_t ans = 0;
68         while (assign_level(source, sink)) {
69             memset(&start[0], 0, sizeof(start[0]) * n);
70             while (flow_t flow = block_flow(source, sink, numeric_limits<
71                 flow_t>::max()))
72                 ans += flow;

```

```

73     return ans;
74 }
75 };

```

## 5.10 Min-cost Maximum Flow

```

1 // precondition: there is no negative cycle.
2 // usage:
3 // MinCostFlow mcf(n);
4 // for(each edges) mcf.addEdge(from, to, cost, capacity);
5 // mcf.solve(source, sink); // min cost max flow
6 // mcf.solve(source, sink, 0); // min cost flow
7 // mcf.solve(source, sink, goal_flow); // min cost flow with total_flow >=
   goal_flow if possible
8 struct MinCostFlow
9 {
10     typedef int cap_t;
11     typedef int cost_t;
12
13     bool iszerocap(cap_t cap) { return cap == 0; }
14
15     struct edge {
16         int target;
17         cost_t cost;
18         cap_t residual_capacity;
19         cap_t orig_capacity;
20         size_t revid;
21     };
22
23     int n;
24     vector<vector<edge>> graph;
25     vector<cost_t> pi;
26     bool needNormalize, ranbefore;
27     int lastStart;
28
29     MinCostFlow(int n) : graph(n), n(n), pi(n, 0), needNormalize(false),
   ranbefore(false) {}
30     void addEdge(int s, int e, cost_t cost, cap_t cap)
31     {
32         if (s == e) return;
33         edge forward={e, cost, cap, cap, graph[e].size()};
34         edge backward={s, -cost, 0, 0, graph[s].size()};
35         if (cost < 0 || ranbefore) needNormalize = true;
36         graph[s].emplace_back(forward);
37         graph[e].emplace_back(backward);
38     }
39     bool normalize(int s) {
40         auto infinite_cost = numeric_limits<cost_t>::max();
41         vector<cost_t> dist(n, infinite_cost);
42         dist[s] = 0;
43         queue<int> q;
44         vector<int> v(n), relax_count(n);
45         v[s] = 1; q.push(s);
46         while(!q.empty()) {
47             int cur = q.front();

```

```

48         v[cur] = 0; q.pop();
49         if (++relax_count[cur] >= n) return false;
50         for (const auto &e : graph[cur]) {
51             if (iszerocap(e.residual_capacity)) continue;
52             auto next = e.target;
53             auto ncost = dist[cur] + e.cost;
54             if (dist[next] > ncost) {
55                 dist[next] = ncost;
56                 if (v[next]) continue;
57                 v[next] = 1; q.push(next);
58             }
59         }
60     }
61     for (int i = 0; i < n; i++) pi[i] = dist[i];
62     return true;
63 }
64
65 pair<cost_t, cap_t> AugmentShortest(int s, int e, cap_t flow_limit) {
66     auto infinite_cost = numeric_limits<cost_t>::max();
67     auto infinite_flow = numeric_limits<cap_t>::max();
68     typedef pair<cost_t, int> pq_t;
69     priority_queue<pq_t, vector<pq_t>, greater<pq_t>> pq;
70     vector<pair<cost_t, cap_t>> dist(n, make_pair(infinite_cost, 0));
71     vector<int> from(n, -1), v(n);
72
73     if (needNormalize || (ranbefore && lastStart != s))
74         normalize(s);
75     ranbefore = true;
76     lastStart = s;
77
78     dist[s] = pair<cost_t, cap_t>(0, infinite_flow);
79     pq.emplace(dist[s].first, s);
80     while(!pq.empty()) {
81         auto cur = pq.top().second; pq.pop();
82         if (v[cur]) continue;
83         v[cur] = 1;
84         if (cur == e) continue;
85         for (const auto &e : graph[cur]) {
86             auto next = e.target;
87             if (v[next]) continue;
88             if (iszerocap(e.residual_capacity)) continue;
89             auto ncost = dist[cur].first + e.cost - pi[next] + pi[cur];
90             auto nflow = min(dist[cur].second, e.residual_capacity);
91             if (dist[next].first <= ncost) continue;
92             dist[next] = make_pair(ncost, nflow);
93             from[next] = e.revid;
94             pq.emplace(dist[next].first, next);
95         }
96     }
97     /** augment the shortest path */
98     auto p = e;
99     auto pathcost = dist[p].first + pi[p] - pi[s];
100     auto flow = dist[p].second;
101     if (iszerocap(flow) || (flow_limit <= 0 && pathcost >= 0)) return pair<
   cost_t, cap_t>(0, 0);

```

```

102     if (flow_limit > 0) flow = min(flow, flow_limit);
103     /* update potential */
104     for (int i = 0; i < n; i++) {
105         if (iszerocap(dist[i].second)) continue;
106         pi[i] += dist[i].first;
107     }
108     while (from[p] != -1) {
109         auto nedge = from[p];
110         auto np = graph[p][nedge].target;
111         auto fedge = graph[p][nedge].revid;
112         graph[p][nedge].residual_capacity += flow;
113         graph[np][fedge].residual_capacity -= flow;
114         p = np;
115     }
116     return make_pair(pathcost * flow, flow);
117 }
118
119 pair<cost_t, cap_t> solve(int s, int e, cap_t flow_minimum = numeric_limits
    <cap_t>::max()) {
120     cost_t total_cost = 0;
121     cap_t total_flow = 0;
122     for(;;) {
123         auto res = AugmentShortest(s, e, flow_minimum - total_flow);
124         if (res.second <= 0) break;
125         total_cost += res.first;
126         total_flow += res.second;
127     }
128     return make_pair(total_cost, total_flow);
129 }
130 };

```

## 5.11 General Min-cut (Stoer-Wagner)

```

1 // implementation of Stoer-Wagner algorithm
2 // O(V^3)
3 //usage
4 // MinCut mc;
5 // mc.init(n);
6 // for (each edge) mc.addEdge(a,b,weight);
7 // mincut = mc.solve();
8 // mc.cut = {0,1}^n describing which side the vertex belongs to.
9 struct MinCutMatrix
10 {
11     typedef int cap_t;
12     int n;
13     vector<vector<cap_t>> graph;
14
15     void init(int _n) {
16         n = _n;
17         graph = vector<vector<cap_t>>(n, vector<cap_t>(n, 0));
18     }
19     void addEdge(int a, int b, cap_t w) {
20         if (a == b) return;
21         graph[a][b] += w;
22         graph[b][a] += w;

```

```

23     }
24
25     pair<cap_t, pair<int, int>> stMinCut(vector<int> &active) {
26         vector<cap_t> key(n);
27         vector<int> v(n);
28         int s = -1, t = -1;
29         for (int i = 0; i < active.size(); i++) {
30             cap_t maxv = -1;
31             int cur = -1;
32             for (auto j : active) {
33                 if (v[j] == 0 && maxv < key[j]) {
34                     maxv = key[j];
35                     cur = j;
36                 }
37             }
38             t = s; s = cur;
39             v[cur] = 1;
40             for (auto j : active) key[j] += graph[cur][j];
41         }
42         return make_pair(key[s], make_pair(s, t));
43     }
44
45     vector<int> cut;
46
47     cap_t solve() {
48         cap_t res = numeric_limits<cap_t>::max();
49         vector<vector<int>> grps;
50         vector<int> active;
51         cut.resize(n);
52         for (int i = 0; i < n; i++) grps.emplace_back(1, i);
53         for (int i = 0; i < n; i++) active.push_back(i);
54         while (active.size() >= 2) {
55             auto stcut = stMinCut(active);
56             if (stcut.first < res) {
57                 res = stcut.first;
58                 fill(cut.begin(), cut.end(), 0);
59                 for (auto v : grps[stcut.second.first]) cut[v] = 1;
60             }
61
62             int s = stcut.second.first, t = stcut.second.second;
63             if (grps[s].size() < grps[t].size()) swap(s, t);
64
65             active.erase(find(active.begin(), active.end(), t));
66             grps[s].insert(grps[s].end(), grps[t].begin(), grps[t].end());
67             for (int i = 0; i < n; i++) { graph[i][s] += graph[i][t]; graph[i]
                ][t] = 0; }
68             for (int i = 0; i < n; i++) { graph[s][i] += graph[t][i]; graph[t]
                ][i] = 0; }
69             graph[s][s] = 0;
70         }
71         return res;
72     }
73 };

```



## 6 Geometry

### 6.1 Basic Operations

```
1 const double eps = 1e-9;
2
3 inline int diff(double lhs, double rhs) {
4     if (lhs - eps < rhs && rhs < lhs + eps) return 0;
5     return (lhs < rhs) ? -1 : 1;
6 }
7
8 inline bool is_between(double check, double a, double b) {
9     if (a < b)
10         return (a - eps < check && check < b + eps);
11     else
12         return (b - eps < check && check < a + eps);
13 }
14
15 struct Point {
16     double x, y;
17     bool operator==(const Point& rhs) const {
18         return diff(x, rhs.x) == 0 && diff(y, rhs.y) == 0;
19     }
20     Point operator+(const Point& rhs) const {
21         return Point{ x + rhs.x, y + rhs.y };
22     }
23     Point operator-(const Point& rhs) const {
24         return Point{ x - rhs.x, y - rhs.y };
25     }
26     Point operator*(double t) const {
27         return Point{ x * t, y * t };
28     }
29 };
30
31 struct Circle {
32     Point center;
33     double r;
34 };
35
36 struct Line {
37     Point pos, dir;
38 };
39
40 inline double inner(const Point& a, const Point& b) {
41     return a.x * b.x + a.y * b.y;
42 }
43
44 inline double outer(const Point& a, const Point& b) {
45     return a.x * b.y - a.y * b.x;
46 }
47
48 inline int ccw_line(const Line& line, const Point& point) {
49     return diff(outer(line.dir, point - line.pos), 0);
50 }
```

```
51
52 inline int ccw(const Point& a, const Point& b, const Point& c) {
53     return diff(outer(b - a, c - a), 0);
54 }
55
56 inline double dist(const Point& a, const Point& b) {
57     return sqrt(inner(a - b, a - b));
58 }
59
60 inline double dist2(const Point &a, const Point &b) {
61     return inner(a - b, a - b);
62 }
63
64 inline double dist(const Line& line, const Point& point, bool segment = false)
65 {
66     double c1 = inner(point - line.pos, line.dir);
67     if (segment && diff(c1, 0) <= 0) return dist(line.pos, point);
68     double c2 = inner(line.dir, line.dir);
69     if (segment && diff(c2, c1) <= 0) return dist(line.pos + line.dir, point);
70     return dist(line.pos + line.dir * (c1 / c2), point);
71 }
72
73 bool get_cross(const Line& a, const Line& b, Point& ret) {
74     double mdet = outer(b.dir, a.dir);
75     if (diff(mdet, 0) == 0) return false;
76     double t2 = outer(a.dir, b.pos - a.pos) / mdet;
77     ret = b.pos + b.dir * t2;
78     return true;
79 }
80
81 bool get_segment_cross(const Line& a, const Line& b, Point& ret) {
82     double mdet = outer(b.dir, a.dir);
83     if (diff(mdet, 0) == 0) return false;
84     double t1 = -outer(b.pos - a.pos, b.dir) / mdet;
85     double t2 = outer(a.dir, b.pos - a.pos) / mdet;
86     if (!is_between(t1, 0, 1) || !is_between(t2, 0, 1)) return false;
87     ret = b.pos + b.dir * t2;
88     return true;
89 }
90
91 Point inner_center(const Point &a, const Point &b, const Point &c) {
92     double wa = dist(b, c), wb = dist(c, a), wc = dist(a, b);
93     double w = wa + wb + wc;
94     return Point{ (wa * a.x + wb * b.x + wc * c.x) / w, (wa * a.y + wb * b.y +
95         wc * c.y) / w };
96 }
97
98 Point outer_center(const Point &a, const Point &b, const Point &c) {
99     Point d1 = b - a, d2 = c - a;
100     double area = outer(d1, d2);
101     double dx = d1.x * d1.x * d2.y - d2.x * d2.x * d1.y
102         + d1.y * d2.y * (d1.x - d2.x);
103     double dy = d1.y * d1.x * d2.x - d2.y * d2.x * d1.x
104         + d1.x * d2.x * (d1.x - d2.x);
105     return Point{ a.x + dx / area / 2.0, a.y - dy / area / 2.0 };
106 }
```

```

104 }
105
106 vector<Point> circle_line(const Circle& circle, const Line& line) {
107     vector<Point> result;
108     double a = 2 * inner(line.dir, line.dir);
109     double b = 2 * (line.dir.x * (line.pos.x - circle.center.x)
110         + line.dir.y * (line.pos.y - circle.center.y));
111     double c = inner(line.pos - circle.center, line.pos - circle.center)
112         - circle.r * circle.r;
113     double det = b * b - 2 * a * c;
114     int pred = diff(det, 0);
115     if (pred == 0)
116         result.push_back(line.pos + line.dir * (-b / a));
117     else if (pred > 0) {
118         det = sqrt(det);
119         result.push_back(line.pos + line.dir * ((-b + det) / a));
120         result.push_back(line.pos + line.dir * ((-b - det) / a));
121     }
122     return result;
123 }
124
125 vector<Point> circle_circle(const Circle& a, const Circle& b) {
126     vector<Point> result;
127     int pred = diff(dist(a.center, b.center), a.r + b.r);
128     if (pred > 0) return result;
129     if (pred == 0) {
130         result.push_back((a.center * b.r + b.center * a.r) * (1 / (a.r + b.r)));
131         return result;
132     }
133     double aa = a.center.x * a.center.x + a.center.y * a.center.y - a.r * a.r;
134     double bb = b.center.x * b.center.x + b.center.y * b.center.y - b.r * b.r;
135     double tmp = (bb - aa) / 2.0;
136     Point cdiff = b.center - a.center;
137     if (diff(cdiff.x, 0) == 0) {
138         if (diff(cdiff.y, 0) == 0)
139             return result; // if (diff(a.r, b.r) == 0): same circle
140         return circle_line(a, Line{ Point{ 0, tmp / cdiff.y }, Point{ 1, 0 } });
141     }
142     return circle_line(a,
143         Line{ Point{ tmp / cdiff.x, 0 }, Point{ -cdiff.y, cdiff.x } });
144 }
145
146 Circle circle_from_3pts(const Point& a, const Point& b, const Point& c) {
147     Point ba = b - a, cb = c - b;
148     Line p{ (a + b) * 0.5, Point{ ba.y, -ba.x } };
149     Line q{ (b + c) * 0.5, Point{ cb.y, -cb.x } };
150     Circle circle;
151     if (!get_cross(p, q, circle.center))
152         circle.r = -1;
153     else
154         circle.r = dist(circle.center, a);
155     return circle;
156 }

```

```

157
158 Circle circle_from_2pts_rad(const Point& a, const Point& b, double r) {
159     double det = r * r / dist2(a, b) - 0.25;
160     Circle circle;
161     if (det < 0)
162         circle.r = -1;
163     else {
164         double h = sqrt(det);
165         // center is to the left of a->b
166         circle.center = (a + b) * 0.5 + Point{ a.y - b.y, b.x - a.x } * h;
167         circle.r = r;
168     }
169     return circle;
170 }

```

## 6.2 Compare angles

## 6.3 Convex Hull

```

1 // find convex hull
2 // O(n*logn)
3 vector<Point> convex_hull(vector<Point>& dat) {
4     if (dat.size() <= 3) return dat;
5     vector<Point> upper, lower;
6     sort(dat.begin(), dat.end(), [](const Point& a, const Point& b) {
7         return (a.x == b.x) ? a.y < b.y : a.x < b.x;
8     });
9     for (const auto& p : dat) {
10         while (upper.size() >= 2 && ccw(++upper.rbegin(), *upper.rbegin(), p)
11             >= 0) upper.pop_back();
12         while (lower.size() >= 2 && ccw(++lower.rbegin(), *lower.rbegin(), p)
13             <= 0) lower.pop_back();
14         upper.emplace_back(p);
15         lower.emplace_back(p);
16     }
17     upper.insert(upper.end(), ++lower.rbegin(), --lower.rend());
18     return upper;

```

## 6.4 Polygon Cut

```

1 // left side of a->b
2 vector<Point> cut_polygon(const vector<Point>& polygon, Line line) {
3     if (!polygon.size()) return polygon;
4     typedef vector<Point>::const_iterator piter;
5     piter la, lan, fi, fip, i, j;
6     la = lan = fi = fip = polygon.end();
7     i = polygon.end() - 1;
8     bool lastin = diff(ccw_line(line, polygon[polygon.size() - 1]), 0) > 0;
9     for (j = polygon.begin(); j != polygon.end(); j++) {
10         bool thisin = diff(ccw_line(line, *j), 0) > 0;
11         if (lastin && !thisin) {
12             la = i;

```

```

13     lan = j;
14 }
15 if (!lastin && thisin) {
16     fi = j;
17     fip = i;
18 }
19 i = j;
20 lastin = thisin;
21 }
22 if (fi == polygon.end()) {
23     if (!lastin) return vector<Point>();
24     return polygon;
25 }
26 vector<Point> result;
27 for (i = fi ; i != lan ; i++) {
28     if (i == polygon.end()) {
29         i = polygon.begin();
30         if (i == lan) break;
31     }
32     result.push_back(*i);
33 }
34 Point lc, fc;
35 get_cross(Line{ *la, *lan - *la }, line, lc);
36 get_cross(Line{ *fip, *fi - *fip }, line, fc);
37 result.push_back(lc);
38 if (diff(dist2(lc, fc), 0) != 0) result.push_back(fc);
39 return result;
40 }

```

## 6.5 Pick's theorem

격자점으로 구성된 simple polygon이 주어짐.  $i$ 는 polygon 내부의 격자점 수,  $b$ 는 polygon 선분 위 격자점 수,  $A$ 는 polygon의 넓이라고 할 때, 다음과 같은 식이 성립한다.

$$A = i + \frac{b}{2} - 1$$

# 7 String

## 7.1 KMP

```

1 typedef vector<int> seq_t;
2
3 void calculate_pi(vector<int>& pi, const seq_t& str) {
4     pi[0] = -1;
5     for (int i = 1, j = -1; i < str.size(); i++) {
6         while (j >= 0 && str[i] != str[j + 1]) j = pi[j];
7         if (str[i] == str[j + 1])
8             pi[i] = ++j;
9         else
10             pi[i] = -1;
11     }

```

```

12 }
13
14 // returns all positions matched
15 // O(|text|+|pattern|)
16 vector<int> kmp(const seq_t& text, const seq_t& pattern) {
17     vector<int> pi(pattern.size()), ans;
18     if (pattern.size() == 0) return ans;
19     calculate_pi(pi, pattern);
20     for (int i = 0, j = -1; i < text.size(); i++) {
21         while (j >= 0 && text[i] != pattern[j + 1]) j = pi[j];
22         if (text[i] == pattern[j + 1]) {
23             j++;
24             if (j + 1 == pattern.size()) {
25                 ans.push_back(i - j);
26                 j = pi[j];
27             }
28         }
29     }
30     return ans;
31 }

```

## 7.2 Aho-Corasick

```

1 #include <algorithm>
2 #include <vector>
3 #include <queue>
4 using namespace std;
5
6 struct AhoCorasick
7 {
8     const int alphabet;
9     struct node {
10         node() {}
11         explicit node(int alphabet) : next(alphabet) {}
12         vector<int> next, report;
13         int back = 0, output_link = 0;
14     };
15     int maxid = 0;
16     vector<node> dfa;
17     explicit AhoCorasick(int alphabet) : alphabet(alphabet), dfa(1, node(
18         alphabet)) { }
19     template<typename InIt, typename Fn> void add(int id, InIt first, InIt
20         last, Fn func) {
21         int cur = 0;
22         for ( ; first != last; ++first) {
23             auto s = func(*first);
24             if (auto next = dfa[cur].next[s]) cur = next;
25             else {
26                 cur = dfa[cur].next[s] = (int)dfa.size();
27                 dfa.emplace_back(alphabet);
28             }
29             dfa[cur].report.push_back(id);
30             maxid = max(maxid, id);
31         }

```

```

31 void build() {
32     queue<int> q;
33     vector<char> visit(dfa.size());
34     visit[0] = 1;
35     q.push(0);
36     while(!q.empty()) {
37         auto cur = q.front(); q.pop();
38         dfa[cur].output_link = dfa[cur].back;
39         if (dfa[dfa[cur].back].report.empty())
40             dfa[cur].output_link = dfa[dfa[cur].back].output_link;
41         for (int s = 0; s < alphabet; s++) {
42             auto &next = dfa[cur].next[s];
43             if (next == 0) next = dfa[dfa[cur].back].next[s];
44             if (visit[next]) continue;
45             if (cur) dfa[next].back = dfa[dfa[cur].back].next[s];
46             visit[next] = 1;
47             q.push(next);
48         }
49     }
50 }
51 template<typename InIt, typename Fn> vector<int> countMatch(InIt first,
52     InIt last, Fn func) {
53     int cur = 0;
54     vector<int> ret(maxid+1);
55     for (; first != last; ++first) {
56         cur = dfa[cur].next[func(*first)];
57         for (int p = cur; p; p = dfa[p].output_link)
58             for (auto id : dfa[p].report) ret[id]++;
59     }
60     return ret;
61 }

```

### 7.3 Suffix Array with LCP

```

1 typedef char T;
2
3 // calculates suffix array.
4 // O(n*logn)
5 vector<int> suffix_array(const vector<T>& in) {
6     int n = (int)in.size(), c = 0;
7     vector<int> temp(n), pos2bckt(n), bckt(n), bpos(n), out(n);
8     for (int i = 0; i < n; i++) out[i] = i;
9     sort(out.begin(), out.end(), [&](int a, int b) { return in[a] < in[b]; });
10    for (int i = 0; i < n; i++) {
11        bckt[i] = c;
12        if (i + 1 == n || in[out[i]] != in[out[i + 1]]) c++;
13    }
14    for (int h = 1; h < n && c < n; h <= 1) {
15        for (int i = 0; i < n; i++) pos2bckt[out[i]] = bckt[i];
16        for (int i = n - 1; i >= 0; i--) bpos[bckt[i]] = i;
17        for (int i = 0; i < n; i++)
18            if (out[i] >= n - h) temp[bpos[bckt[i]]++] = out[i];
19        for (int i = 0; i < n; i++)
20            if (out[i] >= h) temp[bpos[pos2bckt[out[i] - h]]++] = out[i] - h;

```

```

21    c = 0;
22    for (int i = 0; i + 1 < n; i++) {
23        int a = (bckt[i] != bckt[i + 1]) || (temp[i] >= n - h)
24            || (pos2bckt[temp[i + 1] + h] != pos2bckt[temp[i] + h]);
25        bckt[i] = c;
26        c += a;
27    }
28    bckt[n - 1] = c++;
29    temp.swap(out);
30 }
31 return out;
32 }
33
34 // calculates lcp array. it needs suffix array & original sequence.
35 // O(n)
36 vector<int> lcp(const vector<T>& in, const vector<int>& sa) {
37     int n = (int)in.size();
38     if (n == 0) return vector<int>();
39     vector<int> rank(n), height(n - 1);
40     for (int i = 0; i < n; i++) rank[sa[i]] = i;
41     for (int i = 0, h = 0; i < n; i++) {
42         if (rank[i] == 0) continue;
43         int j = sa[rank[i] - 1];
44         while (i + h < n && j + h < n && in[i + h] == in[j + h]) h++;
45         height[rank[i] - 1] = h;
46         if (h > 0) h--;
47     }
48     return height;
49 }

```

### 7.4 Suffix Tree

### 7.5 Manacher's Algorithm

```

1 // find longest palindromic span for each element in str
2 // O(|str|)
3 void manacher(const string& str, int plen[]) {
4     int r = -1, p = -1;
5     for (int i = 0; i < str.length(); ++i) {
6         if (i <= r)
7             plen[i] = min((2 * p - i >= 0) ? plen[2 * p - i] : 0, r - i);
8         else
9             plen[i] = 0;
10        while (i - plen[i] - 1 >= 0 && i + plen[i] + 1 < str.length()
11            && str[i - plen[i] - 1] == str[i + plen[i] + 1]) {
12            plen[i] += 1;
13        }
14        if (i + plen[i] > r) {
15            r = i + plen[i];
16            p = i;
17        }
18    }
19 }

```

## 8 Miscellaneous

### 8.1 Fast I/O

```
1 namespace fio {
2     const int BSIZE = 524288;
3     char buffer[BSIZE];
4     int p = BSIZE;
5     inline char readChar() {
6         if(p == BSIZE) {
7             fread(buffer, 1, BSIZE, stdin);
8             p = 0;
9         }
10        return buffer[p++];
11    }
12    int readInt() {
13        char c = readChar();
14        while ((c < '0' || c > '9') && c != '-') {
15            c = readChar();
16        }
17        int ret = 0; bool neg = c == '-';
18        if (neg) c = readChar();
19        while (c >= '0' && c <= '9') {
20            ret = ret * 10 + c - '0';
21            c = readChar();
22        }
23        return neg ? -ret : ret;
24    }
25 }
```

```
15         System.out.println("Good");
16     }
17 }
18 }
```

### 8.2 Magic Numbers

소수 : 10 007 , 10 009 , 10 111 , 31 567 , 70 001 , 1 000 003 , 1 000 033 , 4 000 037 ,  
1 000 000 007 , 1 000 000 009

### 8.3 Java Examples

```
1 import java.util.Scanner;
2
3 public class example
4 {
5     public static void main(String[] args)
6     {
7         Scanner in = new Scanner(System.in);
8         int T = in.nextInt();
9         while (T --> 0)
10        {
11            String str = in.next();
12            if (str.matches("[A-F]?A+F+C+[A-F]?"))
13                System.out.println("Infected!");
14            else
```