

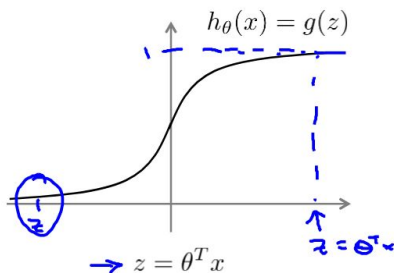
Plan

1. Large margin classification - Take a look at support vector machine supervised algorithm

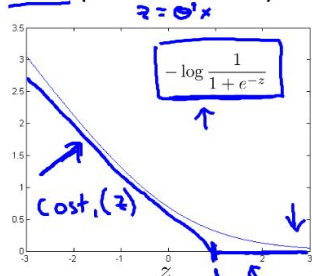
a. Optimization objective

$$\min_{\theta} \frac{1}{m} \left[\sum_{i=1}^m y^{(i)} \left(-\log h_{\theta}(x^{(i)}) \right) + (1 - y^{(i)}) \left(-\log(1 - h_{\theta}(x^{(i)})) \right) \right] + \frac{\lambda}{2m} \sum_{j=1}^n \theta_j^2$$

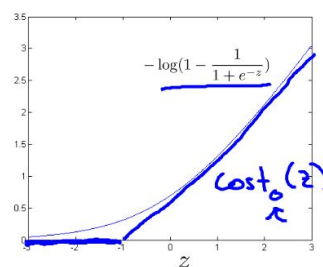
$$\rightarrow h_{\theta}(x) = \frac{1}{1 + e^{-\theta^T x}}$$



If $y = 1$ (want $\theta^T x \gg 0$):

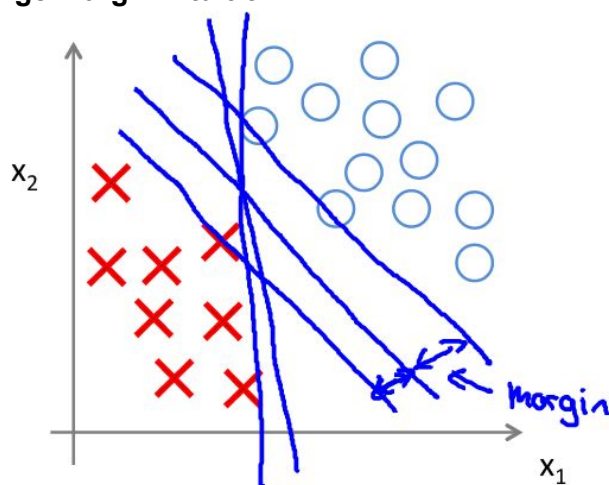


If $y = 0$ (want $\theta^T x \ll 0$):



$$\min_{\theta} C \sum_{i=1}^m \left[y^{(i)} \text{cost}_1(\theta^T x^{(i)}) + (1 - y^{(i)}) \text{cost}_0(\theta^T x^{(i)}) \right] + \frac{1}{2} \sum_{j=1}^n \theta_j^2$$

b. Large margin intuition



c. Math behind LMC

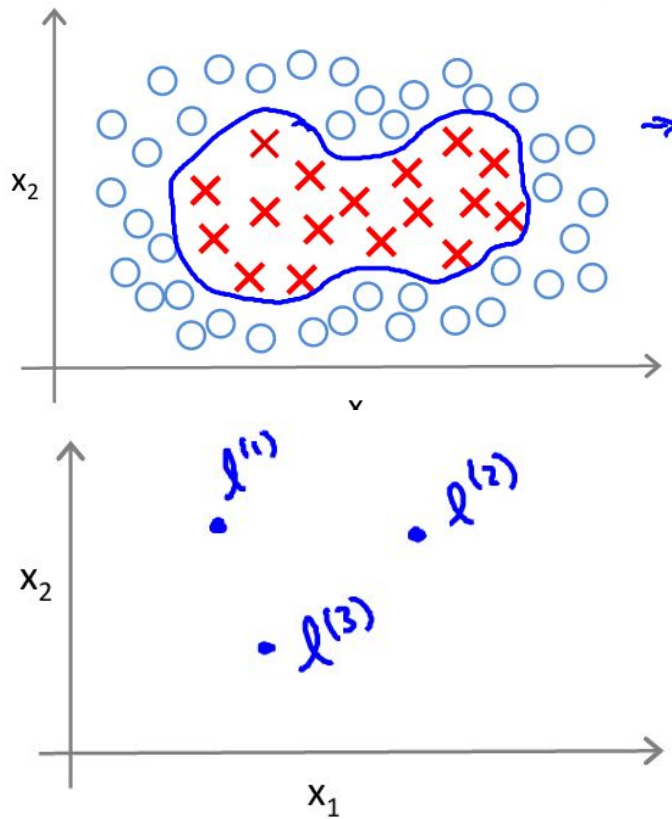
$$\rightarrow \min_{\theta} \frac{1}{2} \sum_{j=1}^n \theta_j^2 = \frac{1}{2} \|\theta\|^2 \leftarrow$$

$$\text{s.t. } \boxed{p^{(i)} \cdot \|\theta\| \geq 1} \quad \text{if } y^{(i)} = 1$$

$$\boxed{p^{(i)} \cdot \|\theta\| \leq -1} \quad \text{if } y^{(i)} = 0$$

2. Kernels - Defining algorithms with non-linear decision boundaries

a. Gaussian kernel



$$l^{(1)} = \begin{bmatrix} 3 \\ 5 \end{bmatrix}$$

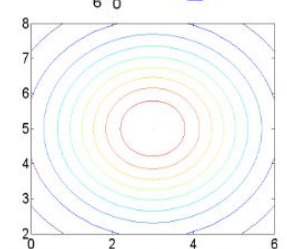
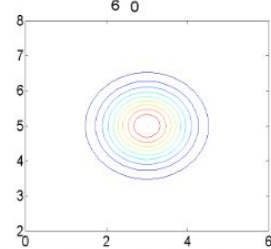
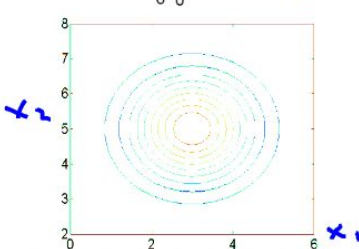
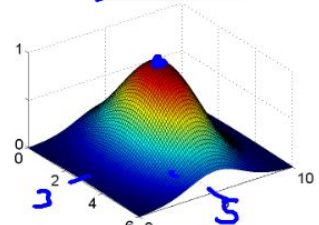
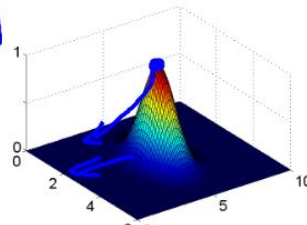
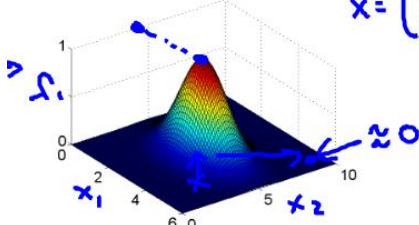
$$f_1 = \exp\left(-\frac{\|x - l^{(1)}\|^2}{2\sigma^2}\right)$$

$$\sigma^2 = 1$$

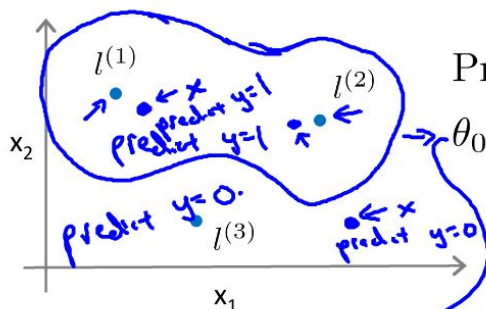
$$x = \begin{bmatrix} 3 \\ 5 \end{bmatrix}$$

$$\sigma^2 = 0.5$$

$$\sigma^2 = 3$$



b. Creating landmarks



Predict "1" when

$$\theta_0 + \theta_1 f_1 + \theta_2 f_2 + \theta_3 f_3 \geq 0$$

$$\theta_0 = -0.5, \theta_1 = 1, \theta_2 = 1, \theta_3 = 0$$

3. Using an SVM

Questions:

1. In which type of ML problems we can apply SVM?
2. An alternative name for SVM?
3. What kind of kernel do you know? (This question isn't about Linux kernels btw)

Glossary

Kernel - point we use as a feature based on our learning datasets - *By default it's highly recommended to use Gaussian kernel*

Support Vector Machine - yet another learning algorithm used in classification problems - *Support Vector Machine aka Large Margin Classifier*

Large Margin Classifier - learning algorithm with an alternative approach on classification problem - *Support Vector Machine aka Large Margin Classifier*