# DS-WEEK 3

# **Tree Concepts**

- > Definition and Properties of Trees
- > Types of Trees
  - Complete Tree
  - Full Tree
  - Perfect Tree
- > Node Properties
  - Height vs. Depth of a Node
  - Degree of a Node
- > Applications of Trees

### **Binary Search Tree (BST) Concepts**

- Definition and Properties of BST
- **❖** Operations on BST
  - > Insertion
  - > Deletion
  - Search (contains)
- ❖ Tree Traversals
  - ➤ In-order Traversal
  - > Pre-order Traversal
  - Post-order Traversal
- Applications of BST
- Advanced BST Concepts
  - > Validating a BST
  - Finding the Closest Value to a Given Number in a BST
  - ➤ Self-Balancing Trees (AVL Trees, Red-Black Trees)
  - Checking if a BST is a Subset of Another Tree

## **Heap Concepts**

- Definition and Properties of Heaps
- Types of Heaps
  - ➤ Max-Heap
  - ➤ Min-Heap
- Operations on Heaps
  - > Insertion
  - > Deletion
  - Peek (get max/min)
- Heapification Methods
  - > Top-Down Heapification
  - > Bottom-Up Heapification
- Advanced Heap Concepts

- > Binomial Heap
- Applications of Heaps
  - > Priority Queues

### **Heap Sort**

- Concept and Algorithm
- **❖** Time Complexity: O(n log n)
- Applications of Heap Sort

## **Trie Concepts**

- Definition and Properties of Tries
- Operations on Tries
  - > Insertion
  - > Deletion
  - > Search
- Applications of Tries
  - > Autocomplete
  - > Spell Checker
- Comparison with Hash Tables

# **Graph Concepts**

- Definition and Properties of Graphs
- ❖ Types of Graphs
  - > Directed vs. Undirected Graphs
  - > Weighted vs. Unweighted Graphs
- Special Types of Graphs
  - Directed Acyclic Graph (DAG)
  - Cyclic Graphs
  - > Isolated Vertex
- Graph Representations
  - > Adjacency List
  - > Adjacency Matrix
- Applications of Graphs

### **Graph Traversals**

- Breadth-First Search (BFS)
  - Concept and Algorithm
  - > Applications
- Depth-First Search (DFS)
  - Concept and Algorithm
  - > Applications

## **Advanced Graph Concepts**

#### Graph Indexing

- > Vertex Indexing
- > Edge Indexing

### Shortest Path Algorithms

- > Dijkstra's Algorithm
- > Bellman-Ford Algorithm

### **Additional Topics**

- Priority Queues Using Heaps
- ❖ Trie vs. Hash Table
- ❖ Self-Balancing Trees
  - > AVL Trees
  - Red-Black Trees
  - > Splay Trees
  - ➤ B-Trees

# **DS-WEEK 3: PRACTICALS**

# **Tree Concepts**

#### 1. Tree Operations

- Implement a basic tree structure.
- Write a function to calculate the height of a tree.
- Write a function to calculate the depth of a node.
- Write a function to find the degree of a node.

#### 2. Tree Traversals

- o Implement in-order traversal.
- o Implement pre-order traversal.
- o Implement post-order traversal.

### 3. Tree Applications

- Write a function to check if a tree is complete.
- o Write a function to check if a tree is full.
- Write a function to check if a tree is perfect.

# **Binary Search Tree (BST) Concepts**

### 1. **BST Operations**

Implement a BST with insertion, deletion, and search (contains) operations.

#### 2. Tree Traversals in BST

- o Implement in-order traversal for a BST.
- Implement pre-order traversal for a BST.
- o Implement post-order traversal for a BST.

#### 3. **BST Applications**

- Write a function to find the closest value to a given number in a BST.
- Write a function to validate if a tree is a BST.
- o Implement self-balancing BSTs (AVL Tree, Red-Black Tree).
- Write a function to check if a BST is a subset of another tree.

### **Heap Concepts**

### 1. Heap Operations

- o Implement a max-heap with insertion, deletion, and peek operations.
- Implement a min-heap with insertion, deletion, and peek operations.

### 2. Heapification Methods

- Implement top-down heapification.
- o Implement bottom-up heapification.

### 3. Heap Applications

• Write a function to implement a priority queue using a heap.

### **Heap Sort**

#### 1. Heap Sort Implementation

- o Implement the heap sort algorithm.
- Write a function to sort an array using heap sort.

### **Trie Concepts**

### 1. Trie Operations

Implement a trie with insertion, deletion, and search operations.

#### 2. Trie Applications

- Write a function for autocomplete using a trie.
- Write a function for spell checking using a trie.

# **Graph Concepts**

#### 1. Graph Representations

- Implement a graph using an adjacency list.
- o Implement a graph using an adjacency matrix.

#### 2. Graph Operations

Write functions to add and remove vertices and edges.

#### 3. Special Graph Types

- Write a function to check if a graph is a Directed Acyclic Graph (DAG).
- Write a function to find isolated vertices.

### **Graph Traversals**

#### 1. Breadth-First Search (BFS)

- o Implement BFS for a graph.
- Write a function to find the shortest path using BFS.

### 2. Depth-First Search (DFS)

o Implement DFS for a graph.

• Write a function to find connected components using DFS.

# **Advanced Graph Concepts**

### 1. Shortest Path Algorithms

- o Implement Dijkstra's algorithm.
- o Implement Bellman-Ford algorithm.

#### 2. Graph Indexing

• Write functions for vertex indexing and edge indexing.

# **Additional Topics**

### 1. Priority Queues Using Heaps

• Write a function to implement a priority queue using a heap.

### 2. Trie vs. Hash Table

• Write a comparison of trie and hash table for different use cases.

### 3. Self-Balancing Trees

- o Implement an AVL tree.
- o Implement a Red-Black tree.
- o Implement a Splay tree.
- o Implement a B-tree.