

## Circular Motion

### Rotational Kinematics

$$\theta = \theta_0 + \omega_0 t + \alpha t^2 / 2$$

$$\omega = \omega_0 + \alpha t$$

$$\omega^2 = \omega_0^2 + 2\alpha(\theta - \theta_0)$$

### Relating rotational and linear quantities

Here  $R$  is the radius and  $s$  is arc length

$$s = R\theta$$

$$v_t = R\omega$$

$$a_t = R\alpha$$

$$a = \sqrt{a_r^2 + a_\theta^2}$$

$$a_c = v^2 / r \text{ (centripetal accel)}$$

$$L = I\omega \text{ (ang mom)}$$

$$2\pi \text{ rad} = 1 \text{ rev}$$

## Newton's Second Law

$$\Sigma \vec{F} = m\vec{a}$$

$$\Sigma \vec{F} = mv^2 / r$$

## Work

Conservative (path independent) is spring, gravity, and normal.  $U$  is potential,  $K$  is kinetic

$$W = \vec{F} \cdot \vec{s}$$

$$W = Fs \cos \theta$$

$$W_{tot} = \Delta k$$

$$W_{tot} = W_c + W_{nc}$$

$$W_c = -\Delta U$$

$$W_{nc} = \Delta K + \Delta U \quad \text{\#\# Energy} \quad ME = KE + PE$$

$$W_{nc} = \Delta ME$$

if  $W_{nc} = 0$  then  $\Delta ME = 0$  (conservation of mechanical energy)

### **Potential Energy**

$$U_{gravity} = mgy$$

$$U_{spring} = kx^2/2$$

### **Kinetic Energy**

$$K = mv^2/2$$

$$Joule = Newton \cdot meter$$