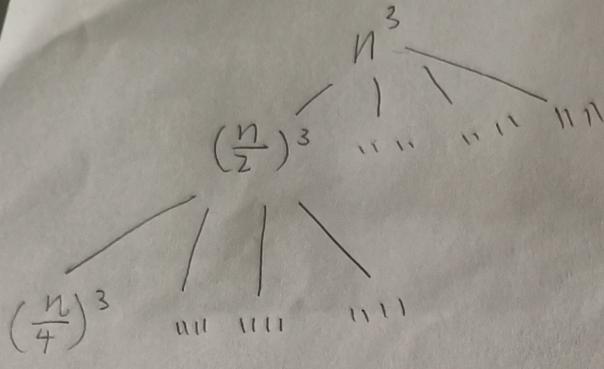


$$b=2 \quad q=4$$

$$4 \left( w \left( \frac{n}{2} \right)^3 \right) + n^3$$



level	$\frac{n}{2^i}$	total cost
0	$\frac{n}{2^0}$	$n^3$
1	$\frac{n}{2^1}$	$c_1 \frac{n^3}{2^1} + 4c_2$
2	$\frac{n}{2^2}$	$c_1 \frac{n^3}{2^2} + 16c_2$
$i$	$\frac{n}{2^i}$	$c_1 \frac{n^3}{2^i} + 4^i c_2$

$$= \sum_{i=0}^{\log n} \left( c_1 \frac{n^3}{2^i} + 4^i c_2 \right)$$

$$= c_1 n^3 \sum_{i=0}^{\log n} 2^i + c_2 \sum_{i=0}^{\log n} 4^i \quad \text{let } c_1 = 1$$

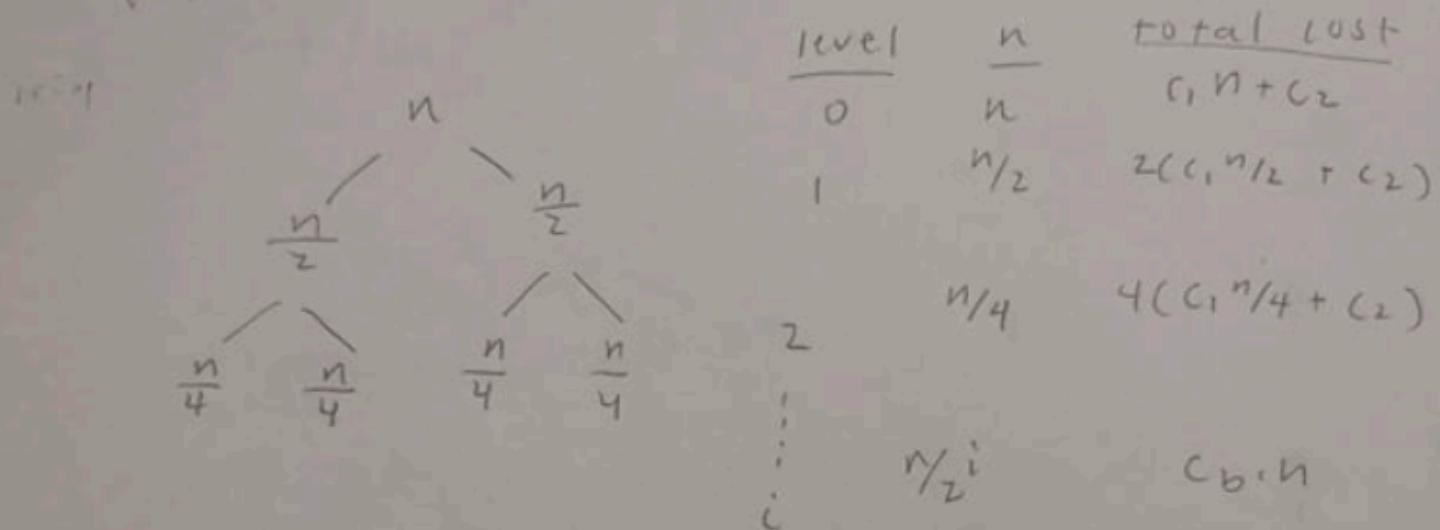
$$= n^3 \sum_{i=0}^{\log n} 2^i + c_2 \sum_{i=0}^{\log n} 4^i$$

$$< 2n^3 + 4c_2 n$$

$$\in O(n^3)$$

$$W(n) = a \cdot W(n/b) + f(n)$$

let  $a = 2, b = 2$



$\log n$

$$\sum_{i=0}^{\log n} (c_1 n + 2^i c_2) \quad \text{let } c_1 = 1$$

$$= \sum_{i=0}^{\log n} (n + 2^i c_2)$$

$$= n \sum_{i=0}^{\log n} 1 + \sum_{i=0}^{\log n} 2^i c_2$$

$$\leq c_1 n \log n + 2 c_2 n$$

$$\in O(n \log n)$$

$$w(n) = a \cdot w(n/b) + f(n^2)$$

$$\text{let } a = 2, b = 2$$

<u>level</u>	$\frac{n}{n}$	<u>Total cost</u>
0	$\frac{n}{2}$	$c_1 n^2 + c_2$
1	$\frac{n}{2}$	$c_1 \left(\frac{n^2}{2}\right)^2 + 2c_2$
2	$\frac{n}{4}$	$c_1 \frac{n^2}{4} + 4c_2$
$\vdots$	$\frac{n}{2^i}$	$c_1 \frac{n^2}{2^i} + 2^i \cdot c_2$

$n^2$

$(\frac{n}{2})^2 (\frac{n}{2})^2$

$(\frac{n}{4})^2 (\frac{n}{4})^2 (\frac{n}{4})^2 (\frac{n}{4})^2$

$\vdots$

$\frac{n}{2^i}$

$$= \sum_{i=0}^{\log n} \left( c_1 \frac{n^2}{2^i} + 2^i c_2 \right)$$

$$= n^2 \sum_{i=0}^{\log n} \frac{1}{2^i} + c_2 \sum_{i=0}^{\log n} 2^i \quad \text{let } c_1 = 1$$

$$< 2c_1 n^2 + 2c_2 n$$

$$\in \boxed{O(n^2)}$$