CMPS 2200 Assignment 2

Name: Joshua Hoddal

In this assignment we'll work on applying the methods we've learned to analyze recurrences, and also see their behavior in practice. As with previous assignments, some of of your answers will go in main.py and test_main.py. You should feel free to edit this file with your answers; for handwritten work please scan your work and submit a PDF titled assignment-02.pdf and push to your github repository.

Part 1. Asymptotic Analysis

Derive asymptotic upper bounds of work for each recurrence below.

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$$W(n) = 2W(n/3) + 1$$
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• $W(n) = 5W(n/4) + n$.

• W(n) = 5W(n/4) + n.

• W(n) = 7W(n/7) + n.

$$7i\left(\frac{\Omega}{7i}\right) = \Omega \quad \text{Balanca}$$

$$Cost per level $\Omega = \frac{1}{2} \quad \text{if } \log_{7}(\Omega)$

$$= 9W(n/3) + n^{2} \quad \text{if } \log_{7}(\Omega)$$$$

•
$$W(n) = 9W(n/3) + n^2$$
.
• $Q^{\dagger} \left(\frac{1}{3}\right)^2 = Q^{\dagger} \frac{n^2}{4!} = n^2 \text{ Balmel} \qquad | = \frac{n}{3!} \qquad | = \log_3(n)|$
• $Cost \text{ per level} \cdot \text{Hot level} = W(n) \qquad | W_n = n^2 \log_3(n)|$

• $W(n) = 8W(n/2) + n^3$. • $g(\frac{\Lambda}{2})^3 = g(\frac{3}{8}) = \Lambda^3$ Balanii)
• (x) + per |evel| + of |evel| = W(n)• (x) + per |evel| + of |evel| = W(n)• (x) + per |evel| + of |evel| = W(n)

$$|V| = \frac{1}{8!} = \frac{1}{8!} = \frac{1}{2!}$$

$$|V| = \frac{1}{3} \log_2(n)$$

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$$|V| = \frac{1}{3} \log_2(n)$$

$$W(n) = 49W(n/25) + n^{3/2} \log n.$$

$$V(a) = \frac{1}{\sqrt{2}} \frac{1}{\sqrt{2}} \log \frac{1}{\sqrt{2}} = 49^{-1} \frac{1}{\sqrt{2}} \log \frac{1}{\sqrt{2}} = \log \frac{1}{\sqrt{2}} = \log \frac{1}{\sqrt{2}} \log \frac{1}$$

Suppose that for a given task you are choosing between the following three algorithms:

- Algorithm A solves problems by dividing them into five subproblems of half the size, recursively solving each subproblem, and then combining the solutions in linear time.
- Algorithm \mathcal{B} solves problems of size n by recursively solving two subproblems of size n-1 and then combining the solutions in constant time.
- Algorithm C solves problems of size n by dividing them into nine subproblems of size n/3, recursively solving each subproblem, and then combining the solutions in $O(n^2)$ time.

What are the asymptotic running times of each of these algorithms? Which algorithm would you choose?

A:
$$W(n) = S W(\frac{\Lambda}{2}) + 1$$
 Leaf
 $S : \frac{\Lambda}{2}$ Dominates
 $N = \frac{\Lambda}{2}$ $W(n) = S = S \log_2(n)$
 $W(n) = N \log_2(s)$

B:
$$W_{(n)}=2W(n-1)+1$$

 $V(n-1)=2v(n-2)+1$
 $2W(n)=2^{i}W(n-1)+2^{i}$
 $1=n-1$
 $w(n)=2^{n-1}W(1)+2^{n-1}$
 $w(n)=2^{n-1}W(1)+2^{n-1}$
 $w(n)=2^{n-1}W(1)+2^{n-1}$

C.) Way =
$$9W(\frac{2}{3}) + \Lambda^2$$

$$Q' \frac{\Lambda^2}{3^2};$$

$$\Lambda^2 : Baland$$

$$Results Multiply:$$

$$1 = \frac{\Lambda}{3};$$

$$1 = \frac{\Lambda}{3}$$

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Part 3: Parenthesis Matching

A common task of compilers is to ensure that parentheses are matched. That is, each open parenthesis is followed at some point by a closed parenthesis. Furthermore, a closed parenthesis can only appear if there is a corresponding open parenthesis before it. So, the following are valid:

• ((a)b)
• a()b(c(d))

but these are invalid:

- ((a)
- (a))b(

Below, we'll solve this problem three different ways, using iterate, scan, and divide and conquer.

3a. iterative solution Implement parens_match_iterative, a solution to this problem using the iterate function. Hint: consider using a single counter variable to keep track of whether there are more open or closed parentheses. How can you update this value while iterating from left to right through the input? What must be true of this value at each step for the parentheses to be matched? To complete this, complete the parens_update function and the parens_match_iterative function. The parens_update function will be called in combination with iterate inside parens_match_iterative. Test your implementation with test_parens_match_iterative.

are their Big Oh solutions?

Span is Ola because the function iterates through every index in the list which is 3c. scan solution Implement parens_match_scan a solution to this problem

using scan. Hint: We have given you the function paren_map which maps (to this spen = 1, Wolk is

using scan. Hint: We have given you the function paren_map which maps (to 1,) to -1 and everything else to 0. How can you pass this function to scan to solve the problem? You may also find the min_f function useful here. Implement parens_match_scan and test with test_parens_match_scan

this span=1. Work in because each index of the 1:51 has to be compared which take OCI but this pecusin times thus work is DCN

3d. Assume that any maps are done in parallel, and that we use the efficient implementation of scan from class. What are the recurrences for the Work and Span of this solution?

enter answer here

Interview of the work and S(n) = n S(n) = (eg(n)) S(n) = n S(n) = (eg(n)) S(n) = n S(n) = (eg(n))

3e. divide and conquer solution Implement parens_match_dc_helper, a divide and conquer solution to the problem. A key observation is that we cannot simply solve each subproblem using the above solutions and combine the results. E.g., consider '((()))', which would be split into '(((' and ')))', neither of which is matched. Yet, the whole input is matched. Instead, we'll have to keep track of two numbers: the number of unmatched right parentheses (R), and the number of unmatched left parentheses (L). parens_match_dc_helper returns a tuple (R,L). So, if the input is just '(', then parens_match_dc_helper returns (0,1), indicating that there is 1 unmatched left parens and 0 unmatched right parens. Analogously, if the input is just ')', then the result should be (1,0). The main difficulty is deciding how to merge the returned values for the two recursive calls. E.g., if (i,j) is the result for the left half of the list, and (k,l) is the output of the right half of the list, how can we compute the proper return value (R,L) using only i,j,k,l? Try a few example inputs to guide your solution, then test with test_parens_match_dc_helper.

3f. Assuming any recursive calls are done in parallel, what are the recurrences

f. Assuming any recursive calls are done in paramet, when it is a solution? What are their Big Oh solutions?

Inter answer here $W(\Omega) = 2W(\frac{1}{2}) + U(1) = \frac{1}{2} = \frac{109U(1)}{109U(1)} = \frac{1152(2)}{109U(1)} = \frac{1152($

poralizable so sper always = log(n)