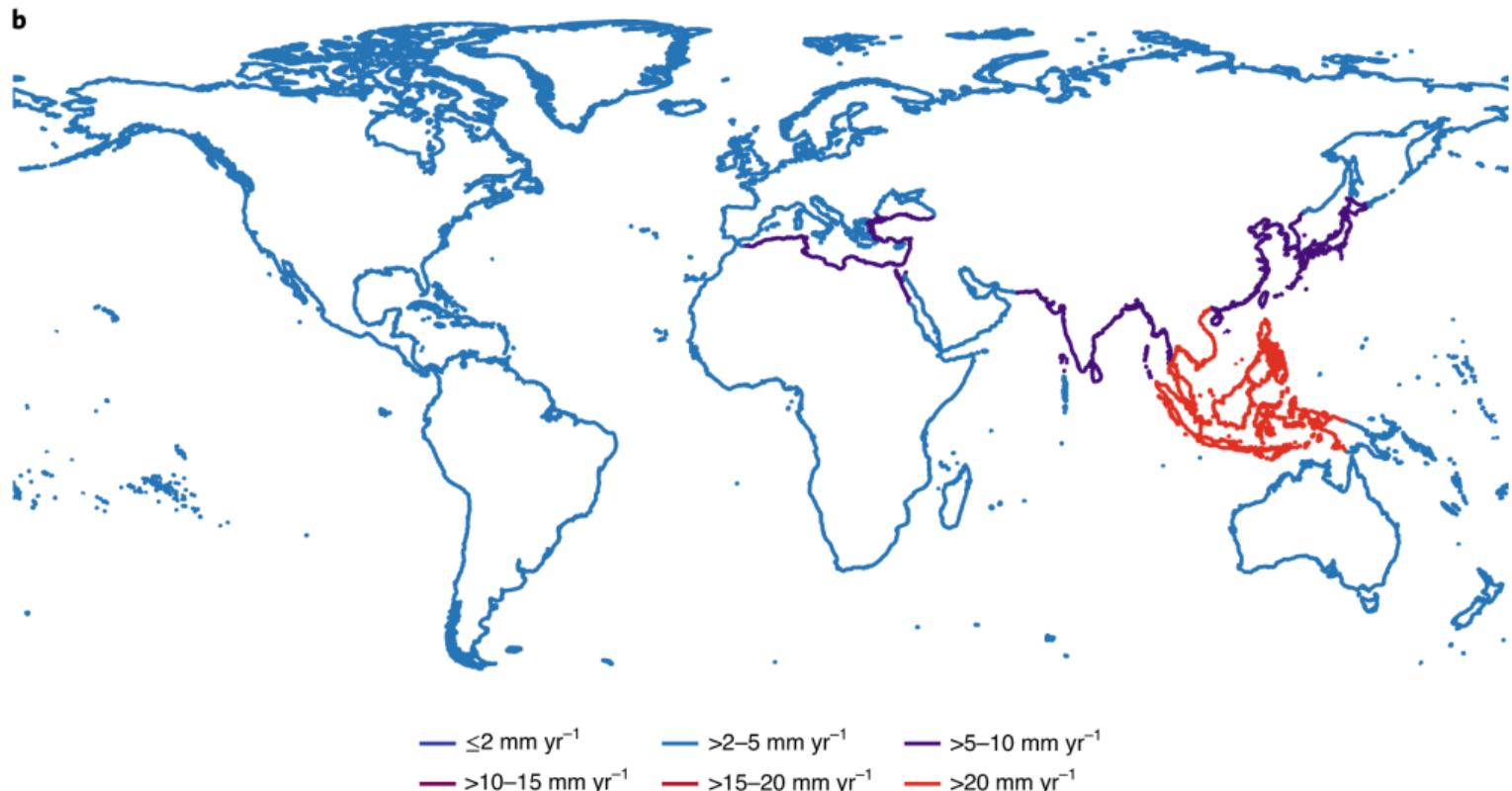


Sea Level Rise and Urban Adaptation in Jakarta

Allan Hsiao
Princeton University

November 15, 2022

Sea levels are rising globally (Nicholls et al. 2021)





Motivation

- **Sea level rise threatens 1B people by 2050** (IPCC 2019)
 - 680M people in low-elevation coastal zones today
- Jakarta will be 35% below sea level by 2050 (Andreas et al. 2018)
 - World's second largest city at 31M (first by 2030)
 - In response, \$40B in proposed infrastructure investments
- **How does government intervention affect long-run adaptation?**
 - How does public adaptation affect private adaptation?

This paper

- **Dynamic spatial model** of coastal development and government defense
 - Estimated with granular spatial data for Jakarta
- Long-run adaptation requires moving inland, but
 - ① Moral hazard from government intervention
 - ② Persistence from durable capital
- **Result:** limited adaptation without government commitment

Contributions

- **Adaptation frictions** under endogenous government intervention
 - Kydland & Prescott 1977, Glaeser & Gyourko 2005, Vigdor 2008, Boustan et al. 2012, Balboni 2021, Desmet et al. 2021, Baylis & Boomhower 2022, Fried 2022, Mulder 2022, Wagner 2022
- **Dynamic spatial model** of urban development
 - Hopenhayn 1992, Ericson & Pakes 1995, Hotz & Miller 1993, Arcidiacono & Miller 2011, Scott 2013, Kalouptsidi 2014, Desmet et al. 2018, Caliendo et al. 2019, Kleinman et al. 2022
- **Sea level rise damages** for Jakarta
 - Budiyono et al. 2015, Takagi et al. 2016, Wijayanti et al. 2017, Andreas et al. 2018

Outline

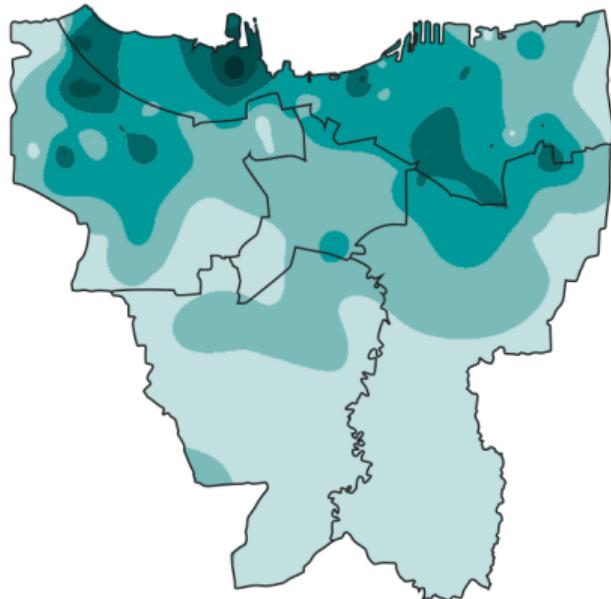
- ① Setting
- ② Theory
- ③ Empirics
- ④ Simulations

Setting

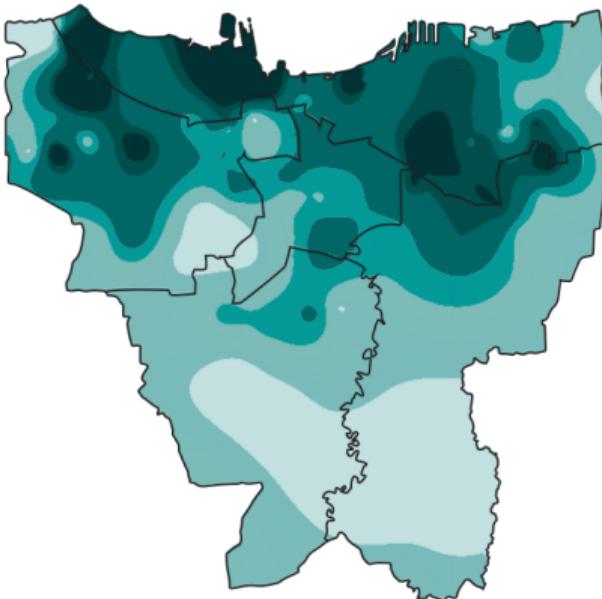




Future land subsidence (SLR 1m by 2100)



2025

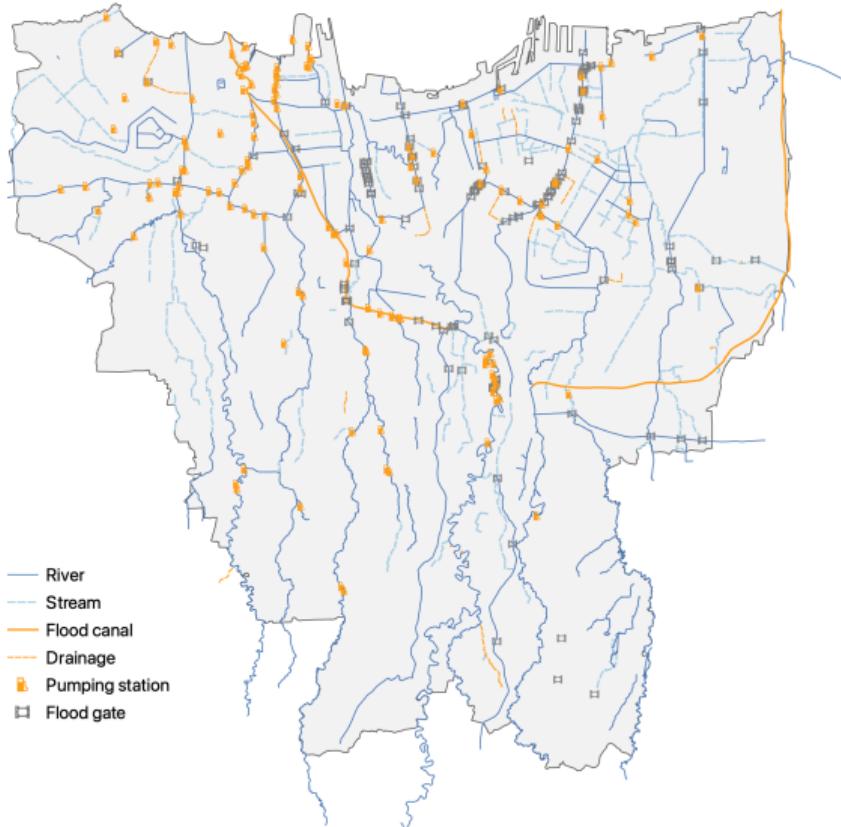


2050



Flood infrastructure

- 1918: West flood canal
- 1960: dams/reservoirs
- 1978: drainage canals
- 2002: East flood canal
- 2011: **sea wall plans**
- 2019: **Nusantara plans**



Profil Proyek NCICD

- Peletakan batu pertama: Oktober 2014
- Target rampung: 2022
- Tahapan pembangunan: 3 (Tahap A, B, dan C)
- Pelaksana: Kementerian PU dan Pemprov DKI
- Biaya investasi: Rp300 triliun
- Reklamasi lahan: 1.000 hektare

Sumber: Kementerian PU-Pera, berbagai sumber, diolah

Wing Park Neighbourhood Waterfront Neighbourhood

Head of Garuda

Wing Park Neighbourhood

Maritime Communities

Core Area

Creative HQ and Research

Tail Area

Creative Living Park

Maritime Communities

Target Konstruksi

Tahap A

Konstruksi: 2014-2017
Flood safety: 2030

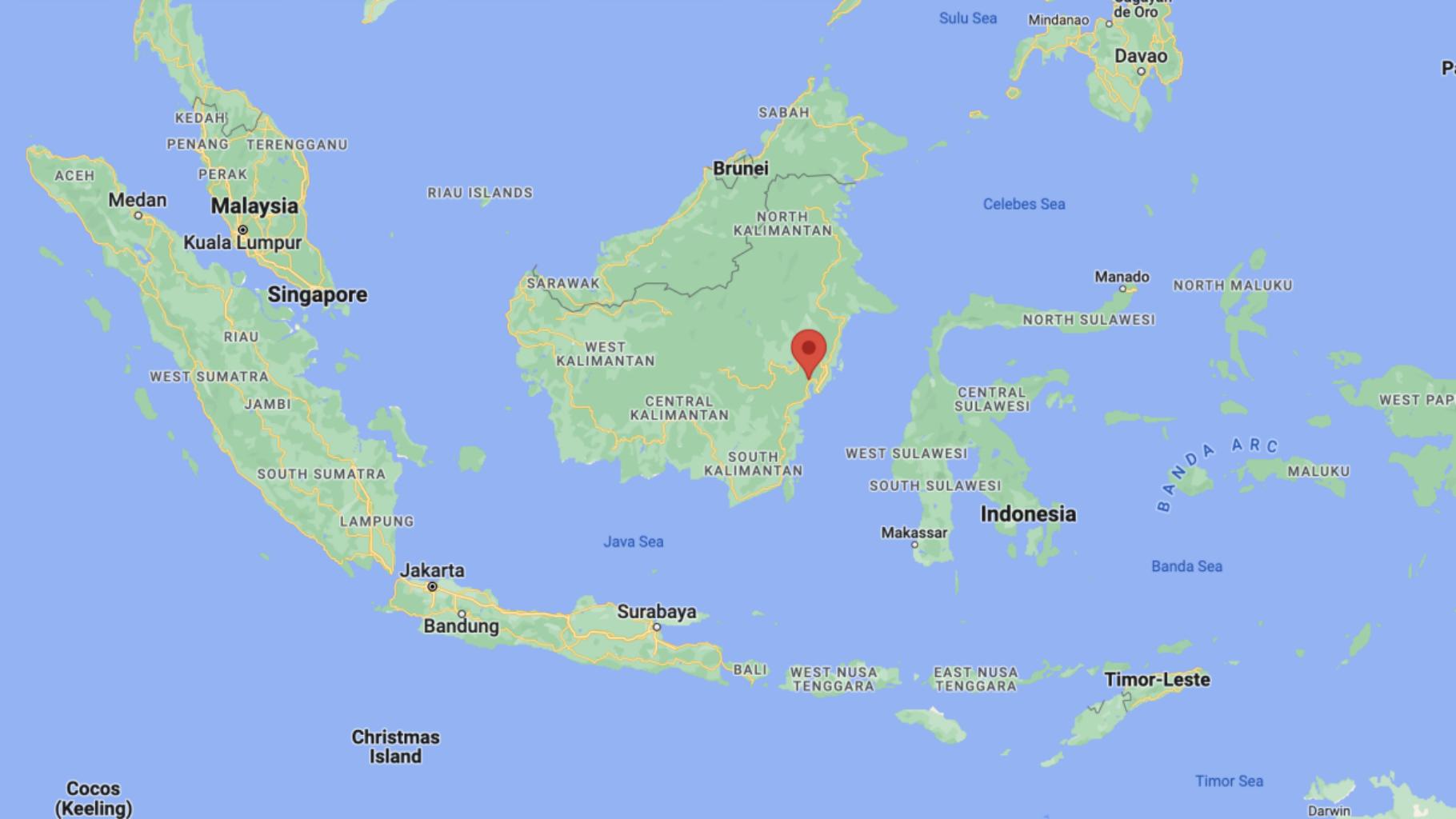
Tahap B

Konstruksi: 2018-2022
Flood Safety: 2030

Tahap C

Konstruksi: 2022





Cocos
(Keeling)

Theory

Coastal development and defense

- ① **Developers** develop d at cost $c(d)$ for $c'' > 0$ (atomistically)
 - ② **Government** defends g at cost $f(g)$ for $f'' > 0$ (wall or otherwise)
 - ③ **Residents** receive $r(d, g)$ for $r_{dg} > 0$ (demand $r'(d; g)$, shifter g)
-
- **Welfare** $W(d, g) = r(d, g) - c(d) - f(g)$
 - **Profits** $\pi(d) = r'(d) - c'(d) + r'(g)g'(d)$ (competed away)

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 - **Profits** $\pi(d) = r'(d) - c'(d) + r'(g) g'(d)$ (competed away)

Moral hazard

- The **social planner** maximizes $W(d, g) = r(d, g) - c(d) - f(g)$

$$[d^*] \quad r'(d) = c'(d)$$

$$[g^*] \quad r'(g) = f'(g)$$

- Developers consider $\pi(d)$, and government $W(g; d)$

$$[d^n] \quad r'(d) + r'(g) g'(d) = c'(d)$$

$$[g^n] \quad r'(g) = f'(g)$$

- Moral hazard when $g'(d) > 0$ implies $d^n > d^*$, $g^n > g^*$

Moral hazard

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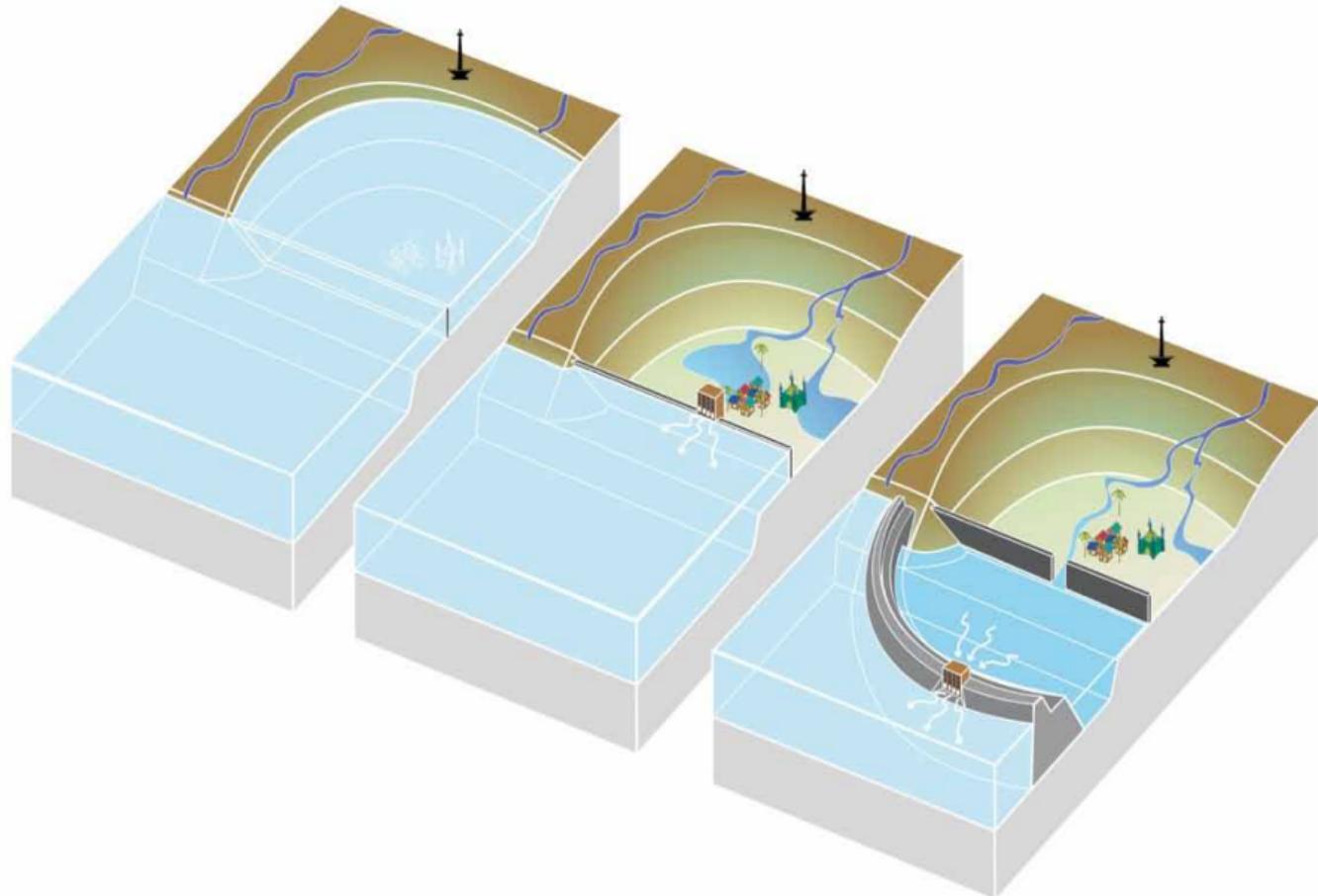
$$[d^n] \quad r'(d) + r'(g) g'(d) = c'(d)$$

$$[g^n] \quad r'(g) = f'(g)$$

- Moral hazard** when $g'(d) > 0$ implies $d^n > d^*$, $g^n > g^*$

Commitment + challenges

- Solution 1: **commit** to g^*
 - $g'(d) = 0$ implies $r'(g) g'(d) = 0$
 - But optimal for government to protect over-development ex post
- Solution 2: **commit** to d^*
 - By taxing or restricting development
 - But developers will lobby against enforcement ex post
- In Jakarta, political pressures demand action
 - In the US, lobbying for zoning expansions and against NFIP re-rating



Dynamics: $r(D_t, G_t)$ for $D_t = D_{t-1} + d_t$

① Moral hazard arises across periods

- Developers exploit both current and future governments (commitment issues)
- Current governments may exploit future governments (political myopia)

② Development has persistent effects

- Current governments can help future governments
- Over-development today raises development tomorrow

Details

Empirics

Empirical framework

$$W = r(d, g) - c(d) - f(g)$$

- $r(d, s(g))$: **spatial model** of residential demand
- $s(g)$: **hydrologic model** of flood risk
- $c(d)$: **dynamic model** of developer supply
- $f(g)$: **engineering estimates**

High-resolution spatial data (2015/2020)

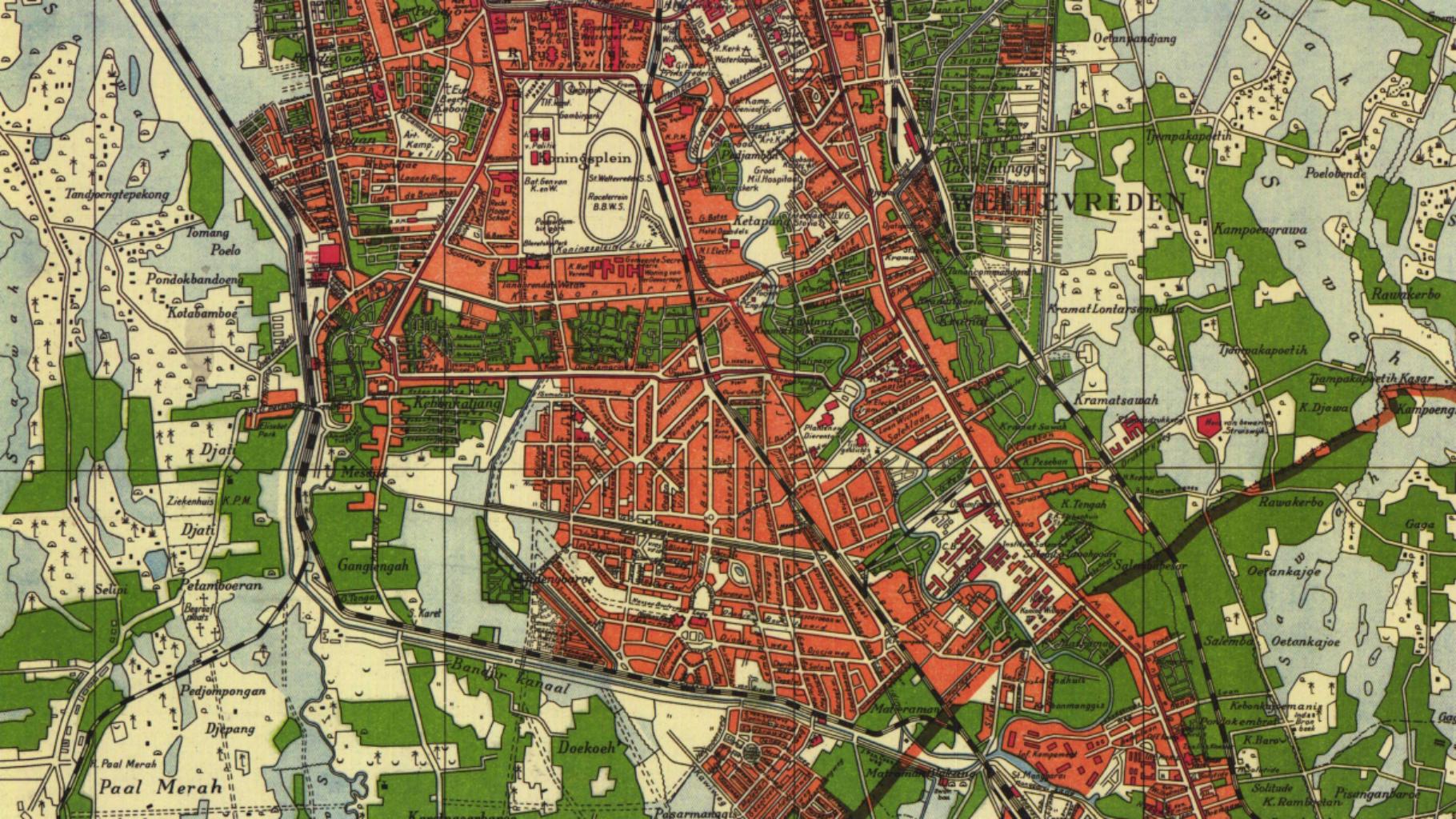
Variable	Source	Map
Building construction	GHSL	Map
Populations	GHSL	Map
Property values	99.co, brickz.id	Map
Land values	Jakarta Smart City	Map
Flood risk	(Hydrological model)	Map

Flooding ↓ ⇒ value ↑ ⇒ construction ↑

	Land value (\$/m ²)			
Flood risk (m/yr)	-2.31*** (3.00)	-1.29*** (3.12)	-0.59** (2.15)	-0.93*** (2.78)
District FE		x		
Sub-district FE			x	
Neighborhood FE				x
Observations	2,722	2,722	2,722	2,722

Flooding ↓ ⇒ value ↑ ⇒ construction ↑

Building construction (m ³)				
Land value (\$/m ²)	0.21*** (0.03)	0.27*** (0.03)	0.37*** (0.05)	0.30*** (0.05)
District FE		x		
Sub-district FE			x	
Neighborhood FE				x
Observations	2,722	2,722	2,722	2,722



Demand from residents

$$U_{ijk} = \underbrace{-\alpha r_k + \rho s_k + \xi_k}_{\delta_k} - \tau m_{jk} + \epsilon_{ijk}$$

- **Spatial model** of residential choice (individual i , origin j , destination k)
 - Static renters consider rents, flood safety, amenities, distances, logit shocks
 - Moving inland abandons high-amenity places and incurs migration costs
 - Will add firms to endogenize (some) amenities
- **Estimation** with 2020 population shares and instruments (BLP 1995)
 - Price endogeneity from correlation of rents and unobserved amenities
 - IV with soil quality and ruggedness as supply shifters

Details

Demand estimates

First stage	Rents	IV	Population
Ruggedness	0.010*** (0.001)	Rents	-0.113*** (0.019)
Flood safety	7.888** (4.018)	Flood safety	1.031** (0.507)
Coastal distance	-0.630*** (0.082)	Coastal distance	-0.072*** (0.016)
District FE	x	District FE	x
Observations	2,181	Observations	2,181
F-stat	76.38		

Supply from developers

$$V_k(w_t) = r_k(w_t)D_{kt} + \mathbb{E}_{kt}[\max\{v_k^1(w_t) + \epsilon_{kt}^1, v_k^0(w_t) + \epsilon_{kt}^0\}]$$

$$v_k^1(w_t) = -c(x_{kt}, \zeta_{kt}) + \beta \mathbb{E}_{kt}[V_k(w_{t+1}^1)]$$

$$v_k^0(w_t) = \beta \mathbb{E}_{kt}[V_k(w_{t+1}^0)]$$

- **Dynamic model** of developer choice (tract k , time t , $\mathbb{E}_{kt} = \mathbb{E}_k[\cdot | w_t]$)
 - Developer-landlords consider state $w_t = (\{D_{kt}\}, \{G_{kt}\})$, rents, costs, logit shocks
 - Moving inland abandons high-rent places and incurs construction costs
- **Estimation:** data as continuation values (Kalouptsidi 2014) [vs. Scott 2013]
 - Price endogeneity from correlation of rents and unobserved costs
 - IV with resident demographics as demand shifters

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Data as continuation values

$$\ln p_{kt}^1 - \ln p_{kt}^0 = v_k^1(w_t) - v_k^0(w_t)$$

$$v_k^1(w_t) = -c_{kt} + \beta \mathbb{E}_{kt}[V_k(w_{t+1}^1)]$$

$$v_k^0(w_t) = \beta \mathbb{E}_{kt}[V_k(w_{t+1}^0)]$$

- Estimation by linear IV: property vs. land values as (V^1, V^0)
 - Assuming competitive real estate markets with rational expectations
 - And atomistic developers

Data as continuation values

$$\ln p_{kt}^1 - \ln p_{kt}^0 = -c(x_{kt}, \zeta_{kt}; \theta) + P_{kt}^1 - P_{kt}^0 + \eta_{kt}$$

$$v_k^1(w_t) = -c_{kt} + \beta \mathbb{E}_{kt}[V_k(w_{t+1}^1)]$$

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Euler CCPs

$$\ln p_{kt}^1 - \ln p_{kt}^0 = v_k^1(w_t) - v_k^0(w_t)$$

$$v_k^1(w_t) = -c_{kt} + \beta \mathbb{E}_{kt}[r_k(w_{t+1}) + \beta V_k(w_{t+2}^{10}) - \ln p_{kt+1}^0]$$

$$v_k^0(w_t) = \beta \mathbb{E}_{kt}[-c_{kt+1} + \beta V_k(w_{t+2}^{01}) - \ln p_{kt+1}^1]$$

- Estimation by linear IV: today vs. tomorrow perturbation ($\Delta X_{kt} = X_{kt} - \beta X_{kt+1}$)
 - Assuming atomistic, long-lived developers with rational expectations
 - Also need $t+1$ data, rent data, and no depreciation

Euler CCPs

$$\Delta \ln p_{kt}^1 - \Delta \ln p_{kt}^0 = -\Delta c(x_{kt}, \zeta_{kt}; \theta) + \beta r_k(w_{t+1}) + \tilde{\eta}_{kt}$$

$$v_k^1(w_t) = -c_{kt} + \beta \mathbb{E}_{kt}[r_k(w_{t+1}) + \beta V_k(w_{t+2}^{10}) - \ln p_{kt+1}^0]$$
$$v_k^0(w_t) = \beta \mathbb{E}_{kt}[-c_{kt+1} + \beta V_k(w_{t+2}^{01}) - \ln p_{kt+1}^1]$$

- Estimation by linear IV: today vs. tomorrow perturbation ($\Delta X_{kt} = X_{kt} - \beta X_{kt+1}$)
 - Assuming atomistic, long-lived developers with rational expectations
 - Also need $t+1$ data, rent data, and no depreciation

Comparing approaches

Estimation	Speed	Expectations
Full-solution (NFP)	Slow	Specified
Two-step (BLP)	Fast	Specified
Euler CCPs	Fast	Rational agents
Baseline	Fast	Rational market

Rents

$$D_{kt}^{\text{res}} = D_{kt}^{\text{dev}}$$

$$[\text{Residents}] \quad D_{kt}^{\text{res}} = \sum_j n_{jt} \left[\frac{\exp\{U_{jk}(r_{kt})\}}{\sum_{\hat{k}} \exp\{U_{j\hat{k}}(r_{\hat{k}t})\}} \right] \phi$$

$$[\text{Developers}] \quad D_{kt+1}^{\text{dev}} = D_{kt} + \frac{\exp\{v_k^1(r_k)\}}{\exp\{v_k^1(r_k)\} + \exp\{v_k^0(r_k)\}}$$

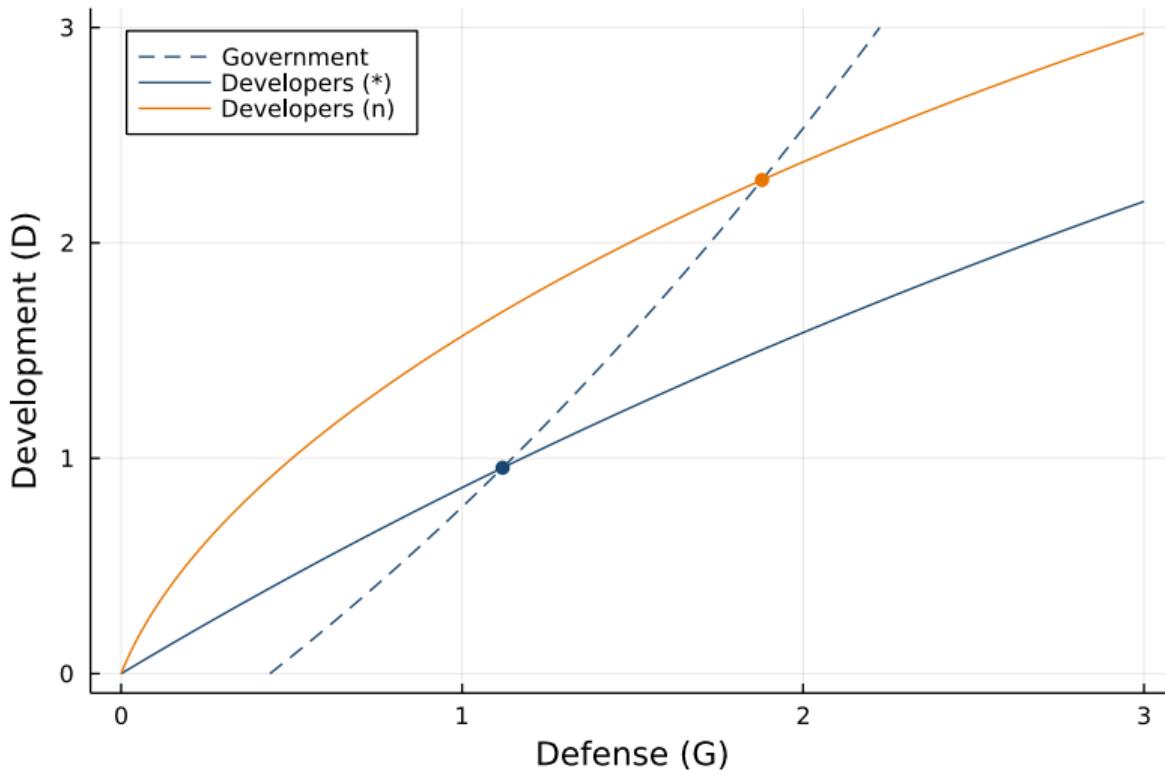
Government

- Commitment level and political turnover by assumption
 - Hydrological model of flood risk $s_k(G)$
 - Engineering estimates of costs $f(G)$
- Counterfactuals

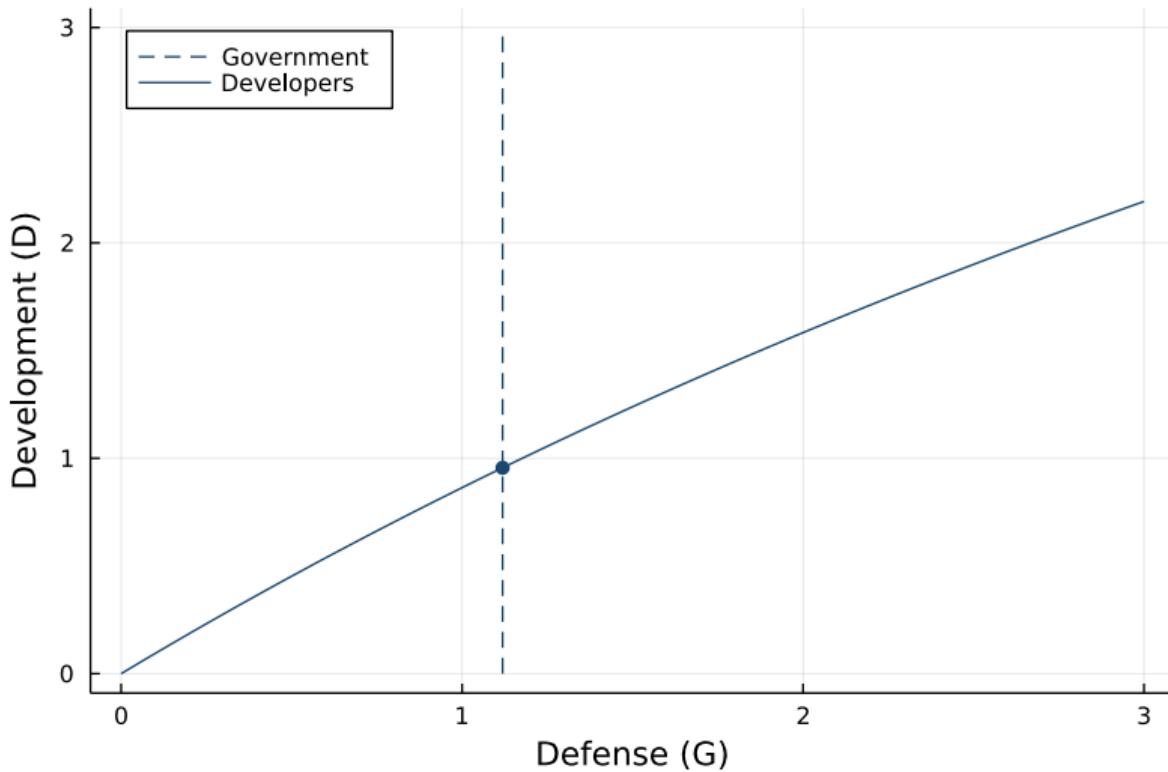
Defense $g \rightarrow$ flooding s by **hydrological** model
 \rightarrow rents r by **demand** model
 \rightarrow development d by **supply** model

Simulations

Over-development and over-defense

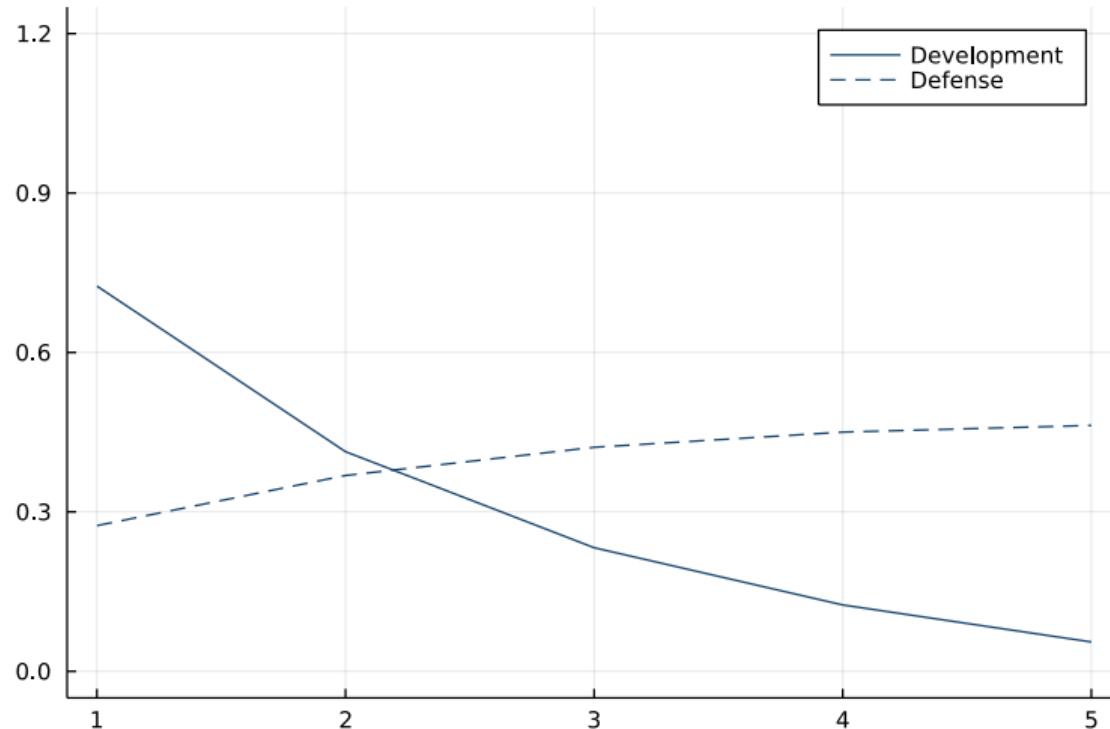


Over-development and over-defense



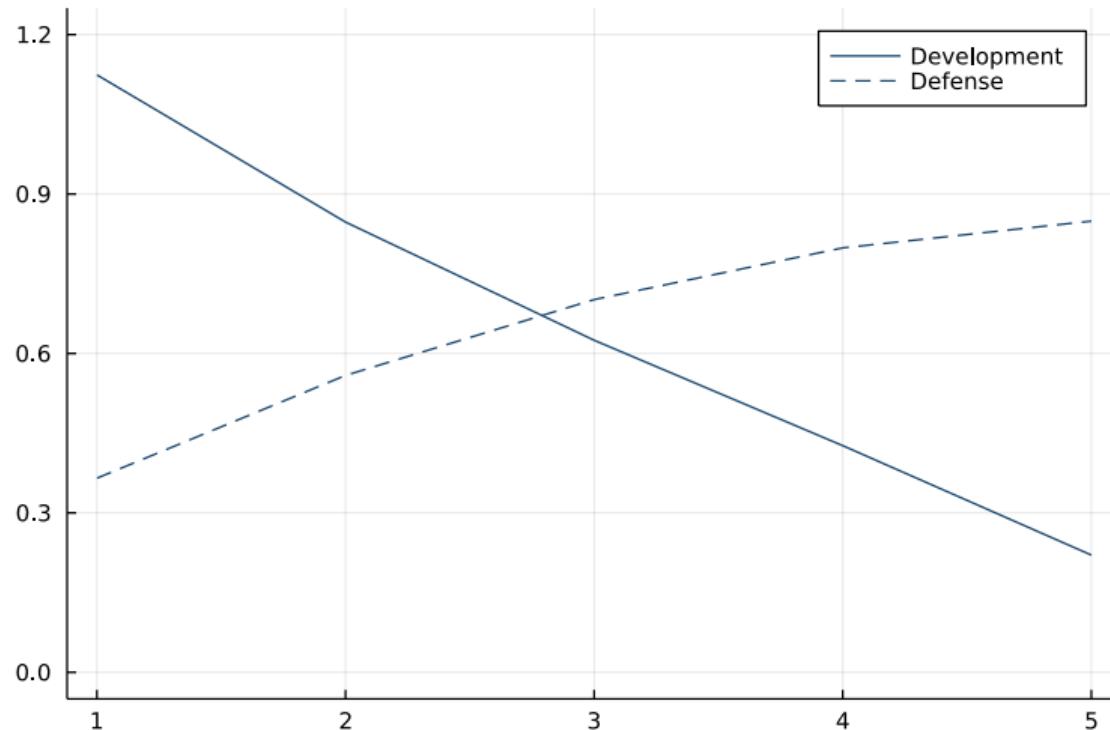
Development and defense

Full commitment



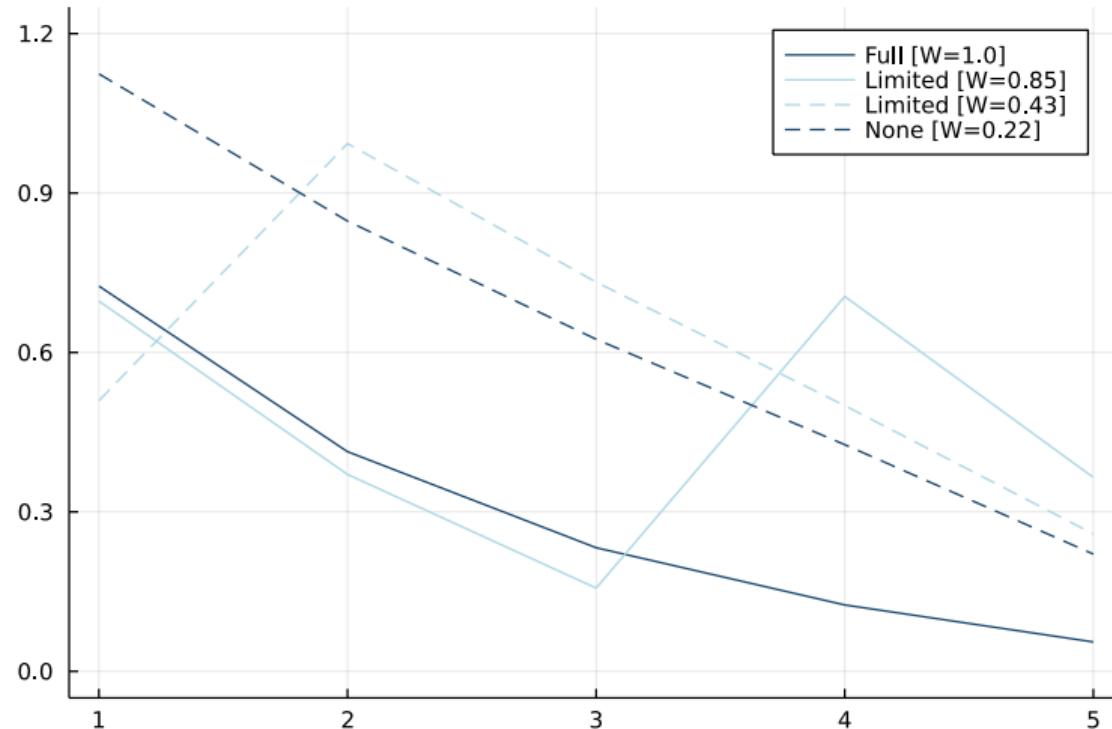
Development and defense

No commitment



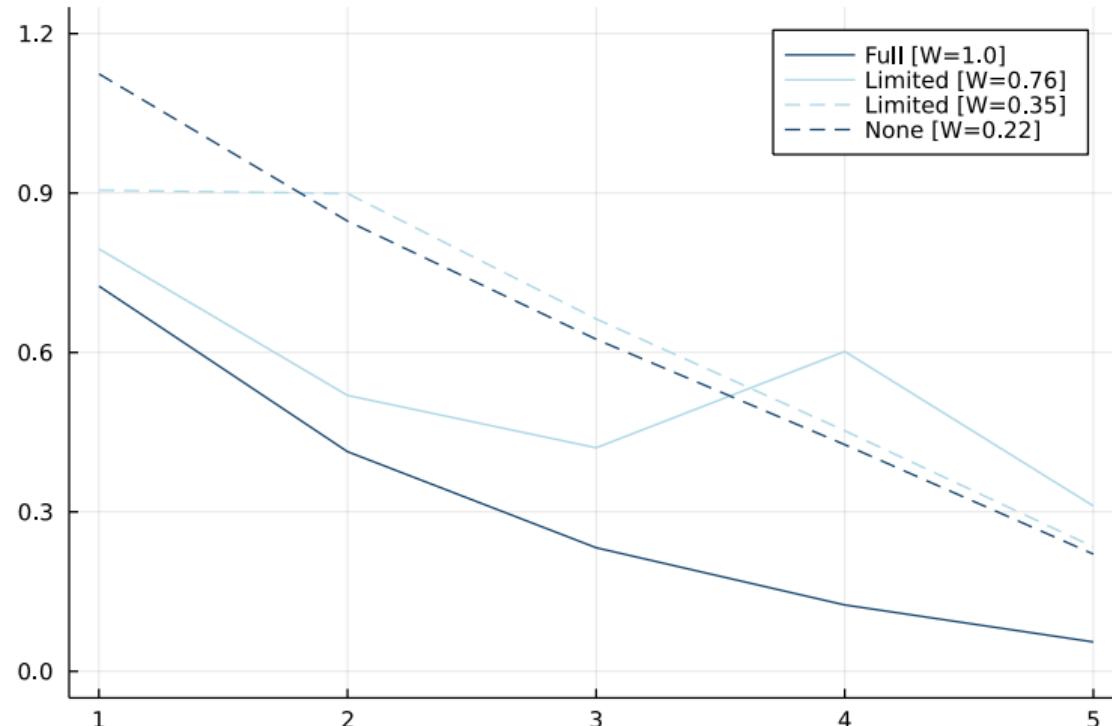
Development

Forward-looking



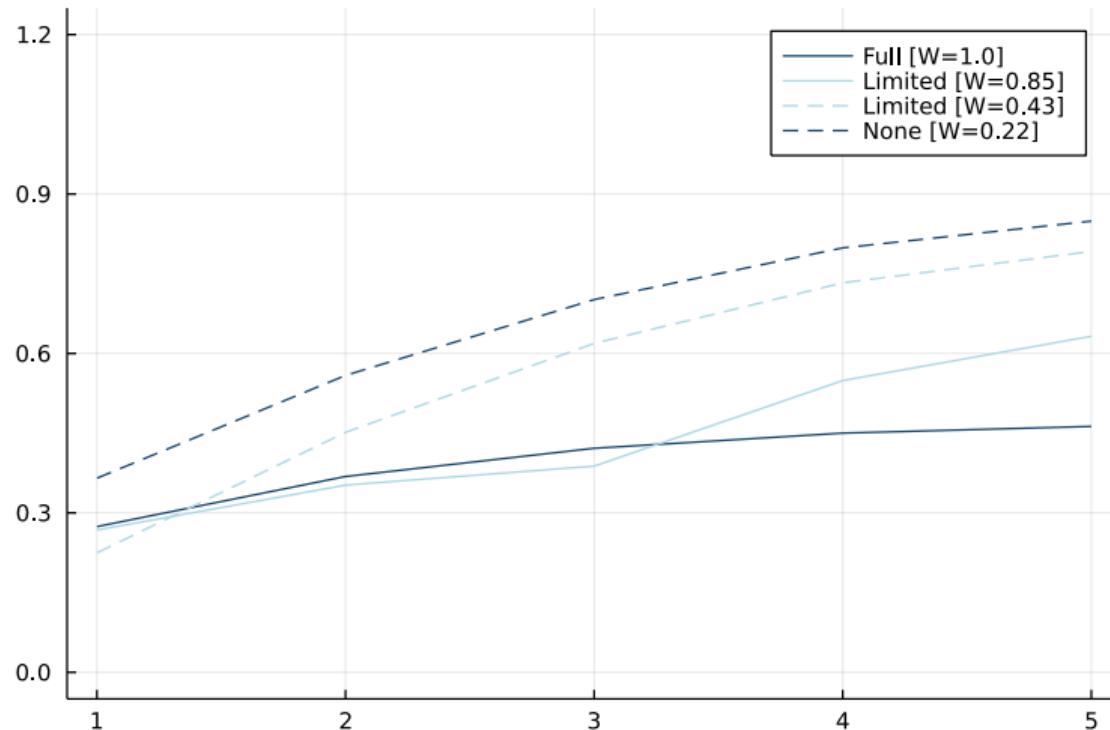
Development

Politically myopic



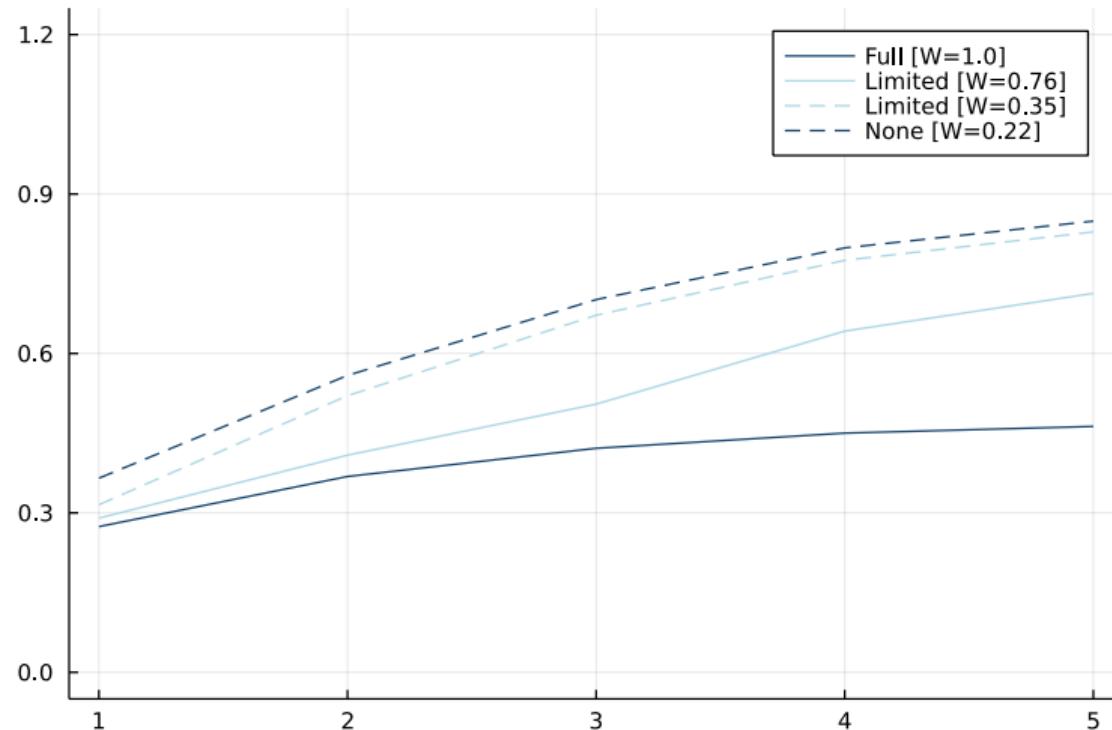
Defense

Forward-looking



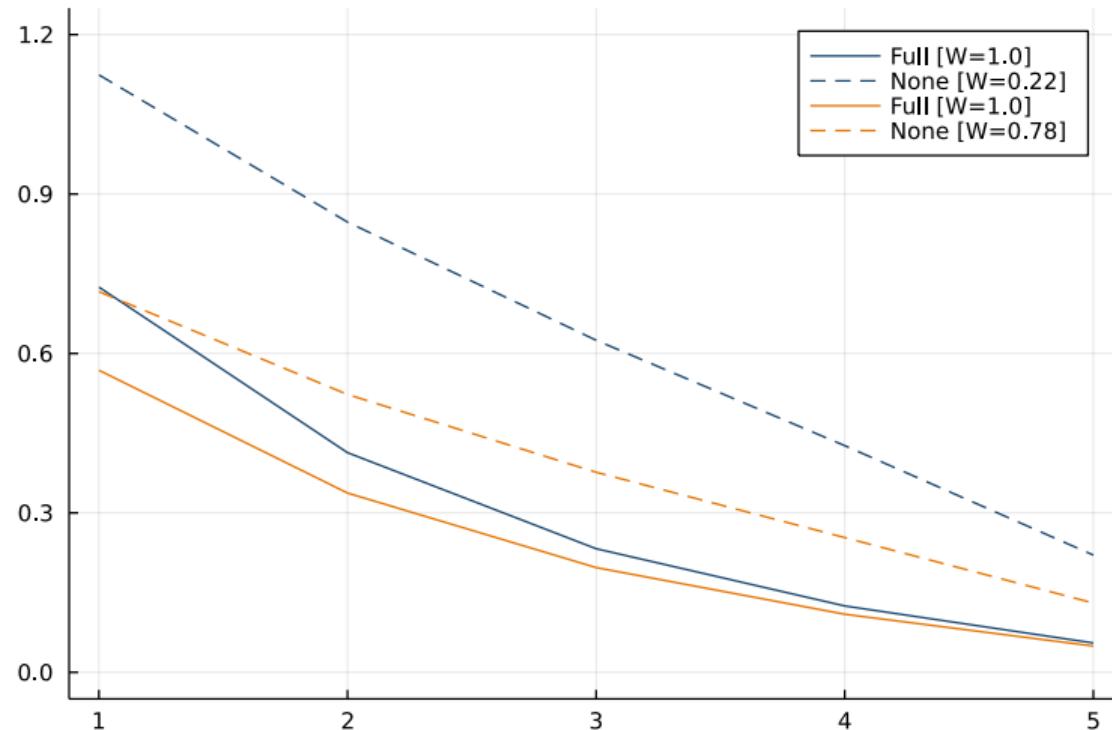
Defense

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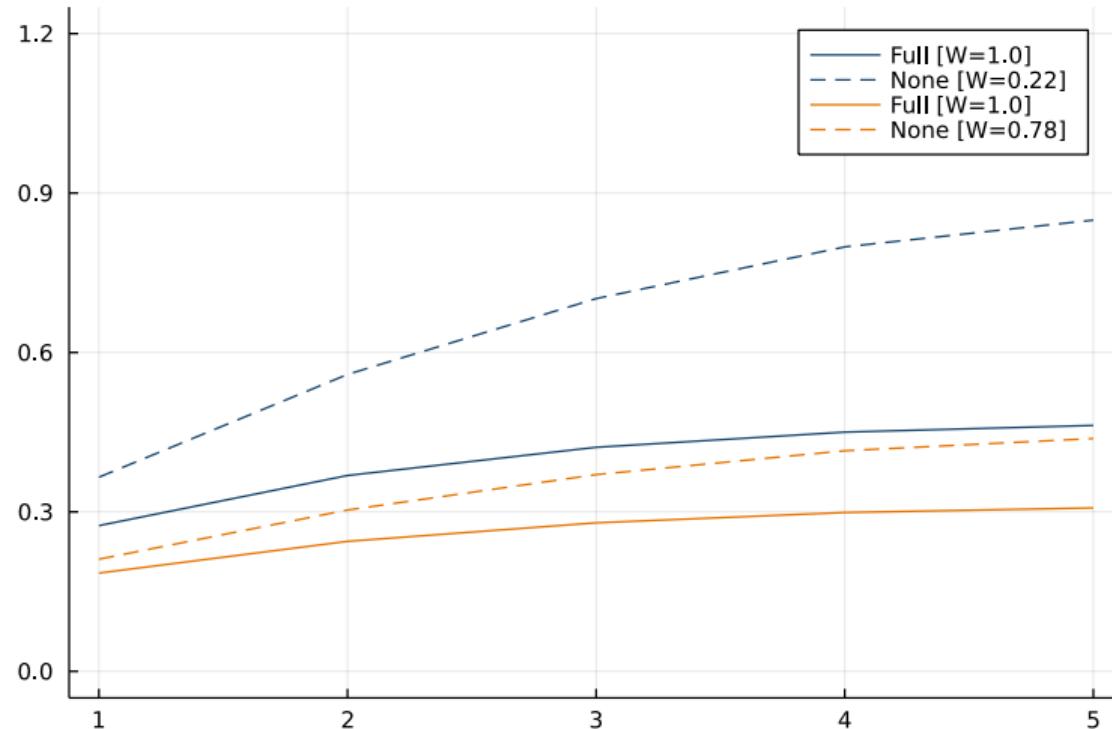
Moving capital

Development



Moving capital

Defense



Conclusion

Summary

- **Major frictions impede adaptation** to climate change
 - Government intervention induces moral hazard and lock-in
 - Commitment helps but faces political challenges
- **Jakarta** foreshadows sea level rise that threatens 1B people by 2050

1	Miami	6	Mumbai
2	Guangzhou	7	Tianjin
3	New York City	8	Tokyo
4	Kolkata	9	Hong Kong
5	Shanghai	10	Bangkok

Hanson et al. (2011)





Appendix

Commitment over time

Consider two periods. Welfare and profits for $\bar{D}_1 = 0$ are

$$W_1 = [r(G_1) + \beta r(G_2)]D_1 - c(D_1) - f(G_1),$$
$$\pi_1 = [r(G_1) + \beta r(G_2)]D_1 - c(D_1),$$

The **social planner** chooses (D_1, G_1, D_2, G_2) to maximize $W_1 + \beta W_2$.

Otherwise, **moral hazard**. Period two same as before; period one worse.

- ① D_1 does not internalize $f(G_1)$ or $f(G_2)$
- ② G_1 may not internalize $f(G_2)$

Commitment over time

Consider two periods. Welfare and profits for $\bar{D}_1 = 0$ are

$$W_2 = r(G_2)D_2 - c(D_2) - f(G_2),$$
$$\pi_2 = r(G_2)D_2 - c(D_2).$$

The **social planner** chooses (D_1, G_1, D_2, G_2) to maximize $W_1 + \beta W_2$.

Otherwise, **moral hazard**. Period two same as before; period one worse.

- ① D_1 does not internalize $f(G_1)$ or $f(G_2)$
- ② G_1 may not internalize $f(G_2)$

Commitment over time (2)

Commitment for $t = 1, 2$: choose (D_1, G_1, D_2, G_2) to max $W_1 + \beta W_2$.

$$[D_1^*] \quad \tilde{r}(G_1, G_2) = c'(D_1)$$

$$[G_1^*] \quad r'(G_1)D_1 = f'(G_1)$$

$$[\tilde{r}(G_1, G_2) = r(G_1) + \beta r(G_2)]$$

Commitment over time (2)

Commitment for $t = 1, 2$: choose (D_1, G_1, D_2, G_2) to max $W_1 + \beta W_2$.

$$[D_1^*] \quad \tilde{r}(G_1, G_2) = c'(D_1)$$

$$[G_1^*] \quad r'(G_1)D_1 = f'(G_1)$$

Commitment for $t = 1$: choose (D_1, G_1) to max $W_1 + \beta W_2$, then G_2 to max W_2 .

$$[D_1] \quad \tilde{r}(G_1, G_2) = c'(D_1) + \beta r'(G_2)D_2G'_2$$

$$[G_1] \quad r'(G_1)D_1 = f'(G_1) + \beta r'(G_2)D_2G'_2$$

Commitment over time (2)

Commitment for $t = 1, 2$: choose (D_1, G_1, D_2, G_2) to max $W_1 + \beta W_2$.

$$[D_1^*] \quad \tilde{r}(G_1, G_2) = c'(D_1)$$

$$[G_1^*] \quad r'(G_1)D_1 = f'(G_1)$$

No commitment: choose G_1 to max $W_1 + \beta W_2$, then G_2 to max W_2 .

$$[D_1] \quad \tilde{r}(G_1, G_2) + r'(G_1)D_1G'_1 + \beta r'(G_2)D_1G'_2 = c'(D_1)$$

$$[G_1] \quad r'(G_1)D_1 = f'(G_1) + \beta r'(G_2)D_2G'_2$$

Commitment over time (2)

Commitment for $t = 1, 2$: choose (D_1, G_1, D_2, G_2) to max $W_1 + \beta W_2$.

$$[D_1^*] \quad \tilde{r}(G_1, G_2) = c'(D_1)$$

$$[G_1^*] \quad r'(G_1)D_1 = f'(G_1)$$

No commitment + political myopia: choose G_1 to max W_1 , then G_2 to max W_2 .

$$[D_1] \quad \tilde{r}(G_1, G_2) + r'(G_1)D_1G'_1 + \beta r'(G_2)D_1G'_2 = c'(D_1)$$

$$[G_1] \quad r'(G_1)D_1 + \beta r'(G_2)D_1G'_2 = f'(G_1)$$

Commitment over time (3)

Lock in: over-development today raises development tomorrow.

$$\begin{aligned}[D_2] \quad & r(G_2) + r'(G_2)D_2 G'_2 = c'(D_2), \\ [G_2] \quad & r'(G_2)(D_1 + D_2) = f'(G_2),\end{aligned}$$

$D_1 \uparrow$ implies $G_2 \uparrow$ given more to defend.

Then $D_2 \uparrow$ implies $G_2 \uparrow\uparrow$ given strategic complementarity $\left(\frac{\partial D_2}{\partial G_2}, \frac{\partial G_2}{\partial D_2} > 0\right)$.

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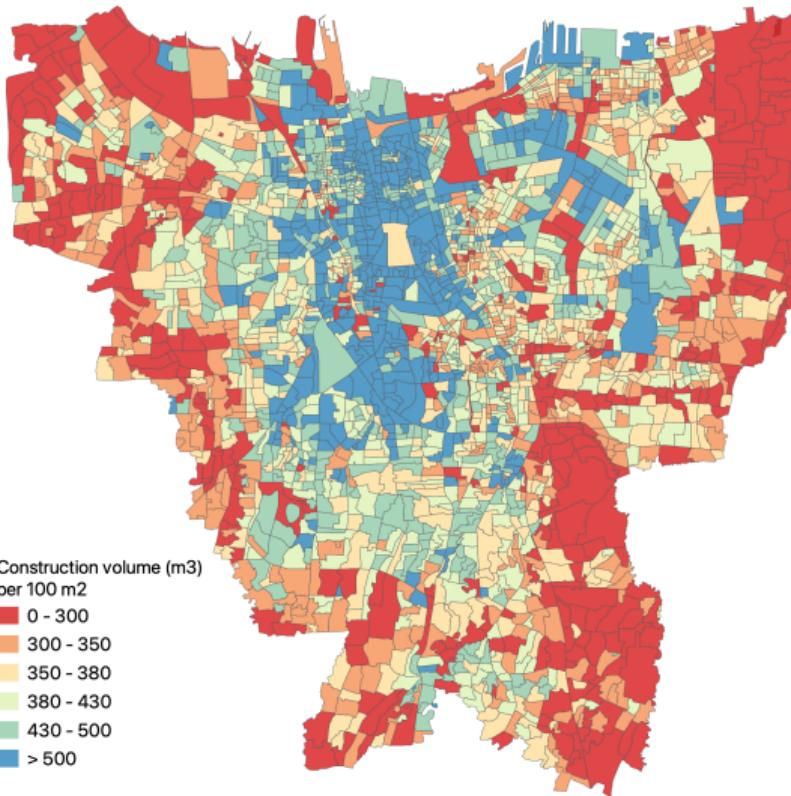
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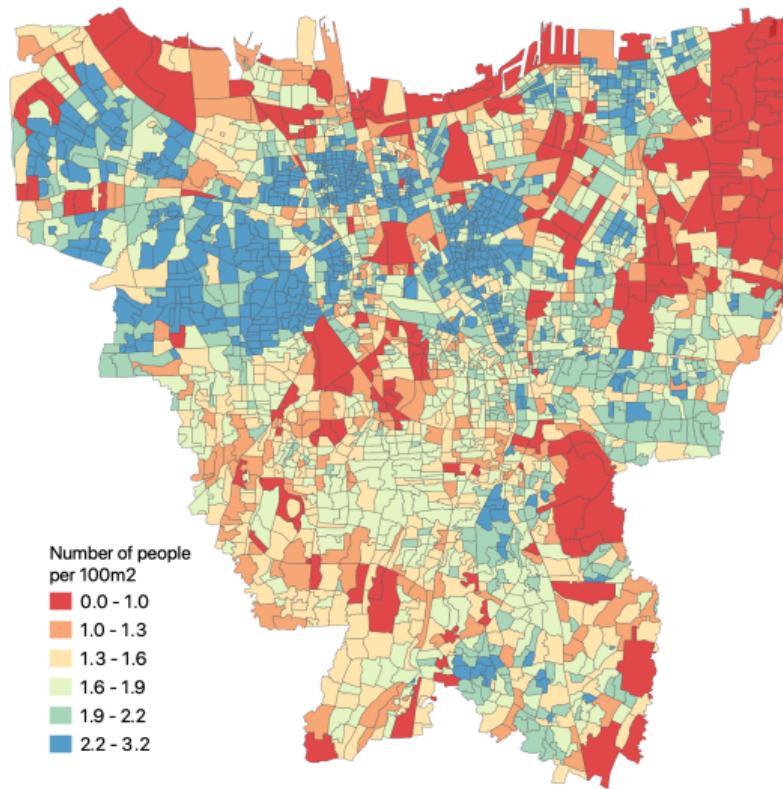
Building construction

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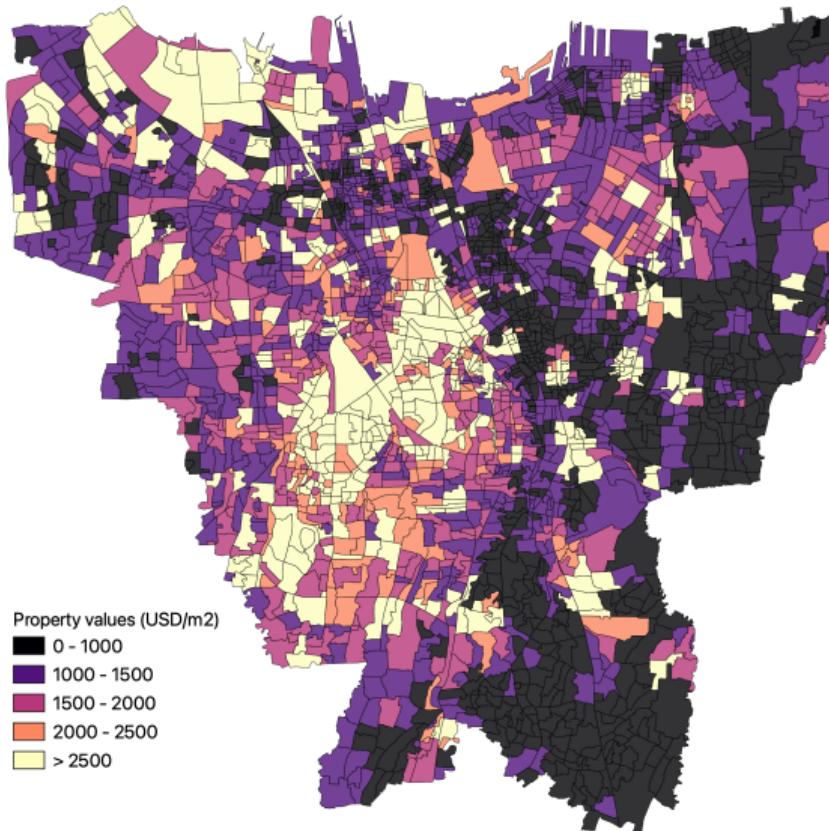
Populations

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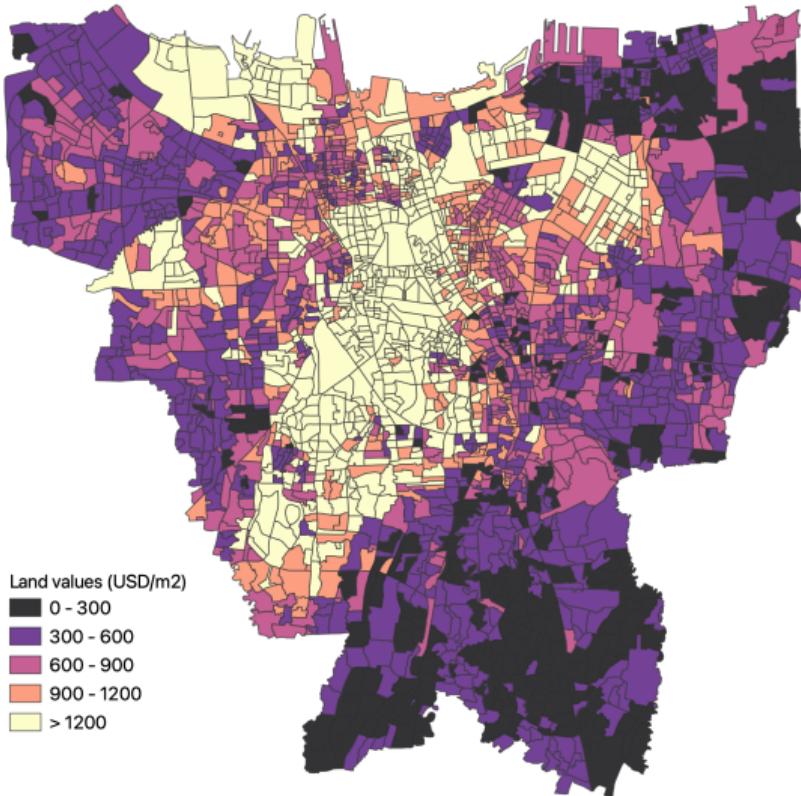
Property values

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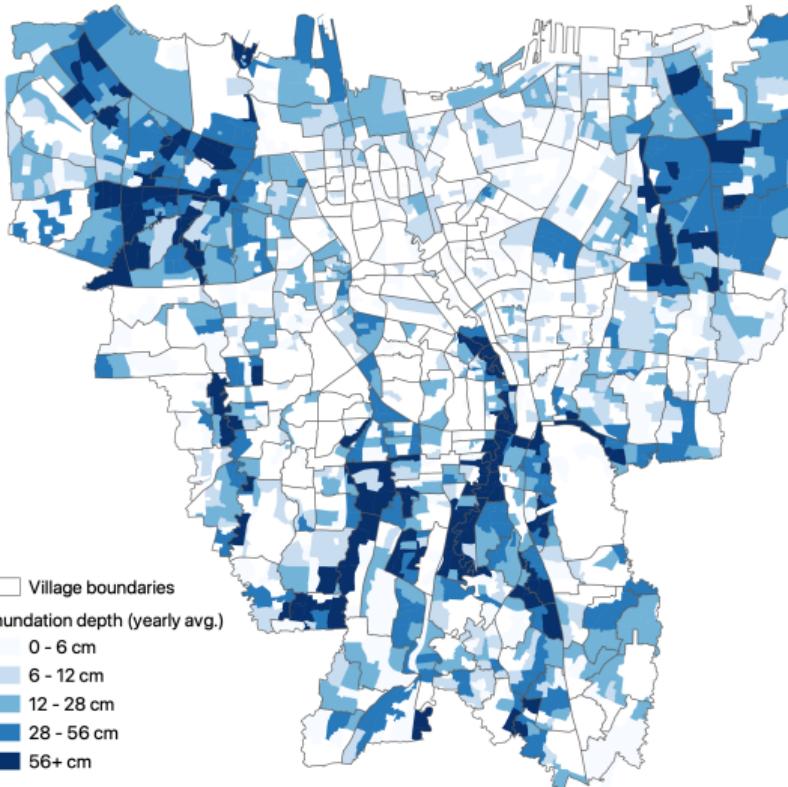
Land values

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Flood risk

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Estimating demand

- Origin populations with 2015 data, destination populations with 2020 data
- Focus on core, but allow one choice aggregating over periphery

① Given $\theta_2 = \tau$, estimate δ by contraction mapping

$$\text{population}_k = \frac{1}{\phi} D_k^{\text{res}}(\delta, \theta_2)$$

② Estimate $\theta_1 = (\alpha, \rho)$ and ξ by regression

$$\xi_k = \delta_k + \alpha r_k - \rho s_k$$

③ Estimate θ_2 by minimizing GMM objective function

$$Q(\theta) = g(\xi(\theta))' W g(\xi(\theta)) \quad \text{for} \quad \mathbb{E}[Z\xi(\theta)] = 0$$