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In [1]: #A routine for plotting quantities relevant to  
#part a of promen 3.28
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from numpy import *  
import pylab as pyl  
from matplotlib import *  
import math
```

```
In [60]: #Defining my starting variables  
xfin = 2*pi  
x = linspace(0,xfin,100); a0=1;phi=0; N = 50#number of terms
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#Building phi with a for loop
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for i in range(N):  
  
    phi = phi + a0*cos(i*pi)*x**(2.*i)/math.factorial(2.*i+1.)
```

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#finding the x intercept
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count = 0  
for i in phi:  
    if i<0:  
        ind1=count-1  
        break  
    count = count +1
```

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In [13]: xint = str(x[ind])[0:5]  
#plotting \phi(x)  
rc('text', usetex=True)  
pyplot.figure()  
p1=pyplot.plot(x,phi,linewidth=2)  
p2=pyplot.plot([pi]*2,[-1,max(phi)+.1*max(phi)], '--k',linewidth=2)  
pyplot.plot([0,xfin+.05*xfin],[0,0], '--k',linewidth=2)  
pyplot.xlim([0,xfin+.05*xfin])  
pyplot.ylim([-1,max(phi)+.1*max(phi)])  
#pyplot.plot([0,0],[min(phi)+.7*min(phi),max(phi)+.2*max(phi)], '--k',line  
pyplot.grid(True)  
pyplot.title(r'Special Case $n=1$', fontsize=16)  
pyplot.xlabel(r'$x$', fontsize=14)  
pyplot.ylabel(r'$\phi(x)$', fontsize=14)  
pyplot.legend([p1[0],p2[0]], [r'\phi(x)', r'$x=\pi$'])  
pyplot.savefig('LanEmdNeq1.png')  
pyplot.show()
```

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In [50]: #the slope of phi, derived from its analytical form  $a_0 \sin(x)/x$ 

Dphi = a0*(x*cos(x)-sin(x))/x**2

#finding finding the local minimum of the slope

for i in array(range(len(Dphi)))+2:
    if count>0:
        if Dphi[i]-Dphi[i-1]>0:
            ind=i-1
            break
```

```
In [59]: #plotting  $d\phi(x)/dx$ 

pyplot.figure()
pyplot.plot(x,Dphi,linewidth=2)
pyplot.plot([pi]**2,[-.5,.2],'-k',linewidth=1)
p1=pyplot.plot([x[ind]]**2,[-.5,.2], '--k',linewidth=2)
p2 = pyplot.plot([pi],0, '*k', markersize=15)
pyplot.plot([0,xfin+.05*xfin],[0,0], '-k',linewidth=1)
pyplot.xlim([0,xfin+.05*xfin])
pyplot.ylim([-0.5,.2])
pyplot.title(r'Slope of  $\phi(x)$ ',fontsize=16)
pyplot.xlabel(r' $x$ ',fontsize=14)
pyplot.ylabel(r' $d\phi(x)/dx$ ',fontsize=14)
pyplot.grid(True)
xint = str(x[ind])[0:4]
pyplot.legend([p1[0],p2[0]], [r' $x=$ ' + xint + ' $'$ ', r' $\rho=0$ ' ],loc=4)
pyplot.savefig('SlopePhi.png')
pyplot.show()
```