

Chapter 1: Introduction to fluid mechanics:

1- Introduction:

The fluid mechanics is the study of laws of fluid flow. It is divided into two parts.

1- Statics:

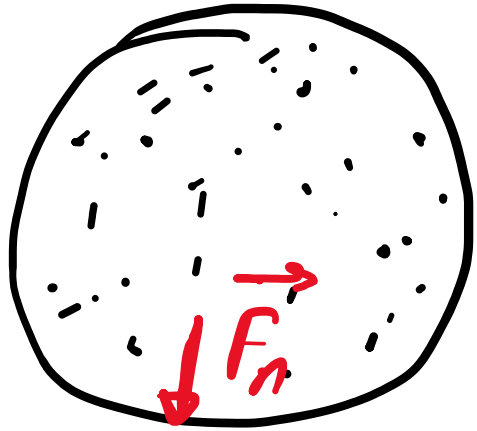
↳ dynamics and Kinematics of fluid.

2-Types of fluids:

there are 2 types of fluids:

- 1- Newtonian: the viscosity of fluid depends only on temperature
- 2- Non-Newtonian fluids: the viscosity changes with the velocity of flow and other parameters.

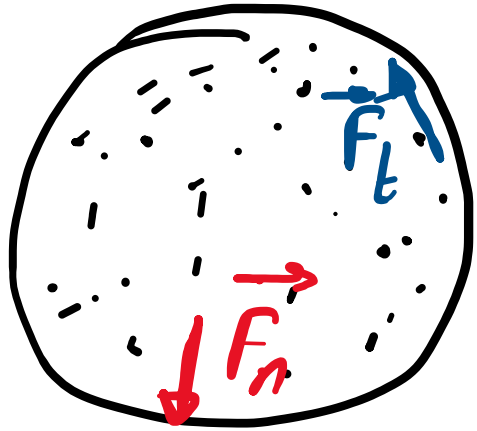
3.1 Ideal fluid:



the force exerted by ideal fluid on the wall of the tank is always perpendicular to the surface.

In ideal fluid the viscosity is 0.

3.2 - Real fluid.



the force exerted by ideal fluid on the wall of the tank has a tangential component to the wall surface.

the viscosity in this case does not equal to 0.

3.3 - Compressible and incompressible fluid.

\Rightarrow incompressible fluid $\Rightarrow \rho = \text{constant}$.

$$\frac{d\rho}{dt} = 0, \quad \text{incompressible fluid (liquid fluid)} \\ \text{water, oil, ---}$$

$$\text{compressible fluid} = (\text{gas}). \quad \frac{d\rho}{dt} \neq 0.$$

4 - Physical properties:

4.1 - density.

$$\rho = \frac{\text{mass of fluid}}{\text{volume of fluid}} = \left(\frac{\text{Kg}}{\text{m}^3} \right)$$

$$\rho_{\text{water}} = 10^3 \text{ Kg/m}^3$$

$$\rho_{\text{air}} = 1.2 \text{ Kg/m}^3$$

$$\rho_{\text{Mercury}} = 13.546 \times 10^3 \text{ Kg/m}^3$$

$$\rho_{\text{oil}} < \rho_{\text{water}}$$

$$\rho_{\text{gasoline}} = 0.88 \times 10^3 \text{ Kg/m}^3$$

relative density is the density of the fluid relative to water.

(specific gravity).

$$S.g. = \frac{\rho_{\text{fluid}}}{\rho_{\text{water}}}$$

$$S.g._{\text{gasoline}} = \frac{880 \rightarrow \rho_{\text{gasoline}}}{1000 \rightarrow \rho_{\text{water}}} = 0.88.$$

4.2 - Specific weight.

$$\gamma = \frac{\text{weight of fluid}}{\text{volume of fluid}} = \frac{m g}{V} = \rho \cdot g \quad \left(\frac{N}{m^3} \right).$$

ideal:

gas:

$$\gamma = \rho \cdot g = \frac{m}{V} \cdot g = \frac{m g}{\frac{n R T}{P}} = \frac{P m g}{n R T} = \frac{P m g}{\frac{m}{M} R T}$$

$$\gamma = \frac{P g}{\frac{R}{M} T} = \frac{P g}{R' T}$$

$$R' = \frac{R}{M} \quad \frac{J}{K \text{ g mol}^{-1}}.$$

$$\rho = \frac{p}{R'T}$$

For air.

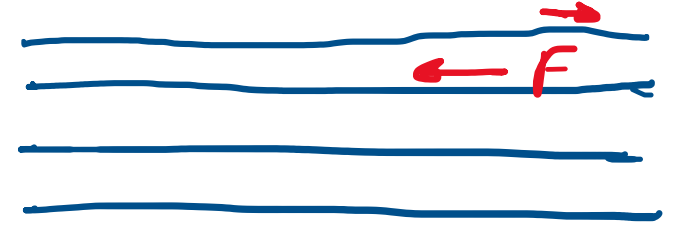
$$R' = 287 \frac{\text{J}}{\text{kg K}}$$

For oxygen :

$$R' = 260 \frac{\text{J}}{\text{kg K}} .$$

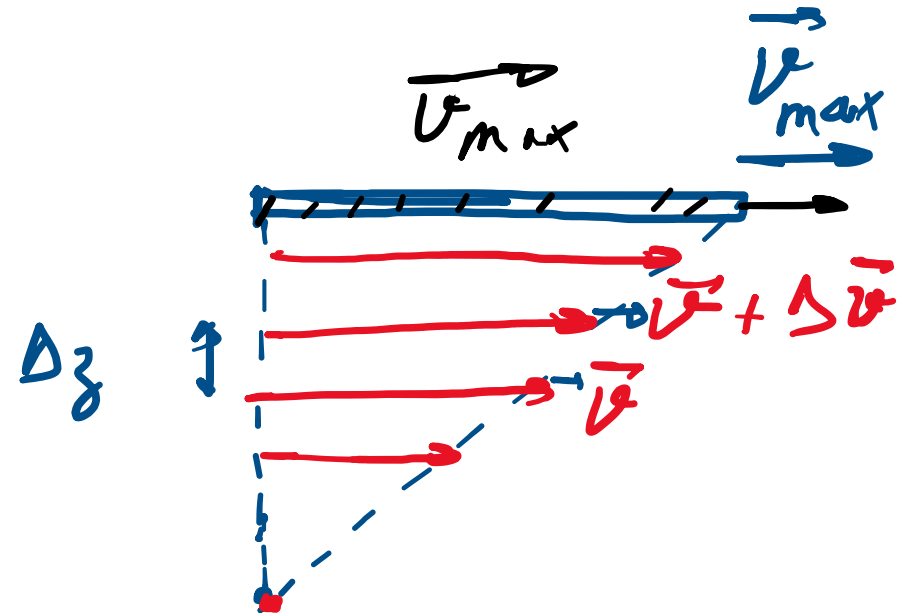
4.3 - Viscosity:

the viscosity is the parameter that describes the friction force between 2 layers of the same fluid.



the velocity of flow depends on the depth z .

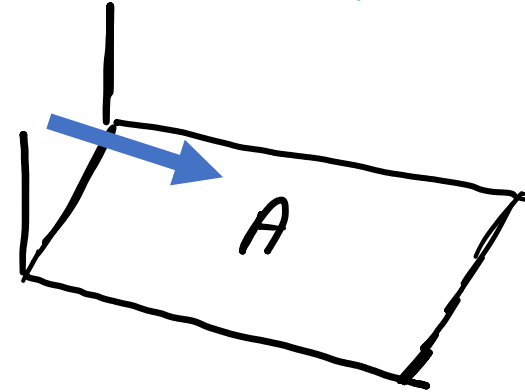
z



The force of friction between 2 layers is:

$$F = \mu \cdot A \cdot \frac{\Delta v}{\Delta z}$$

N $\frac{N \cdot s}{m^2}$ m^2 $\frac{1}{s}$ Δz

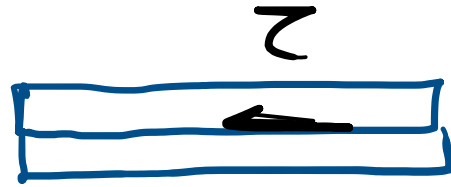


μ : dynamic viscosity. $(\frac{N}{m^2} \cdot s) = (Pa \cdot s) = \text{Poise}$.

$\frac{\Delta v}{\Delta z}$: change of velocity with respect to z . $(\frac{m/s}{m})$

A : Area of layer. (m^2)

τ = shear stress : pressure exerted by
friction parallel to the layer.



$$\tau = \frac{F}{A} = \mu \frac{\Delta v}{\Delta z} = \mu \frac{dv}{dz}$$

* Kinematic viscosity: $\nu = \frac{\mu}{\rho}$

$$\frac{\frac{N}{m^2} \cdot s}{\frac{kg}{m^3}} = \frac{\frac{kg \cdot \frac{m}{s} \cdot s}{m^2}}{\frac{kg}{m^3}} = \frac{\frac{1}{m} \cdot \frac{1}{s}}{\frac{1}{m^3}} = \frac{1}{\frac{1}{m^2} \cdot s} = \frac{m^2}{s}$$

unit ν is Stokes (St) $1 \text{ St} = 10^{-4} \frac{m^2}{s}$

Example:

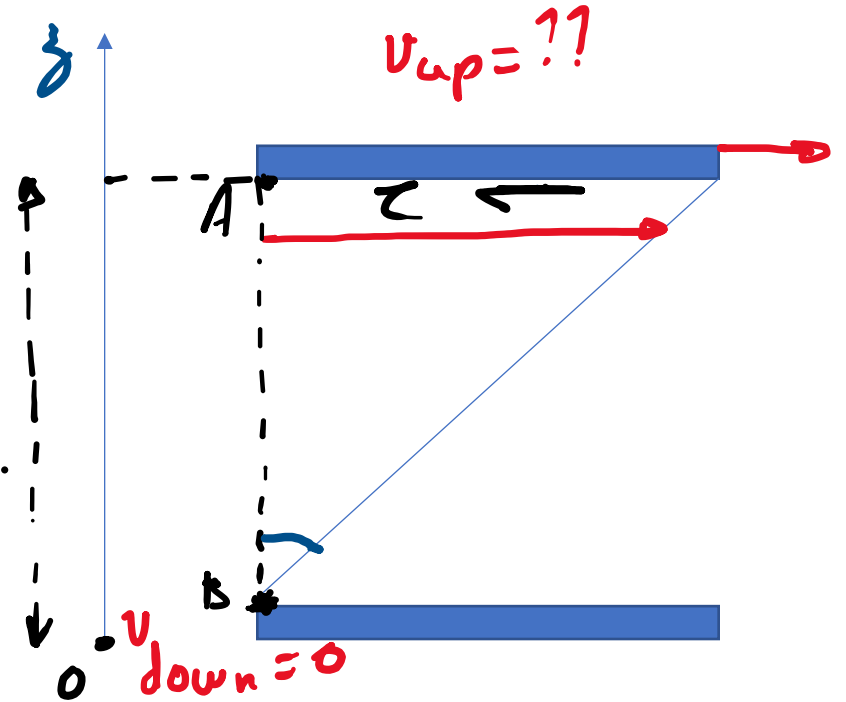
Two parallel plates separated by 5 mm of glycerin at $T = 20^\circ\text{C}$. The friction force applied on the upper plate is 26 N per 1 m^2 of area. Find the velocity of the upper plate.

$$\mu_{\text{glyc}} = 1.49 \text{ Pa}\cdot\text{s}$$

$$\tau = 26 \frac{\text{N}}{\text{m}^2} = 26 \text{ Pa}$$

$$\tau = \mu \frac{\Delta v}{\Delta z} \Rightarrow 26 = 1.49 \frac{v_{\text{up}} - 0}{5 \times 10^{-3} - 0}$$

$$5 \text{ mm} = 5 \times 10^{-3} \text{ m}$$



$$v_{up} = \frac{26 \times 5 \times 10^{-3}}{1.49} = 0.087 \text{ m/s.}$$

$\mu =$ dynamic viscosity (Pa.s). $\tau = \mu \frac{\Delta u}{\Delta z}$

$\nu =$ Kinematic viscosity ($\frac{m^2}{s}$). $\left[\nu = \frac{\mu}{\rho} \right]$