

# Materials Science

## Lecture 7

Lebanese University - Faculty of Engineering – Branch 3

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## **Lecture 7:**

### **Chap3: Crystalline Structure — Perfection**

3.1. Crystal Structures Fundamentals

3.2. Metallic Structures

3.3. Crystal Systems, Positions, Directions, and Planes

3.4. Linear and planar densities

3.5. Close-packed crystal structures

## 3.5. Close-packed crystal structures



- ◎ You may remember from the discussion on metallic crystal structures that both face-centered cubic and hexagonal close-packed crystal structures have **atomic packing factors of 0.74**, which is the most efficient packing of equal-size spheres or atoms.

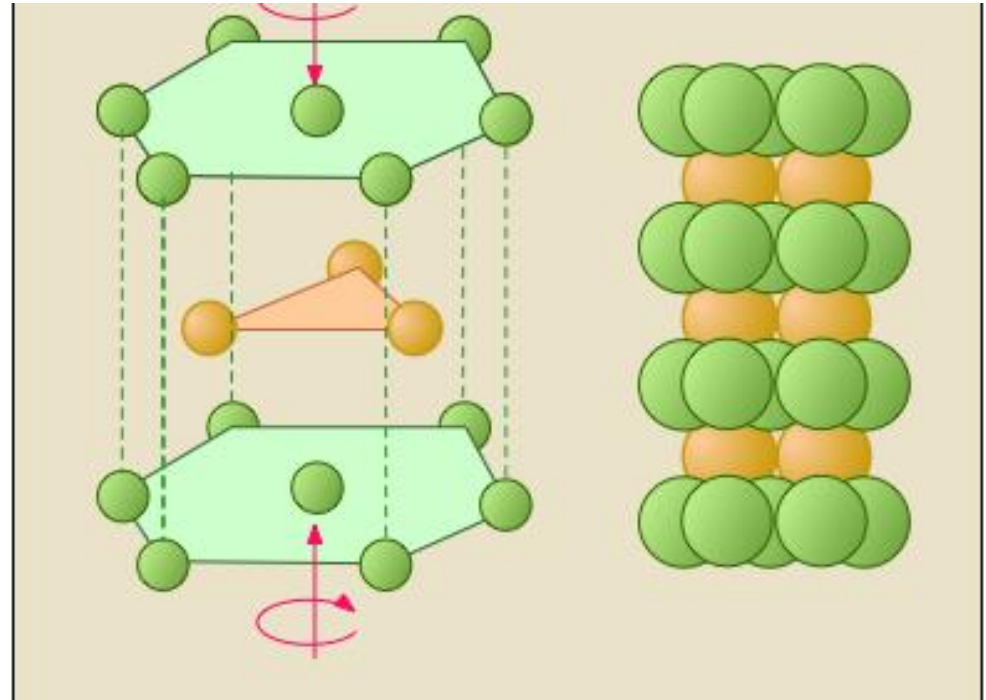
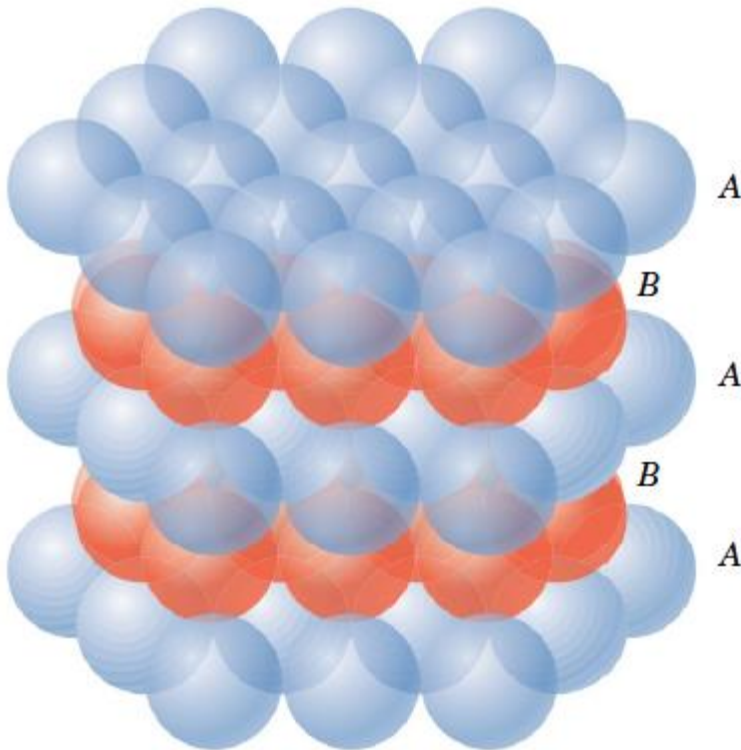


*Watch the attached videos*

# 3.5. Close-packed crystal structures



- ⦿ For HCP, the **centers of the third layer (the second A) are aligned directly above the original A positions**. This stacking sequence, ABABAB . . . , is repeated over and over.
- ⦿ These close-packed planes for HCP are (0001)-type planes.



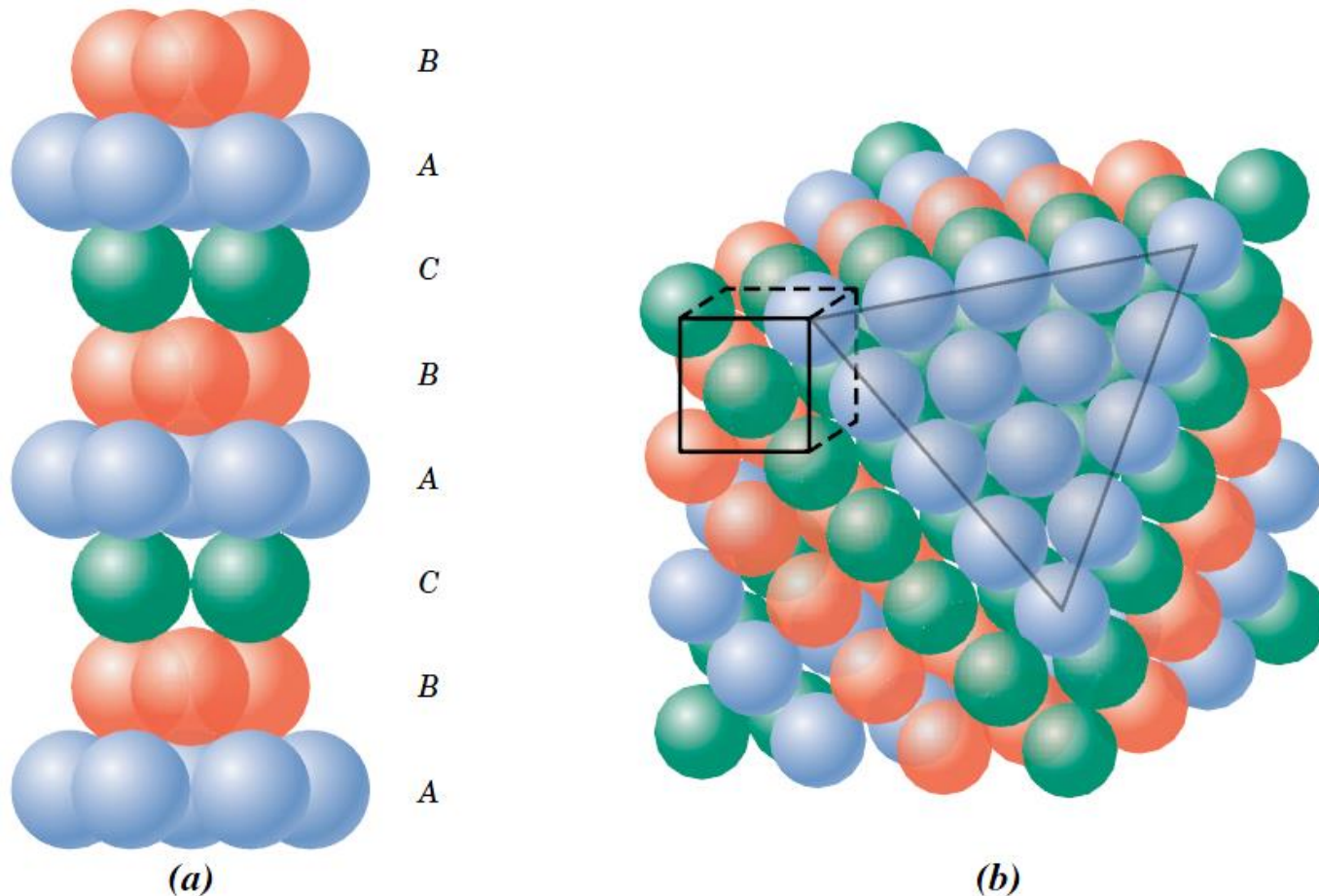
*Close-packed plane stacking sequence for the hexagonal close-packed structure.*

## 3.5. Close-packed crystal structures



- ⦿ For the face-centered crystal structure **FCC**, the centers of the third plane are situated over the **C** sites of the first plane (**Figure**).
- ⦿ This yields an ABCABCABC . . . stacking sequence; that is, the atomic alignment repeats every third plane.
- ⦿ It is more difficult to correlate the stacking of close-packed planes to the FCC unit cell. However, this relationship is demonstrated in the **next Figure**. These planes are of the (111) type.

## 3.5. Close-packed crystal structures

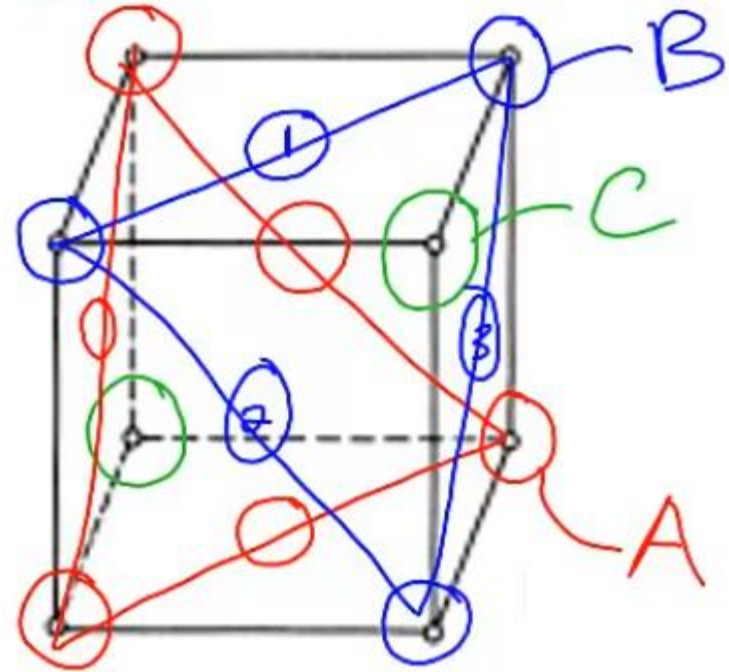
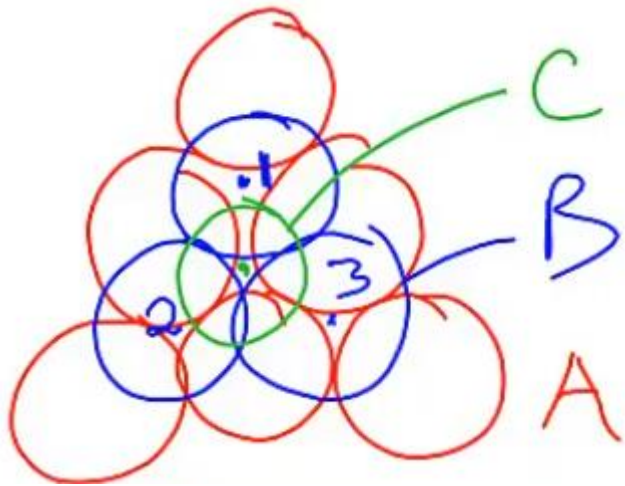


*(a) Close-packed stacking sequence for the face-centered cubic structure.*

*(b) A corner has been removed to show the relation between the stacking of close-packed planes of atoms and the FCC crystal structure; the heavy triangle outlines a (111) plane.*



## 3.5. Close-packed crystal structures



*Close-packed stacking sequence for the face-centered cubic structure FCC.*

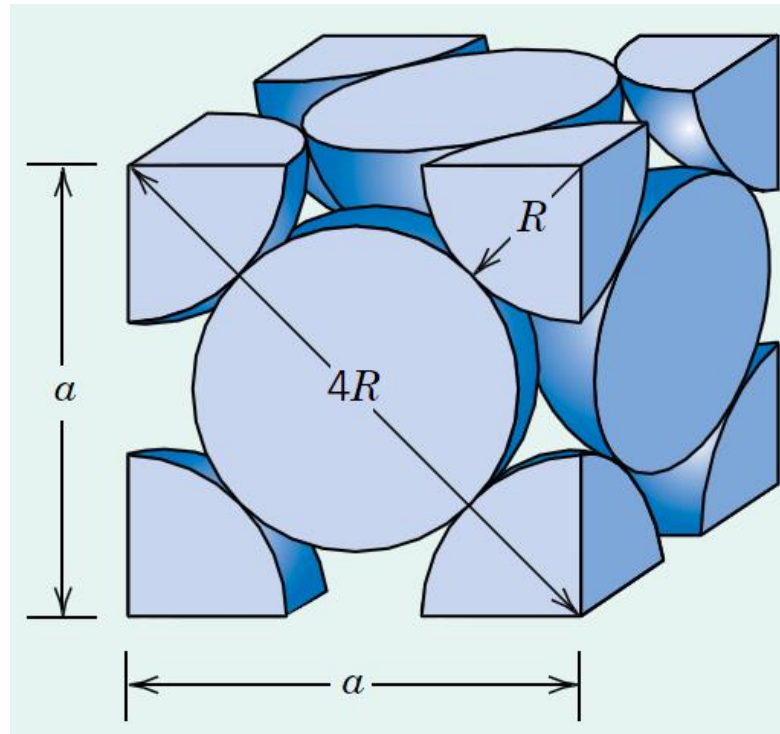
## Chap 3

# Exercises



# Exercise 1

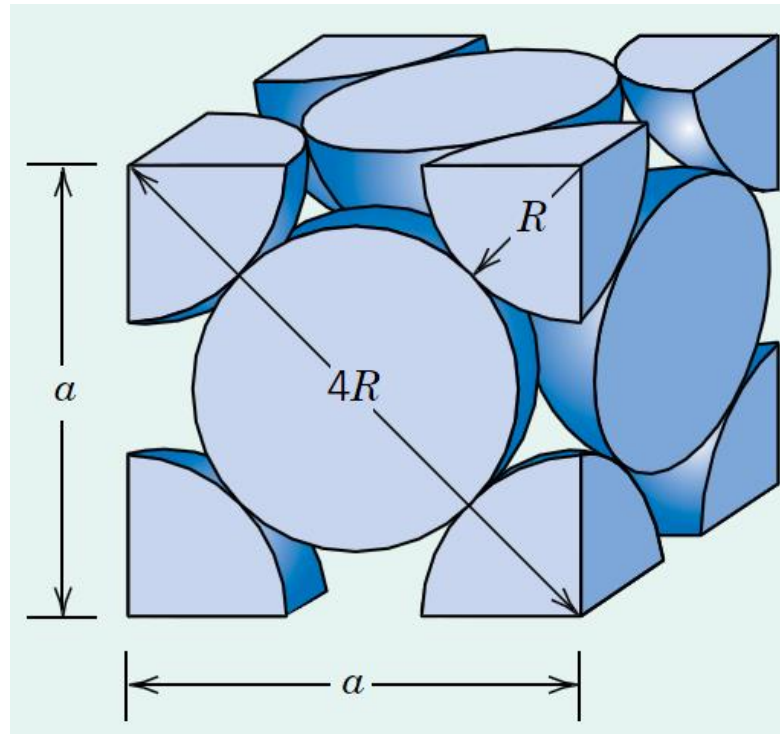
Calculate the volume of an FCC unit cell in terms of the atomic radius  $R$ .



# Exercise 2

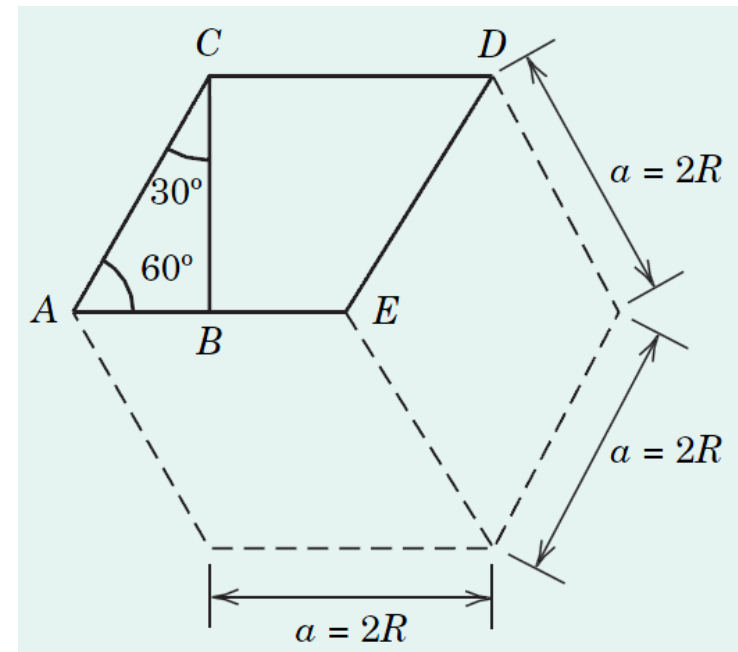
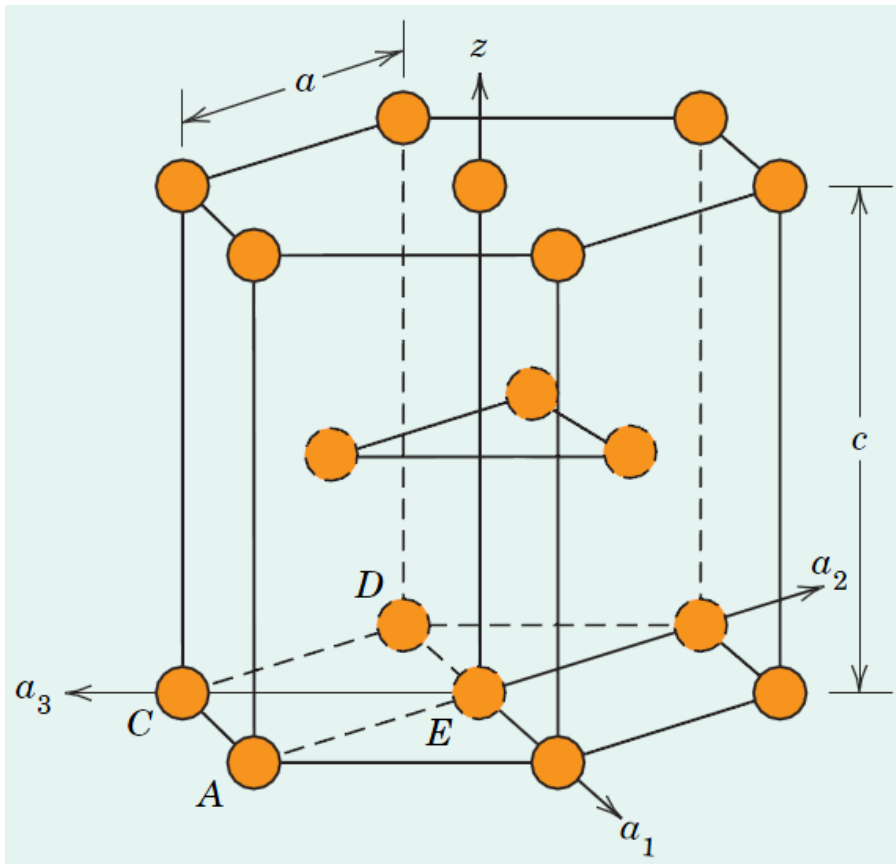


Using volumes, Show that the atomic packing factor for the FCC crystal structure is 0.74.



# Exercise 3

- (a) Calculate the volume of an HCP unit cell in terms of its  $a$  and  $c$  lattice parameters.
- (b) Now provide an expression for this volume in terms of the atomic radius,  $R$ , and the  $c$  lattice parameter.



# Exercise 4



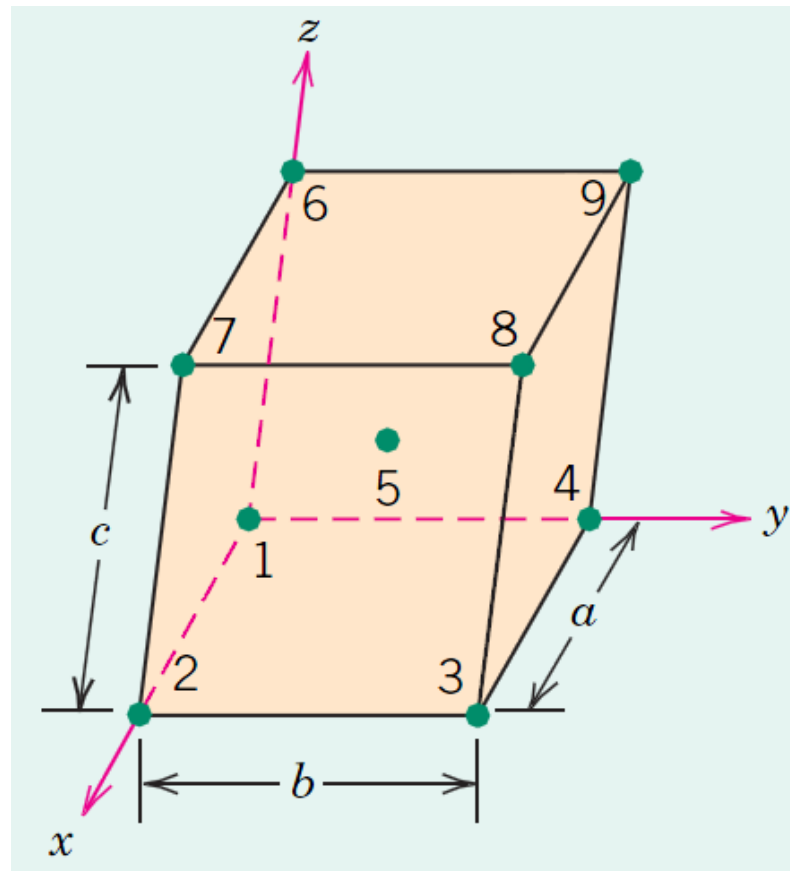
## Theoretical Density Computation for Copper

Copper has an atomic radius of 0.128 nm, an FCC crystal structure, and an atomic weight of 63.5 g/mol. Compute its theoretical density, and compare the answer with its measured density.

# Exercise 5

## Specification of Point Coordinate Indices

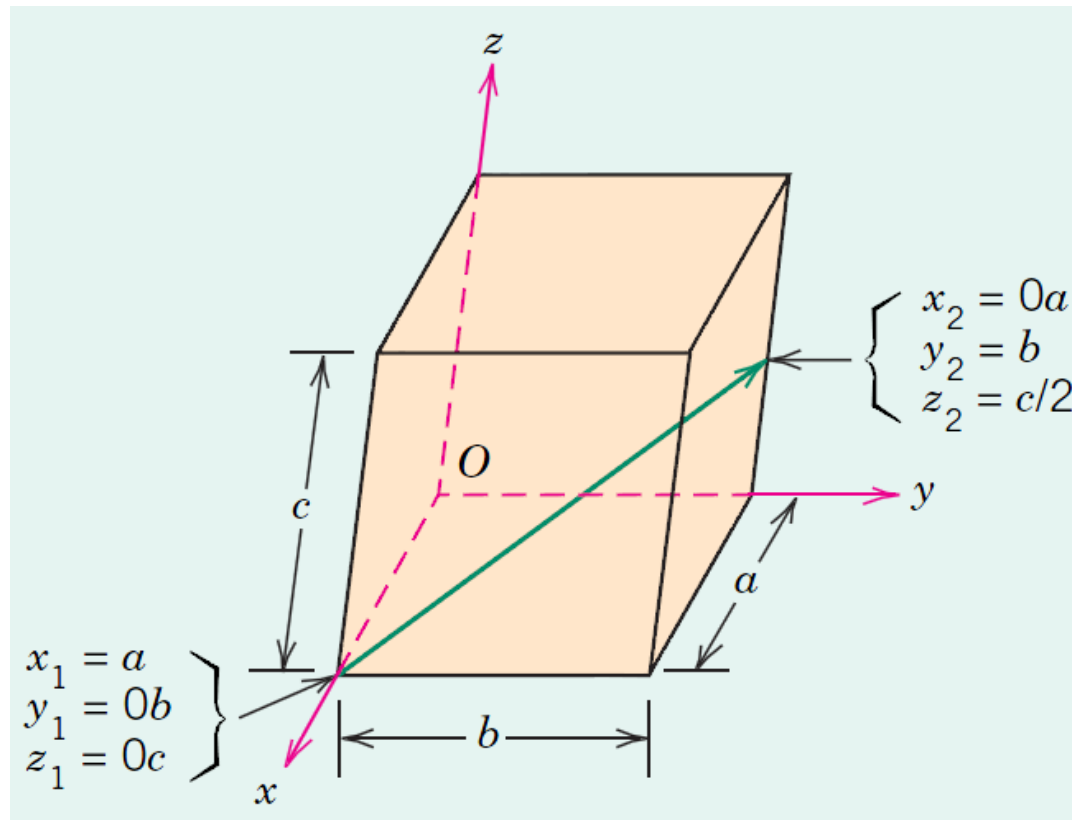
Specify coordinate indices for all numbered points of the unit cell in the illustration on the next page.



# Exercise 6

## Determination of Directional Indices

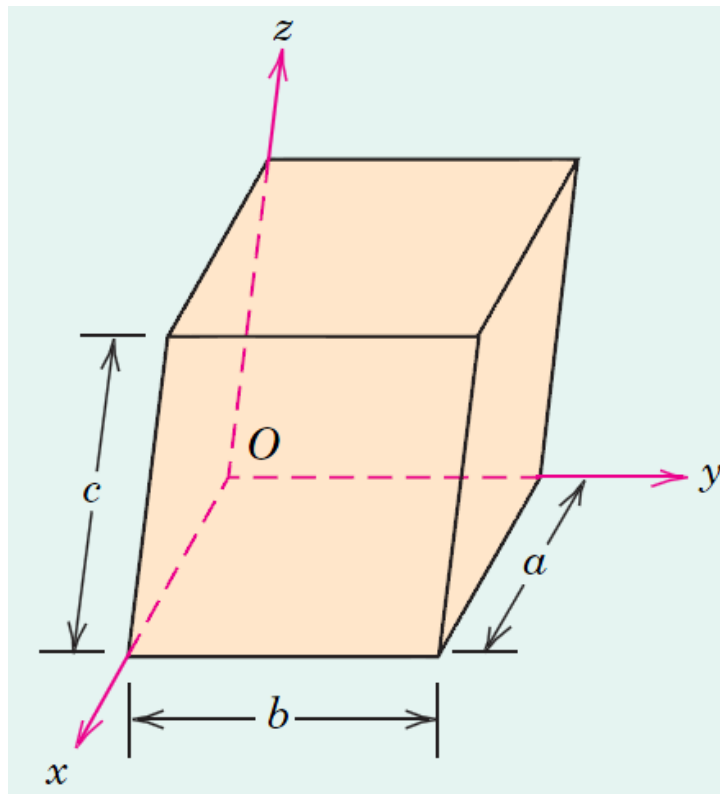
Determine the indices for the direction shown in the accompanying figure.



# Exercise 7

## Construction of a Specified Crystallographic Direction

Within the following unit cell draw a  $[1\bar{1}0]$  direction with its tail located at the origin of the coordinate system, point  $O$ .





# Exercise 8



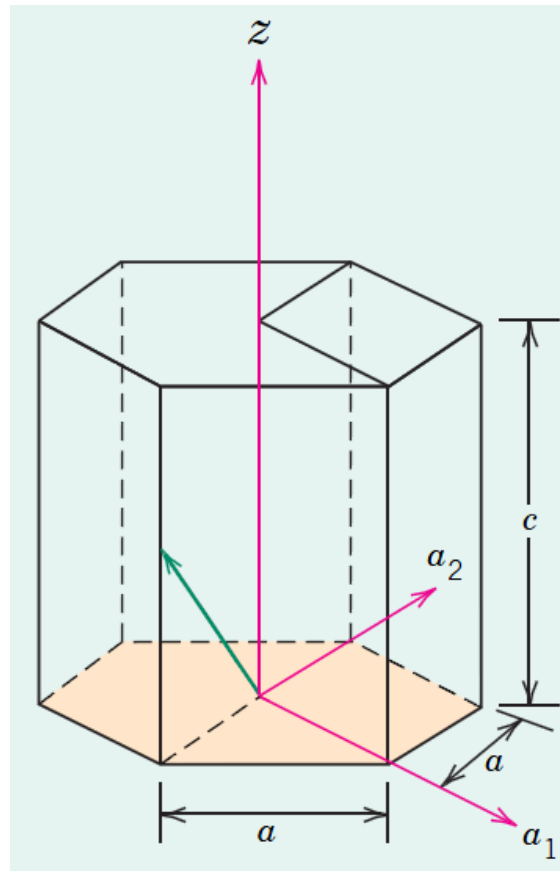
## Conversion and Construction of Directional Indices for a Hexagonal Unit Cell

- (a) Convert the  $[111]$  direction into the four-index system for hexagonal crystals.
- (b) Draw this direction within a ruled-net coordinate system (per Figure 3.10).
- (c) Now draw the  $[111]$  direction within a hexagonal unit cell that utilizes a three-axis ( $a_1, a_2, z$ ) coordinate scheme.

# Exercise 9

## Determination of Directional Indices for a Hexagonal Unit Cell

Determine the indices (four-index system) for the direction shown in the accompanying figure.



# Exercise 10



## Determination of Planar (Miller) Indices

Determine the Miller indices for the plane shown in the accompanying sketch (a).

