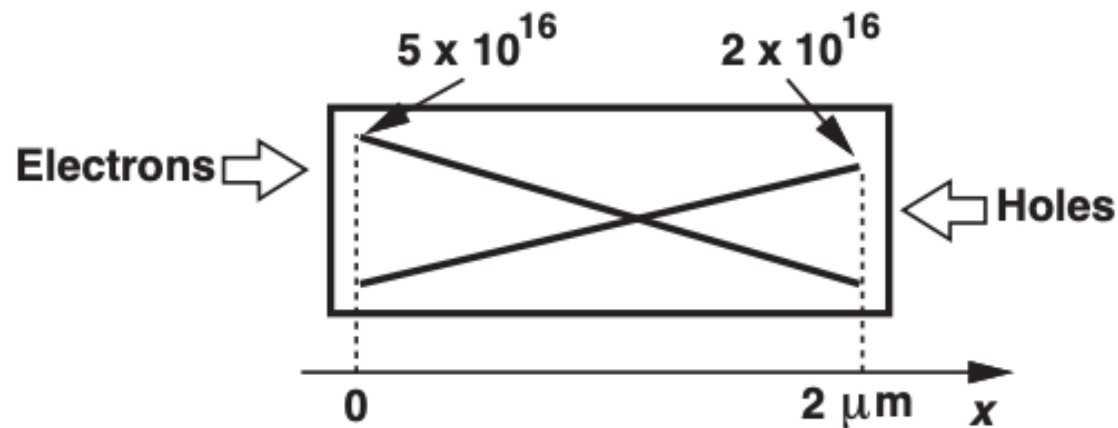


# Problem 1

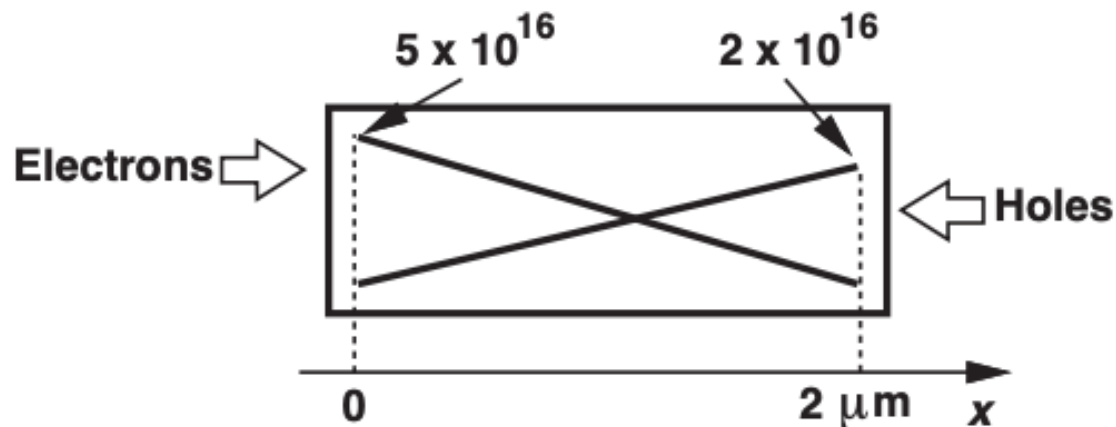
- Figure below shows a  $p$ -type bar of silicon that is subjected to electron injection from the left and hole injection from the right. Determine the total current flowing through the device if the cross section area is equal to  $1\ \mu\text{m} \times 1\ \mu\text{m}$ .

$$D_n = 34\text{cm}^2/\text{s} \quad D_p = 12\text{cm}^2/\text{s}$$



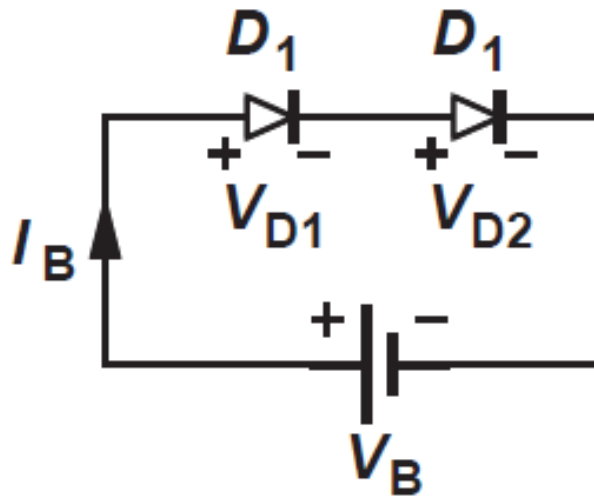
# Problem 1: Solution

- given:  $L=2\ \mu\text{m}$ ,  $A=1\ \mu\text{m}^2$   $D_n = 34\text{cm}^2/\text{s}$   $D_p = 12\text{cm}^2/\text{s}$
- $I_{tot} = A \cdot J_{tot}$
- $I_{tot} = A \cdot q(D_n \frac{dn}{dx} - D_p \frac{dp}{dx})$
- $I_{tot} = (1\mu\text{m}^2) \times 10^{-8} \times 1.6 \times 10^{-19} (34(\text{cm}^2/\text{s}) \frac{-5 \times 10^{16}(\text{cm}^{-3})}{10^{-4} \times 2\mu\text{m}} - 12(\text{cm}^2/\text{s}) \frac{2 \times 10^{16}(\text{cm}^{-3})}{10^{-4} \times 2\mu\text{m}})$
- $I_{tot} = -1.552 \times 10^{-5} \text{A} \rightarrow -15.52\mu\text{A}$  to verify



# Problem 2

- Figure below shows two diodes with reverse saturation currents of  $I_{S1}$  and  $I_{S2}$  placed in series. Calculate  $I_B$ ,  $V_{D1}$ , and  $V_{D2}$  in terms of  $V_B$ ,  $I_{S1}$ , and  $I_{S2}$ .



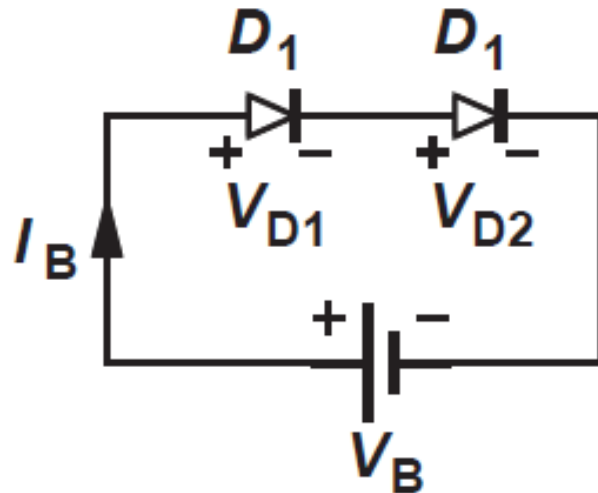
# Problem 2: Solution

- $V_B = V_{D1} + V_{D2}$

- Knowing that  $I_D \simeq I_s \exp \frac{V_D}{V_T} \Rightarrow V_D = V_T \ln \left( \frac{I_D}{I_s} \right)$

- $V_B = V_{D1} + V_{D2} = V_T \ln \left( \frac{I_B}{I_{s1}} \right) + V_T \ln \left( \frac{I_B}{I_{s2}} \right) = V_T \ln \left( \frac{I_B^2}{I_{s2} I_{s1}} \right)$

- $\Rightarrow I_B = \sqrt{I_{s1} I_{s2} \exp \left( \frac{V_B}{V_T} \right)} = \sqrt{I_{s1} I_{s2}} \exp \left( \frac{V_B}{2V_T} \right)$

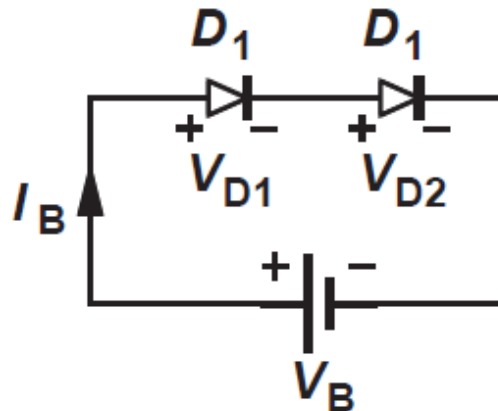


# Problem 2: Solution

$$\Rightarrow I_B = \sqrt{I_{s1}I_{s2}\exp\left(\frac{V_B}{V_T}\right)} = \sqrt{I_{s1}I_{s2}}\exp\left(\frac{V_B}{2V_T}\right)$$

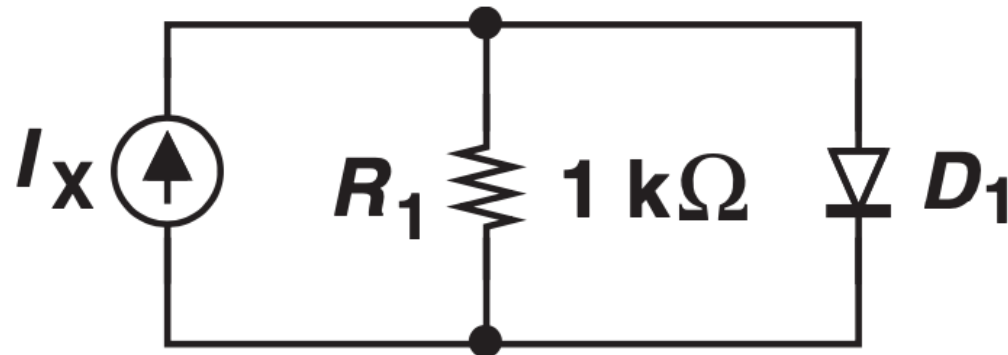
$$\Rightarrow V_{D1} = V_T \ln\left(\frac{I_B}{I_{s1}}\right) = V_T \ln\left(\sqrt{\frac{I_{s2}}{I_{s1}}}\right) + \frac{V_B}{2}$$

$$\Rightarrow V_{D2} = V_T \ln\left(\frac{I_B}{I_{s2}}\right) = V_T \ln\left(\sqrt{\frac{I_{s1}}{I_{s2}}}\right) + \frac{V_B}{2}$$



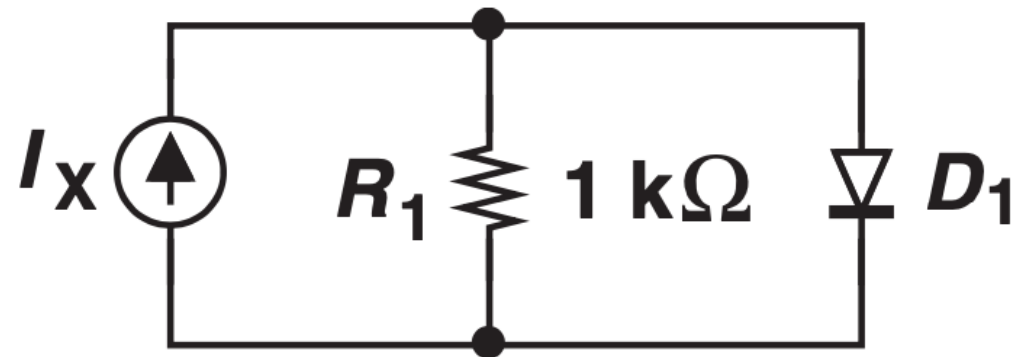
# Problem 3

- In the circuit of Fig. below, we wish  $D_1$  to carry a current of 0.5mA for  $I_X = 1.3\text{mA}$ . Determine the required reverse saturation current  $I_S$ .



# Problem 3: Solution

- $I_{D1} \simeq I_s \exp \frac{V_{D1}}{V_T} \Rightarrow I_s \simeq I_{D1} \exp \frac{-V_{D1}}{V_T}$
- $I_{D1} = 0.5 \text{ mA}, V_{D1} ?$
- $V_{D1} = R I_R = R(I_x - I_{D1}) = 0.8 \text{ V}$
- $I_s \simeq I_{D1} \exp \frac{-V_{D1}}{V_T} = 2.168 \times 10^{-17} \text{ A}$



$$I_s = A q n_i^2 \left( \frac{D_n}{N_A L_n} + \frac{D_p}{N_D L_p} \right)$$