

Sets

Sets by the Math

Functions Make Sets

What is a Set?

Sets in Python

Lists in Python

Tuples in Python

Dictionaries

Randomly Choosing Elements

This week's Lab

# Discrete Structures: CMPSC 102

Oliver BONHAM-CARTER

Fall 2019 Week 4



# Georg Ferdinand Ludwig Philipp Cantor Creator of Set theory

Sets by the Math

Functions Make Sets

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- German mathematician: 19 February 1845 6 January 1918
- Function definition: established the importance of one-to-one correspondence between the members of two sets ( more on that in a moment!)
- Defined infinite and well-ordered sets
- Proved that the real numbers (*rational* and *irrational*) are more numerous than the natural numbers (*counting* numbers)



### Functions as Sets

Regular Set: one-to-one relationship maintained

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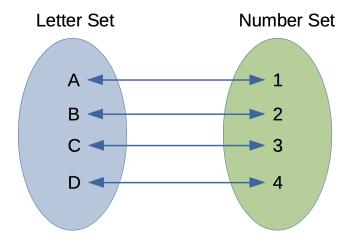
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- The Letter set maps to the Number set.
- $LetterSet(x) \rightarrow NumberSet$





### **Functions Sets**

Regular Set: one-to-one-ism is maintained

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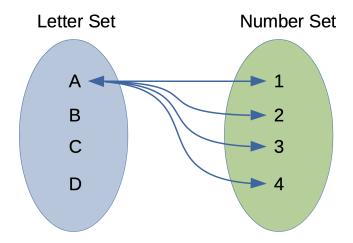
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- The Letter set maps to the Number set.
- $LetterSet(x) \rightarrow NumberSet$





# Functions as Sets One-to-one-ism is NOT maintained!

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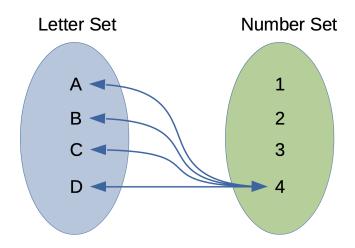
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- The Letter set maps to the Number set.
- $LetterSet(x) \rightarrow NumberSet$





### **General Sets**

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#### What is a set?

- For example, the numbers 1, 2, and 3 are distinct objects when considered separately, but when they are considered collectively they form a single set of size three, written {1,2,3}.
- Set theory is now a ubiquitous part of mathematics,
- May be used as a foundation from which nearly all of mathematics can be derived (From 19<sup>th</sup> century mathematical thinking!)



# Types of Sets Intensional and Extensional

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**Intentional** definition of sets: I intend this set to be ...

 Defines a set by specifying the necessary and sufficient conditions for when the set should be used.

**Extensional** definition of sets: Logically this set is ...

• Defines a set by some definition of a concept or a term.



# Types of Sets

Intentional: One decides which elements make up a set

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Set of Circles

Set of Triangles

Intentional definition of sets: I intend that these set be ...

- The set of blue, grey and pink circles
- The set of blue triangles
- The set of colors of the Union Jack (i.e., the British flag)



# Types of Sets Extensional: Sets of members in curly brackets

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#### Extensional definition of sets

- $A_2 = \{4, 2, 1, 3\}$ 
  - The first four positive numbers
- $B_2 = \{ Blue, Red and White \}$ 
  - The set of colors of the Union Jack (the British flag)
- $F = \{n^2 4 : n \text{ is an integer; and } 0 \le n \le 19\}$ 
  - The set of all values gained from plugging in n between 0 and 19 into the equation  $n^2-4$



# Types of Sets Extensional definition of sets: a list of its members in curly brackets

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#### • Intentional Definition:

- ullet  $A_1$  is the set are the first four positive integers.
- ullet  $B_1$  is the set of colors of the Union Jack
- Extensional Definition:
  - $\bullet \ A_2 = \{4, 2, 1, 3\}$
  - $B_2 = \{ Blue, Red and White \}$

### Specify a set intensionally or extensionally

In the examples above, for instance,  $A_1 = A_2$  and  $B_1 = B_2$ 



# Infinite Sets: an Extensional set example Sets that go on forever

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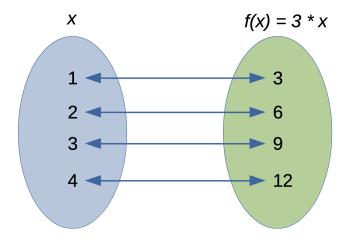
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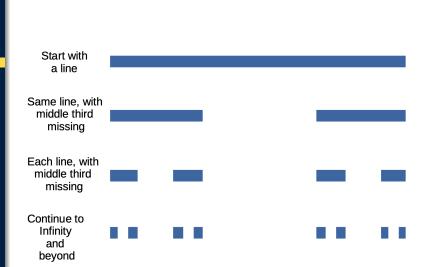
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## Listing Elements in Sets

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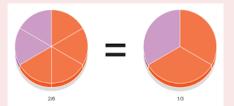
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 In extensionally defined sets, members in braces can be listed two or more times,

- For example, {11, 6, 6} is identical to the set {11, 6}
- Order of members is not important
  - For example,  $\{6, 11\} = \{11, 6\} = \{11, 6, 6, 11\}$

Similar to the equivalence of these pie charts: the content is the same in both cases





# Sets with Notation Venn Diagram

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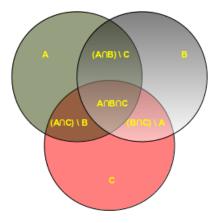
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- ullet Union:  $A\cup B$  of a collection of sets A and B is the set of all elements in the collection
- $\cap$ , Intersection  $A\cap B$  of two sets A and B is the set that contains all elements of A that also belong to B

An array of non-redundant elements

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## Creating a set of chars

```
x_st = set("This is a set")
x_st  # or print(x_st)
  # the unordered chars are the elements
  # {'s', 'T', '', 'e', 't', 'h', 'i', 'a'}
print(type(x_st))
  # <class 'set'>
```

### Creating a set of string(s)

```
x_st = set(["This is a set"])
x_st # or print(x_st)
    # only one element in set; the string itself
    #{'This is a set'}
x_st = set(["This", "is", "a", "set"])
    # each word is an element
    #{'This', 'is', 'set', 'a'}
```

```
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```

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### Adding new elements

```
cities_st = set(["Frankfurt", "Basel", "Freiburg"])
cities_st.add("Meadville")
cities_st # or print(cities_st)
    # {'Freiburg', 'Meadville', 'Basel', 'Frankfurt'}
```

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### Removing elements

```
cities_st = set(["Frankfurt", "Basel", "Meadville"])
cities_st.remove("Meadville")  # Meadville is a key
cities_st  # or print(cities_st)
  # {'Basel', 'Frankfurt'}
```

### Frozensets cannot be changed

```
cities_st = frozenset(["Frankfurt", "Basel", "Freiburg"])
cities_st.add("Meadville")
    # AttributeError:
    # 'frozenset' object has no attribute 'add'
cities_st # or print(cities_st)
    # frozenset({'Freiburg', 'Basel', 'Frankfurt'})
type(cities_st)
    # <class 'frozenset'>
```



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### Removing all elements of set

```
cities_st = {"Stuttgart", "Konstanz", "Freiburg"}
cities_st
    # {'Freiburg', 'Konstanz', 'Stuttgart'}
cities_st.clear()
cities_st
    # set()
```

### Determining difference between sets

```
x = {"a","b","c","d","e"}
y = {"b","c"}
z = {"c","d"}
x.difference(y) # {'a', 'e', 'd'}
x.difference(y).difference(z) # {'a', 'e'}
```

 Returns the characters which are never repeated across {x, y, y}



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### Difference and subtraction

```
x = {'c', 'a', 'd', 'b', 'e'}
y = {'c', 'b'}
x.difference_update(y)
print(x) # {'a', 'd', 'e'}
print(y) # {'c', 'b'}

print(x) # {'a', 'e', 'd'}
x = {"a", "b", "c", "d", "e"}
y = {"b", "c"}
x = x - y
print(x) # {'e', 'd', 'a'}
```

• Top: Returns an updated set of x of the characters which are never repeated across  $\{x, y, y\}$ 



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### Cloning and removing from original

```
x = {'e', 'd', 'a'}
v = x
print(x) # {'a', 'e', 'd'}
print(v) # {'a', 'e', 'd'}
x.remove('a')
x # {'e', 'd'}
v # {'e', 'd'}
v.remove('d')
x # {'e'}
y # {'e'}
```

• x = v does not make a copy of x. Instead this is a reference from one object to another.



## Checking for Particular Elements

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#### Is an element in a List?

```
x = {"a","b","c","d","e"}
"e" in x # True
"e" and "a" in x # True
"e" and "i" in x # False
```

## Iterating Through Elements in Sets

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#### Iteration

```
abc_set = {"a","b","c","d","e"}
for i in abc_set:
    print(i)
```

#### Note

• Since there is no order control in the set, you cannot know which element will be printed first (from above).



# Lists in Python

Lists, similar to arrays, are collections which are ordered and changeable.

```
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```

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```
Creating lists with append maintains position information
```

```
myList_list = []
myList_list #or print(myList_list)
    # []
myList_list.append("x")
myList_list.append("x") # again
myList_list # ['x', 'x']
```

### Creating lists in entirety

```
myList_list = ["a","b","c","d"]
myList_list #or print(myList_list)
    #['a', 'b', 'c', 'd']
type(myList_list)
    #<class 'list'>
```

• With a list, position of character is maintained, not so with a set.

# Lists in Python

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### Removing an element

```
myList_list = ["a"]
print(myList_list)
    # ['a']
myList_list.remove("a")
print(myList_list)
    # []
```

### Reverse the entire list, no assignment necessary

```
myList_list = ["a","b","c","d"]
myList_list.reverse()
myList_list #or print(myList_list)
    # ['d', 'c', 'b', 'a']
```



# Lists in Python

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### Each element has a location

```
myList_list = ["a","b","c","d"]
myList_list[0] # 'a'
myList_list[3] # 'd'
myList_list[300] #IndexError
```

### Print each element by location

```
for i in range(len(myList_list)):
    print("index = ",i)
    print(" myList_list[i] = ",myList_list[i])
# index = 0
# myList_list[i] = a
# ...
# index = 3
# myList_list[i] = d
```



### Iterating Through Elements in Lists

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#### Iteration

```
l_list = ["a","b","c","d"]
for i in l_list:
    print(i)
```

#### Iteration

```
l_list = ["a","b","c","d"]
for i in range(len(l_list)):
    print("i = ",i," and l_list[i] = ",l_list[i])
```

#### Note

• With lists, we know which element will be printed first (the first element, from above).

## Lambda Functions

We will use these to create lists ...

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### Lambda function definition

 The lambda operator or lambda function is a way to create small anonymous functions (i.e. functions without a name), and are throw-away functions

#### General syntax

lambda argument\_list: expression

$$g = lambda x: 3*x + 1$$
  
 $g(2) # 7$ 

$$sum = lambda x, y : x + y$$
  
 $sum(3,4) # 7$ 



## List Comprehensions to build lists

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### List comprehensions definition

 List comprehensions provide a concise way to create lists (or sets)

### General syntax

[ expression for item in list if conditional ]

#### Make list

```
[i for i in range(10)]
[0, 1, 2, 3, 4, 5, 6, 7, 8, 9]
```

### Assign list to variable

```
b_list = [i for i in range(10)]
type(b_list)
<class 'list'>
```



## List Comps and Lambda Functions to build lists

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### Build a list with an anonymous function

```
g_list = lambda x: list(i for i in range(x))
g_list(4)  # [0, 1, 2, 3]
myList_list = g_list(4)
myList_list # [0, 1, 2, 3]
# slicing particular elements
myList_list[0:2] # [0, 1]
```

# Tuples

A Tuple is a collection of Python objects separated by commas

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# An empty tuple

```
empty_tuple = ()
print (empty_tuple)
type(empty_tuple) # <class 'tuple'>
```

### A non-empty tuple

```
nonEmpty_tuple = ("a","b","c","d")
nonEmpty_tuple[0] # 'a'
nonEmpty_tuple[len(nonEmpty_tuple)-1] # 'd'
```

### Check to see that elements are in a tuple

```
nonEmpty_tuple # ('a', 'b', 'c', 'd', 4, 'Hi')
"Hi" in nonEmpty_tuple # True
4 in nonEmpty_tuple # True
3 in nonEmpty_tuple # False
```

# **Tuples**

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### Checking for sub-elements of elements at a tuple location

```
nonEmpty_tuple = ("a","b","c","d", 4, "Hi", "My music")
nonEmpty_tuple
# ('a', 'b', 'c', 'd', 4, 'Hi', 'My music')
```

"my" in nonEmpty\_tuple # False

"My" in nonEmpty\_tuple # False

# check to see if detail is in a substring in tuple

"My" in nonEmpty\_tuple[6] # True

## Adding to Tuples

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### Convert tuple to list, add element, convert back

```
a_tuple = ('2',) #define Tuple
items = ['a', 'b', 'c', 'd'] # elements to add
l_list = list(a_tuple)# make a list
for x in items:
    l_list.append(x) # add items to list
#output as a tuple
print(tuple(l_list))
```

# Iterating Through Elements in Tuples

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### Iteration

```
nonEmpty_tuple = ("a","b","c","d", 4, "Hi", "My music")
for i in nonEmpty_tuple:
    print(i)
```

#### Iteration

```
for i in range(len(nonEmpty_tuple)):
   print("i= ",i, "nonEmpty_tuple[i]=",nonEmpty_tuple[i])
```

#### Note

• With tuples (like lists), we know which element will be printed first (the first element, from above).

### Dictionaries

An array of a key and a value that is connected for quick searching

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- A dictionary maps a set of objects (keys) to another set of objects (values).
- A Python dictionary is a mapping of unique keys to values.
- Dictionaries are mutable, which means they can be changed.
- The values that the keys point to can be any Python value

### An empty dictionary

```
myDictionary_dict = {}
print (myDictionary_dict)
type(myDictionary_dict) # <class 'dict'>
```



### **Dictionaries**

#### Sets

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### Adding to a dictionary

```
myDictionary_dict = {}
myDictionary_dict[0] = "zero"
myDictionary_dict[0] # gives 'zero'

myDictionary_dict[1] = "one"
print (myDictionary_dict) #{1: 'one', 0: 'zero'}
```

### Removing elements from a dictionary

```
myDictionary_dict = {}
myDictionary_dict[3] = "three"

del myDictionary_dict[3]
print (myDictionary_dict) #{} (is empty)
```

## Randomly Choosing Elements

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### Choosing Elements from a List

```
import random
abc_list = ['a','b','c','d','e']
random.choice(abc_list) # 'c'
random.choice(abc_list) # 'd'
```

### Choosing Elements from a List

```
import random
abc_set = set(['a','b','c','d','e'])
    # convert to list
abc2_list = list(abc_set)
random.choice(abc2_list) # 'd'
```



### Randomly Choosing Elements

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### Choosing Elements from a Dictionary



# This Week: You will be comparing Lists import random

```
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```

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```
import random
aliceVocab_list = ["I like cats", "I like dogs",
"I like rabbits", "I gave carrots to horses",
"I live on a farm"]
# choose random element
aliceSays_str = random.choice(aliceVocab_list)
print(" This is Alice. I say to Bob :", aliceSays_str)
bobVocab_list = ["I have two cats", "I have three dogs",
"I know several rabbits", "I love carrots",
"I love horses", "I also live on a farm"]
bobSays_str = random.choice(bobVocab_list)
print(" This is Bob. I reply to Alice :",bobSays_str)
```



### Removing Stop-Words

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```
This week's lab: Remove Words from Strings using Lists
```

```
stopWords_list =["I", "have","know",
"like", "love", " to ", " a "]

# we remove stop words
# as they do not add specificity to the strings

def removeStopWords(in_str): # string input
  for s in stopWords_list:
    in_str = in_str.replace(s,"") #word with empty space
  return in_str.strip() # remove spaces, return.
  #end of removeStopWords()
```

- Remove stop-words and compare the lists for common words.
- When you find the common words between two lists, you have found a contextual link between them.