



Sets

Sets by the
Math

Functions
Make Sets

What is a
Set?

Sets in
Python

Lists in
Python

Tuples in
Python

Dictionaries

Randomly
Choosing
Elements

This week's
Lab

Discrete Structures: CMPSC 102

Oliver BONHAM-CARTER

Fall 2019
Week 4

Georg Ferdinand Ludwig Philipp Cantor

Creator of Set theory

Sets

Sets by the
Math

Functions
Make Sets

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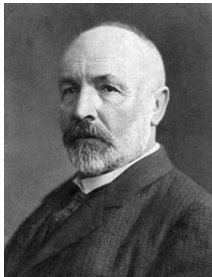
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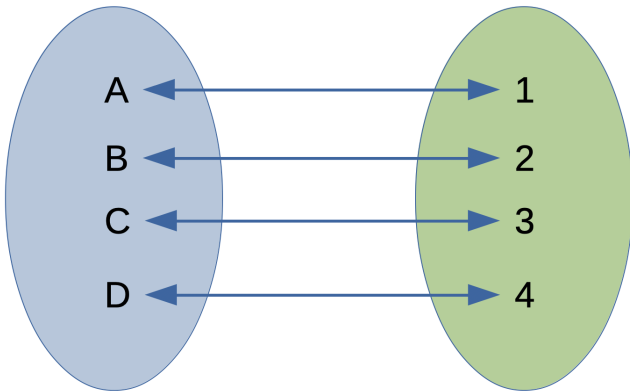
- German mathematician: 19 February 1845 - 6 January 1918
- Function definition: established the importance of one-to-one correspondence between the members of two sets (more on that in a moment!)
- Defined infinite and well-ordered sets
- Proved that the real numbers (*rational* and *irrational*) are more numerous than the natural numbers (*counting* numbers)

Functions as Sets

Regular Set: one-to-one relationship maintained

Letter Set

Number Set



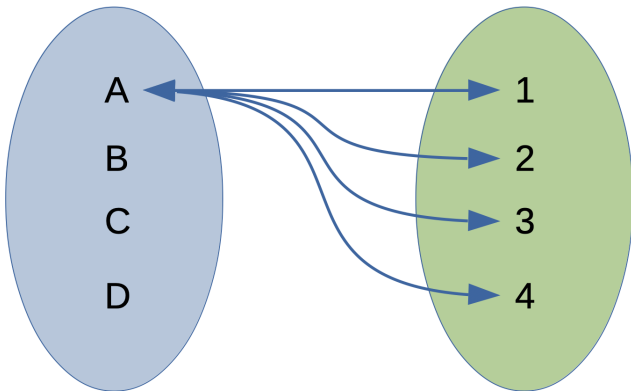
- The Letter set maps to the Number set.
- $LetterSet(x) \rightarrow NumberSet$

Functions Sets

Regular Set: one-to-one-ism is maintained

Letter Set

Number Set



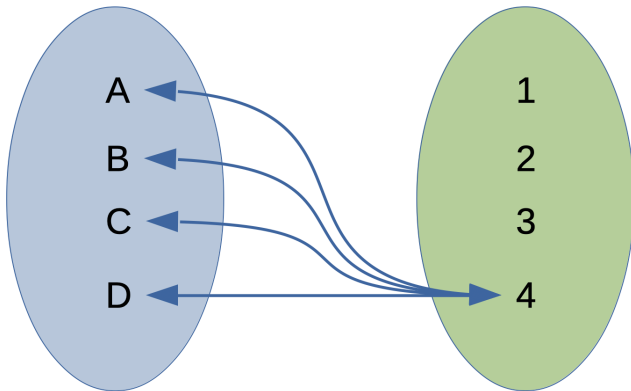
- The Letter set maps to the Number set.
- $LetterSet(x) \rightarrow NumberSet$

Functions as Sets

One-to-one-ism is NOT maintained!

Letter Set

Number Set



- The Letter set maps to the Number set.
- $LetterSet(x) \rightarrow NumberSet$

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What is a set?

- For example, the numbers 1, 2, and 3 are distinct objects when considered separately, but when they are considered collectively they form a single set of size three, written $\{1,2,3\}$.
- Set theory is now a ubiquitous part of mathematics,
- May be used as a foundation from which nearly all of mathematics can be derived (From 19th century mathematical thinking!)

Types of Sets

Intensional and Extensional

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Intentional definition of sets: *I intend this set to be ...*

- Defines a set by specifying the necessary and sufficient conditions for when the set should be used.

Extensional definition of sets: *Logically this set is ...*

- Defines a set by some definition of a concept or a term.

Types of Sets

Intentional: One decides which elements make up a set

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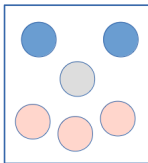
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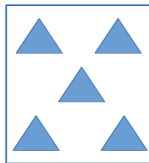
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Set of Circles



Set of Triangles

Intentional definition of sets: *I intend that these set be ...*

- The set of blue, grey and pink circles
- The set of blue triangles
- The set of colors of the Union Jack (i.e., the British flag)



Types of Sets

Extensional: Sets of members in curly brackets

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Extensional definition of sets

- $A_2 = \{4, 2, 1, 3\}$
 - The first four positive numbers
- $B_2 = \{\text{Blue, Red and White}\}$
 - The set of colors of the Union Jack (the British flag)
- $F = \{n^2 - 4 : n \text{ is an integer; and } 0 \leq n \leq 19\}$
 - The set of all values gained from plugging in n between 0 and 19 into the equation $n^2 - 4$

Types of Sets

Extensional definition of sets: a list of its members in curly brackets

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- **Intentional Definition:**

- A_1 is the set are the first four positive integers.
- B_1 is the set of colors of the Union Jack

- **Extensional Definition:**

- $A_2 = \{4, 2, 1, 3\}$
- $B_2 = \{\text{Blue, Red and White}\}$

Specify a set *intensionally* or *extensionally*

In the examples above, for instance, $A_1 = A_2$ and $B_1 = B_2$

Infinite Sets: an Extensional set example

Sets that go on forever

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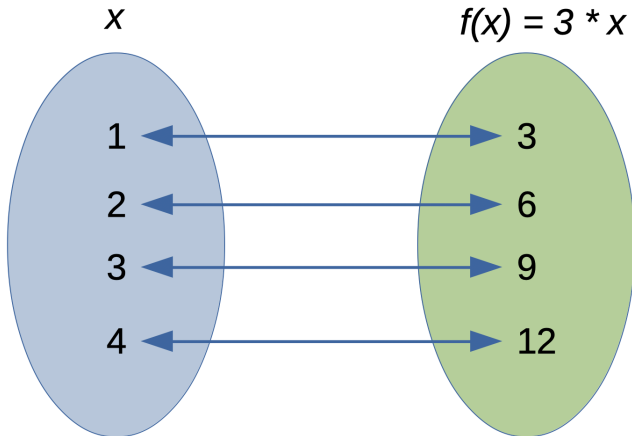
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Infinite Sets: an Extensional set example

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Start with
a line



Same line, with
middle third
missing



Each line, with
middle third
missing



Continue to
Infinity
and
beyond



Listing Elements in Sets

Sets

Functions Make Sets

What is a Set?

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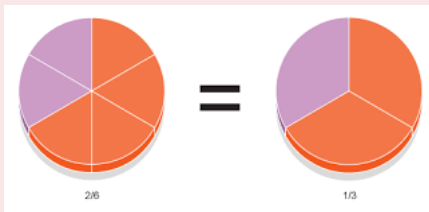
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Randomly Choosing Elements

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- In extensionally defined sets, members in braces can be listed two or more times,
 - For example, $\{11, 6, 6\}$ is identical to the set $\{11, 6\}$
- Order of members is not important
 - For example, $\{6, 11\} = \{11, 6\} = \{11, 6, 6, 11\}$

Similar to the equivalence of these pie charts:
the content is the same in both cases



Sets with Notation

Venn Diagram

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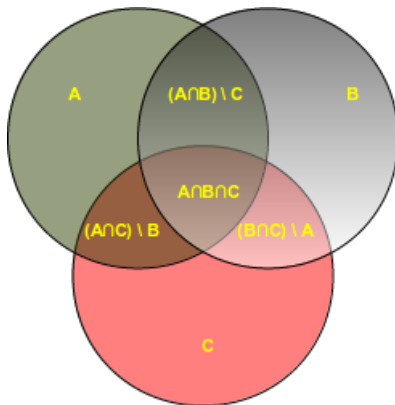
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- \cup , Union: $A \cup B$ of a collection of sets A and B is the set of all elements in the collection
- \cap , Intersection $A \cap B$ of two sets A and B is the set that contains all elements of A that also belong to B

Sets in Python

An array of non-redundant elements

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Creating a set of chars

```
x_st = set("This is a set")
x_st    # or print(x_st)
        # the unordered chars are the elements
        # {'s', 'T', ' ', 'e', 't', 'h', 'i', 'a'}
print(type(x_st))
        # <class 'set'>
```

Creating a set of string(s)

```
x_st = set(["This is a set"])
x_st    # or print(x_st)
        # only one element in set; the string itself
        # {'This is a set'}
x_st = set(["This", "is", "a", "set"])
        # each word is an element
        # {'This', 'is', 'set', 'a'}
```

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```
# next line on one line
cities_st = set(("Paris", "Lyon",
                "London","Berlin","Birmingham", "Paris"))
print(cities_st)
# {'Berlin', 'Paris', 'Birmingham', 'London', 'Lyon'}
```

Adding new elements

```
cities_st = set(["Frankfurt", "Basel", "Freiburg"])
cities_st.add("Meadville")
cities_st # or print(cities_st)
# {'Freiburg', 'Meadville', 'Basel', 'Frankfurt'}
```


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Removing elements

```
cities_st = set(["Frankfurt", "Basel", "Meadville"])
cities_st.remove("Meadville")    # Meadville is a key
cities_st    # or print(cities_st)
           # {'Basel', 'Frankfurt'}
```

Frozensets cannot be changed

```
cities_st = frozenset(["Frankfurt", "Basel", "Freiburg"])
cities_st.add("Meadville")
           # AttributeError:
           # 'frozenset' object has no attribute 'add'
cities_st # or print(cities_st)
           # frozenset({'Freiburg', 'Basel', 'Frankfurt'})
type(cities_st)
           # <class 'frozenset'>
```

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Removing all elements of set

```
cities_st = {"Stuttgart", "Konstanz", "Freiburg"}
cities_st
# {'Freiburg', 'Konstanz', 'Stuttgart'}
cities_st.clear()
cities_st
# set()
```

Determining difference between sets

```
x = {"a","b","c","d","e"}
y = {"b","c"}
z = {"c","d"}
x.difference(y) # {'a', 'e', 'd'}
x.difference(y).difference(z) # {'a', 'e'}
```

- Returns the characters which are never repeated across {x, y, y}

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Difference and subtraction

```
x = {'c', 'a', 'd', 'b', 'e'}
```

```
y = {'c', 'b'}
```

```
x.difference_update(y)
```

```
print(x) # {'a', 'd', 'e'}
```

```
print(y) # {'c', 'b'}
```

```
print(x) # {'a', 'e', 'd'}
```

```
x = {"a","b","c","d","e"}
```

```
y = {"b","c"}
```

```
x = x - y
```

```
print(x) # {'e', 'd', 'a'}
```

- Top: Returns an updated set of x of the characters which are never repeated across $\{x, y, y\}$

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Cloning and removing from original

```
x = {'e', 'd', 'a'}
v = x
print(x)    # {'a', 'e', 'd'}
print(v)    # {'a', 'e', 'd'}
x.remove('a')
x    # {'e', 'd'}
v    # {'e', 'd'}
v.remove('d')
x    # {'e'}
v    # {'e'}
```

- $x = v$ does not make a copy of x . Instead this is a reference from one object to another.

Checking for Particular Elements

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Is an element in a List?

```
x = {"a","b","c","d","e"}  
"e" in x      # True  
"e" and "a" in x  # True  
"e" and "i" in x  # False
```

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Iteration

```
abc_set = {"a","b","c","d","e"}  
for i in abc_set:  
    print(i)
```

Note

- Since there is no order control in the set, you cannot know which element will be printed first (from above).

Lists in Python

Lists, similar to arrays, are collections which are ordered and changeable.

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Creating Lists with append maintains position information

```
myList_list = []  
myList_list #or print(myList_list)  
# []  
myList_list.append("x")  
myList_list.append("x")    # again  
myList_list    # ['x', 'x']
```

Creating lists in entirety

```
myList_list = ["a","b","c","d"]  
myList_list #or print(myList_list)  
#['a', 'b', 'c', 'd']  
type(myList_list)  
#<class 'list'>
```

- With a list, position of character is maintained, not so with a set.

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Removing an element

```
myList_list = ["a"]  
print(myList_list)  
#    ['a']  
myList_list.remove("a")  
print(myList_list)  
#    []
```

Reverse the entire list, no assignment necessary

```
myList_list = ["a","b","c","d"]  
myList_list.reverse()  
myList_list #or print(myList_list)  
# ['d', 'c', 'b', 'a']
```


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Each element has a location

```
myList_list = ["a","b","c","d"]  
myList_list[0] # 'a'  
myList_list[3] # 'd'  
myList_list[300] #IndexError
```

Print each element by location

```
for i in range(len(myList_list)):  
    print("index = ",i)  
    print("    myList_list[i] = ",myList_list[i])  
#     index = 0  
#     myList_list[i] = a  
#     ...  
#     index = 3  
#     myList_list[i] = d
```

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Iteration

```
l_list = ["a","b","c","d"]
for i in l_list:
    print(i)
```

Iteration

```
l_list = ["a","b","c","d"]
for i in range(len(l_list)):
    print("i = ",i," and l_list[i] = ",l_list[i])
```

Note

- With lists, we know which element will be printed first (the first element, from above).

Lambda Functions

We will use these to create lists ...

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Lambda function definition

- The lambda operator or lambda function is a way to create small anonymous functions (i.e. functions without a name), and are *throw-away* functions

General syntax

lambda argument_list: expression

```
g = lambda x: 3*x + 1
g(2) # 7
```

```
sum = lambda x, y : x + y
sum(3,4) # 7
```

List Comprehensions to build lists

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List comprehensions definition

- List comprehensions provide a concise way to create lists (or sets)

General syntax

[expression for item in list if conditional]

Make list

```
[i for i in range(10)]  
[0, 1, 2, 3, 4, 5, 6, 7, 8, 9]
```

Assign list to variable

```
b_list = [i for i in range(10)]  
type(b_list)  
<class 'list'>
```

List Comps and Lambda Functions to build lists

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Build a list with an anonymous function

```
g_list = lambda x: list(i for i in range(x))
g_list(4)    #    [0, 1, 2, 3]
myList_list = g_list(4)
myList_list #    [0, 1, 2, 3]
# slicing particular elements
myList_list[0:2] #    [0, 1]
```

Tuples

A Tuple is a collection of Python objects separated by commas

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An empty tuple

```
empty_tuple = ()  
print (empty_tuple)  
type(empty_tuple)    # <class 'tuple'>
```

A non-empty tuple

```
nonEmpty_tuple = ("a","b","c","d")  
nonEmpty_tuple[0]    #    'a'  
nonEmpty_tuple[len(nonEmpty_tuple)-1]    #    'd'
```

Check to see that elements are in a tuple

```
nonEmpty_tuple    #    ('a', 'b', 'c', 'd', 4, 'Hi')  
"Hi" in nonEmpty_tuple    #    True  
4 in nonEmpty_tuple    #    True  
3 in nonEmpty_tuple    #    False
```

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Check to see that elements are in an element at a tuple location

```
nonEmpty_tuple = ("a","b","c","d", 4, "Hi", "My music")
nonEmpty_tuple
# ('a', 'b', 'c', 'd', 4, 'Hi', 'My music')
"my" in nonEmpty_tuple    # False
"My" in nonEmpty_tuple    # False

# check to see if detail is in a substring in tuple
"My" in nonEmpty_tuple[6] # True
```

Adding to Tuples

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Convert tuple to list, add element, convert back

```
a_tuple = ('2',) #define Tuple
items = ['a', 'b', 'c', 'd'] # elements to add
l_list = list(a_tuple)# make a list
for x in items:
    l_list.append(x) # add items to list
#output as a tuple
print(tuple(l_list))
```


Iterating Through Elements in Tuples

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Iteration

```
nonEmpty_tuple = ("a","b","c","d", 4, "Hi", "My music")
for i in nonEmpty_tuple:
    print(i)
```

Iteration

```
for i in range(len(nonEmpty_tuple)):
    print("i= ",i, "nonEmpty_tuple[i]="nonEmpty_tuple[i])
```

Note

- With tuples (like lists), we know which element will be printed first (the first element, from above).

Dictionaries

An array of a key and a value that is connected for quick searching

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- A dictionary maps a set of objects (keys) to another set of objects (values).
- A Python dictionary is a mapping of unique keys to values.
- Dictionaries are mutable, which means they can be changed.
- The values that the keys point to can be any Python value

An empty dictionary

```
myDictionary_dict = {}  
print (myDictionary_dict)  
type(myDictionary_dict)    # <class 'dict'>
```

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Adding to a dictionary

```
myDictionary_dict = {}  
myDictionary_dict[0] = "zero"  
myDictionary_dict[0] # gives 'zero'  
  
myDictionary_dict[1] = "one"  
print (myDictionary_dict) #{1: 'one', 0: 'zero'}
```

Removing elements from a dictionary

```
myDictionary_dict = {}  
myDictionary_dict[3] = "three"  
  
del myDictionary_dict[3]  
print (myDictionary_dict) #{} (is empty)
```

Randomly Choosing Elements

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Choosing Elements from a List

```
import random
abc_list = ['a','b','c','d','e']
random.choice(abc_list)    # 'c'
random.choice(abc_list)    # 'd'
```

Choosing Elements from a List

```
import random
abc_set = set(['a','b','c','d','e'])
    # convert to list
abc2_list = list(abc_set)
random.choice(abc2_list)    # 'd'
```

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Choosing Elements from a Dictionary

```
import random
abc_dict = {1:"one",2:"two",3:"Three"} # {vals : keys}
num_list = list(abc_dict) # convert dict to list
n = random.choice(num_list) # pick a number in list
abc_dict[n] # sub in n to get key value
# 'two'
```

This Week: You will be comparing Lists

import random

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```
import random

aliceVocab_list = ["I like cats", "I like dogs",
                  "I like rabbits", "I gave carrots to horses",
                  "I live on a farm"]

# choose random element
aliceSays_str = random.choice(aliceVocab_list)
print("  This is Alice. I say to Bob :", aliceSays_str)

bobVocab_list = ["I have two cats", "I have three dogs",
                 "I know several rabbits","I love carrots",
                 "I love horses","I also live on a farm"]

bobSays_str = random.choice(bobVocab_list)
print("  This is Bob. I reply to Alice :", bobSays_str)
```

Removing Stop-Words

Sets

Functions
Make Sets

What is a
Set?

Sets in
Python

Lists in
Python

Tuples in
Python

Dictionaries

Randomly
Choosing
Elements

This week's
Lab

This week's lab: Remove Words from Strings using Lists

```
stopWords_list = ["I", "have", "know",  
"like", "love", " to ", " a "]
```

```
# we remove stop words
```

```
# as they do not add specificity to the strings
```

```
def removeStopWords(in_str): # string input  
    for s in stopWords_list:  
        in_str = in_str.replace(s,"") #word with empty space  
    return in_str.strip() # remove spaces, return.  
#end of removeStopWords()
```

- Remove stop-words and compare the lists for common words.
- When you find the common words between two lists, you have found a contextual link between them.