### **Contents**

# 1 Setting

### 1.1 /.vimrc

```
1 syntax on
2 color torte
3 set nu ts=4 sw=4 ai mouse=a bs=2 ci hls ru nocp
       showmatch ar fencs=utf-8
4 set guifont=Consolas:h10
5 filetype plugin indent on
6 so $VIMRUNTIME/mswin.vim
7 behave mswin
8
  autocmd CursorMoved * exe printf('match VisualNOS /\V
       \<%s\>/', escape(expand('<cword>'), '/\'))
10 autocmd CursorMovedi * exe printf('match VisualNOS /\V
       \<%s\>/', escape(expand('<cword>'), '/\'))
11
12 map <F5> :r ~/sample.cpp<CR>
13 map <F9> :call Compile()<CR>
14 map! <F9> <ESC>:call Compile()<CR>
15 map <F10> :call Run()<CR>
16 map! <F10> <ESC>:call Run()<CR>
17
18 func! Compile()
19
      exec "w"
       exec "!g++ -Wall -Wshadow -std=gnu++0x % -o %< 2>
20
           log.txt"
21
       exe "cg log.txt"
22
      cw 5
23 endfunc
24
25 func! Run()
      exec "!./%<" # "!%<" if windows
26
27 endfunc
29 cd ~/Desktop # C:\Users\???\Desktop
```

#### 2 Basic

#### 2.1 Builtin

```
1 - Built-in Function: int __builtin_ffs (T x)
3 Returns one plus the index of the least significant 1-
      bit of x, or if x is zero, returns zero.
4|返回右起第一个'1'的位置。
   — Built-in Function: int __builtin_clz (T x)
8 Returns the number of leading 0-bits in x, starting at
      the most significant bit position. If x is 0, the
      result is undefined.
9 返回左起第一个'1'之前0的个数。
10
   — Built-in Function: int __builtin_ctz (T x)
11
Returns the number of trailing 0-bits in x, starting at \frac{1}{14}
       the least significant bit position. If x is 0, the \frac{1}{15}
       result is undefined.
14 返回右起第一个'1'之后的0的个数。
15
  — Built-in Function: int __builtin_popcount (T x)
17
18 Returns the number of 1-bits in x.
  |返回'1'的个数。
19
20
21 - Built-in Function: int __builtin_parity (T x)
```

### 2.2 BinarySearch

```
1 | lower_bound(a, a+n, k); //最左邊 ≥ k 的位置
2 | upper_bound(a, a+n, k); //最左邊 > k 的位置
3 | upper_bound(a, a+n, k) - 1; //最右邊 ≤ k 的位置
4 | lower_bound(a, a+n, k) - 1; //最右邊 < k 的位置
5 | [lower_bound, upper_bound) //等於 k 的範圍
6 | equal_range(a, a+n, k);
```

### 2.3 int128

```
1 istream &operator >> (istream &is, __int128 &x) {
       char buf[30];
 3
       is >> buf;
       bool minus = false;
 5
       int len = strlen(buf);
 6
       x = 0:
 7
       for (int i=0; i<len; i++) {</pre>
            if (i==0 && buf[i]=='-') minus = true;
 ጸ
 9
            else x = x*10 + buf[i] - 48;
10
11
       if (minus) x^*=-1;
12
       return is;
13
14
   ostream &operator << (ostream &os, __int128 &x) {
15
       vector<int> v;
16
         int128 tmp = x;
17
       bool minus = tmp < 0;</pre>
18
       if (minus) tmp *= -1;
19
20
       while(tmp > 0) {
            v.push_back(tmp%10);
21
22
            tmp/=10;
23
24
       if (minus) os << "-";</pre>
25
       for (int i=(int)v.size()-1; i>=0; i--) os << v[i];</pre>
26
       return os;
27 }
```

### 2.4 Mergesort

```
1 long long sol(int L, int R) {
     if (R - L <= 1)return 0;</pre>
 3
     int M = (R + L) / 2;
     long long ans = sol(L, M) + sol(M, R);
 5
     int i = L, j = M, k = L;
     while (i < M \mid \mid j < R) {
 6
       if (i >= M)
 8
         buf[k] = arr[j++];
       else if (j >= R)
10
         buf[k] = arr[i++];
11
       else
12
          if (arr[i]<=arr[j])</pre>
13
            buf[k] = arr[i++];
          else {
            buf[k] = arr[j++];
16
            ans += M - i;
17
         }
18
       }
19
       k++;
20
21
     for (int k = L; k < R; k++) arr[k] = buf[k];</pre>
22
     return ans;
23 }
```

3.3

Treap

#### 2.5 ThreeSearch

```
1 struct Treap{
1 #include <bits/stdc++.h>
                                                                   Treap *1, *r;
                                                               2
2 using namespace std;
                                                               3
                                                                   int val, key, pri;
 3 #define N 20
                                                                   Treap(int _val, int _key) :
                                                               4
4 int t,n,i,j;
                                                               5
                                                                      val(_val), key(_key), l(NULL), r(NULL), pri(rand())
  struct happy{
     double a,b,c;
                                                               6
                                                                   Treap(){};
 7 }h[N];
                                                               7
8 double f2(double x,double a,double b,double c){return a
                                                                 Treap* merge(Treap* a, Treap* b){
       *(x-b)*(x-b)+c;}
                                                                   if (!a || !b)return a ? a : b;
9
   double f(double x){
                                                              10
                                                                   if (a->pri > b->pri){
10
     double ans=0;
                                                              11
                                                                     a->r = merge(a->r, b);
     for(int i=0;i<n;i++){</pre>
11
                                                              12
                                                                     return a;
12
       ans=max(ans,f2(x,h[i].a,h[i].b,h[i].c));
                                                              13
         cout<<ans<<'\n';</pre>
                                                                   }else{
13 //
                                                              14
                                                                      b->1 = merge(a, b->1);
14
                                                              15
                                                                      return b;
15
     return ans;
                                                              16
16|}
                                                              17
17 int main(){
                                                                 void split(Treap* t, int k, Treap *&a, Treap *&b){
                                                              18
     cin.tie(NULL);
18
                                                              19
                                                                   if (!t)a = b = NULL;
19
     for(cin>>t;i<t;i++){</pre>
                                                              20
20
       for(cin>>n,j=0;j<n;j++)</pre>
                                                                   else if (t->key <= k){</pre>
                                                              21
                                                                     a = t:
21
         cin>>h[j].a>>h[j].b>>h[j].c;
                                                              22
                                                                      split(t->r, k, a->r, b);
22
       double L=0,R=300,M,MM;
                                                              23
                                                                   }else {
23
       while(R-L>1e-9){
                                                              24
                                                                     b = t;
24
         M=L+(R-L)/3;
                                                              25
                                                                     split(t->1, k, a, b->1);
25
         MM=(M+R)/2;
                                                              26
           cout<<L<<' '<<M<<' '<<MM<<' '<<R<<'\n';
26
                                                              27
                                                                   return;
         if(f(M)>f(MM))L=M;
27
                                                              28
                                                                 }
28
         else R=MM;
                                                              29
                                                                 Treap* insert(Treap* t, int k){
29
                                                              30
                                                                   Treap *tl, *tr;
30
       cout<<fixed<<setprecision(5)<<f(L)<<'\n';</pre>
                                                              31
                                                                   split(t, k, tl, tr);
31
32 }
                                                              32
                                                                   return merge(tl, merge(new Treap(k, ti++), tr));
                                                              33
                                                              34
                                                                 Treap* remove(Treap* t, int k){
                                                              35
                                                                   Treap *tl, *tr;
                                                              36
                                                                   split(t, k - 1, tl, t);
        Data and Structure
                                                              37
                                                                   split(t, k, t, tr);
```

### 3.1 Disjoint Set

```
1 void init(){for (int i = 0; i < N; i++)p[i] = i;}
2 int find(int x){return x == p[x] ? x : p[x]=find(p[x])
    ;}
3 void Union(int a, int b){p[find(a)] = find(b);}</pre>
```

## 3.2 Segment Tree

```
1 int bulit(int L,int R,int x) {
2
     if(L==R)return heap[x - 1]=arr[L];
3
     int M=(L+R)>>1;
 4
     return heap[x-1]=bulit(L, M, (x << 1))+bulit(M + 1, R 8</pre>
          (x << 1) + 1);
5
  }
                                                                10
6
  void modify(int L,int R,int x,int a,int b,int mo) {
                                                                11
7
       if(b<L||R<a)return;</pre>
                                                                12
8
     if(L==R){heap[x-1]+=mo; return;}
                                                                13
9
     int M=(L+R)>>1;
                                                                14
10
     modify(L,M,(x<<1),a,b,mo);</pre>
                                                                15
11
     modify(M+1,R,(x<<1)+1,a,b,mo);
                                                                16
12
     heap[x - 1] += mo;
                                                                17
13
                                                                18
14|}
                                                                19
15
  int quest(int L,int R,int x,int a,int b) {
                                                                20
       if(b<L||R<a)return 0;</pre>
16
                                                                21
17
     if(a<=L&&R<=b)return heap[x - 1];</pre>
                                                                22
18
     int M=(L+R)>>1;
                                                                 23
19
     return quest(L,M,(x<<1),a,b)+quest(M+1,R,(x<<1)+1,a,b24</pre>
          );
                                                                25
20 }
                                                                 26
```

#### 4 DP

38

39 }

#### 4.1 CounterLine

return merge(tl, tr);

```
1 #include <bits/stdc++.h>
 2
   using namespace std;
 3 const int N=1<<15;
   int n,m,cur;
 5
   long long int dp[2][N];
   void update(int a,int b){
       if(b&(1<<m)){
            dp[cur][b^(1<<m)]+=dp[1-cur][a];</pre>
       }
   }
   int main(){
       while(cin>>n>>m){
            if((n*m)&1){
                cout << "0 \ n";
                continue:
            if(n==1||m==1){
                cout << "1 \n";
                continue;
            if(n<m)swap(n,m);</pre>
            memset(dp,0,sizeof(dp));
            cur=0;
            dp[0][(1<< m)-1]=1;
27
            for(int i=0;i<n;i++){</pre>
```

```
28
                for(int j=0;j<m;j++){</pre>
                                                                 9
                                                                            for(int jj=0;jj<n;jj++)b[n-jj-1]=(jj<i);</pre>
                    cur^=1;
                                                                10
29
                                                                            do{
30
                     memset(dp[cur],0,sizeof(dp[cur]));
                                                                                btb(st);
                                                                11
                                                                                for(int x=0;x<n;x++){</pre>
31
                     for(int k=0;k<(1<<m);k++){</pre>
                                                                12
32
                         update(k,k<<1);
                                                                13
                                                                                     if(!b[x])continue;
33
                         if(i&&!(k&(1<<m-1)))update(k,(k<<1)14</pre>
                                                                                     if(i==1)dp[x][st]=dis[x][0];
                              ^(1<<m)^1);
                                                                15
                                                                                     for(int y=0;y<n;y++){</pre>
34
                         if(j&&!(k&1))update(k,(k<<1)^3);</pre>
                                                                16
                                                                                         if(x!=y\&\&b[y]\&\&(dp[x][st]==0||dp[x]
35
                    }
                                                                                              ][st]>dp[y][st-(1<<x)]+dis[y][x
36
                }
37
                                                               17
                                                                                              dp[x][st]=dp[y][st-(1<<x)]+dis[
38
            cout<<dp[cur][(1<<m)-1]<<'\n';
                                                                                                  y][x];
39
                                                                18
40|}
                                                                19
                                                                                     }
                                                                20
                                                                            }while(next_permutation(b,b+n));
                                                                21
                                                                22
   4.2
          LCS
                                                                23
                                                                       cout<<dp[0][(1<<n)-1]<<'\n';
                                                                24
1 #include <bits/stdc++.h>
  using namespace std;
                                                                   5
                                                                        Graph
   int main() {
 5
     int n, m;
     vector<int>a, b, dp[2];
                                                                   5.1 Articulation Point
     cin >> n >> m;
8
     a.resize(n):
9
     b.resize(m);
                                                                   vector<int>v[N],bcc[N];//clear
                                                                 1
10
     for(int i=0;i<a.size();i++){</pre>
                                                                   LL dep[N],low[N],bccno[N],time_cnt,bcc_cnt;//set dep
11
       cin>>a[i];
                                                                        low -1 else 0
12
                                                                 3 bitset<N>is_AP;//0
13
     for(int i=0;i<b.size();i++){</pre>
                                                                   struct Edge{int s,t;};
14
       cin>>b[i];
                                                                 5
                                                                   stack<Edge>st;//clear
15
                                                                 6
                                                                   int dfs(int s,int fa){
16
     dp[0].resize(m+1);
                                                                       int child=0;
17
     dp[1].resize(m+1);
                                                                       dep[s]=low[s]=time_cnt++;
                                                                 8
18
     for(int i=1;i<=n;i++){</pre>
                                                                 9
                                                                        for(auto t:v[s]){
19
       for(int j=1;j<=m;j++){</pre>
                                                                10
                                                                            Edge e=(Edge){s,t};
          if(a[i-1]==b[j-1])dp[i&1][j]=dp[(i&1)^1][j-1]+1; 11
20
                                                                            if(dep[t]==-1){
          else dp[i&1][j]=max(dp[i&1][j-1],dp[(i&1)^1][j]);12
21
                                                                                st.push(e);
22
                                                                                child++;
23
                                                                14
                                                                                dfs(t,s);
24
     cout << dp[n&1][m] << '\n';
                                                                15
                                                                                low[s]=min(low[s],low[t]);
25 }
                                                                16
                                                                                if(dep[s]<=low[t]){</pre>
                                                                17
                                                                                     is_AP[s]=1;
                                                                18
                                                                                     bcc_cnt++;
                                                                19
                                                                                     bcc[bcc_cnt].clear();
   4.3
          LIS
                                                                20
                                                                                     while(1){
                                                                21
                                                                                         Edge x=st.top(); st.pop();
1 #include <bits/stdc++.h>
                                                                                         if(bccno[x.s]!=bcc_cnt){
                                                                22
  using namespace std;
                                                                23
                                                                                              bcc[bcc_cnt].push_back(x.s);
 3
                                                                24
                                                                                              bccno[x.s]=bcc_cnt;
 4
   int main(){
                                                                25
5
                                                                26
                                                                                         if(bccno[x.t]!=bcc_cnt){
       while(cin>>n){
                                                                                              bcc[bcc_cnt].push_back(x.t);
6
                                                                27
 7
            vector<int>v;
                                                                28
                                                                                              bccno[x.t]=bcc_cnt;
8
            for(int i=0,x;i<n;i++){</pre>
                                                                29
9
                cin>>x:
                                                                30
                                                                                         if(x.s==s&&x.t==t)break;
                if(!v.size()||x>v.back())v.push_back(x);
                                                                                     }
10
                                                                31
11
                else *lower_bound(v.begin(), v.end(),x)=x;
                                                               32
12
                                                                33
                                                                            }else if(low[s]>dep[t]){
13
            cout<<v.size()<<'\n';</pre>
                                                                34
                                                                                st.push(e);
                                                                35
14
                                                                                low[s]=dep[t];
15 }
                                                                36
                                                                37
                                                                38
                                                                       if(fa<0&&child==1)is_AP[s]=0;</pre>
                                                                39
                                                                       return low[s];
   4.4
          TSP
                                                                40
 1 void btb(int &x){
 2
                                                                          BellmanFord
 3
     for(int i=0,j=1;i<n;i++,j*=2)x+=b[i]*j;</pre>
 4
     return;
 5
  }
                                                                 1
                                                                   void bellman_ford(int s){
6
                                                                 2
  int main(){
                                                                       d[s]=0;
```

3

4

p[s]=s;

for(int i=0;i<n\*1;i++){</pre>

7

memset(dp,0,sizeof(dp));

for(int i=1,st;i<=n;i++){//st:state</pre>

```
for(int ss=0;ss<n;ss++){</pre>
6
                 for(auto:tt:v[ss]){
7
                      if(d[ss]+w[ss][tt]<d[tt]){</pre>
8
                           d[tt]=d[ss]+w[ss][tt];
9
                           p[tt]=ss;
10
                      }
11
                 }
12
             }
13
14
   }
15
   void has_negative_cycle(){
        for(int s=0;s<n;s++){</pre>
16
17
             for(int j=0;j<n;j++){</pre>
18
                 if(d[s]+w[s][t]<d[t])return true;</pre>
19
20
21
        return false;
22 }
```

### 5.3 Bipartite

1 #include <iostream>

```
2 #include <vector>
 3 #include <stack>
4 #include <cstring>
6 #define S 50050
8 using namespace std;
9
10 | vector<int> map[S];
11 int visit[S];
12 bool valid;
13
14
   void check(int start) {
15
       stack<int> st;
16
       st.push(start);
17
       visit[start] = 1;
18
19
       while(valid && !st.empty()) {
20
            int cur = st.top();
21
           st.pop();
22
23
           for(int i = 0; i < map[cur].size(); i++) {</pre>
24
                int next = map[cur][i];
25
26
                if(visit[next] == -1) {
27
                    st.push(next);
28
29
                    if(visit[cur] == 1) visit[next] = 2;
                    else visit[next] = 1;
30
31
32
                else if(visit[cur] == visit[next]) valid =
                     false:
33
           }
34
35 }
36
   int main() {
37
       int n, m;
38
       cin >> n >> m;
39
40
41
       for(int i = 0; i < m; i++) {</pre>
           int a, b;
42
43
           cin >> a >> b;
44
45
           map[a].push_back(b);
46
           map[b].push_back(a);
47
       }
48
49
       // -1 : not visit, 1 : tsudere, 2 : proud
50
       memset(visit, -1, sizeof(visit));
51
       valid = true;
52
53
       for(int i = 1; i <= n; i++) {</pre>
54
           if(valid && visit[i] == -1) {
```

### 5.4 dijkstra

```
1 void dijkstra(int s){
     //set vis[]=0 d[]=inf
 3
     priority_quque<Node>pq;
     d[s]=0;
 5
     p[s]=s;
 6
     pq.push(Node(s,0));
 7
     while(!pq.empty()){
 8
       while(!pq.empty()&&vis[pq.top().p])pq.top();
 9
       if(pq.empty())break;
10
       vis[pq.top().p]=1;
11
       Node k=pq.top(); pq.pop();
12
       for(auto t:v[k.p]){
13
         if(d[k.p]+w[k.p][t]<d[t]){</pre>
14
           d[t]=d[k.p]+w[k.p][t];
15
            p[t]=k.p;
16
           pq.push((Node){t,d[t]})
17
18
       }
19
20
   }
```

#### 5.5 Convex Hull

```
1
   struct loc {
     int x, y;
 2
     loc() {};
 3
 4
     loc(int x, int y): x(x), y(y) {}
 5
     bool operator <(const loc& b)const {return x != b.x ?</pre>
           x < b.x : y < b.y;
 6
     bool operator ==(const loc& b)const {return x == b.x
          && y == b.y;}
 7
     loc operator -(const loc& b)const {return loc(x - b.x
          , y - b.y);}
     int cross(const loc& b)const {return x * b.y - y * b.
 8
         x;}
     int dis(loc a, loc b) {return (x - b.x) * (x - b.x) +
           (y - b.y) * (y - b.y);
10
   };
11
   vector<loc>p, p1;
12
   int n;
13
   void convexhull() {
     sort(p.begin(), p.end());
15
     p.erase(unique(p.begin(), p.end()), p.end());
16
     p1.clear();
17
     p1.resize(p.size());
18
     int m = 0;
19
     for (int i = 0; i < p.size(); i++) {</pre>
20
       while (m > 1 \& (p1[m - 1] - p1[m - 2]).cross(p[i])
            - p1[m - 2]) <= 0)m--;
21
       p1[m++] = p[i];
22
23
     for (int i = p.size() - 2; i >= 0; i--) {
24
25
       while (m > k \&\& (p1[m - 1] - p1[m - 2]).cross(p[i])
            - p1[m - 2]) <= 0)m--;
26
       p1[m++] = p[i];
27
     if (n > 1)m--;
28
29
     p1.resize(m);
30
```

cin >> dis[i][j];

5.6 Dinic

17

```
if(dis[i][j] == 0) dis[i][j] = INF;
                                                               18
                                                               19
1 struct dinic{
                                                               20
     struct Edge{int v,f,re;}; //residual flow
                                                                           for(int i = 0; i < n; i++) {</pre>
                                                               21
3
     int n, s, t, level[M], now[M];
                                                                               for(int j = 0; j < n; j++) {</pre>
                                                               22
     vector<Edge> e[M];
4
                                                                                   if(i == j) continue;
                                                               23
     void init(int _n, int _s, int _t){
                                                               24
                                                                                    ans = min(ans, dis[i][j] + dis[j][i]);
       n = _n; s = _s; t = _t;
                                                                                   for(int k = 0; k < n; k++) {
                                                               25
7
       for (int i = 0; i <= n; i++)e[i].clear();</pre>
                                                                                        dis[i][j] = min(dis[i][j], dis[i][k
                                                               26
8
                                                                                             ] + dis[k][j]);
     void add_edge(int u, int v, int f){
9
                                                               27
10
       e[u].push_back({ v, f, e[v].size() });
                                                               28
                                                                                        ans = min(ans, dis[i][j] + dis[k][i
11
       e[v].push_back({ u, f, e[u].size() - 1 });
                                                                                            ] + dis[j][k]);
12
                                                               29
                                                                                   }
13
     bool bfs(){
                                                                               }
                                                               30
       fill(level, level + n + 1, -1);
14
                                                               31
                                                                           }
15
       queue<int> q;
                                                               32
16
       q.push(s); level[s] = 0;
                                                               33
                                                                           if(ans == INF) cout << -1 << endl;</pre>
17
       while (!q.empty()){
                                                               34
                                                                           else cout << ans << endl;</pre>
18
         int u = q.front(); q.pop();
                                                               35
19
         for (auto it : e[u]){
                                                               36
20
            if (it.f > 0 && level[it.v] == -1){
                                                               37
                                                                      return 0;
21
              level[it.v] = level[u] + 1;
                                                               38 }
22
              q.push(it.v);
23
           }
24
         }
25
                                                                  5.8
                                                                         KM
26
       return level[t] != -1;
27
                                                                1|bool match(int i) {
28
     int dfs(int u, int nf){
                                                                2
                                                                    vx[i] = true;
29
       if (u == t)return nf;
                                                                3
                                                                    for (int j = 1; j <= n; j++) {</pre>
       int res = 0;
30
                                                                      if ((fabs(Lx[i] + Ly[j] - w[i][j]) < 1e-9) && !vy[j</pre>
                                                                4
31
       while (now[u] < e[u].size()){</pre>
         Edge &it = e[u][now[u]];
                                                                           ]) {
32
                                                                        vy[j] = 1;
33
         if (it.f>0 && level[it.v] == level[u] + 1){
           int tf = dfs(it.v, min(nf, it.f));
                                                                6
                                                                         if (!Left[j] || match(Left[j])) {
34
                                                                7
                                                                           Left[j] = i;
35
           res += tf; nf -= tf; it.f -= tf;
                                                                8
                                                                           return true;
36
           e[it.v][it.re].f += tf;
                                                                9
37
           if (nf == 0)return res;
                                                               10
                                                                      }
38
39
                                                               11
         else now[u]++;
                                                               12
                                                                    return false;
40
41
       if (!res)level[u] = -1;
                                                               13
                                                               14
                                                                  void update() {
42
       return res;
                                                                    double a = 1e30;
43
                                                                    for (int i = 1; i <= n; i++) {</pre>
                                                               16
44
     int flow(int res = 0){
                                                               17
                                                                      if (vx[i])for (int j = 1; j <= n; j++) {</pre>
45
       while (bfs()){
                                                               18
                                                                           if (!vy[j])a = min(a, Lx[i] + Ly[j] - w[i][j]);
46
         int temp;
                                                               19
47
         memset(now, 0, sizeof(now));
                                                               20
48
         while (temp = (dfs(s, INF))){
                                                               21
                                                                    for (int i = 1; i <= n; i++) {</pre>
49
           res += temp;
                                                               22
                                                                      if (vx[i])Lx[i] -= a;
50
                                                               23
                                                                      if (vy[i])Ly[i] += a;
51
                                                               24
52
       return res;
                                                               25
53
                                                               26
                                                                  void KM() {//reset lx ly left
54|};
                                                               27
                                                                    for (int i = 1; i <= n; i++) {
                                                               28
                                                                      Left[i] = Lx[i] = Ly[i] = 0;
                                                               29
                                                                      for (int j = 1; j <= n; j++) {</pre>
          FloydWarshall
                                                               30
                                                                        Lx[i] = max(Lx[i], w[i][j]);
                                                               31
                                                                      }
                                                               32
```

```
1 #include <iostream>
3 #define INF 1e9
4 #define LL long long
6 using namespace std;
8 int main() {
9
       int n;
10
11
       while(cin >> n) {
12
            LL dis[n][n];
13
            LL ans = INF;
14
15
            for(int i = 0; i < n; i++)</pre>
                for(int j = 0; j < n; j++) {</pre>
16
```

# 5.9 Longest Common Ancestor

```
1 void preprocess() {
2 for (int i = 1; i <= 25; i++) {</pre>
```

for (int i = 1; i <= n; i++) {</pre>

vx.reset(); vy.reset();

if (match(i))break;

while (1) {

update();

33 34

35

36

37

38 39

40 | }

}

66

```
67 }
 3
       for (int j = 1; j <= n; j++) {</pre>
4
         if (par[j][i - 1] == -1 || par[par[j][i - 1]][i -68
               1] == -1)continue;
                                                               69
                                                                  bool book[S];
         par[j][i] = par[par[j][i - 1]][i - 1];
                                                               70
 6
                                                               71
                                                                  void dfs(int start) {
7
                                                               72
                                                                       stack<int> st;
 8 }
                                                               73
                                                                       st.push(start);
                                                               74
                                                               75
                                                                       memset(book, false, sizeof(book));
                                                               76
   5.10 MST
                                                               77
                                                               78
                                                                       while(!st.empty()) {
1 #include <iostream>
                                                               79
                                                                           int cur = st.top();
 2 #include <vector>
                                                               80
                                                                           // cout << cur << endl;</pre>
3 #include <stack>
                                                               81
                                                                           st.pop();
 4 #include <cstring>
                                                               82
5 #include <algorithm>
                                                               83
                                                                           book[cur] = true;
                                                               84
7 #define LL long long
                                                               85
                                                                           for(int i = 0; i < map[cur].size(); i++) {</pre>
8 #define MAX 1e11
                                                               86
                                                                               int next = map[cur][i].d;
9 #define S 50050
                                                               87
                                                                               if(!book[next]) {
10 using namespace std;
                                                               88
                                                                                    st.push(next);
11
                                                               89
                                                                               }
12 int n, m;
                                                               90
                                                                           }
13 int sum;
                                                               91
                                                                       }
14
                                                               92
                                                                  }
   typedef struct {
15
                                                               93
16
       int a, b, 1;
                                                               94
                                                                  void init() {
17
  } edge;
                                                               95
                                                                      memset(disjoint, -1, sizeof(disjoint));
18 bool cmp(edge l, edge r) { return l.l < r.l; }
                                                               96
                                                                       sum = 0;
19
                                                               97
20 vector<edge> v;
                                                               98
21
                                                               99
                                                                  bool check() {
  typedef struct {
22
                                                              100
                                                                       for(int i = 1; i <= n; i++)</pre>
23
       int d;
                                                              101
                                                                           if(!book[i]) return false;
24
       LL 1;
                                                              102
25 } node;
                                                              103
                                                                       return true;
26
                                                              104
27 vector<node> map[S];
                                                              105
                                                              106
                                                                  int main() {
29 int disjoint[S];
                                                              107
                                                                      init();
30
                                                              108
31
   int root(int x) {
                                                              109
                                                                      cin >> n >> m;
       if(disjoint[x] < 0) return x;</pre>
32
                                                              110
33
                                                                       for(int i = 0; i < m; i++) {</pre>
                                                              111
34
            disjoint[x] = root(disjoint[x]);
                                                              112
                                                                           edge tmp;
35
           return disjoint[x];
                                                              113
                                                                           cin >> tmp.a >> tmp.b >> tmp.l;
36
                                                              114
37 }
                                                              115
                                                                           v.push_back(tmp);
38
                                                              116
                                                                      }
39 bool same(int a, int b) {
                                                              117
40
       return root(a) == root(b);
                                                              118
                                                                       sort(v.begin(), v.end(), cmp);
41
                                                              119
42
                                                              120
                                                                      kruskal();
43
   void connect(int a, int b) {
                                                              121
                                                                       dfs(1);
       // cout << "CONNECT " << a << " " << b << endl;
44
                                                              122
45
       int ra = root(a);
                                                              123
                                                                       if(!check()) cout << -1 << endl;</pre>
       int rb = root(b);
46
                                                              124
                                                                       else cout << sum << endl;</pre>
47
                                                              125
48
       disjoint[ra] += disjoint[rb];
                                                              126
                                                                       return 0;
49
       disjoint[rb] = ra;
                                                              127 }
50|}
51
52
   void kruskal() {
                                                                  5.11 SPFA
53
       int remain = n - 1;
54
       for(auto i : v) {
55
            if(remain == 0) break;
                                                                1 #include <iostream>
                                                                  #include <vector>
56
57
            if(!same(i.a, i.b)) {
                                                                  #include <stack>
58
                connect(i.a, i.b);
                                                                  #include <queue>
59
                                                                5
                                                                  #include <cstring>
60
                map[i.a].push_back((node){i.b, i.l});
                                                                6
61
                map[i.b].push_back((node){i.a, i.l});
                                                                7
                                                                  #define S 50050
62
                                                                8
                                                                  #define MAX 1e11
                                                                9
                                                                  #define LL long long
63
                sum += i.l;
                                                               10
64
                remain--;
65
           }
                                                               11
                                                                  using namespace std;
       }
                                                               12
```

```
13 typedef struct {
                                                               89
                                                                            cin >> a >> b >> c;
       int d;
                                                               90
14
15
       LL 1;
                                                               91
                                                                            map[a].push_back((XXX) {b, c});
16 } XXX;
                                                               92
                                                                       }
                                                               93
17
  vector<XXX> map[S];
                                                               94
18
                                                                       spfa(1);
19
                                                                95
20 LL lon[S];
                                                               96
                                                                       if(lon[n] >= MAX || lon[n] <= -MAX) cout << "QAQ"
21 int cnt[S];
                                                                            << endl;
                                                               97
                                                                       else cout << lon[n] << endl;</pre>
22 int n, m;
23 bool cycle;
                                                               98
24 bool inqueue[S];
                                                               99
                                                                       return 0;
25
                                                              100 }
26 void dfs(int start) {
27
       stack<int> st;
28
       st.push(start);
                                                                   5.12 SumOfDistanceInTree
29
30
       bool book[S];
31
       memset(book, false, sizeof(book));
                                                                1 #include <bits/stdc++.h>
32
                                                                 2 | #pragma comment(linker, "/STACK:10240000,10240000")//递
33
       while(!st.empty()) {
                                                                       归太深,导致爆栈,所以使用扩栈语句
34
           int cur = st.top();
                                                                   using namespace std;
35
           // cout << cur << endl;</pre>
36
           st.pop();
                                                                   const int N = 100009;
37
           lon[cur] = -MAX;
                                                                 6
                                                                   int dp[N] = {}, num[N];
38
           book[cur] = true;
                                                                   vector<int> p[N];
                                                                 7
39
                                                                 8
                                                                   bool f[N] = {};
40
           for(int i = 0; i < map[cur].size(); i++) {</pre>
41
                int next = map[cur][i].d;
                                                                10
                                                                   void dfs(int s, int depth)
42
                if(!book[next]) st.push(next);
                                                               11
43
           }
                                                               12
                                                                       int len = p[s].size();
44
       }
                                                               13
                                                                       f[s] = 1;
45|}
                                                               14
                                                                       num[s] = 1;
46
                                                               15
                                                                       dp[1] += depth;
47
   void spfa(int start) {
48
       memset(inqueue, false, sizeof(inqueue));
                                                               16
                                                                       for(int i=0; i<len; i++)</pre>
                                                               17
49
       for(int i = 0; i < S; i++) lon[i] = MAX;</pre>
                                                               18
                                                                            if(!f[p[s][i]])
50
       cycle = false;
                                                               19
                                                                            {
51
                                                                20
                                                                                dfs(p[s][i], depth+1);
       queue<int> q;
52
                                                               21
                                                                                num[s] += num[p[s][i]];
53
       q.push(start);
                                                                22
                                                                            }
54
       lon[start] = 0;
                                                               23
                                                                       }
55
       inqueue[start] = true;
                                                               24
                                                                   }
56
                                                               25
57
       while(!q.empty()) {
                                                               26
                                                                   void solve(int s, int n)
58
           int cur = q.front();
                                                               27
59
           q.pop();
                                                                28
                                                                       int len = p[s].size();
60
            inqueue[cur] = false;
           // cout << "AT: " << cur << " " << cnt[cur] <<
                                                                       f[s] = 1:
61
                                                                30
                                                                       for(int i=0; i<len; i++)</pre>
                endl:
                                                               31
62
            cnt[cur]++;
                                                                32
                                                                            if(!f[p[s][i]])
63
           if(cnt[cur] > n) {
                                                               33
                dfs(cur);
64
                                                                34
                                                                                dp[p[s][i]] = dp[s]+n-num[p[s][i]]*2;
65
                return ;
                                                                35
                                                                                solve(p[s][i], n);
           }
66
                                                               36
                                                                            }
67
                                                               37
                                                                       }
68
           for(int i = 0; i < map[cur].size(); i++) {</pre>
                                                               38
                int next = map[cur][i].d;
69
70
                                                               40
                                                                   int main()
71
                if(lon[next] > lon[cur] + map[cur][i].1) {
                                                               41
72
                    lon[next] = lon[cur] + map[cur][i].1;
                                                               42
73
                    if(!inqueue[next] && cnt[cur] <= n) {</pre>
                                                                       scanf("%d", &n);
                                                               43
74
                         q.push(next);
                                                               44
                                                                       for(int i=1; i<n; i++)</pre>
75
                         inqueue[next] = true;
                                                               45
76
                    }
                                                                            int a, b;
scanf("%d%d", &a, &b);
                                                               46
77
                }
78
                                                               47
           }
                                                                            p[a].push_back(b);
                                                               48
79
                                                               49
                                                                            p[b].push_back(a);
80|}
                                                               50
81
                                                                51
                                                                       dfs(1, 0);
82
                                                               52
                                                                       memset(f, 0, sizeof(f));
83 int main() {
                                                               53
       cin >> n >> m;
                                                                       solve(1, n);
84
                                                               54
                                                                       for(int i=1; i<=n; i++)</pre>
85
                                                                            printf("%d \setminus n", dp[i]);
                                                               55
86
       for(int i = 0; i < m; i++) {</pre>
                                                               56
                                                                       return 0;
87
           int a, b;
                                                               57 }
           LL c;
88
```

### 5.13 TopologicalSort

```
1 #include <iostream>
 2 #include <stack>
3 #include <vector>
 4 #include <cstring>
6 #define S 50050
8 using namespace std;
10 vector<int> map[S];
11 stack<int> ans;
12 int state[S];
13 bool head[S];
14 bool valid;
15 int n, m;
16
17 void dfs(int cur) {
18
       state[cur] = 1;
19
20
       for(auto next : map[cur])
21
           if(!state[next]) dfs(next);
22
            else if(state[next] == 1) {
                valid = false;
23
24
                return ;
25
           }
26
27
       state[cur] = 2;
28
29
       ans.push(cur);
30|}
31
32
   void topology_sort() {
       for(int i = 1; i <= n; i++)</pre>
33
34
           if(valid && head[i]) dfs(i);
35
36
       if(!valid) {
           cout << -1 << endl;
37
           return ;
38
39
40
41
       while(!ans.empty()) {
42
           cout << ans.top() << endl;</pre>
43
           ans.pop();
44
45 }
46
47 int main() {
48
       cin >> n >> m;
49
50
       memset(head, true, sizeof(head));
51
52
       for(int i = 0; i < m; i++) {</pre>
53
           int a, b;
54
           cin >> a >> b;
55
56
           head[b] = false;
57
58
           map[a].push_back(b);
59
60
61
       memset(state, 0, sizeof(state));
62
       valid = true;
63
64
       topology_sort();
65
       return 0;
66
67 }
```

### 6 Number

#### 6.1 Catalan

```
C_0 = 1 and C_{n+1} = \frac{2(2n+1)}{n+2}C_n,
```

### 6.2 Extend Euclidean.cpp

```
1 int extgcd(int a,int b,int &x,int &y){
2    int d=a;
3    if(b){d=extgcd(b,a%b,y,x),y-=(a/b)*x;}
4    else x=1,y=0;
5    return d;
6 }//ax+by=1 ax同餘 1 mod b
```

#### 6.3 GaussElimination

```
1 const int MAXN = 300;
   const double EPS = 1e-8;
 3 int n;
   double A[MAXN][MAXN];
   void Gauss() {
  for(int i = 0; i < n; i++) {</pre>
 5
        bool ok = 0;
 8
        for(int j = i; j < n; j++) {</pre>
 9
          if(fabs(A[j][i]) > EPS) {
10
            swap(A[j], A[i]);
            ok = 1;
11
12
            break;
13
          }
14
        if(!ok) continue;
15
        double fs = A[i][i];
16
17
        for(int j = i+1; j < n; j++) {</pre>
          double r = A[j][i] / fs;
18
19
          for(int k = i; k < n; k++) {</pre>
            A[j][k] -= A[i][k] * r;
20
21
22
        }
23
     }
24 }
```

#### 6.4 Matrix

```
1 template < typename T, int N=2>
   struct Mat {//Matrix
     unsigned long long v[N][N];
 4
     Mat operator*(Mat b)const {
 5
       Mat val;
 6
       for (int i = 0; i < N; i++) {</pre>
         for (int j = 0; j < N; j++) {
 7
 8
            val.v[i][j] = 0;
           for (int k = 0; k < N; k++) {
9
10
              val.v[i][j] += v[i][k] * b.v[k][j];
11
12
         }
13
       }
14
       return val:
15
16|};
```

#### 6.5 Prime table

```
1 void PrimeTable(){
2    is_notp.reset();
3    is_notp[0] = is_notp[1] = 1;
4    for (int i = 2; i < N; i++){
5        if (is_notp[i])continue;
6        p.push_back(i);</pre>
```

7.3

Zvalue

```
7
        for (int j=0;i*p[j]<N&&j<p.size();j++){</pre>
                                                                 19
                                                                         for(int j=i;j<s.size();j++){</pre>
 8
          is_notp[i*p[j]] = 1;
                                                                 20
                                                                              v=s[j]-'a';
 9
          if(i%p[j]==0)break;
                                                                 21
                                                                              if(!trie[u][v])return;
10
                                                                 22
                                                                              u=trie[u][v];
                                                                 23
11
     }
                                                                              if(val[u])dp[i]=(dp[i]+dp[j+1])%MOD;
12 }
                                                                 24
                                                                 25
                                                                         return;
                                                                 26 }
```

# 7 String

#### 7.1 KMP

```
void z_value(){
                                                                2
                                                                    int lens = s.size(), l = 0, r = 0;
1 void bulid_fail_funtion(string B, int *fail){
                                                                3
                                                                    z[0] = 0;
     int len = B.length(), current_pos;
                                                                    for (int i = 1; i < lens; i++){</pre>
                                                                4
     current_pos = fail[0] = -1;
                                                                      if (i>r)z[i] = 0;
4
     for (int i = 1; i<len; i++){</pre>
                                                                      else{
       while (current_pos != -1 && B[current_pos + 1] != B
5
                                                                        int ip = i - 1;
           [i]){
                                                                8
                                                                        if (ip + z[ip] < z[l])z[i] = z[ip];</pre>
         current_pos = fail[current_pos];
6
                                                                        else z[i] = r - l + 1;
                                                                9
7
                                                               10
       if (B[current_pos + 1] == B[i])current_pos++;
8
                                                               11
                                                                      while (i + z[i] < lens\&&s[i + z[i]] == s[z[i]])z[i]
9
       fail[i] = current_pos;
                                                                          ]++;
10
                                                               12
                                                                      if (i + z[i] - 1 > r){
11|}
                                                                        l = i;
                                                               13
  void match(string A, string B, int *fail){
12
                                                               14
                                                                        r = 1 + z[i] - 1;
13
     int lenA = A.length(), lenB = B.length();
                                                               15
     int current_pos = -1;
14
                                                               16
                                                                    }
15
     for (int i = 0; i<lenA; i++){</pre>
       while (current_pos != -1 && B[current_pos + 1] != A<sup>17</sup>|}
16
            [i]){
17
         current_pos = fail[current_pos];
18
19
       if (B[current_pos + 1] == A[i])current_pos++;
20
       if (current_pos == lenB - 1){//match! A[i-lenB+1,i
           1=B
21
         current_pos = fail[current_pos];
22
23
     }
24 }
25 int main(){
26
     int t, i;
27
     string s;
     for (i = 0, cin >> t; i<t; i++){
28
29
       cin >> s;
30
       int fail[N];
       bulid_fail_funtion(s, fail);
31
32
       int p = s.length() - 1;
33
       if (fail[p] != -1 && (p + 1) % (p - fail[p]) == 0)
            printf("%d \ n", p - fail[p]);
34
       else printf("%d \setminus n", p + 1);
35
36 }
```

### 7.2 Trie

```
1 //init sz=1 trie[0]=0
 2
   void insert(string s){
 3
       int u=0,v;
       for(int i=0;i<r.size();i++){</pre>
 5
           v=r[i]-'a';
 6
           if(!trie[u][v]){
 7
                memset(trie[sz],0,sizeof(trie[sz]));
 8
                val[sz]=0:
 9
                trie[u][v]=sz++;
10
           }
11
           u=trie[u][v];
12
13
       val[u]=1;
14
       return;
15|}
16
  void search(string s,int i){
17
       int u=0,v;
18
       dp[i]=0;
```