## DS5230/DS4420 Unsupervised Machine Learning and Data Mining – Fall 2018 – Homework 3

## Submission Instructions

- It is recommended that you complete this exercises in **Python 3** and submit your solutions as a **Jupyter notebook**.
- You may use any other language, as long as you **include a README** with simple, clear instructions on how to run (and if necessary compile) your code.
- Please upload all files (code, README, written answers, etc.) to **blackboard** in a single **zip file** named { firstname}\_{lastname}\_DS5230/DS4220\_HW3.zip.

## Exercise 1: Understanding clustering algorithms (40pts)

1. (10pts) Consider density-based clustering algorithm DBSCAN with parameters  $\epsilon = \sqrt{2}, MinPts = 3$ , and Euclidean distance measures. Given the following points:

$$([0,1],[5,2],[2,3],[6,1],[10,2],[0,6],[3,4],[6,3],[0,7],[7,2],[1,2])$$

- (a) List the clusters in terms of their points.
- (b) What are the density-connected points?
- (c) What points (if any) does DBSCAN consider as noise?
- 2. (15pts) Given two clusters

$$C_1 = \{(5,6), (8,7), (7,3)\}$$
  $C_2 = \{(6,5), (4,5), (9,2), (3,5), (8,4)\}$ 

compute the values in (a) - (f). Use the definition for scattering criteria presented in class. Note that tr in the scattering criterion is referring to the trace of the matrix.

- (a) The mean vectors  $m_1$  and  $m_2$
- (b) The total mean vector m
- (c) The scatter matrices  $S_1$  and  $S_2$
- (d) The within-cluster scatter matrix  $S_W$
- (e) The between-cluster scatter matrix  $S_B$

- (f) The scatter criterion  $\frac{tr(S_B)}{tr(S_W)}$
- 3. (15pts) Present three graphs (drawn by-hand is fine) illustrating cases where agglomerative hierarchical clustering would produce different results, depending on the distance metrics used. In particular consider the following distances: Minimum, Maximum, and Average.

## Exercise 2: Implementing and Comparing Clustering Algorithms (60pts)

In this section, you will implement 2 algorithms: K-means, and DBSCAN. You will then use these algorithms to compare clustering on 3 datasets, dataset1.txt, dataset2.txt, and dataset3.txt. Each dataset contains two columns of features and a third column with labels.

To evaluate your clustering results, consider 3 different metrics:

• The normalized mutual information (NMI)

$$NMI(Y; Z) = \frac{I(Y; Z)}{\sqrt{H(Y)H(Y)}}$$

scikit-learn: scklearn.metrics.normalized\_mutual\_info\_score

- The Calinski-Harabaz (CH) index  $tr(S_B)/tr(S_W)$ . scikit-learn: sklearn.metrics.calinski\_harabaz\_score
- The Silhouette coefficient (SC) (see attached note).

  scikit-learn: sklearn.metrics.calinski\_harabaz\_score
- 4. (25pts) Implement the DBSCAN algorithm. Run the algorithm with the following Eps and MinPts values

 $\begin{aligned} &\texttt{dataset1.txt:} \ Eps \in \{0.2, 0.3, 0.4\}, \ MinPts \in \{2, 3, 4\} \\ &\texttt{dataset2.txt:} \ Eps \in \{0.8, 0.85, 0.9\}, \ MinPts \in \{6, 7, 8\} \\ &\texttt{dataset3.txt:} \ Eps \in \{0.2, 0.3, 0.4\}, \ MinPts \in \{5, 6, 7\} \end{aligned}$ 

Report the following information

• Make tables for the NMI, CH index and SC values as a function of *Eps* and *MinPts*.

- For the best result (based on NMI) make a scatter plot in which different shapes are used to show the true label, and different colors represent the learned cluster assignments. Noise points should be given a special color.
- 5. (25pts) Implement K-means. Your implementation should perform multiple random initializations and keep the best result. Make sure that your code does not crash when one of your initializations results in an empty cluster. Finally, make sure that your implementation accepts the initial value of means as an input. We will check your implementation against a set of predetermined initializations.
  - For each dataset, plot the sum of squared errors (SSE), the CH index, the SC, and the NMI for the best restart (based on SSE) as a function of the number of clusters K = 1, 2, 3, 4, 5. For each K value, again include a scatter plot, in which different symbols are used to signify each label, and different colors represent the learned cluster assignments.
- 6. (10pts) From above implementations, you may see different models perform differently on these three datasets:
  - Which model performs best on dataset1, dataset2 and dataset3? Can you explain why?