



4. 解:

(1)

设  $z_1 = x_1 + x_2 + x_3, z_2 = x_4 + x_5 + x_6$ , 则  $z_1, z_2 \sim N(0, 3)$  且  $z_1, z_2$  相互独立。

故,

$$Y = z_1^2 + z_2^2, CY = (\sqrt{C}z_1)^2 + (\sqrt{C}z_2)^2$$

令  $CY \sim \chi^2$ , 则,

$$\begin{aligned}\sqrt{C}z_1, \sqrt{C}z_2 &\sim N(0, 1) \\ C &= \pm \frac{1}{3}\end{aligned}$$