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## 1 Basic

1	1.1 vimrc	
2	1	set nocompatible
2	2	filetype plugin indent on
2	3	set t_Co=256
2	4	set term=screen-256color
2	5	set number
2	6	set tabstop=4
3	7	set shiftwidth=4
3	8	set softtabstop=4
3	9	set expandtab
3	10	set wrap
4	11	set showcmd
4	12	colorscheme darkblue
4	13	map <F2> :w <CR> :call OP() <CR>
4	14	map! <F2> <ESC> :w <CR> :call OP() <CR> <ESC>
5	15	map <F9> :w <CR> :call CP_R() <CR> <ESC>
5	16	map! <F9> <ESC> :w <CR> :call CP_R() <CR> <ESC>
5	17	map <HOME> ^
6	18	map! <HOME> <ESC>^i
6	19	map <ESC>OH <HOME>
7	20	map! <ESC>OH <HOME>
7	21	map <END> \$
7	22	map <ESC>OF <END>
23	23	map! <ESC>OF <ESC><END>a
7	24	function CP_R()
7	25	
8	26	if( &ft == 'cpp')
8	27	let cpl = 'g++ -w -o "%:r.exe" -std=c++11 "%"
9	28	let exc = '"./%:r.exe"'
9	29	elseif( &ft == 'python')
9	30	let exc = 'python "%"'
11	31	endif
11	32	let pause = 'printf "Press any key to continue..." &&
11	33	read -n 1 && exit'
12	34	if !exists('exc')
13	35	echo 'Can't compile this filetype...'
13	36	return
13	37	endif
13	38	if exists('cpl')
14	39	let cp_r = cpl . ' && time ' . exc
14	40	else
14	41	let cp_r = 'time ' . exc
14	42	endif
15	43	execute '! clear && ' . cp_r . ' && ' . pause
15	44	endfunction
16	45	function OP()
16	46	execute '! \$COLORTERM -x gedit ' . "%" . ";"
16	47	endfunction

## 2 Number

### 2.1 Extended GCD

```

1 ll ext_gcd(ll a, ll b, ll &x, ll &y){
2     ll d=a;
3     if(b!=0ll){
4         d=ext_gcd(b, a%b, y, x);
5         y--=(a/b)*x;
6     }
7     else x=1ll, y=0ll;
8     return d;
9 }

```

### 2.2 Modular Inverse

```

1 /*
2  * find the inverse of n modular p
3  */
4 ll mod_inverse(ll n, ll p){
5     ll x, y;
6     ll d = ext_gcd(n, p, x, y);
7     return (p+x%p) % p;
8 }

```

### 2.3 Line Modular Equation

```

1 /*
2  * ax = b (mod n)
3  * return a set of answer(vector<ll>)
4  */
5 vector<ll> line_mod_equation(ll a, ll b, ll n){
6     ll x, y, d;
7     d = ext_gcd(a, n, x, y);
8     vector<ll> ans;
9     if(b%d==0ll){
10        x = (x%n + n) % n;
11        ans.push_back((x*(b/d))%(n/d));
12        for(ll i=1; i<d; i++){
13            ans.push_back((ans[0]+i*n/d)%n);
14        }
15        return ans;
16 }

```

### 2.4 Chinese Remainder Theorem

```

1 /*
2  * solve the chinese remainder theorem(CRT)
3  * if a.size() != m.size(), return -1
4  * return the minimum positive answer of CRT
5  * x = a[i] (mod m[i])
6  */
7 int CRT(vector<int> a, vector<int> m) {
8     if(a.size() != m.size()) return -1;
9     int M = 1;
10    for(int i=0; i<(int)m.size(); i++)
11        M *= m[i];
12    int res = 0;
13    for(int i=0; i<(int)a.size(); i++)
14        res = (res + (M/m[i])*mod_inverse(M/m[i], m[i])
15            *a[i]) % M;
16    return (res + M) % M;
17 }

```

### 2.5 C(N,M)

```

1 /* P is the modular number */
2 #define P 24851
3 int fact[P+1];
4 /* called by Cmod */
5 int mod_fact(int n, int &e){
6     e = 0;
7     if(n == 0) return 1;
8     int res = mod_fact(n/P, e);
9     e += n / P;
10    if((n/P) % 2 == 0)

```

```

11        return res * (fact[n%P]%P);
12    return res * ((P-fact[n%P])%P);
13 }
14 /*
15  * return C(n, m) mod P
16  */
17 int Cmod(int n, int m){
18     /* this section only need to be done once */
19     fact[0] = 1;
20     for(int i=1; i<=P; i++){
21         fact[i] = fact[i-1] * i%P;
22     }
23     /* end */
24     int a1, a2, a3, e1, e2, e3;
25     a1 = mod_fact(n, e1);
26     a2 = mod_fact(m, e2);
27     a3 = mod_fact(n-m, e3);
28     if(e1 > e2 + e3) return 0;
29     return a1 * mod_inverse(a2 * (a3%P), P) % P;
30 }

```

### 2.6 Phi

```

1 /*
2  * gen phi from 1~MAXN
3  * store answer in phi
4  */
5 #define MAXN 100
6 int mindiv[MAXN], phi[MAXN];
7 void genphi(){
8     for(int i=1; i<MAXN; i++){
9         mindiv[i] = i;
10        for(int i=2; i*i<MAXN; i++){
11            if(mindiv[i] == i)
12                for(int j=i*i; j<MAXN; j+=i)
13                    mindiv[j] = i;
14        }
15        phi[1] = 1;
16        for(int i=2; i<MAXN; i++){
17            phi[i] = phi[i/mindiv[i]];
18            if((i/mindiv[i])%mindiv[i] == 0)
19                phi[i] *= mindiv[i];
20            else phi[i] *= (mindiv[i]-1);
21        }
22 }

```

### 2.7 Miller Rabin

```

1 ll pow_mod(ll x, ll N, ll M) {
2     ll res = 1;
3     x %= M;
4     while(N){
5         if(N&1ll) res = mul_mod(res, x, M);
6         x = mul_mod(x, x, M);
7         N >>= 1;
8     }
9     return res;
10 }
11 bool PrimeTest(ll n, ll a, ll d) {
12     if(n == 2 || n == a) return true;
13     if((n&1) == 0) return false;
14     while((d&1) == 0) d >>= 1;
15     ll t = pow_mod(a, d, n);
16     while((d!=n-1) && (t!=1) && (t!=n-1)){
17         t = mul_mod(t, t, n);
18         d <<= 1;
19     }
20     return (t==n-1) || ((d&1)==1);
21 }
22 bool MillerRabin(ll n){
23     // test set
24     vector<ll> a = {2, 325, 9375, 28178, 450775,
25         9780504, 1795265022};
26     for(int i=0; i<(int)a.size(); i++)
27         if(!PrimeTest(n, a[i], n-1)) return false;
28     return true;
29 }

```

## 2.8 FFT

```

1  /*
2  * called by FFT
3  * build the sequence of a that used to calculate FFT
4  * return a reversed sequence
5  */
6  vector<Complex> reverse(vector<Complex> a){
7      vector<Complex> res(a);
8      for (int i=1,j=0;i<(int)res.size();i++){
9          for(int k=((int)res.size())>>1;!(j^=k)&k;k
10             >>=1);
11             if(i > j) swap(res[i], res[j]);
12         }
13     }
14     /*
15     * calculate the FFT of sequence
16     * a.size() must be 2^k
17     * flag = 1 -> FFT(a)
18     * falg = -1 -> FFT-1(a)
19     * return FFT(a) or FFT-1(a)
20     */
21     vector<Complex> FFT(vector<Complex> a, int flag=1){
22         vector<Complex> res = reverse(a);
23         for(int k=2;k<=(int)res.size();k<=1){
24             double p0 = -pi / (k>>1) * flag;
25             Complex unit_p0(cos(p0), sin(p0));
26             for(int j=0;j<(int)res.size();j+=k){
27                 Complex unit(1.0, 0.0);
28                 for(int i=j;i<j+k/2;i++,unit*=unit_p0){
29                     Complex t1 = res[i], t2 = res[i+k/2] *
30                         unit;
31                     res[i] = t1 + t2;
32                     res[i+k/2] = t1 - t2;
33                 }
34             }
35         }
36     }

```

## 2.9 Function

```

1  /*
2  * class of polynomial function
3  * coef is the coefficient
4  * f(x) = sigma(c[i]*x^i)
5  */
6  class Function {
7  public:
8      vector<double> coef;
9      Function(const vector<double> c=vector<double>()):
10         coef(c){}
11     double operator () (const double &rhs) const {
12         double res = 0.0;
13         double e = 1.0;
14         for(int i=0;i<(int)coef.size();i++,e*=rhs)
15             res += e * coef[i];
16         return res;
17     }
18     Function derivative() const {
19         vector<double> dc((int)this->coef.size()-1);
20         for(int i=0;i<(int)dc.size();i++)
21             dc[i] = coef[i+1] * (i+1);
22         return Function(dc);
23     }
24     int degree() const {
25         return (int)coef.size()-1;
26     }
27     /*
28     * calculate the integration of f(x) from a to b
29     * divided into n piece
30     * the bigger the n is, the more accurate the answer is
31     */
32     template<class T>
33     double simpson(const T &f, double a, double b){

```

```

34     double c = (a+b) / 2.0;
35     return (f(a)+4.0*f(c)+f(b)) * (b-a) / 6.0;
36 }
37 template<class T>
38 double simpson(const T &f, double a, double b, double
39     eps, double A){
40     double c = (a+b) / 2.0;
41     double L = simpson(f, a, c), R = simpson(f, c, b);
42     if(fabs(A-L-R) <= 15.0*eps) return L + R + (A-L-R)
43         / 15.0;
44     return simpson(f, a, c, eps/2, L) + simpson(f, c, b
45         , eps/2, R);
46 }
47 template<class T>
48 double simpson(const T &f, double a, double b, double
49     eps){
50     return simpson(f, a, b, eps, simpson(f, a, b));
51 }

```

## 2.10 Equation

```

1  /*
2  * called by find
3  * 1 = positive, -1 = negative, 0 = zero
4  */
5  int sign(double x){
6      return x < -EPS ? -1 : x > EPS;
7  }
8  /* called by equation */
9  template<class T>
10 double find(const T &f, double lo, double hi){
11     int sign_lo, sign_hi;
12     if((sign_lo=sign(f(lo))) == 0) return lo;
13     if((sign_hi=sign(f(hi))) == 0) return hi;
14     if(sign_lo * sign_hi > 0) return INF;
15     while(hi-lo>EPS){
16         double m = (hi+lo) / 2;
17         int sign_mid = sign(f(m));
18         if(sign_mid == 0) return m;
19         if(sign_lo * sign_mid < 0)
20             hi = m;
21         else lo = m;
22     }
23     return (lo+hi) / 2;
24 }
25 /*
26 * return a set of answer of f(x) = 0
27 */
28 template<class T>
29 vector<double> equation(const T &f){
30     vector<double> res;
31     if(f.degree() == 1){
32         if(sign(f.coef[1]))res.push_back(-f.coef[0]/f.
33             coef[1]);
34         return res;
35     }
36     vector<double> droot = equation(f.derivative());
37     droot.insert(droot.begin(), -INF);
38     droot.push_back(INF);
39     for(int i=0;i<(int)droot.size()-1;i++){
40         double tmp = find(f, droot[i], droot[i+1]);
41         if(tmp < INF) res.push_back(tmp);
42     }
43     return res;
44 }

```

## 2.11 Permutation

```

1  /*
2  * return the sequence of x-th of n!
3  * max(n) = 12
4  * 0 of 3! -> 123
5  * 5 of 3! -> 321
6  */
7  int factorial[] = {1, 1, 2, 6, 24, 120, 720, 5040,
8  40320, 362880, 3628800, 39916800, 479001600};
9  vector<int> idx2permutation(int x, int n){

```

```

9   vector<bool> used(n+1, false);
10  vector<int> res(n);
11  for(int i=0;i<n;i++){
12      int tmp = x / factorial[n-i-1];
13      int j;
14      for(j=1;j<=n;j++){if(!used[j]){
15          if(tmp == 0) break;
16          tmp--;
17      }
18      res[i] = j, used[j] = true;
19      x %= factorial[n-i-1];
20  }
21  return res;
22 }
23 /*
24  * a is x-th og n!
25  * return x(0~n!)
26  * 123 of 3! -> 0
27  * 321 of 3! -> 5
28  */
29 int permutation2idx(vector<int> a){
30     int res = 0;
31     for(int i=0;i<(int)a.size();i++){
32         int tmp = a[i] - 1;
33         for(int j=0;j<i;j++){
34             if(a[j] < a[i]) tmp--;
35         }
36         res += factorial[(int)a.size()-i-1] * tmp;
37     }
38     return res;
39 }

```

## 3 Matrix

### 3.1 Guass Elimination

```

1  /*
2  * return guass eliminated matrix
3  * r will be changed to the number of the non-free
   variables
4  * l[i] will be set to true if i-th variable is not
   free
5  * ignore flag
6  */
7  Matrix GuassElimination(int &r, vector<bool> &l, int
   flag=0) {
8      l = vector<bool>(C);
9      r = 0;
10     Matrix res(*this);
11     for(int i=0;i<res.C-flag;i++){
12         for(int j=r;j<res.R;j++){
13             if(fabs(res.at(j, i)) > EPS){
14                 swap(res.D[r], res.D[j]);
15                 break;
16             }
17         }
18         if(fabs(res.at(r, i)) < EPS){
19             continue;
20         }
21         for(int j=0;j<res.R;j++){
22             if(j != r && fabs(res.at(j, i)) > EPS){
23                 double tmp = (double)res.at(j, i) / (
24                     double)res.at(r, i);
25                 for(int k=0;k<res.C;k++){
26                     res.at(j, k) -= tmp * res.at(r, k);
27                 }
28             }
29             r++;
30             l[i] = true;
31         }
32     }
33     return res;
34 }

```

### 3.2 Solve Matrix (Ax=B)

```

1  /*
2  * Ax = b
3  * it will return the answer(x)
4  * if row != column or there is any free variable, it
   will return an empty vector
5  */
6  vector<double> Solve(vector<double> a) {
7      if(R != C) return vector<double>();
8      vector<double> res(R);
9      Matrix t(R, C+1);
10     for(int i=0;i<R;i++){
11         for(int j=0;j<C;j++){
12             t.at(i, j) = a[i];
13         }
14         t.at(i, C) = a[i];
15     }
16     int r = 0;
17     vector<bool> l;
18     t = t.GuassElimination(r, l, 1);
19     if(r != R) return vector<double>();
20     for(int i=0;i<C;i++){
21         if(l[i])for(int j=0;j<R;j++){
22             if(fabs(t.at(j, i)) > EPS)
23                 res[i] = t.at(j, C) / t.at(j, i);
24         }
25     }
26     return res;
27 }

```

### 3.3 Inverse Matrix

```

1  /*
2  * return an inverse matrix

```

```

3  * if row != column or the inverse matrix doesn't exist
4  , it will return an empty matrix
5  */
6  Matrix Inverse() {
7      if(R != C) return Matrix();
8      Matrix t(R, R*2);
9      for(int i=0;i<R;i++){
10         for(int j=0;j<C;j++){
11             t.at(i, j) = at(i, j);
12             t.at(i, i+R) = 1;
13         }
14         int r = 0;
15         vector<bool> l;
16         t = t.GuassElimination(r, l, R);
17         if(r != R) return Matrix();
18         for(int i=0;i<C;i++){
19             if(l[i])for(int j=0;j<R;j++){
20                 if(fabs(t.at(j, i)) > EPS){
21                     for(int k=0;k<C;k++){
22                         t.at(j, C+k) /= t.at(j, i);
23                     }
24                 }
25             }
26             Matrix res(R, C);
27             for(int i=0;i<R;i++){
28                 for(int j=0;j<C;j++){
29                     res.at(i, j) = t.at(i, j+C);
30                 }
31             }
32         }
33     }
34 }

```

## 4 Graph

### 4.1 Bridge And Cut

```

1  /* called by cut_bridge */
2  void _cut_bridge(int x, int f, int d){
3      vis[x] = 1;
4      dfn[x] = low[x] = d;
5      int children = 0;
6      for(int i=0;i<(int)vc[x].size();i++){
7          Edge e = vc[x][i];
8          if(e.to != f && vis[e.to] == 1)
9              low[x] = min(low[x], dfn[e.to]);
10         if(vis[e.to] == 0){
11             _cut_bridge(e.to, x, d+1);
12             children++;
13             low[x] = min(low[x], low[e.to]);
14             if((f == -1 && children > 1) || (f != -1 &&
15                 low[e.to] >= dfn[x]))
16                 cut[x] = true;
17             if(low[e.to] > dfn[x])
18                 bridge[x][e.to] = bridge[e.to][x] =
19                     true;
20         }
21     }
22 }
23 /*
24  * solve the cut and bridge
25  * store answer in cut(vector<bool>) ans bridge(vector<
26  * vector<bool> >)
27  * cut[i] == true iff i-th node is cut
28  * bridge[i][j] == true iff edge between i-th ans j-th
29  * is bridge
30  */
31 void cut_bridge(){
32     vis = vector<int>(N+1, 0);
33     dfn = low = vector<int>(N+1);
34     cut = vector<bool>(N+1);
35     bridge = vector<vector<bool>>(N+1, vector<bool>(N
36         +1, false));
37     for(int i=0;i<N;i++){
38         if(!vis[i])
39             _cut_bridge(i, -1, 0);
40     }
41 }

```

### 4.2 BCC

```

1  /* called by BCC */
2  void _BBC(int x, int d){
3      stk[++top] = x;
4      dfn[x] = low[x] = d;
5      for(int i=0;i<(int)vc[x].size();i++){
6          Edge e = vc[x][i];
7          if(dfn[e.to] == -1){
8              _BBC(e.to, d+1);
9              if(low[e.to] >= dfn[x]){
10                 vector<int> l;
11                 do{
12                     l.push_back(stk[top]);
13                     top--;
14                 }while(stk[top+1] != e.to);
15                 l.push_back(x);
16                 bcc.push_back(l);
17             }
18             low[x] = min(low[x], low[e.to]);
19             }else low[x] = min(low[x], dfn[e.to]);
20         }
21     }
22 }
23 /*
24  * solve the biconnected components(BCC)
25  * store answer in bcc(vector<vector<int> >)
26  * bcc.size() is the number of BCC
27  * bcc[i] is the sequence of a BCC
28  */
29 void BCC(){
30     dfn = low = vector<int>(N+1, -1);

```

```

30     bcc = vector<vector<int>> >();
31     stk = vector<int>(N+1, -1);
32     top = -1;
33     for(int i=0; i<N; i++){
34         if(dfn[i] == -1)
35             _BBC(i, 0);
36     }

```

### 4.3 SCC

```

1  /* called by SCC */
2  void _SCC(int x, int d){
3      stk[++top] = x;
4      dfn[x] = low[x] = d;
5      vis[x] = 1;
6      for(int i=0; i<(int)vc[x].size(); i++){
7          Edge e = vc[x][i];
8          if(dfn[e.to] != -1){
9              if(vis[e.to] == 1)
10                 low[x] = min(low[x], dfn[e.to]);
11             }else{
12                 _SCC(e.to, d+1);
13                 low[x] = min(low[x], low[e.to]);
14             }
15         }
16         if(low[x] == dfn[x]){
17             while(stk[top] != x){
18                 scc[stk[top]] = scc_cnt;
19                 vis[stk[top]] = 2;
20                 top--;
21             }
22             scc[stk[top]] = scc_cnt++;
23             vis[stk[top]] = 2;
24             top--;
25         }
26     }
27     /*
28     * solve the strongly connected component(SCC)
29     * store answer in scc(vector<int>)
30     * the value of scc[i] means the id of the SCC which i-
31       th node in (id is based 0)
32     * scc_cnt id the number of SCC
33     */
34     void SCC(){
35         dfn = low = vector<int>(N+1, -1);
36         vis = vector<int>(N+1, 0);
37         scc = vector<int>(N+1, 0);
38         scc_cnt = 0;
39         stk = vector<int>(N+1, -1);
40         top = -1;
41         for(int i=0; i<N; i++){
42             if(dfn[i] == -1)
43                 _SCC(i, 0);
44         }

```

### 4.4 Two Sat

```

1  /*
2  * called by TwoSat
3  * get the value of i-th
4  * 1 = true, 0 = false, -1 = undefined
5  */
6  int TwoSatGet(int x){
7      int r = x > N/2 ? x-N/2 : x;
8      if(twosatans[r] == -1)
9          return -1;
10     return x > N/2 ? !twosatans[r] : twosatans[r];
11 }
12 /*
13 * solve the 2SAT
14 * return true if there exists a set of answer
15 * store the answer in twosatans
16 */
17 bool TwoSat(){
18     SCC();
19     twosatans = vector<int>(N/2+1, -1);
20     for(int i=0; i<N/2; i++)

```

```

21     if(scc[i] == scc[i+N/2])
22         return false;
23     vector<vector<int>> > c(scc_cnt+1);
24     for(int i=0; i<N; i++){
25         c[scc[i]].push_back(i);
26     }
27     for(int i=0; i<scc_cnt; i++){
28         int val = 1;
29         for(int j=0; j<(int)c[i].size(); j++){
30             int x = c[i][j];
31             if(TwoSatGet(x) == 0)
32                 val = 0;
33             for(int k=0; k<(int)vc[x].size(); k++){
34                 if(TwoSatGet(vc[x][k].to) == 0)
35                     val = 0;
36             }
37             if(!val)
38                 break;
39         }
40         for(int j=0; j<(int)c[i].size(); j++){
41             if(c[i][j] > N/2)
42                 twosatans[c[i][j]-N/2] = !val;
43             else
44                 twosatans[c[i][j]] = val;
45         }
46     }
47     return true;

```

## 5 Path

### 5.1 Kth Shortest

```

1 int KthShortestPath(int s, int t, int k){
2     Graph RG(N);
3     for(int i=0;i<N;i++){
4         for(int j=0;j<(int)vc[i].size();j++){
5             Edge e = vc[i][j];
6             RG.add_edge(e.to, Edge(i, e.w));
7         }
8     }
9     RG.AllDijkstra(t);
10    dis = RG.dis;
11    priority_queue<PI> pq;
12    pq.push(PI(-dis[s], s));
13    while(!pq.empty()){
14        PI v = pq.top();
15        pq.pop();
16        int real = -v.FF - dis[v.SS];
17        if(v.SS == t && (!--k))
18            return real;
19        for(int i=0;i<(int)vc[v.SS].size();i++){
20            Edge e = vc[v.SS][i];
21            pq.push(PI(-(real+e.w+dis[e.to]), e.to));
22        }
23    }
24    return -1;
}

```

### 5.2 EulerCircuit

```

1 #define eid w
2 void _EulerCircuit(int x){
3     for(int i=0;i<(int)vc[x].size();i++){
4         Edge e = vc[x][i];
5         if(vis[e.eid]) continue;
6         vis[e.eid] = 1;
7         _EulerCircuit(e.to);
8         eulercircuit.push_back(e.eid);
9     }
10 }
11 bool EulerCircuit(){ // undirected
12     if(!Connected()) return false;
13     vis = vector<int>(M+1, 0);
14     for(int i=0;i<N;i++){
15         if(vc[i].size()&1)
16             return false;
17         //sort
18         sort(vc[i].begin(), vc[i].end());
19     }
20     eulercircuit.clear();
21     _EulerCircuit(0);
22     //sort
23     reverse(eulercircuit.begin(), eulercircuit.end());
24     return true;
25 }

```

## 6 Flow

### 6.1 Dinic

```

1 /*
2  * Maximum Flow Dinic
3  * Solve() returns answer
4  */
5 class Dinic{
6 public:
7     class Edge{
8     public:
9         int v1, v2, f, c;
10        Edge(int _v1=0, int _v2=0, int _f=0, int _c=0):
11            v1(_v1), v2(_v2), f(_f), c(_c){}
12    };
13    int N;
14    vector<vector<int>> >vc;
15    vector<Edge> E;
16    vector<int> dep;
17
18    Dinic(int n=0): N(n), vc(vector<vector<int>>(N+1))
19        , dep(vector<int>(N+1)) {}
20    void add_edge(int a, int b, int c){
21        vc[a].push_back(E.size());
22        E.push_back(Edge(a, b, c, c));
23        vc[b].push_back(E.size());
24        E.push_back(Edge(b, a, 0, c));
25    }
26    int Bfs(int s, int t){
27        fill(dep.begin(), dep.end(), -1);
28        dep[s] = 0;
29        queue<int> q;
30        q.push(s);
31        while(!q.empty()){
32            int v = q.front(); q.pop();
33            for(int i=0;i<(int)vc[v].size();i++){
34                Edge e = E[vc[v][i]];
35                if(e.f > 0 && dep[e.v2] == -1){
36                    dep[e.v2] = dep[v] + 1;
37                    q.push(e.v2);
38                }
39            }
40        }
41        return dep[t];
42    }
43    int Dfs(int x, int df, int t){
44        if(x == t) return df;
45        int res = 0;
46        for(int i=0;i<(int)vc[x].size();i++){
47            Edge &e = E[vc[x][i]];
48            if(e.f > 0 && dep[e.v2] == dep[x] + 1){
49                int f = Dfs(e.v2, min(df, e.f), t);
50                e.f -= f;
51                E[vc[x][i]^1].f += f;
52                df -= f;
53                res += f;
54            }
55        }
56        return res;
57    }
58    int Solve(int s, int t){
59        int flow = 0;
60        while(Bfs(s, t) != -1){
61            flow += Dfs(s, 0x3f3f3f3f, t);
62        }
63        return flow;
64    }
65 };

```

### 6.2 StoerWanger

```

1 /*
2  * Stoer Wanger
3  * Undirected Min Cut
4  * Solve() returns answer if graph is connected else 0
5  */

```

```

6 class StoerWanger{
7 public:
8     int N, wN;
9     vector<vector<int>> >G;
10    vector<int> bln, dis;
11    StoerWanger(int n=0): N(n), G(vector<vector<int>> >(
12        N, vector<int>(N))), bln(vector<int>(N, -1)),
13        dis(vector<int>(N)) {}
14    void add_edge(int a, int b, int c){
15        G[a][b] += c;
16        G[b][a] += c;
17    }
18    int Mst(int r, int &x, int &y){
19        int t;
20        bln[t=0] = r;
21        for(int i=0;i<wN;i++){
22            if(bln[i] != r)
23                dis[i] = G[0][i];
24        }
25        for(int k=0;k<wN-1;k++){
26            x = t; t = 0;
27            for(int i=0;i<wN;i++){
28                if(bln[i] != r && (!t || dis[i] > dis[t
29                    ]))
30                    t = i;
31            }
32            bln[t] = r;
33            for(int i=0;i<wN;i++){
34                if(bln[i] != r)
35                    dis[i] += G[t][i];
36            }
37            y = t;
38            return dis[t];
39        }
40    }
41    void Merge(int x, int y){
42        if(x > y) swap(x, y);
43        for(int i=0;i<wN;i++){
44            if(i != x && i != y)
45                G[i][x] += G[i][y], G[x][i] += G[y][i];
46        }
47        if(y == wN-1) return;
48        for(int i=0;i<wN-1;i++){
49            if(i != y)
50                swap(G[i][y], G[i][wN-1]), swap(G[y][i
51                    ], G[wN-1][i]);
52        }
53    }
54    int Solve(){
55        wN = N;
56        int res = 0x3f3f3f3f;
57        for(int i=0;wN>1;i++, wN--){
58            int x, y;
59            res = min(res, Mst(i, x, y));
60            Merge(x, y);
61        }
62        return res;
63    }
64 };

```

### 6.3 Mixed Euler

```

1 /*
2  * Mixed Euler
3  * Solve() returns if there is a euler circuit or not
4  */
5 class MEuler{
6 public:
7     class Edge{
8     #define DIRECTED 1
9     #define UNDIRECTED 0
10    public:
11        int to, dir;
12        Edge(int t=0, int d=0): to(t), dir(d){}
13    };
14    int N;
15    Dinic dinic;
16    vector<int> deg;
17    vector<vector<Edge>> > vc;
18
19    MEuler(int n=0): N(n), dinic(Dinic(N+2)), deg(
20        vector<int>(N, 0)), vc(vector<vector<Edge>> >(N

```

```

21    )) {}
22    void add_edge(int a, int b, int d){
23        vc[a].push_back(Edge(b, d));
24        deg[a]++, deg[b]--;
25    }
26    bool Solve(){
27        for(int i=0;i<N;i++){
28            if(abs(deg[i])>1) return false;
29        }
30        for(int i=0;i<N;i++){
31            for(int j=0;j<(int)vc[i].size();j++){
32                Edge e = vc[i][j];
33                if(e.dir == UNDIRECTED)
34                    dinic.add_edge(i, e.to, 1);
35            }
36        }
37        int ans = 0;
38        for(int i=0;i<N;i++){
39            if(deg[i] > 0){
40                dinic.add_edge(N, i, deg[i]/2);
41            }else if(deg[i] < 0){
42                dinic.add_edge(i, N+1, -deg[i]/2);
43                ans += -deg[i] / 2;
44            }
45        }
46        if(dinic.Solve(N, N+1) < ans) return false;
47        return true;
48    }
49 };

```



## 7 Match

### 7.1 BiMatch

```

1  /*
2  * Bipartite Matching
3  * Nx = number of x nodes
4  * Ny = number of y nodes
5  * store matching answer in mx, my
6  * Solve() returns the number of matching
7  */
8  class BiMatch{
9  public:
10     int Nx, Ny;
11     vector<vector<int> > vc;
12     vector<int> mx, my;
13     vector<int> visy;
14
15     BiMatch(int _x=0, int _y=0): Nx(_x), Ny(_y), vc(
        vector<vector<int> >(Nx+1)){}
16
17     void add(int x, int y){
18         vc[x].push_back(y);
19     }
20
21     bool Match(int x){
22         for(int i=0;i<(int)vc[x].size();i++){
23             int y = vc[x][i];
24             if(!visy[y]){
25                 visy[y] = 1;
26                 if(my[y] == -1 || Match(my[y])){
27                     mx[x] = y, my[y] = x;
28                     return true;
29                 }
30             }
31         }
32         return false;
33     }
34     int Solve(){
35         mx = vector<int>(Nx+1, -1);
36         my = vector<int>(Ny+1, -1);
37         int ans = 0;
38         for(int i=0;i<Nx;i++){
39             visy = vector<int>(Ny+1, 0);
40             ans += Match(i);
41         }
42         return ans;
43     }
44 };

```

### 7.2 KM

```

1  /*
2  * solve Maximun Bipartite Matching
3  * store matching answer in mx ,my
4  * Solve() returns themaximun weight of perfect
   matching
5  */
6  class KM{
7  public:
8      #define FF first
9      #define SS second
10     typedef pair<int, int> PI;
11     const static int INF = 0x3f3f3f3f;
12     int Nx, Ny;
13     vector<vector<int> > mp;
14     vector<int> visx, visy;
15     vector<int> lx, ly, slack;
16     vector<int> mx, my;
17     KM(int x=0, int y=0): Nx(x), Ny(y), mp(vector<
        vector<int> >(Nx+1, vector<int>(Ny+1, 0))) {}
18     void add(int x, int y, int w){
19         mp[x][y] = w;
20     }
21
22     bool Match(int x){
23         visx[x] = 1;

```

```

24         for(int i=0;i<Ny;i++){
25             int y = i;
26             if(visy[y]) continue;
27             if(lx[x] + ly [y] > mp[x][y])
28                 slack[y] = min(slack[y], lx[x] + ly[y]
                    - mp[x][y]);
29             else{
30                 visy[y] = 1;
31                 if(my[y] == -1 || Match(my[y])){
32                     mx[x] = y, my[y] = x;
33                     return true;
34                 }
35             }
36         }
37         return false;
38     }
39
40     int Solve(){
41         mx = vector<int>(Nx+1, -1);
42         my = vector<int>(Ny+1, -1);
43         lx = vector<int>(Nx+1, -INF);
44         ly = vector<int>(Ny+1, 0);
45         for(int i=0;i<Nx;i++){
46             for(int j=0;j<Ny;j++){
47                 lx[i] = max(lx[i], mp[i][j]);
48             }
49             slack = vector<int>(Ny+1, INF);
50             while(true){
51                 visx = vector<int>(Nx+1, 0);
52                 visy = vector<int>(Ny+1, 0);
53                 if(Match(i)) break;
54                 int d = INF;
55                 for(int j=0;j<Ny;j++){
56                     if(!visy[j]) d = min(d, slack[j]);
57                 }
58                 if(d == INF)break;
59                 for(int i=0;i<Nx;i++){
60                     if(visx[i]) lx[i] -= d;
61                 }
62                 for(int i=0;i<Ny;i++){
63                     if(visy[i]) ly[i] += d;
64                     else slack[i] -= d;
65                 }
66             }
67             int res = 0;
68             for(int i=0;i<Nx;i++){
69                 if(mx[i] != -1)
70                     res += mp[i][mx[i]];
71             }
72             return res;
73         }
74     }
75 };

```

### 7.3 General Match

```

1  /*
2  * Maximun General Graph Matching
3  * store answer in m
4  * Solve() returns the number of matching
5  * important!!!
6  * notice the order of disjoint set when unioning
7  */
8  class GMatch{
9  public:
10     int N;
11     vector<vector<int> > vc;
12     DisjointSet djs;
13     vector<int> m, d, c1, c2, p, vis;
14     queue<int> q;
15     int ts;
16     GMatch(int n): N(n), vc(vector<vector<int> >(N+1)),
        djs(DisjointSet(N)), ts(0){}
17
18     void add(int a, int b){
19         vc[a].push_back(b);
20         vc[b].push_back(a);
21     }
22
23     void path(int x, int r){
24         if(x==r)return;

```

```

25     if(d[x] == 0){                                100    }
26         int i = p[x], j = p[p[x]];                101    };
27         path(j, r);
28         m[i] = j, m[j] = i;
29     }
30     else if(d[x] == 1){
31         int i = c1[x], j = c2[x];
32         path(i, m[x]);
33         path(j, r);
34         m[i] = j, m[j] = i;
35     }
36 }
37
38 void blossom(int x, int y, int bi){
39     for(int i=djs.find(x);i!=bi;i=djs.find(p[i])){
40         djs.U(bi, i);
41         if(d[i] == 1)
42             c1[i] = x, c2[i] = y, q.push(i);
43     }
44 }
45
46 int lca(int x,int y,int r){
47     ts++;
48     vis[r] = ts;
49     for(int i=djs.find(x);i!=r;i=djs.find(p[i]))
50         vis[i] = ts;
51     int b;
52     for(b=djs.find(y);vis[b]!=ts;b=djs.find(p[b]));
53     return b;
54 }
55
56 bool Match(int x){
57     djs.init();
58     d = vector<int>(N+1, -1);
59     d[x] = 0;
60     q = queue<int>();
61     q.push(x);
62     while(!q.empty()){
63         int u = q.front(); q.pop();
64         for(int i=0;i<(int)vc[u].size();i++){
65             int v = vc[u][i];
66             if(m[v] != v && djs.find(u) != djs.find
67                 (v)){
68                 if(d[v] == -1){
69                     if(m[v] == -1){
70                         path(u, x);
71                         m[u] = v, m[v] = u;
72                         return true;
73                     }else{
74                         p[v] = u, p[m[v]] = v;
75                         d[v] = 1, d[m[v]] = 0;
76                         q.push(m[v]);
77                     }
78                 }else{
79                     if(d[djs.find(v)] == 0){
80                         int bi=lca(u, v, x);
81                         blossom(u, v, bi);
82                         blossom(v, u, bi);
83                     }
84                 }
85             }
86         }
87     }
88     return false;
89 }
90
91 int Solve(){
92     m = c1 = c2 = d = p = vis = vector<int>(N+1,
93         -1);
94     int ans = 0;
95     for(int i=0;i<N;i++){
96         if(m[i] == -1){
97             if(Match(i)) ans++;
98             else m[i]=i;
99         }
100     }
101     return ans;

```



```

33     bool tf = false;
34     for(int i=0;i<N;i++){
35         if(mrg[i]) continue;
36         if(pre[i] == -1 && i != r) return -1;
37         if(pre[i] != -1) tmpw += dis[i];
38         int s;
39         for(s=i;s!=-1&&vis[s]==-1;s=pre[s])
40             vis[s] = i;
41         if(s != -1 && vis[s] == i){
42             tf = true;
43             int j = s;
44             do{
45                 bln[j] = s;
46                 mrg[j] = true;
47                 allw += dis[j];
48                 j = pre[j];
49             }while(j != s);
50             mrg[s] = false;
51         }
52     }
53     if(tf == false) break;
54     for(int i=0;i<(int)E.size();i++){
55         PII &e = E[i];
56         if(bln[e.v2] != -1) e.w -= dis[e.v2];
57         if(bln[e.v1] != -1) e.v1 = bln[e.v1];
58         if(bln[e.v2] != -1) e.v2 = bln[e.v2];
59         if(e.v1 == e.v2) {
60             e = E.back();
61             E.pop_back();
62             i--;
63         }
64     }
65 }
66 return allw + tmpw;
67 }
68 };

```

```

35         if(!vis[i] && dis[i] > wG[v][i])
36             dis[i] = wG[v][i], pre[i] = v;
37     double mn = 1e9;
38     for(int i=0;i<N;i++){
39         if(!vis[i] && mn > dis[i])
40             mn = dis[i], v = i;
41     }
42     if(mn == 1e9)
43         return -1;
44     W += G[pre[v]][v].w;
45     U += G[pre[v]][v].u;
46 }
47 return W / U;
48 }
49 double Solve(){
50     double last = -1, cur = 0;
51     const double EPS = 1e-9;
52     while(fabs(last - cur) > EPS){
53         last = cur;
54         cur = Mst(last);
55     }
56     return cur;
57 };

```

### 8.3 Minimal Rational Spanning Tree

```

1  /*
2  * Minimum Ratio Spanning Tree
3  * Solve() returns answer of MRST if there exists an
4  * answer else -1
5  * notice: if you want make it faster, move G, wG to
6  * normal array
7  */
8  class MRST {
9  public:
10     #define w first
11     #define u second
12     typedef pair<double, double> PD;
13     int N;
14     vector<vector<PD>> > G;
15     vector<vector<double>> > wG;
16     MRST(int n=0): N(n), G(vector<vector<PD>> >(N,
17         vector<PD>(N))), wG(vector<vector<double>> >(N,
18         vector<double>(N))) {
19     }
20     void add_edge(int a, int b, double _w, double _u){
21         G[a][b] = PD(_w, _u);
22     }
23     void build(double chk){
24         for(int i=0;i<N;i++){
25             for(int j=0;j<N;j++){
26                 wG[i][j] = G[i][j].w - chk * G[i][j].u;
27             }
28         }
29     }
30     double Mst(double chk){
31         build(chk);
32         vector<bool> vis(N+1, false);
33         vector<double> dis(N+1, 1e9);
34         vector<int> pre(N+1);
35         double W = 0, U = 0;
36         int v = 0;
37         int times = 0;
38         while(++times < N){
39             vis[v] = true;
40             for(int i=0;i<N;i++){

```

## 9 Geometry

### 9.1 Point

```

1 class Point{
2 public:
3     double x, y;
4     Point(double _x=0, double _y=0): x(_x), y(_y) {}
5     Point operator + (const Point &rhs) const {
6         return Point(x+rhs.x, y+rhs.y);
7     }
8     Point operator - (const Point &rhs) const {
9         return Point(x-rhs.x, y-rhs.y);
10    }
11    Point operator * (const double &rhs) const {
12        return Point(x*rhs, y*rhs);
13    }
14    Point operator / (const double &rhs) const {
15        return Point(x/rhs, y/rhs);
16    }
17    bool operator == (const Point &rhs) const {
18        return x == rhs.x && y == rhs.y;
19    }
20    double Abs() const {
21        return sqrt(x*x + y*y);
22    }
23    /*
24     * range: 0 ~ 2*PI
25     */
26    double Arg() const {
27        double res = atan2(y, x);
28        if(cmp(res) < 0) res += PI*2.0;
29        return res;
30    }
31    double Dot(const Point &rhs) const {
32        return (x*rhs.x + y*rhs.y);
33    }
34    double Cross(const Point &rhs) const {
35        return (x*rhs.y - y*rhs.x);
36    }
37    double Dist(const Point &rhs) const {
38        return (*this-rhs).Abs();
39    }
40    /*
41     * unit of d is radian
42     */
43    Point Rotate(double d) const {
44        return Rotate(cos(d), sin(d));
45    }
46    Point Rotate(double cost, double sint) const {
47        return Point(x*cost-y*sint, x*sint+y*cost);
48    }
49    bool operator < (const Point &rhs) const {
50        if(x == rhs.x)
51            return y < rhs.y;
52        return x < rhs.x;
53    }
54    friend ostream& operator << (ostream &out, const
55        Point &rhs){
56        out << "(" << rhs.x << ", " << rhs.y << ")";
57        return out;
58    }
59    Point& update(){
60        if(cmp(x) == 0)
61            x = 0;
62        if(cmp(y) == 0)
63            y = 0;
64        return *this;
65    }
66 } nilPoint(INF, INF);

```

### 9.2 Line

```

1 class Line{
2 public:
3     Point a, b;

```

```

4     Line(Point _a=Point(), Point _b=Point()): a(_a), b(
5         _b) {}
6     double Dist(const Point &rhs){
7         if(cmp((rhs-a).Dot(b-a)) < 0) return (rhs-a).
8             Abs();
9         if(cmp((rhs-b).Dot(a-b)) < 0) return (rhs-b).
10            Abs();
11        return fabs((a-rhs).Cross(b-rhs) / a.Dist(b));
12    }
13    /*
14     * the pedal of rhs on line
15     */
16    Point Proj(const Point &rhs){
17        double r = (a-b).Dot(rhs-b) / (a-b).Dot(a-b);
18        return b+(a-b)*r;
19    }
20    bool OnLine(const Point &rhs){
21        /* for segment */
22        return cmp((rhs-b).Cross(a-b)) == 0 && cmp((rhs
23            -b).Dot(rhs-a)) <= 0;
24        /* for line */
25        return cmp((rhs-b).Cross(a-b)) == 0;
26    }
27    bool Parallel(const Line &rhs){
28        return !cmp((a-b).Cross(rhs.a-rhs.b));
29    }
30    bool IsIntersect(const Line &rhs){
31        if(cmp((rhs.a-a).Cross(rhs.b-a) * (rhs.a-b).
32            Cross(rhs.b-b)) > 0) return false;
33        if(cmp((a-rhs.a).Cross(b-rhs.a) * (a-rhs.b).
34            Cross(b-rhs.b)) > 0) return false;
35        return true;
36    }
37    /* default is line */
38    Point Intersection(const Line &rhs, bool flag=false
39        ){
40        if(Parallel(rhs)) return nilPoint;
41        /* for segment */
42        if(flag && IsIntersect(rhs) == false) return
43            nilPoint;
44        /* end */
45        double s1 = (a-rhs.a).Cross(rhs.b-rhs.a);
46        double s2 = (b-rhs.a).Cross(rhs.b-rhs.a);
47        return (b*s1-a*s2) / (s1-s2);
48    }
49    /*
50     * move d units along the direction of line
51     * example: {(0, 0) -> (1, 1)} move _/2 becomes
52     * {(1, 1) -> (2, 2)}
53     */
54    Line Move(const double &d){
55        Point tmp = b - a;
56        tmp = tmp / tmp.Abs();
57        tmp = tmp.Rotate(PI/2);
58        return Line(a+tmp*d, b+tmp*d);
59    }
60    friend ostream& operator << (ostream &out, const
61        Line &rhs){
62        out << "[" << rhs.a << ", " << rhs.b << "]"";
63        return out;
64    }
65 } nilLine(nilPoint, nilPoint);

```

### 9.3 Polygon

```

1 /*
2  * default is counterclockwise
3  */
4 class Polygon{
5 #define COUNTERCLOCKWISE 1
6 #define CLOCKWISE -1
7 public:
8     int N;
9     vector<Point> s;
10    vector<double> A;
11    Polygon(int n=0): N(n) {}

```

```

12 Polygon& add(const Point &n){
13     s.push_back(n);
14     return *this;
15 }
16 /*
17  * counterclockwise or clockwise
18  * defined as above
19  */
20 int Order(){
21     int t = 0;
22     for(int i=0;i<N&&t==0;i++){
23         int a = i, b = (i+1)%N, c = (i+2)%N;
24         t = (s[b]-s[a]).Cross(s[c]-s[b]);
25     }
26     return t;
27 }
28 double Perimeter(){
29     double res = 0;
30     for(int i=0;i<N;i++){
31         res += s[i].Dist(s[(i+1)%N]);
32     }
33     return res;
34 }
35 double Area(){
36     double res = 0;
37     for(int i=0;i<N;i++){
38         res += s[i].Cross(s[(i+1)%N]);
39     }
40     return fabs(res/2.0);
41 }
42 #define INSIDE 1
43 #define ONEDGE 2
44 #define OUTSIDE 0
45 int OnPolygon(const Point &n){
46     Point rfn = Point(-INF, n.y);
47     Line l = Line(n, rfn);
48     int cnt = 0;
49     for(int i=0;i<N;i++){
50         if(Line(s[i], s[(i+1)%N]).OnLine(n))
51             return ONEDGE;
52         if(cmp(s[i].y - s[(i+1)%N].y) == 0)
53             continue;
54         if(l.OnLine(s[i])){
55             if(cmp(s[i].y - s[(i+1)%N].y) >= 0)
56                 cnt++;
57         }else if(l.OnLine(s[(i+1)%N])){
58             if(cmp(s[(i+1)%N].y - s[i].y) >= 0)
59                 cnt++;
60         }else if(l.IsIntersect(Line(s[i], s[(i+1)%N])))
61             cnt++;
62     }
63     return (cnt&1);
64 }
65 bool IsIntersect(const Line &rhs){
66     int i = (upper_bound(A.begin(), A.end(), (rhs.b - rhs.a).Arg()) - A.begin()) % N;
67     int j = (upper_bound(A.begin(), A.end(), (rhs.a - rhs.b).Arg()) - A.begin()) % N;
68     if(cmp((rhs.b-rhs.a).Cross(s[i]-rhs.a)*(rhs.b-rhs.a).Cross(s[j]-rhs.a)) <= 0)
69         return true;
70     return false;
71 }
72 };

```

### 9.3.1 Pick's Theorem

```

1 int PointsOnedge(){
2     int res = 0;
3     for(int i=0;i<N;i++){
4         res += __gcd(abs(s[(i+1)%N].x-s[i].x), abs(s[(i+1)%N].y-s[i].y));
5     }
6     return res;
7 }
8 int PointsInside(){
9     return int(Area()) + 1 - PointsOnedge()/2;
10 }

```

### 9.3.2 Mass Center

```

1 Point MassCenter(){
2     if(cmp(Area()) == 0) return nilPoint;
3     Point res;
4     for(int i=0;i<N;i++){
5         res = res + (s[i] + s[(i+1)%N]) * s[i].Cross(s[(i+1)%N]);
6     }
7     return res / Area() / 6.0;
8 }

```

### 9.3.3 Convex

```

1 Polygon ConvexHull(){
2     Polygon res, that = *this;
3     sort(that.s.begin(), that.s.end());
4     that.s.erase(unique(that.s.begin(), that.s.end()), that.s.end());
5     vector<Point> &w = res.s;
6     for(int i=0;i<(int)that.s.size();i++){
7         int sz;
8         while((sz=w.size()),
9                sz > 1 && cmp((w[sz-1]-w[sz-2]).Cross(that.s[i]-w[sz-2])) <= 0)
10            w.pop_back();
11        w.push_back(that.s[i]);
12    }
13    int k = w.size();
14    for(int i=(int)that.s.size()-2;i>=0;i--){
15        int sz;
16        while((sz=w.size()),
17               sz > k && cmp((w[sz-1]-w[sz-2]).Cross(that.s[i]-w[sz-2])) <= 0)
18            w.pop_back();
19        w.push_back(that.s[i]);
20    }
21    if((int)that.s.size() > 1) w.pop_back();
22    res.N = w.size();
23    res.A = vector<double>(res.N);
24    for(int i=0;i<res.N;i++){
25        res.A[i] = (res.s[(i+1)%res.N]-res.s[i]).Arg();
26    }
27    return res;
28 }

```

### 9.3.4 OnConvex

```

1 /*
2  * O(lg N)
3  */
4 int OnConvex(const Point &rhs){
5     Point rfn = (s[0]+s[N/3]+s[2*N/3]) / 3.0;
6     int l = 0, r = N;
7     while(l+1 < r){
8         int mid = (l+r) / 2;
9         if(cmp((s[l]-rfn).Cross(s[mid]-rfn)) > 0){
10             if(cmp((s[l]-rfn).Cross(rhs-rfn)) >= 0 && cmp((s[mid]-rfn).Cross(rhs-rfn)) < 0)
11                 r = mid;
12             else l = mid;
13         }else{
14             if(cmp((s[l]-rfn).Cross(rhs-rfn)) < 0 && cmp((s[mid]-rfn).Cross(rhs-rfn)) >= 0)
15                 l = mid;
16             else r = mid;
17         }
18     }
19     r %= N;
20     int z = cmp((s[r]-rhs).Cross(s[l]-rhs));
21     if(z == 0) return ONEDGE;
22     else if(z == 1) return OUTSIDE;
23     else return INSIDE;
24 }

```

### 9.3.5 Convex Diameter

```

1 /*
2  * farthest node pair

```

```

3  */
4  pair<double, pair<Point, Point> > Diameter(){
5      if(N == 1)
6          return make_pair(0, make_pair(s[0], s[0]));
7      double maxd = 0;
8      Point pa, pb;
9      for(int i=0, j=1; i<N; i++){
10         while(cmp((s[next(i)]-s[i]).Cross(s[j]-s[i])-(s
            [next(i)]-s[i]).Cross(s[next(j)]-s[i])) <
                0)
11             j = next(j);
12         double d = s[i].Dist(s[j]);
13         if(d > maxd)
14             maxd = d, pa = s[i], pb = s[j];
15         d = s[next(i)].Dist(s[next(j)]);
16         if(d > maxd)
17             maxd = d, pa = s[next(i)], pb = s[next(j)];
18     }
19     return make_pair(maxd, make_pair(pa, pb));
20 }

```

### 9.3.6 Circle

```

1  class Circle{
2  public:
3      Point O;
4      double R;
5      Circle(const Point &o, const double &r): O(o), R(r) {}
6      double Area() const {
7          return PI * R * R;
8      }
9      double Perimeter() const {
10         return 2.0 * PI * R;
11     }
12     /*
13     * default not includes on the edge
14     */
15     bool InCircle(const Point &rhs) const {
16         return cmp(O.Dist(rhs) - R) < 0;
17     }
18     /*
19     * default is segment
20     * if want to change it to line, remove the if
21     * which judge t
22     */
23     vector<Point> Intersection(const Line &rhs){
24         vector<Point> res;
25         Point d1 = rhs.b - rhs.a, d2 = rhs.a - O;
26         double A = d1.x*d1.x + d1.y*d1.y;
27         double B = 2.0 * d1.Dot(rhs.a-O);
28         double C = d2.x*d2.x + d2.y*d2.y - R*R;
29         double D = B*B - 4*A*C;
30         if(cmp(D) >= 0){
31             double t1 = (-B - sqrt(max(0.0, D))) /
32                 (2.0*A);
33             double t2 = (-B + sqrt(max(0.0, D))) /
34                 (2.0*A);
35             if(cmp(t1-1) <= 0 && cmp(t1) >= 0)
36                 res.push_back(rhs.a + d1*t1);
37             if(cmp(t1-t2) != 0 && cmp(t2-1) <= 0 && cmp
38                 (t2) >= 0)
39                 res.push_back(rhs.a + d1*t2);
40         }
41         return res;
42     }
43     /*
44     * the intersections of two circle
45     */
46     pair<Point, Point> Intersection(const Circle &rhs)
47     const {
48         double d = (O-rhs.O).Abs();
49         double cost = (R*R+d*d-rhs.R*rhs.R) / (2.0*R*d)
50         ;
51         double sint = sqrt(1.0 - cost*cost);
52         Point rfn = (rhs.O-O) / d * R;
53         return make_pair(O+rfn.Rotate(cost, sint), O+
54             rfn.Rotate(cost, -sint));
55     }
56 }

```

```

57 }
58 friend ostream& operator << (ostream& out, const
59     Circle &rhs){
60     out << "C{" << rhs.O << ", " << rhs.R << "}";
61     return out;
62 }
63 bool operator < (const Circle &rhs) const {
64     if(cmp(R-rhs.R) != 0) return cmp(R-rhs.R) < 0;
65     return 0 < rhs.O;
66 }
67 bool operator == (const Circle &rhs) const {
68     return cmp(R-rhs.R) == 0 && 0 == rhs.O;
69 }
70 };

```

### 9.3.7 Circle Polygon Cover

```

1  double SectorArea(const Point &rhs1, const Point &rhs2)
2  {
3      double theta = rhs1.Arg() - rhs2.Arg();
4      while(cmp(theta) <= 0) theta += 2.0 * PI;
5      while(cmp(theta - 2.0*PI) > 0) theta -= 2.0 * PI;
6      theta = min(theta, 2.0*PI - theta);
7      return R * R * theta / 2.0;
8  }
9  /* called by Area(const Polygon&) */
10 double calc(const Point &rhs1, const Point &rhs2){
11     vector<Point> p;
12     bool in1 = (cmp(rhs1.Abs()-R) < 0);
13     bool in2 = (cmp(rhs2.Abs()-R) < 0);
14     if(in1){
15         if(in2)
16             return fabs(rhs1.Cross(rhs2)) / 2.0;
17         else{
18             p = Intersection(Line(rhs1, rhs2));
19             return SectorArea(rhs1, p[0]) + fabs(rhs1.
20                 Cross(p[0])) / 2.0;
21         }
22     }else{
23         if(in2){
24             p = Intersection(Line(rhs1, rhs2));
25             return SectorArea(p[0], rhs1) + fabs(rhs2.
26                 Cross(p[0])) / 2.0;
27         }else{
28             p = Intersection(Line(rhs1, rhs2));
29             if((int)p.size() == 2){
30                 return SectorArea(rhs1, p[0]) +
31                     SectorArea(p[1], rhs2) + fabs(p
32                         [0].Cross(p[1])) / 2.0;
33             }else{
34                 return SectorArea(rhs1, rhs2);
35             }
36         }
37     }
38 }
39 /*
40 * the area of overlap between circle and polygon
41 */
42 double Area(const Polygon &rhs){
43     Polygon that = rhs;
44     for(int i=0; i<that.N; i++){
45         that.s[i] = that.s[i] - O;
46     }
47     double res = 0;
48     for(int i=0; i<that.N; i++){
49         int sng = cmp(that.s[i].Cross(that.s[(i+1)%that
50             .N]));
51         if(sng){
52             res += sng * calc(that.s[i], that.s[(i+1)%
53                 that.N]);
54         }
55     }
56     return res;
57 }

```

### 9.3.8 Minimal Circle Cover

```

1  /*

```



```

2  * circumcircle of two points
3  */
4  Circle Center(const Point &rhs1, const Point &rhs2){
5      return Circle((rhs1+rhs2)/2.0, rhs1.Dist(rhs2)/2.0);
6  }
7  /*
8  * circumcircle of three points
9  */
10 Circle Center(const Point &rhs1, const Point &rhs2,
11               const Point &rhs3){
12     Circle res(rhs1, 0);
13     Point d1 = rhs2 - rhs1, d2 = rhs3 - rhs1;
14     double c1 = (d1.x*d1.x+d1.y*d1.y) / 2.0, c2 = (d2.x*
15               *d2.x+d2.y*d2.y) / 2.0;
16     double d = d1.Cross(d2);
17     res.O.x += (c1*d2.y-c2*d1.y) / d;
18     res.O.y += (c2*d1.x-c1*d2.x) / d;
19     res.R = res.O.Dist(rhs1);
20     return res;
21 }
22 Circle MinCircleCover(vector<Point> rhs){
23     random_shuffle(rhs.begin(), rhs.end());
24     Circle res(rhs[0], 0);
25     for(int i=1; i<(int)rhs.size(); i++){
26         if(!res.InCircle(rhs[i])){
27             res = Circle(rhs[i], 0);
28             for(int j=0; j<i; j++){
29                 if(!res.InCircle(rhs[j])){
30                     res = Center(rhs[i], rhs[j]);
31                     for(int k=0; k<j; k++){
32                         if(!res.InCircle(rhs[k])){
33                             res = Center(rhs[i], rhs[j],
34                                           rhs[k]);
35                         }
36                     }
37                 }
38             }
39         }
40     }
41     return res;
42 }

```

### 9.3.9 Halfplane

```

1 class HalfPlane{
2 public:
3     Point a, b;
4     /* a -> b left side */
5     HalfPlane(const Point &a=Point(), const Point &b=
6               Point()): a(_a), b(_b) {}
7     double Value(const Point &rhs) const {
8         return (rhs-a).Cross(b-a);
9     }
10    bool Satisfy(const Point &rhs) const {
11        return cmp(Value(rhs)) <= 0;
12    }
13    Point Intersection(const Point &rhs1, const Point &
14                      rhs2){
15        return Line(a, b).Intersection(Line(rhs1, rhs2));
16    }
17    Point Intersection(const HalfPlane &rhs){
18        return Line(a, b).Intersection(Line(rhs.a, rhs.
19                      b));
20    }
21    /*
22    * return the polygon cut by halfplane
23    */
24    Polygon Cut(const Polygon &rhs){
25        Polygon res;
26        const vector<Point> &w = rhs.s;
27        int N = w.size();
28        for(int i=0; i<(int)w.size(); i++){
29            if(cmp(Value(w[i])) <= 0)
30                res.s.push_back(w[i]);
31            else{
32                if(cmp(Value(w[prev(i)])) < 0)

```

```

33                res.s.push_back(Intersection(w[prev
34                (i)], w[i]));
35                if(cmp(Value(w[next(i)])) < 0)
36                    res.s.push_back(Intersection(w[i],
37                w[next(i)]));
38            }
39        }
40        res.N = res.s.size();
41        return res;
42    }
43    bool operator < (const HalfPlane &rhs) const {
44        int res = cmp((b-a).Arg() - (rhs.b-rhs.a).Arg())
45        );
46        return res == 0 ? rhs.Satisfy(a) : (res<0);
47    }
48    friend ostream& operator << (ostream& out, const
49    HalfPlane &rhs){
50        out << "\"" << rhs.a << ", " << rhs.b << "\"";
51        return out;
52    }
53 }

```

### 9.3.10 Halfplane Set

```

1 class HalfPlaneSet{
2 public:
3     vector<HalfPlane> s;
4     HalfPlaneSet& add(const HalfPlane &rhs){
5         s.push_back(rhs);
6         return *this;
7     }
8     /*
9     * return the polygon that satisfies all halfplanes
10    */
11    Polygon Solve(){
12        Polygon res;
13        sort(s.begin(), s.end());
14        deque<HalfPlane> q;
15        deque<Point> ans;
16        q.push_back(s[0]);
17        for(int i=1; i<(int)s.size(); i++){
18            if(cmp((s[i].b-s[i].a).Arg()-(s[i-1].b-s[i-1].a).Arg()) == 0) continue;
19            while(ans.size() > 0 && cmp(s[i].Value(ans.
20            back())) >= 0){
21                ans.pop_back();
22                q.pop_back();
23            }
24            while(ans.size() > 0 && cmp(s[i].Value(ans.
25            front())) >= 0){
26                ans.pop_front();
27                q.pop_front();
28            }
29            ans.push_back(q.back().Intersection(s[i]));
30            q.push_back(s[i]);
31        }
32        while(ans.size() > 0 && cmp(q.front().Value(ans.
33            back())) >= 0){
34            ans.pop_back();
35            q.pop_back();
36        }
37        while(ans.size() > 0 && cmp(q.back().Value(ans.
38            front())) >= 0){
39            ans.pop_front();
40            q.pop_front();
41        }
42        ans.push_back(q.back().Intersection(q.front()));
43        for(int i=0; i<(int)ans.size(); i++){
44            res.add(ans[i]);
45        }
46        res.N = res.s.size();
47        return res;
48    }
49 }

```

### 9.3.11 Kernel of Polygon

```
1 /*
```



```

2  * the kernel of the polygon
3  */
4  Polygon Kernel(const Polygon &rhs){
5      HalfPlaneSet hpls;
6      for(int i=0;i<rhs.N;i++)
7          hpls.add(HalfPlane(rhs.s[i], rhs.s[(i+1)%rhs.N]));
8      return hpls.Solve();
9  }

```

## 10 Data Structure

### 10.1 Splay Tree

```

1  #include <bits/stdc++.h>
2  using namespace std;
3  template <class T>
4  class SplayTree{
5  public:
6      class Node{
7      public:
8          Node *L, *R, *P;
9          T val;
10         int sz;
11         Node(const T &rhs=T()):
12             L(NULL), R(NULL), P(NULL), val(rhs), sz(1)
13         {}
14         void Up(){
15             sz = 1 + NodeSize(L) + NodeSize(R);
16         }
17     };
18     static int NodeSize(Node *rhs){
19         return rhs?rhs->sz:0;
20     }
21     Node *root;
22     SplayTree(): root(NULL){}
23     SplayTree(const T &rhs): root(new Node(rhs)){}
24     ~SplayTree(){
25     }
26     void Free(){
27         this->Free(this->root);
28     }
29     void Free(Node *rhs){
30         if(!rhs) return;
31         if(rhs->L) Free(rhs->L);
32         if(rhs->R) Free(rhs->R);
33         delete rhs;
34         rhs = NULL;
35     }
36     int Size() const {
37         return NodeSize(root);
38     }
39     void LeftRotate(Node *rhs){
40         Node *x = rhs, *y = x->R;
41         x->R = y->L;
42         if(y->L) y->L->P = x;
43         y->P = x->P;
44         if(!x->P) root = y;
45         else if(x->P->L == x) x->P->L = y;
46         else x->P->R = y;
47         y->L = x; x->P = y;
48         x->Up(); y->Up();
49     }
50     void RightRotate(Node *rhs){
51         Node *x = rhs, *y = x->L;
52         x->L = y->R;
53         if(y->R) y->R->P = x;
54         y->P = x->P;
55         if(!x->P) root = y;
56         else if(x->P->L == x) x->P->L = y;
57         else x->P->R = y;
58         y->R = x; x->P = y;
59         x->Up(); y->Up();
60     }
61     void Splay(Node *rhs){
62         while(rhs->P != NULL){
63             if(rhs->P->P == NULL){
64                 if(rhs->P->L == rhs) RightRotate(rhs->P);
65                 else LeftRotate(rhs->P);
66             }else if(rhs->P->L == rhs && rhs->P->P->L
67                     == rhs->P){
68                 RightRotate(rhs->P->P);
69                 RightRotate(rhs->P);
70             }else if(rhs->P->L == rhs && rhs->P->P->R
71                     == rhs->P){
72                 RightRotate(rhs->P);
73             }
74         }
75     }
76 }

```

```

70         LeftRotate(rhs->P);
71     }else if(rhs->P->R == rhs && rhs->P->P->R
145     }
146 };
147 int main(){
72         == rhs->P){
148     const int size = 10;
73         LeftRotate(rhs->P->P);
149     const int time = 100000000;
74         LeftRotate(rhs->P);
150     SplayTree<int> s[size];
75     }else{
151     for(int i=0;i<time;i++){
76         LeftRotate(rhs->P);
152         s[rand()%size].Insert(rand());
77         RightRotate(rhs->P);
153         int a,b;
78     }
154     do{
79     }
155         a = rand()%size;
80     Node* FindMin() const {
156         b = rand()%size;
81         Node *tr = root;
157     }while(a == b);
82         while(tr->L)tr = tr->L;
158     s[a].Merge(s[b]);
83         return tr;
159     s[b].root = NULL;
84     }
160 }
85     Node* FindMax() const {
161     for(int i=0;i<size;i++){
86         Node *tr = root;
162         printf("%d\n", i);
87         while(tr->R)tr = tr->R;
163     }
88         return tr;
164     return 0;
89     }
165 }
90     Node* Find(int k) const {
91         Node *tr = root;
92         while(tr){
93             if(NodeSize(tr->L) >= k)
94                 tr = tr->L;
95             else if(NodeSize(tr->L)+1 == k)
96                 break;
97             else if(tr->R)
98                 k -= (NodeSize(tr->L)+1), tr = tr->R;
99         }
100         return tr;
101     }
102     void Merge(SplayTree rhs){
103         if(rhs.Size() == 0)
104             return;
105         if(this->Size() == 0){
106             *this = rhs;
107             return;
108         }
109         this->Splay(this->FindMax());
110         this->root->R = rhs.root;
111         this->root->R->P = this->root;
112         this->root->Up();
113     }
114     void Insert(const T &rhs){
115         this->Merge(SplayTree(rhs));
116     }
117     void Split(int k, SplayTree &rhs1, SplayTree &rhs2)
118     {
119         this->Splay(this->Find(k));
120         rhs1.root = this->root;
121         rhs2.root = this->root->R;
122         rhs1.root->R = NULL;
123         if(rhs2.root)rhs2.root->P = NULL;
124         rhs1.root->Up();
125     }
126     void Delete(int k){
127         this->Splay(this->Find(k));
128         SplayTree a, b;
129         a.root = this->root->L;
130         b.root = this->root->R;
131         if(a.root)a.root->P = NULL;
132         if(b.root)b.root->P = NULL;
133         delete this->root;
134         a.Merge(b);
135         this->root = a.root;
136     }
137     void Print() const {
138         print(this->root);
139         puts("");
140     }
141     void print(Node *rhs, int a=0) const {
142         if(rhs == NULL)return;
143         print(rhs->L, a+1);
144         cout << rhs->val << " ";
145         print(rhs->R, a+1);

```

## 11 String

### 11.1 Z Value

```

1 vector<int> z_value(string s){
2     int len = s.size();
3     vector<int> z(0, len);
4     int l=0, r=0;
5     z[0] = len;
6     for(int i=1; i<len; i++){
7         j = max(min(z[i-1], r-i), 0);
8         while(i+j<len&&s[i+j]==s[j])j++;
9         if(i+z[i]>r)r=(l=i)+z[i];
10    }
11    return z;
12 }

```

```

25         if(tp[0][sa[j]]==tp[0][sa[j-1]]&&tp[1][sa[j-1]]==tp[1][sa[j]]){
26             rank[sa[j]] = rank[sa[j-1]];
27         }else rank[sa[j]] = j;
28     }
29 }
30 return sa;
31 }

```

### 11.2 Z Value Longest Palindrome

```

1 vector<int> zvaule_pali(string s1){
2     int len1=s1.size(), len2=len1*2-1;
3     vector<int> z(len2, 0);
4     string s2(len2, '@');
5     for(int i=0; i<len2; i++)
6         if(!(i&1))s2[i] = s1[i/2];
7     z[0] = 1;
8     int l=0, r=0;
9     for(int i=1; i<len2; i++){
10        if(i>r){
11            l = r = i;
12            while(l>0&&r<len2-1&&s2[l-1]==s2[r+1])l--, r++;
13            z[i] = r-l+1;
14        }else{
15            z[i] = z[((l+r)&(~1))-i];
16            int nr = i+z[i]/2;
17            if(nr==r){
18                l = i*2-r;
19                while(l>0&&r<len2-1&&s2[l-1]==s2[r+1])l--, r++;
20                z[i] = r-l+1;
21            }else if(nr>r){
22                z[i] = (r-i)*2+1;
23            }
24        }
25    }
26    return z;
27 }

```

### 11.3 Suffix Array

```

1 vector<int> SuffixArray(string s){
2     int len = s.size();
3     int alpha = 256;
4     vector<int> cnt(0, alpha), rank(0, len), sa(0, len), tsa(0, len), tp[2];
5     tp[0] = tp[1] = vector<int>(0, len);
6     for(int i=0; i<len; i++)cnt[s[i]+1]++;
7     for(int i=1; i<alpha; i++)cnt[i] += cnt[i-1];
8     for(int i=0; i<len; i++)rank[i] = cnt[s[i]];
9     for(int i=1; i<len; i++){
10        for(int j=0; j<len; j++){
11            if(i+j>len)tp[1][j] = 0;
12            else tp[1][j] = rank[i+j]+1;
13            tp[0][j] = rank[j];
14        }
15        fill(cnt.begin(), cnt.end(), 0);
16        for(int j=0; j<len; j++)cnt[tp[1][j]+1]++;
17        for(int j=1; j<alpha; j++)cnt[j] += cnt[j-1];
18        for(int j=0; j<len; j++)tsa[cnt[tp[1][j]]++] = j;
19        fill(cnt.begin(), cnt.end(), 0);
20        for(int j=0; j<len; j++)cnt[tp[0][j]+1]++;
21        for(int j=1; j<alpha; j++)cnt[j] += cnt[j-1];
22        for(int j=0; j<len; j++)tsa[cnt[tp[0][j]]++] = j;
23        rank[sa[0]] = 0;
24        for(int j=1; j<len; j++){

```