

9.25
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$$1. x(t) = \begin{cases} A & 0 < t < \tau \\ 0 & \tau < t < T \end{cases}$$

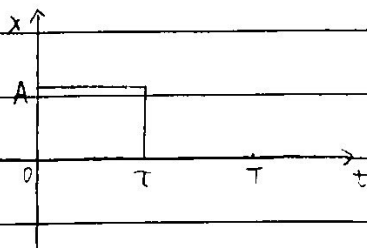
$$= \sum_{n=-\infty}^{\infty} C_n e^{jn\omega t}$$

$$C_n = \frac{1}{T} \int_0^T x(t) e^{-jn\omega t} dt = \frac{1}{T} \int_0^{\tau} A e^{-j(\frac{2\pi}{T})nt} dt$$

$$= \frac{1}{T} A \frac{T}{-2\pi j n} e^{-j\frac{2\pi}{T}nt} \Big|_0^{\tau}$$

$$= -\frac{A}{2\pi j n} (e^{-j\frac{2\pi}{T}n\tau} - 1)$$

$$\therefore x(t) = \sum_{n=-\infty}^{\infty} -\frac{A}{j 2\pi n} (e^{-j\frac{2\pi}{T}n\tau} - 1) e^{j\frac{2\pi}{T}nt}$$



2. No, the signal does not have finite ^{energy} power.

$$\text{Energy} = \int_{-\infty}^{\infty} |x(t)|^2 dt \quad \text{where } x(t) = \begin{cases} A & 0 < t < \tau \\ 0 & \tau < t < T \end{cases}$$

$$\text{For one period: } E_x = \int_0^T |x(t)|^2 dt = \int_0^{\tau} |A|^2 dt + \int_{\tau}^T |0|^2 dt = A^2 \tau.$$

However, $x(t)$ is a continuous periodic function; therefore, the

$$\text{energy } E_x = \int_{-\infty}^{\infty} |x(t)|^2 dt \rightarrow \infty$$

$$\text{Power} = \lim_{T \rightarrow \infty} \frac{1}{T} \int_{-\frac{T}{2}}^{\frac{T}{2}} |x(t)|^2 dt \quad P_x = \lim_{T \rightarrow \infty} \frac{1}{T} \int_0^T |x(t)|^2 dt$$

$$= \lim_{T \rightarrow \infty} \frac{1}{T} \left(\int_0^{\tau} A^2 dt + \int_{\tau}^T 0^2 dt \right)$$

$$= \lim_{T \rightarrow \infty} A^2 \frac{\tau}{T}$$

no! as T grows?
75/1

\therefore I think the power is finite, as the result shows that

the power is a fraction of A^2 , depending on the

duty cycle ($0 \leq \frac{\tau}{T} \leq 1$).

$A^2 \frac{\tau}{T}$

$$\begin{aligned} 3. \text{sinc}(t) * \text{sinc}(t) &= \frac{\sin(t)}{t} * \frac{\sin(t)}{t} = \left(\int_{-\infty}^{\infty} \frac{\sin(t)}{t} e^{-j\frac{\omega}{2}t} dt \right) \cdot \left(\int_{-\infty}^{\infty} \frac{\sin(t)}{t} e^{-j\frac{\omega}{2}t} dt \right) \\ &= \left(\int_{-\infty}^{\infty} \frac{\sin(t)}{t} e^{-j\frac{\omega}{2}t} dt \right)^2 \\ &= \text{rect}(\omega) \cdot \text{rect}(\omega) \\ &= \text{sinc}(t) \end{aligned}$$

4. $y(t) = |x(t+3)|$

No, the system is not linear. (Because of the absolute value)

Yes, the system is time invariant. $|x(t+3-t_0)| = y(t-t_0)$

No, the system is not causal. $(t+3)$ term \rightarrow depends on future input

5. $x(t) = \begin{cases} \cos(2\pi ft) & 0 \leq t \leq T \\ 0 & \text{otherwise} \end{cases} \quad T = \frac{1}{f}$

$X(\omega) = \int_{-\infty}^{\infty} x(t) e^{-j\omega t} dt = \int_0^T \cos(2\pi ft) e^{-j\omega t} dt$
 $= \frac{1}{2} \int_0^T (e^{j\omega t} + e^{-j\omega t}) e^{-j\omega t} dt = \frac{1}{2} \int_0^T (1 + e^{-j2\omega t}) dt$
 $= \frac{1}{2} \left[t - \frac{1}{j(2\omega)} e^{-j2\omega t} \right]_0^T$
 $= \frac{1}{2} \left(T + \frac{1}{j(2\omega)} - \frac{1}{j(2\omega)} e^{-j2\omega T} \right)$

MATLAB

5: 1/1

6: 1/1

7: 1/1

8: 1/1

9: 1/1

Style: 5/1

literally
no
Comments
lol