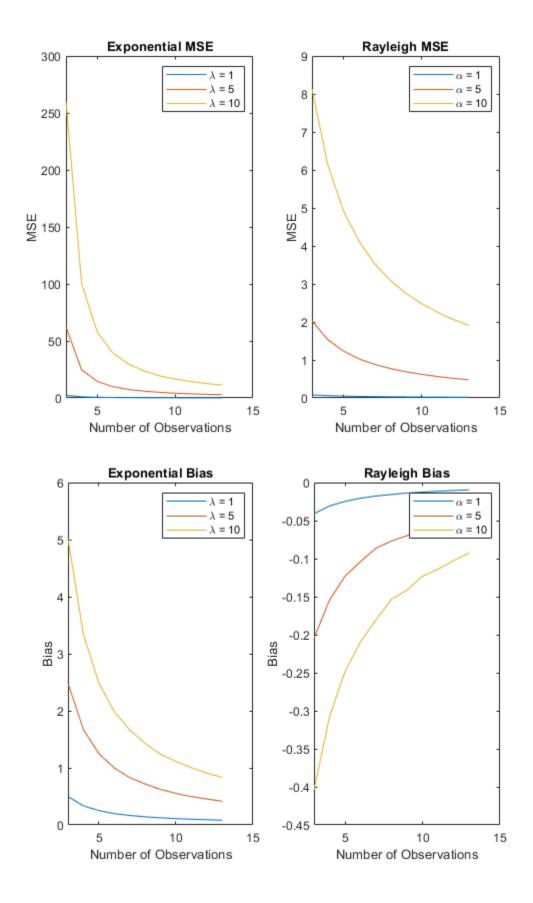
```
%Allister Liu, Min (Ella) Cheng, Amy Leong
%Stochastics Project 3

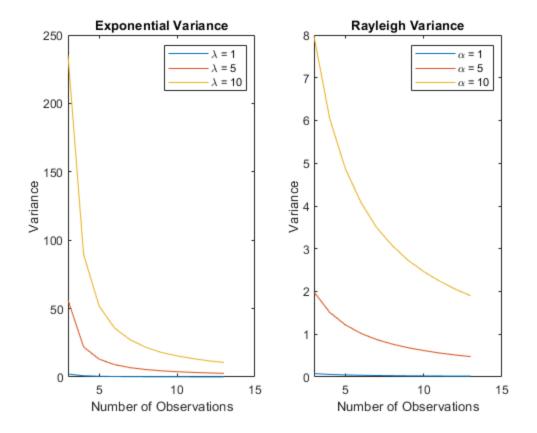
clc;
clear;
close all;
```

Part 1

```
%setup
N = 1000000;
observation = 3:13;
lambda = [1 5 10];
alpha = [1 5 10];
ind=1;
for i = observation
    %calculate the MSE, bias and variance for each distribution and
 for
    %each # of observation
    %MSE is found by taking the mean square of the ML
    %estimator-lambda/alpha
    %bias is found by taking the mean of the ML estimator -lambda/
alpha
    %variance is found by taking the variance of the ML estimator
    [MSE_exp1(ind),bias_exp1(ind),var_exp1(ind)]=
 exponential_mse_bias_variance(N,i,lambda(1));
    [MSE exp2(ind), bias exp2(ind), var exp2(ind)]=
 exponential_mse_bias_variance(N,i,lambda(2));
    [MSE exp3(ind), bias exp3(ind), var exp3(ind)]=
 exponential_mse_bias_variance(N,i,lambda(3));
 [MSE_rayleigh1(ind),bias_ray1(ind),var_ray1(ind)]=rayleigh_mse_bias_variance(N,i,
 [MSE_rayleigh2(ind), bias_ray2(ind), var_ray2(ind)] = rayleigh_mse_bias_variance(N,i,
 [MSE_rayleigh3(ind), bias_ray3(ind), var_ray3(ind)] = rayleigh_mse_bias_variance(N,i,
    ind=ind+1;
end
% plot the MSE for exponential and rayleigh distributions
figure;
subplot(1,2,1);
plot(observation, MSE_exp1, observation, MSE_exp2,
 observation, MSE_exp3);
title("Exponential MSE");
```

```
xlabel("Number of Observations");
ylabel("MSE");
legend("\lambda = " + lambda(1), "\lambda = " + lambda(2),"\lambda = "
 + lambda(3));
subplot(1,2,2);
plot(observation, MSE_rayleigh1, observation, MSE_rayleigh2,
 observation, MSE rayleigh3);
title("Rayleigh MSE");
xlabel("Number of Observations");
ylabel("MSE");
legend("\alpha = " + alpha(1), "\alpha = " + alpha(2), "\alpha = " +
 alpha(3));
%plot the bias for exponential and rayleigh distributions
figure;
subplot(1,2,1);
plot(observation, bias_expl, observation, bias_exp2, observation,
bias exp3);
title("Exponential Bias");
xlabel("Number of Observations");
ylabel("Bias");
legend("\lambda = " + lambda(1), "\lambda = " + lambda(2), "\lambda = "
 + lambda(3));
subplot(1,2,2);
plot(observation, bias_ray1, observation,
bias_ray2,observation,bias_ray3);
title("Rayleigh Bias");
xlabel("Number of Observations");
ylabel("Bias");
legend("\alpha = " + alpha(1), "\alpha = " + alpha(2), "\alpha = " +
 alpha(3));
%plot the variance for exponential and rayleigh distributions
figure;
subplot(1,2,1);
plot(observation, var_expl, observation, var_exp2, observation,
var_exp3);
title("Exponential Variance");
xlabel("Number of Observations");
ylabel("Variance");
legend("\lambda = " + lambda(1), "\lambda = " + lambda(2),"\lambda = "
 + lambda(3));
subplot(1,2,2);
plot(observation, var ray1, observation,
var_ray2,observation,var_ray3);
title("Rayleigh Variance");
xlabel("Number of Observations");
ylabel("Variance");
legend("\alpha = " + alpha(1), "\alpha = " + alpha(2), "\alpha = " +
 alpha(3));
```





Part 2

```
load data.mat;
data1 = data.';
[~, size] = size(data);
                         %get the size of data
%calculate the ML estimators
alphaEstimator = sqrt(.5 * mean(data.^2, 2));
lambdaEstimator = size./sum(data,2);
*get the sum of log likelihoods for exponential and rayleigh
distribution
%the pdf of an exponential distribution is given as lambdaEstimator *
exp(-lambdaEstimator * data1
%the pdf of a Rayleigh distribution is given as data1/
alphaEstimator^2 .*
%exp(-data1.^2/(2*alphaEstimator^2))
exponentialLikelihood=sum(log(lambdaEstimator * exp(-lambdaEstimator *
data1)));
rayleighLikelihood= sum(log(data1/alphaEstimator^2 .* exp(-data1.^2/
(2*alphaEstimator^2))));
disp("The sum of log likelihoods for exponential distribution is "
 +exponentialLikelihood)
```

```
disp("The sum of log likelihoods for rayleigh distribution is
 "+rayleighLikelihood)
The log likelihood value measures how well a model fits. The higher
the value, the better
%the fit is. Since the rayleigh distribution has a higher likelihood,
the data was most
*likely drawn from a rayleigh distribution.
function [mse, bias, variance] = rayleigh_mse_bias_variance(N,i,alpha)
   random draws
   avg=mean(rayleigh.^2,2);
   alpha2 = sqrt(.5 * avg);
                               %ML estimator
   mse= mean((alpha - alpha2).^2);
                              %get MSE
   variance = var(alpha2);
                            %get variance
end
function [mse, bias, variance] =
exponential_mse_bias_variance(N,i,lambda)
   exponential = exprnd(1/lambda, [N i]); %getting i samples with
random draws
   add=sum(exponential,2);
   lambda2 =i ./ add;
                              %ML estimator
   variance = var(lambda2);
                                %get the variance
end
The sum of log likelihoods for exponential distribution is 1053.4625
The sum of log likelihoods for rayleigh distribution is 1365.5161
```

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