LINEAR WAVE THEORY WITH SNELL'S LAW

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LINEAR WAVE THEORY WITH SNELL'S LAW

DESCRIPTION

This application provides a simple estimate for wave shoaling and refraction using Snell's law with wave properties predicted by linear wave theory. Given wave properties and a crest angle at a known depth, it predicts the values in deep water and at a subject location specified by a new water depth. An important assumption for this application is that all depth contours are assumed to be straight and parallel. The criteria of Singamsetti and Wind (1980) and Weggel (1972) are employed to provide an estimate for breaker parameters.

INPUT

The coordinate system and terminology used to define wave motion and Snell's law are shown in Figures 3-1-1 and 3-1-2.

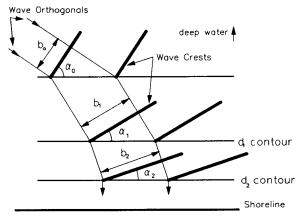


Figure 3-1-1. Snell's Law and Wave Refraction

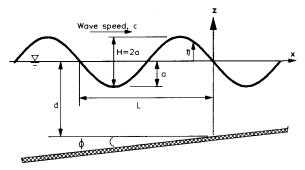


Figure 3-1-2. Progressive Wave on a Nearshore Slope

> All data input for this application is done on one screen. The following list describes the necessary input parameters with their corresponding units and range of data recognized by this application:

Location	<u>Item</u>	<u>Symbol</u>	<u>Units</u>	Data Range		inge
Known	Wave height	H_{1}	ft, m	0.1	to	200.0
	Wave period	T	sec	1.0	to	1000.0
	Water depth	d_1	ft, m	0.1	to	5000.0
	Wave crest angle	α_1	deg	0.0	to	90.0
	Cotan of nearshore slope	cotф		5.0	to	1000.0
Subject	Water depth	d_{2}	ft, m	0.1	to	5000.0

OUTPUT

Results from this application are displayed on one screen. Those data include the original input values (in final units) and the following parameters:

Wave Location						
<u>Item</u>	<u>Known</u>	<u>Deep</u>	<u>Subject</u>	<u>English</u>	<u>Metric</u>	
		<u>Water</u>		<u>Units</u>	<u>Units</u>	
Wave height	H_{1}	H_{0}	H_{2}	ft	m	
Wave crest angle	α_1	α_{o}	α_2	deg	deg	
Wavelength	L_1	L_{0}	L_{2}	ft	m	
Wave celerity	c_1	c_{0}	c_{2}	ft/sec	m/sec	
Group velocity	$C_{\mathbf{g}1}$	$C_{\mathbf{g0}}$	$C_{\mathbf{g2}}$	ft/sec	m/sec	
Energy density	$\boldsymbol{E_1}$	E_{0}	E_{2}	ft-lb/ft²	$N-m/m^2$	
Energy flux	P_1	P_{0}	P_{2}	ft-lb/sec-ft	N-m/sec-m	
Deepwater wave steepness		H_0/L_0				
Ursell number	$\frac{H_1L_1^2}{d_1^3}$		$\frac{H_2L_2^2}{d_2^3}$			

Breaker parameters			
<u>Item</u>	<u>Symbol</u>	English	<u>Metric</u>
		<u>Units</u>	<u>Units</u>
Height	и	£+	m

PROCEDURE

The bulleted items in the following lists indicate potentially optional instruction steps. Any application in ACES may be executed in a given session without quitting the program. The bulleted items provide instructions for accessing the application from various menu areas of the ACES program. Ignore bulleted instruction steps that are not applicable.

Single Case Mode

- Press [F1] on the Main Menu to select Single Case Mode.
- Fill in the highlighted input fields on the General Specifications screen (or leave the default values). Press F1 when all data on this screen are correct.
- ° Press [F3] on the Functional Area Menu to select Wave Transformation.
- ° Press F1 on the Wave Transformation Application Menu to select Linear Wave Theory with Snell's Law.
- 1. Fill in the highlighted input fields on the Linear Wave Theory with Snell's Law screen. Respond to any corrective instructions appearing at the bottom of the screen. Press [F1] when all data on this screen are correct.
- 2. All input and output data are displayed on the screen in the final system of units.
- 3. Press one of the following keys to select the appropriate action:
 - (F1) Return to Step 1 for a new case.
 - F3 Send a summary of this case to the print file or device.
 - Exit this application and return to the Wave Transformation Application Menu.

Multiple Case Mode

- ° Press [F2] on the Main Menu to select Multi Case Mode.
- ° Fill in the highlighted input fields on the General Specifications screen (or leave the default values). Press F1 when all data on this screen are correct.
- ° Press F3 on the Functional Area Menu to select Wave Transformation.
- Press F1 on the Wave Transformation Application Menu to select Linear Wave Theory with Snell's Law.

1. Move the cursor to select a variable on the Linear Wave Theory with Snell's Law screen (the selected variable name blinks). The current set of values for the variable is displayed on the right portion of the screen. When all variable sets are correct, go to Step 3.

- 2. Enter a set of values for the subject variable by following one of the input methods:
 - a. Press (R) to select random method. Enter up to 20 values constituting a set for this variable (one in each field) on the right side of the screen. The set of 20 values originally displayed (first execution) in these fields contains the "delimiting" value, which "delimits" or "ends" the set. The "delimiting" value is not included as a member in the set unless it is the sole member.
 - b. Press 1 to select incremental method. Fill in the fields for minimum, maximum, and increment values for this variable on the right side of the screen. In this method, the members of the set include all values from the minimum to the maximum (both inclusive) at the specified increment.

The units field should also be specified for the variable regardless of input method. All members of a set of values for a subject variable are assigned the specified units. When all data are correct for the subject variable, press F10 to return to Step 1. Errors are reported at the bottom of the screen and are corrected by pressing F1 to allow respecification of the data for the subject variable.

- 3. Press F1 to process the cases resulting from the combinations of the sets of data for all variables. The summary of each case will be sent to the print file or device. The screen will display the total number of cases to be processed as well as report progress. Errors are reported at the bottom of the screen and are corrected by pressing F1 to allow respecification of variable sets.
- 4. Press one of the following keys to select the appropriate action:
 - (F1) Return to Step 1 to specify new sets.
 - Exit this application and return to the Wave Transformation Application Menu.

EXAMPLE PROBLEM

Input

All data input for this application is done on one screen. The values and corresponding units selected for this example problem are shown below.

Location	<u>Item</u>	<u>Symbol</u>	<u>Value</u>	<u>Units</u>
Known	Wave height	H_{1}	10.00	ft
	Wave period	T	7.50	sec
	Water depth	d_1	25.00	ft
	Wave crest angle	α_1	10.00	deg
	Cotan of nearshore slope	cotф	100.00	
Subject	Water depth	d_{2}	20.00	ft

Output

Results from this application are displayed on one screen. Those data include the original input values and the following parameters (see Figure 3-1-3 for location of calculated parameters):

Wave Location							
<u>Item</u>	<u>Known</u>	<u>Deep</u>	<u>Subject</u>	<u>Units</u>			
		<u>Water</u>					
Wave height	10.00	10.68	10.27	ft			
Wave crest angle	10.00	15.00	9.12	deg			
Wavelength	193.27	288.00	176.34	ft			
Wave celerity	25.77	38.40	23.51	ft/sec			
Group velocity	21.46	19.20	20.31	ft/sec			
Energy density	799.83	911.50	843.04	ft-lb/ft ²			
Energy flux	17165.59	17500.84	17121.06	ft-lb/sec-ft			
Ursell number	23.91		39.91				
Deepwater wave steepness		0.04					

Dicaker parameters			
<u>Item</u>	<u>Symbol</u>	<u>Value</u>	<u>Units</u>
Height	$H_{ m b}$	12.29	ft
Depth	$d_{ m b}$	15.25	ft

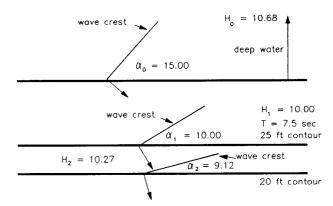


Figure 3-1-3. Snell's Law Example Output

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IRREGULAR WAVE TRANSFORMATION (GODA'S METHOD)

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IRREGULAR WAVE TRANSFORMATION (GODA'S METHOD)

DESCRIPTION

This application yields cumulative probability distributions of wave heights as a field of irregular waves propagate from deep water through the surf zone. The application is based on two random-wave theories by Yoshimi Goda (1975 and 1984). The 1975 paper concerns transformation of random waves shoaling over a plane bottom with straight parallel contours. This analysis treated breaking and broken waves and resulted in cumulative probability distributions for wave heights given a water depth. It did not include refraction, however. The 1984 book details a refraction procedure for random waves propagating over a plane bottom with straight parallel contours assuming a particular incident spectrum. This ACES application combines the two approaches by treating directional random waves propagating over a plane bottom with straight parallel contours. This application also uses the theory of Shuto (1974) for the shoaling calculation. The theories assume a Rayleigh distribution of wave heights in the nearshore zone and a Bretschneider-Mitsuyasu incident directional spectrum.

INPUT

All data input for this application is done on one screen. The following list describes the necessary input parameters with their corresponding units and range of data recognized by this application:

<u>Item</u>	<u>Symbol</u>	<u>Units</u>	Data Rai	nge
Significant deepwater wave height	H_{o}	ft m	2.00 to 0.61 to	20.0 6.09
Water depth	d	ft, m	10.00 to	5000.0
Significant wave period	$T_{\mathbf{s}}$	sec	4.00 to	16.0
Cotan of nearshore slope	coto		30.00 to	100.0
Principal direction of incident wave spectrum	θ	deg	-75.00 to	75.0

OUTPUT

Results from this application are displayed on one screen. In addition, there is an option (available in the Single Case Mode only) to send data to plot output file 1 (default name **PLOTDAT1.OUT**). This application also generates two screen plots. Each of these outputs is described below.

Screen Output

Results from this application are displayed on one screen. Those data include the original input values (in final units) and the following parameters:

<u>Item</u>	Symbol	English Units	<u>Metric</u> <u>Units</u>
Significant wave height	$H_{\mathbf{s}}$	ft	m
Mean wave height	H	ft	m
Root-mean-square wave height	$H_{ m rms}$	ft	m
Average of highest 10 percent of all waves	H_{10}	ft	m
Average of highest 2 percent of all waves	H_2	ft	m
Maximum wave height	H_{\max}	ft	m
Shoaling coefficient	$K_{\mathbf{s}}$		
Root-mean-square surf beat	ξ	ft	m
Wave setup	$S_{\mathbf{w}}$	ft	m
Deepwater wave steepness	$H_{ m o}/L_{ m o}$		
Effective refraction coefficient	$K_{\mathbf{r}}$		
Ratio of water depth to deepwater wave height	d/H_{o}		
Relative water depth	d/L_{o}		

Plot Output File 1

Plot output file 1 contains wave heights with their cumulative probability distribution of exceedance for both deep water and the specified depth and is available in Single Case Mode only. The data are written to plot output file 1 in the following format (refer to the Example Problem section for a paradigm):

Field	Columns	Format	Data
1	1-10	F10.3	Wave height in deep water
2	11-20	F10.3	Cumulative probability distribution of exceedance (CDF)
3	21-30	F10.3	Wave height in water depth of interest
4	31-40	F10.3	Cumulative probability distribution of exceedance (CDF2)

Screen Plots

This application generates two plots. These plots may be accessed by selecting the **Plot Data** option (F2) from the **Options** menu on the data output screen. The plots generated are shown in Figures 3-2-1 and 3-2-2 in the example problem below. The first plot displayed is the cumulative probability distribution of exceedance (CDF) versus wave height in deep water. The second plot is the CDF versus wave height in water depth of interest.

PROCEDURE

The bulleted items in the following lists indicate potentially optional instruction steps. Any application in ACES may be executed in a given session without quitting the program. The bulleted items provide instructions for accessing the application from various menu areas of the ACES program. Ignore bulleted instruction steps that are not applicable.

Single Case Mode

- Press (F1) on the Main Menu to select Single Case Mode.
- Fill in the highlighted input fields on the General Specifications screen (or leave the default values). Press F1 when all data on this screen are correct.
- ° Press F3 on the Functional Area Menu to select Wave Transformation.
- ° Press F2 on the Wave Transformation Application Menu to select Goda's Wave Transformation.
- 1. Fill in the highlighted input fields on the Goda's Wave Transformation screen. Respond to any corrective instructions appearing at the bottom of the screen. Press F1 when all data on this screen are correct.
- All input and output data are displayed on the screen in the final system of units.
- 3. Press one of the following keys to select the appropriate action:

- F1 Return to Step 1 for a new case.
- F2 Plot the data.
- F3 Send a summary of this case to the print file or device.
- Generate a file containing plot data (cumulative probability versus wave height).
- Exit this application and return to the Wave Transformation Application Menu.

Multiple Case Mode

- ° Press F2 on the Main Menu to select Multi Case Mode.
- ° Fill in the highlighted input fields on the General Specifications screen (or leave the default values). Press F1 when all data on this screen are correct.
- ° Press [F3] on the Functional Area Menu to select Wave Transformation.
- ° Press F2 on the Wave Transformation Application Menu to select Goda's Wave Transformation.
- 1. Move the cursor to select a variable on the Goda's Wave Transformation screen (the selected variable name blinks). The current set of values for the variable is displayed on the right portion of the screen. When all variable sets are correct, go to Step 3.
- 2. Enter a set of values for the subject variable by following one of the input methods:
 - a. Press R to select random method. Enter up to 20 values constituting a set for this variable (one in each field) on the right side of the screen. The set of 20 values originally displayed (first execution) in these fields contains the "delimiting" value, which "delimits" or "ends" the set. The "delimiting" value is not included as a member in the set unless it is the sole member.
 - b. Press 1 to select incremental method. Fill in the fields for minimum, maximum, and increment values for this variable on the right side of the screen. In this method, the members of the set include all values from the minimum to the maximum (both inclusive) at the specified increment.

The units field should also be specified for the variable regardless of input method. All members of a set of values for a subject variable are assigned the specified units. When all data are correct for the subject variable, press F10 to return to Step 1. Errors are reported at the bottom of the screen and are corrected by pressing F1 to allow respecification of the data for the subject variable.

3. Press F1 to process the cases resulting from the combinations of the sets of data for all variables. The summary of each case will be sent to the print file or device. The screen will display the total number of cases to be processed as well as report progress. Errors are reported at the bottom of the screen and are corrected by pressing F1 to allow respecification of variable sets.

- 4. Press one of the following keys to select the appropriate action:
 - F1 Return to Step 1 to specify new sets.
 - Exit this application and return to the Wave Transformation Application Menu.

NOTE: Multiple Case Mode does not generate any plot output files or plots.

EXAMPLE PROBLEM

Input

All data input for this application is done on one screen. The values and corresponding units selected for this example problem are shown below.

<u>Item</u>	Symbol	<u>Value</u>	<u>Units</u>
Significant deepwater wave height	H_{o}	20.00	ft
Water depth	d	50.00	ft
Significant wave period	$T_{\mathbf{s}}$	8.00	sec
Cotan of nearshore slope	cotφ	100.00	
Principal direction of incident wave spectrum	θ	10.00	deg

Output

Results from this application are displayed on one screen and, if requested, written to plot output file 1 (default name **PLOTDAT1.OUT**). In addition, two plots are generated. Each of these outputs for the example problem is presented below.

Screen Output

Results from this application are displayed on one screen. Those data include the original input values and the following parameters:

<u>Item</u>	<u>Symbol</u>	Subject	Deep Water	<u>Units</u>
Significant wave height	$H_{\mathbf{s}}$	17.7	20.1	ft
Mean wave height	Н	11.2	12.5	ft
Root-mean-square wave height	$H_{ m rms}$	12.5	14.1	ft
Average of highest 10 percent of all waves	H_{10}	22.5	27.0	ft
Average of highest 2 percent of all waves	H_2	26.7	32.1	ft
Maximum wave height	$H_{ m max}$	30.1	37.6	ft
Shoaling coefficient	$K_{\mathbf{g}}$	0.9133	1.0000	
Root-mean-square surf beat	ξ	0.4350	0.1766	ft
Wave setup	$S_{\mathbf{w}}$	-0.0763	-0.0218	ft
Deepwater wave steepness	$H_{\rm o}/L_{\rm o}$	0.0611	0.0611	
Effective refraction- coefficient	$K_{\mathbf{r}}$	0.9638		
Ratio of water depth to deepwater wave height	$d/H_{\rm o}$	2.4655	20.0000	
Relative water depth	d/L_{o}	0.1505	1.2212	

Plot Output File 1

Table 3-2-1 below is a partial listing of plot output file 1 generated by this application.

Table 3-2-1
Wave Height versus Cumulative Probability
Distribution of Exceedance

Deep	Water	Water De	epth = 50 ft
H (ft)	CDF	H (ft)	CDF2
0.328	0.001	0.328	0.001
0.656	0.004	0.656	0.003
0.984	0.007	0.984	0.007
1.312	0.011	1.312	0.012
1.640	0.017	1.640	0.018
1.968	0.023	1.968	0.026
2.296	0.030	2.296	0.034
2.624	0.039	2.624	0.044
2.952	0.048	2.952	0.055
3.280	0.058	3.280	0.067
1		1	1
26.240	0.970	26.240	0.995
26.568	0.972	26.568	0.996
26.896	0.975	26.896	0.997
27.224	0.977	27.224	0.998
27.552	0.979	27.552	0.998
27.880	0.981	27.880	0.999
28.208	0.982		
28.536	0.984		
28.864	0.985		
29.192	0.987		
1	#		
33.784	0.997		
34.112	0.997		
34.440	0.998		
34.768	0.998		
35.096	0.998		
35.424	0.998		
35.752	0.998		
36.080	0.999		
36.408	0.999		
36.736	0.999		

Screen Plots

This application generates two plots. These plots may be accessed by selecting the **Plot Data** option (F2) from the **Options** menu on the data output screen. The plots generated for the example problem are shown in Figures 3-2-1 and 3-2-2 below. The first plot displayed is the cumulative probability distribution of exceedance (CDF) versus wave height in deep water. The second plot is the CDF versus wave height in water depth of interest. After viewing the first plot, the second plot may be displayed by selecting the **NEXT** option in the graphics package (see Appendix C).

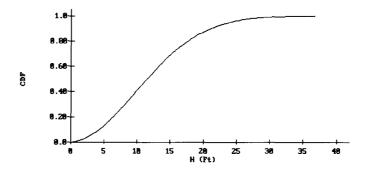


Figure 3-2-1. Wave Height versus Cumulative Probability Distribution of Exceedance (Deep Water)

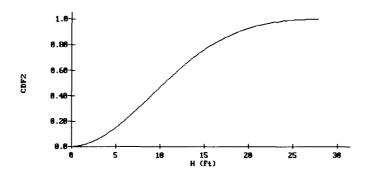


Figure 3-2-2. Wave Height versus Cumulative Probability Distribution of Exceedance (Water Depth = 50 ft)

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COMBINED DIFFRACTION AND REFLECTION BY A VERTICAL WEDGE

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COMBINED DIFFRACTION AND REFLECTION BY A VERTICAL WEDGE

DESCRIPTION

This application estimates wave height modification due to combined diffraction and reflection near jettied harbor entrances, quay walls, and other such structures. Jetties and breakwaters are approximated as a single straight, semi-infinite breakwater by setting the wedge angle to zero. Corners of docks and quay walls may be represented by setting the wedge angle equal to 90 deg. Additionally, such natural diffracting and reflecting obstacles as rocky headlands can be approximated by setting a particular value for the wedge angle. Assumptions include monochromatic, linear waves, and constant water depth.

COORDINATE SYSTEM

The coordinate system and terminology used in the diffraction and reflection by a vertical wedge is shown in Figure 3-3-1.

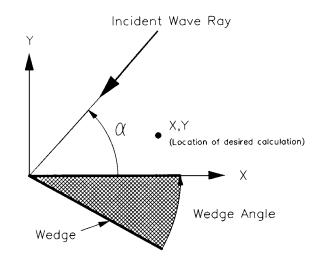


Figure 3-3-1. Diffraction/Reflection by Vertical Wedge System

PROCEDURE

This section provides instructions for running this application in the Single Case and Multiple Case modes.

Single Case Mode

- ° Press [F1] on the Main Menu to select Single Case Mode.
- ° Fill in the highlighted input fields on the General Specifications screen (or leave the default values). Press F1 when all data on this screen are correct.
- ° Press F3 on the Functional Area Menu to select Wave Transformation.
- ° Press F3 on the Wave Transformation Application Area Menu to select Combined Diffraction and Reflection by a Vertical Wedge.

In Single Case mode, this application allows two options for calculating a modification factor and modified wave height.

- ° At a single location.
- Upon a uniform grid.

From the Activity Menu, select either the Single Location or Uniform Grid option. These two options are described below.

F1 Evaluate at a Single Location

All data input for this option is done on one screen. The following list describes the necessary input parameters with their corresponding units and range of data recognized by this application:

<u>Item</u>	<u>Symbol</u>	<u>Units</u>	Data Range		ge
Incident Wave Height	H_{i}	ft,m	0.1	to	200
Wave Period	T	sec	1	to	1000

Water Depth	d	ft,m	0.01	to	5000
Wave Angle	α	deg	0	to	180
Wedge Angle		deg	0	to	180
X Coordinate	X	ft,m	-5280	to	5280
Y Coordinate	Y	ft,m	-5280	to	5280

NOTE: In practice, the range for X and Y should be limited to plus or minus 10 wavelengths.

When all the data have been entered press, F1 to begin calculations. When calculations have been completed, all input and output data are displayed on the screen in the selected system of units. Output data include the following parameters:

<u>Item</u>	<u>Symbol</u>	English Units	Metric Units
Wave Length	L	ft	m
Modification Factor (ratio of calculated wave height to incident wave height)	ф		
Wave Phase	β	rad	rad
Modified Wave Height	Н	ft	m

After data have been displayed, press one of the following keys to select the appropriate action:

- F1 Return to Step 1 for a new case.
- F3 Send a summary of this case to the print file or device.
- (F10) Exit this application and return to the Activity Menu.

F2 Evaluate Upon a Uniform Grid

All data input for this option is done on one screen. The following list describes the necessary input parameters with their corresponding units and range of data recognized by this application:

<u>Item</u>	<u>Symbol</u>	<u>Units</u>	Dat	a Rar	<u>ige</u>
Incident Wave Height	H_{i}	ft,m	0.1	to	200
Wave Period	T	sec	1	to	1000
Water Depth	d	ft,m	0.01	to	5000
Wave Angle	α	deg	0	to	180
Wedge Angle		deg	0	to	180
X Start Coordinate	X_{0}	ft,m	-5280	to	5280
X End Coordinate	X_{m}	ft,m	-5280	to	5280
Spatial Increment (X-direction)	ΔX		0.1	to	5280
Y Start Coordinate	Y_{0}	ft,m	-5280	to	5280
Y End Coordinate	Y_{m}	ft,m	-5280	to	5280
Spatial Increment (Y-direction)	ΔY		0.1	to	5280

CAUTION: For the application to function properly, the **Start Coordinate** for both the X- and Y-directions **must** be *less than* the corresponding End Coordinate.

When all the data have been entered, press [1] to begin calculations. When calculations have been completed, all input and output data are sent to the print file or device and also to plot output file 1 (default name **PLOTDAT1.OUT**). See the section titled Plot Output File 1 for the description and format of the contents of plot output file 1.

After calculations have been completed, press one of the following keys to select the appropriate action:

- F1 Return to Step 1 for a new case.
- F10 Exit this application and return to the Activity Menu.

Plot Output File 1

Plot output file 1 (default name **PLOTDAT1.OUT**) contains the Modification Factors, Modified Wave Heights, and Wave Phase differences between the incident and the modified waves at the grid points defined by the X and Y start and end coordinates. Plot output file 1 is written in the following format (see Table 3-3-2 in Example Problem 3):

Field	Columns	Format	Data
1	1-10	G10.3	X-coordinate
2	11-20	G10.3	Y-coordinate
3	21-30	G10.3	Modified wave height
4	31-40	G10.3	Modification factor
5	41-50	G10.3	Wave phase difference

Multiple Case Mode

- ° Press F2 on the Main Menu to select Multi Case Mode.
- Fill in the highlighted input fields on the General Specifications screen (or leave the default values). Press F1 when all data on this screen are correct.
- ° Press [F3] on the Functional Area Menu to select Wave Transformation.
- ° Press F3 on the Wave Transformation Application Menu to select Combined Diffraction and Reflection by a Vertical Wedge.
- 1. Move the cursor to select a variable on the Combined Diffraction and Reflection by a Vertical Wedge screen (the selected variable name blinks). The current set of values for the variable is displayed on the right portion of the screen. When all variable sets are correct, go to Step 3.
- 2. Enter a set of values for the subject variable by following one of the input methods:

a. Press R to select random method. Enter up to 20 values constituting a set for this variable (one in each field) on the right side of the screen. The set of 20 values originally displayed (first execution) in these fields contains the "delimiting" value, which "delimits" or "ends" the set. The "delimiting" value is not included as a member in the set unless it is the sole member.

b. Press 1 to select incremental method. Fill in the fields for minimum, maximum, and increment values for this variable on the right side of the screen. In this method, the members of the set include all values from the minimum to the maximum (both inclusive) at the specified increment.

The units field should also be specified for the variable regardless of input method. All members of a set of values for a subject variable are assigned the specified units. When all data are correct for the subject variable, press F10 to return to Step 1. Errors are reported at the bottom of the screen and are corrected by pressing F1 to allow respecification of the data for the subject variable.

- 3. Press [F1] to process the cases resulting from the combinations of the sets of data for all variables. The summary of each case will be sent to the print file or device. The screen will display the total number of cases to be processed as well as report progress. Errors are reported at the bottom of the screen and are corrected by pressing [F1] to allow respecification of variable sets.
- 4. Press one of the following keys to select the appropriate action:
 - F1 Return to Step 1 to specify new sets.
 - Exit this application and return to the Wave Transformation Application Menu.

EXAMPLE PROBLEMS

Example 1 - Semi-Infinite Breakwater (Single Point)

Input

All data input for this application is done on one screen. The values and corresponding units selected for this first example problem are shown below.

<u>Item</u>	<u>Symbol</u>	<u>Value</u>	<u>Units</u>
Incident Wave Height	H_{i}	2.0	ft
Wave Period	T	6.0	sec
Water Depth	d	12.0	ft
Wave Angle	α	135.0	deg
Wedge Angle		0.0	deg
X Coordinate	X	35.0	ft
Y Coordinate	Y	-17.0	ft

Output

Results from this application are displayed on one screen. These data include the original input values and the following parameters (see Figure 3-3-2):

<u>Item</u>	<u>Symbol</u>	<u>Value</u>	<u>Units</u>
Wave Length	L	109.82	ft
Modification Factor (ratio of calculated wave height to incident wave height)	ф	0.58	
Wave Phase	β	-2.58	rad
Modified Wave Height	H	1.16	ft

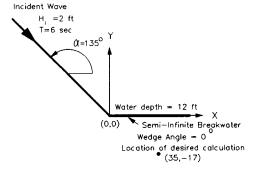


Figure 3-3-2. Semi-Infinite Breakwater Diffraction/Reflection Example Output

Example 2 - 90-Deg Wedge (Single Point)

Input

All data input for this application is done on one screen. The values and corresponding units selected for this second example problem are shown below.

<u>Item</u>	<u>Symbol</u>	<u>Value</u>	<u>Units</u>
Incident Wave Height	H_{i}	5	m
Wave Period	T	8	sec
Water Depth	d	10	m
Wave Angle	α	47	deg
Wedge Angle		90	deg
X Coordinate	X	-10	m
Y Coordinate	Y	-40	m

Output

Results from this application are displayed on one screen. These data include the original input values and the following parameters (see Figure 3-3-3):

<u>Item</u>	<u>Symbol</u>	<u>Value</u>	<u>Units</u>
Wave Length	L	70.88	m
Modification Factor (ratio of calculated wave height to incident wave height)	ф	0.60	
Wave Phase	β	2.12	rad
Modified Wave Height	H	3.01	m

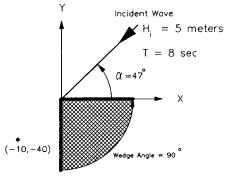


Figure 3-3-3. 90-Deg Wedge Diffraction/Reflection Example Output

Example 3 - Semi-Infinite Breakwater (Uniform Grid)

Input

All data input for this application is done on one screen. The values and corresponding units selected for this second example problem are shown below (see Figure 3-3-4).

<u>Item</u>	Symbol Symbol	Value	<u>Units</u>
Incident Wave Height	H_{i}	4	ft
Wave Period	T	12	sec
Water Depth	d	30	ft
Wave Angle	α	52	deg
Wedge Angle		0	deg
X Start Coordinate	X_{o}	-600	ft
X End Coordinate	X_{m}	200	ft
Spatial Increment (X-direction)	ΔX	200	ft
Y Start Coordinate	Y_{o}	-400	ft
Y End Coordinate	Y_{m}	200	ft
Spatial Increment (Y-direction)	ΔY	100	ft

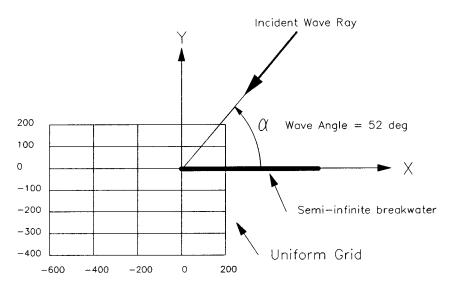


Figure 3-3-4. Semi-Infinite Breakwater Diffraction/Reflection (uniform grid)

Output

Results from this application are sent to the print file or device (see Table 3-3-1) and to plot output file 1 (default name **PLOTDAT1.OUT**) (see Table 3-3-2).

Print File or Device

Table 3-3-1 Combined Reflection and Diffraction by a Vertical Wedge

	t Wave Height	= 4.0		Wave Period	=	12.00 sec	
Water	-	= 30.0		Wavelength	=	356.85 ft	
Wave A	Angle	= 52.0	0 deg	Wedge Angle	=	0.00 deg	3
*****	Modification Fa	ctors:					
	x =	-600.00	-400.00	-200.00	0.00	200.00	
y =	200.00	1.00	1.15	1.27	1.67	1.88	
y=	100.00	1.04	1.00	0.83	0.74	0.20	
y=	0.00	1.00	1.00	1.00	1.00	1.77	
y=	-100.00	1.04	1.03	0.86	0.46	0.23	
y=	-200.00	1.06	0.93	0.66	0.37	0.22	
y=	-300.00	1.00	0.80	0.53	0.32	0.21	
y==	-400.00	0.90	0.67	0.44	0.28	0.20	
	x=	-600.00	400.00	~ - _2 00.00	0.00	<u>2</u> 00.00	
*****]	Modified Wave	Heights (ft):				
	x =	-600.00	-400.00	-200.00	0.00	200.00	
y =	200.00	4.02	4.59	5.07	6.68	7.52	
y=	100.00	4.17	4.00	3.33	2.96	0.81	
y=	0.00	4.00	4.00	4.00	4.00	7.08	
y=	-100.00	4.17	4.10	3.42	1.84	0.92	
y=	-200.00	4.25	3.74	2.66	1.48	0.88	
y=	-300.00	4.02	3.19	2.12	1.27	0.84	
y=	-400.00	3.61	2.68	1.77	1.14	0.80	
	x=	-6ō0.0ō	400.00	200.00	- 0.00	200.00	
***** Phase Angles (rad):							
•	x=	-600.00	-400.00	-200.00	0.00	200.00	
y =	200.00	2.47	-1.60	ö. 7 9	-2.97	-1.09	
, y≕	100.00	1.18	-2.87	-0.75	0.52	2.77	
y=	0.00	-0.22	1.95	-2.17	0.00	2.18	
y=	-100.00	-1.61	0.63	2.82	-2.22	1.64	
y=	-200.00	-2.93	-0.68	1.34	2.22	0.60	
y=	-300.00	2.04	-2.07	-0.27	0.42	-0.77	
y=	-400.00	0.69	2.75	-1.94	-1.37	-2.30	
•	x=	-600.00	400.00	200.00	0.00	<u>200</u> .00	

Plot Output File 1

Plot output file 1 (default name **PLOTDAT1.OUT**) contains at grid points defined by the X and Y start and end coordinates the Modified Wave Heights, Modification Factors, and Wave Phase differences between the incident and modified waves. Table 3-3-2 is a listing of plot output file 1 for Example 3.

Table 3-3-2
Listing of Plot Output File 1 for Example Problem 3

Combined Refl	ection and Diffra	action by a Vert	ical Wedge	
Wedge Angle:	0 Inciden	t Wave Angle:	52	
ft	ft	ft		rad
-600.	- 400 .	3.61	0.903	0.690
-400.	-400.	2.68	0.670	2.75
-200 .	-400.	1.77	0.442	-1.94
0.000	-400 .	1.14	0.285	-1.37
200.	-400.	0.804	0.201	-2.30
-600.	-300.	4.02	1.00	2.04
-400.	-300.	3.19	0.798	-2.07
-200.	-300.	2.12	0.531	-0.273
0.000	- 300 .	1.27	0.319	0.419
200.	-300.	0.843	0.211	-0.772
-600.	-200 .	4.25	1.06	-2.93
-400.	- 200 .	3.74	0.934	-0.684
-200 .	- 2 00.	2.66	0.665	1.34
0.000	- 2 00.	1.48	0.369	2.22
200.	- 2 00.	0.882	0.221	0.599
-600.	-100.	4.17	1.04	-1.61
-400.	-100.	4.10	1.03	0.629
-200 .	-100.	3.42	0.856	2.82
0.000	-100.	1.84	0.460	-2.22
200.	-100.	0.916	0.229	1.64
-600.	0.000	4.00	1.00	-0.221
-400 .	0.000	4.00	1.00	1.95
- 200 .	0.000	4.00	1.00	-2.17
0.000	0.000	4.00	1.00	0.000
200.	0.000	7.08	1.77	2.18
-600.	100.	4.17	1.04	1.18
-400.	100.	4.00	1.00	-2.87
-200 .	100.	3.33	0.833	-0.754

(Table 3-3-2 Continued on the Next Page)

	(Table 3-	3-2 Conclud	ied)	
0.000	100.	2.96	0.740	0.517
200.	100.	0.809	0.202	2.77
-600.	200.	4.02	1.00	2.47
-400.	200.	4.59	1.15	-1.60
- 20 0.	200.	5.07	1.27	0.787
0.000	200.	6.68	1.67	-2.97
200	200	7.52	1.88	-1.09

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