

# Musical Tapestry: Re-composing Natural Sounds

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## Abstract

*A system to aid composition with analysis, transformation, and resynthesis of natural sounds is described. Sinusoidal analysis is used to isolate and extract deterministic sounds, and transients are also isolated/extracted, leaving the stochastic background sound which is parameterized by wavelet tree analysis. All of these components become templates for the synthesis phase, which is controlled 1) by placing templates on timelines or in groups, 2) by real-time manipulation of parameters, and 3) via scripting using the ChucK language. The result is a flexible “workbench” for doing modern day musique concrète or acousmatic composition, sound design, and other sonic sculpting tasks.*

## 1 Motivation

Around 1950, Pierre Schaeffer developed *musique concrète* (Schaeffer 1950; Schaeffer 1952). Unlike traditional music, *musique concrète* starts with existing or concrete recorded sounds, which are organized into abstract musical structures. The existing recordings often include natural and industrial sounds that are not conventionally musical, but can be manipulated to make music, either by editing magnetic tape or now more commonly through digital sampling. Typical manipulations include cutting, copying, reversing, looping and changing the speed of recorded segments.

Today, several other forms of electronic/electroacoustic music also involve manipulating a set of recorded sounds. Acousmatic music (Dhomont 1995), for instance, evolved from *musique concrète* and refers to compositions designed for environments that emphasize the sound itself rather than the performance-oriented aspects of the piece.

The acoustic ecology (Schafer 1977) movement gave rise to soundscape composition (Truax 2002) or the creation of realistic soundscapes from recorded environmental audio. One of the key features of soundscape composition, according to Truax, is that “most pieces can be placed on a continuum between what might be called ‘found sound’ and ‘abstracted’ approaches.” However, while “contemporary signal processing techniques can easily render such sounds unrecognizable

and completely abstract,” a soundscape composition piece is expected to remain recognizable even at the abstract end of the continuum.

Sound designers for movies, theater and art often have a related goal of starting with real world sounds and creating emotionally evocative sound scenes, which are still real, yet transformed and transformative. Classic examples include mixing a transformed lion’s roar with other sounds to accompany the wave sounds in *The Perfect Storm*, and incorporating a helicopter theme into the sound design for *Black Hawk Down* (Rudy 2004). These sound designers are “sound sculptors” as well, but transform sounds to enhance or create a sense of reality, rather than for purely musical purposes.

Artists from all of the above backgrounds share the process of manipulating recordings, but aim to achieve different effects. We present a single framework for starting with recordings and producing sounds that can lie anywhere on a ‘found’ to ‘unrecognizable’ continuum. ‘Found’ sounds can be modified in subtle ways or extended indefinitely, while moving towards the ‘unrecognizable’ end of the spectrum unleashes a range of manipulations beyond time-domain techniques. In fact, the same set of techniques apply throughout the continuum, differing only in how they are used. We call this framework TAPESTREA: Techniques and Paradigms for Expressive Synthesis, Transformation and Rendering of Environmental Audio.

TAPESTREA integrates sinusoidal analysis, stochastic background modeling, transient detection, and a new class of user interface that lends itself to any composition that originates in recorded environmental audio. This envelopes a novel form of *musique concrète* that extends to manipulations in the frequency as well as time domain. Advantages of the TAPESTREA approach include:

- TAPESTREA allows the sound sculptor to select a region in both time and frequency, essentially specifying, “Give me *this* part of *that* sound,” to extract a reusable *sound template*. While existing techniques based on manipulating recordings are often time-domain-centric, with even spectrally oriented tools like the phase vocoder supporting only moderate transformations, TAPESTREA leverages sinusoidal

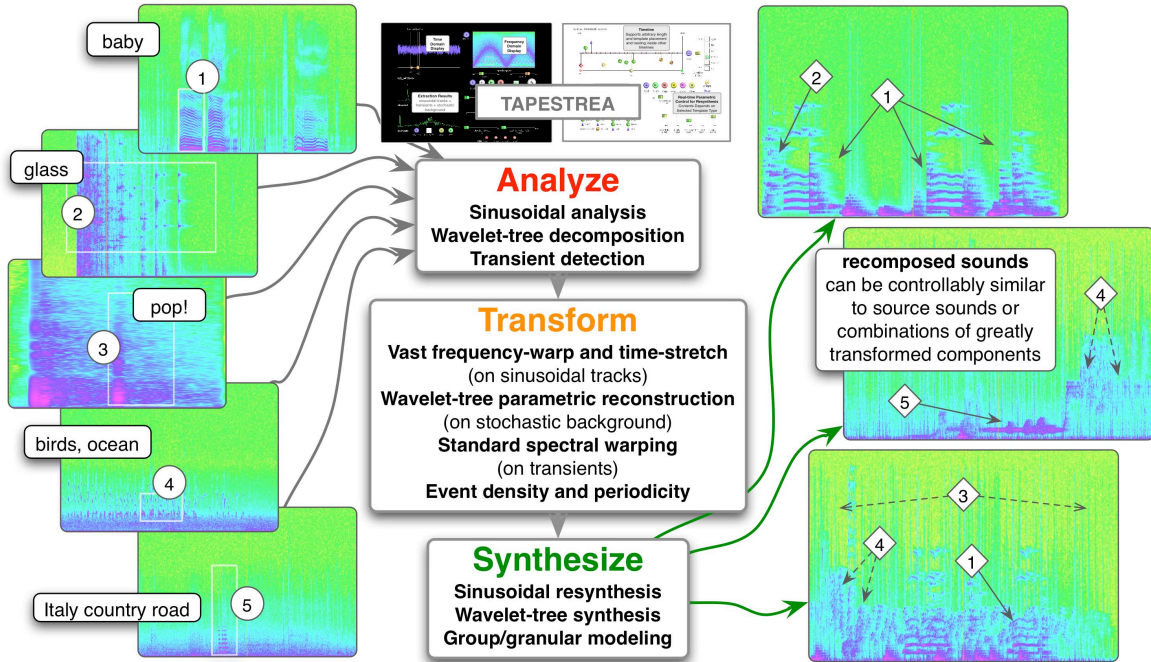


Figure 1: **Creating musical tapestries.** User-selected regions of input sounds (left) are analyzed into reusable templates, which are separately transformed and resynthesized into new sounds (right). Numbered diamonds (right) correspond to instances of original sound components (circled, left). The framework allows flexible control at every stage in the process.

modeling to enable high-quality, potentially extreme, time and frequency transformations on appropriate template types.

- TAPESTREA defines three fundamental types of sound components, based on the modeling techniques for which they are best suited. *Deterministic* (sinusoidal), *transient*, and *stochastic background* components are modeled separately, using methods to which they are most amenable, leading to specialized control and more powerful transformations on each type.
- To realize these ideas, TAPESTREA provides a set of interfaces that allow the sound designer or composer to assert parametric control over each phase in the process, from component extraction to the final resynthesis.

TAPESTREA manipulates recorded sounds in two phases. In the analysis phase, the sound is separated into reusable components that map to individual foreground events or background. In the synthesis phase, these components are transformed, combined and re-synthesized using time- and frequency-domain techniques that can be controlled on multiple levels. While we highlight the synthesis methods here, the analysis phase is also integral as it enables the most flexible means for dealing with real-world sonic material.

## 2 Related Work

Related techniques used for musical composition include spectral modeling synthesis (Serra 1989) and granular synthesis (Truax 1990; Roads 2002). Spectral modeling synthesis separates a sound into sinusoids and noise, and was originally used for modeling instrument sounds. Granular synthesis, in contrast, functions in the time-domain and involves continuously controlling very brief sonic events or sound grains. TAPESTREA employs aspects of both, using separation techniques on environmental sounds and controlling the temporal placement of resulting events.

Another technique used in TAPESTREA is an extension of a wavelet tree learning algorithm (Dubnov et al. 2002) for sound texture synthesis. This method performs a wavelet decomposition on a sound clip and uses machine learning on the wavelet coefficients to generate similar non-repeating sound texture. The algorithm works well for sounds that are mostly stochastic, but can break extended pitched portions in objectionable ways. It can also be slow in its original form. TAPESTREA takes advantage of this technique by improving the speed of the algorithm, and only using it on the types of (non-deterministic) sound for which it works well.

### 3 Analysis Phase

TAPESTREA starts by separating a recording into *deterministic events* or the stable sinusoidal components of the sound, *transient events* or brief noisy bursts of energy, and the remaining *stochastic background* or din. This separation can be parametrically controlled and takes place in the analysis phase.

The analysis interface is shown in the accompanying figures. A loaded sound is simultaneously displayed as a waveform and a spectrogram (Figure 2). The spectrogram display can also be toggled with a frame-by-frame spectrum view (Figure 3). Selecting a rectangle on the spectrogram, or selecting an analysis region on the waveform and the frame-by-frame spectrum, limits the analysis to the associated time and frequency ranges, facilitating the selection and extraction of specific events.

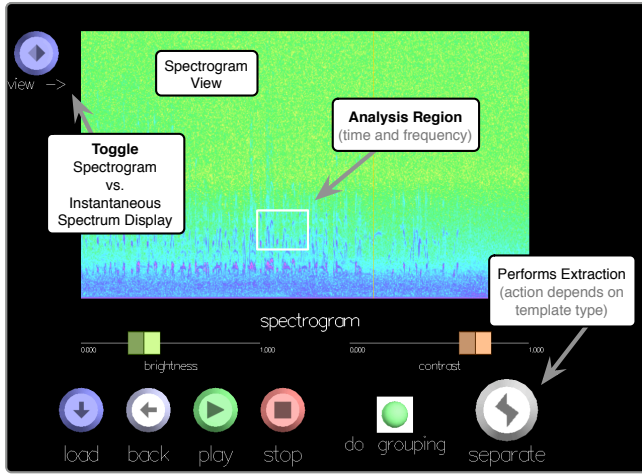


Figure 2: Spectrogram view in analysis face.

*Deterministic events* are foreground events extracted by sinusoidal modeling based on the spectral modeling framework (Serra 1989). Overlapping frames of the sound are transformed into the frequency domain using the FFT. For each spectral frame, the  $n$  highest peaks above a specified magnitude threshold (Figure 3) are recorded, where  $n$  can range from 1 to 50. These peaks can also be loaded from a preprocessed file. The highest peaks from every frame are then matched across frames by frequency, subject to a controllable “frequency sensitivity” threshold, to form sinusoidal tracks. Tracks can be “mute” (below the magnitude threshold) for a specified maximum number of frames, or can be discarded if they fail to satisfy a minimum track length requirement (Figure 4). Undiscarded tracks are optionally grouped (Ellis 1994; Melih and Gonzalez 2000) by harmonicity, common amplitude and frequency modulation, and common

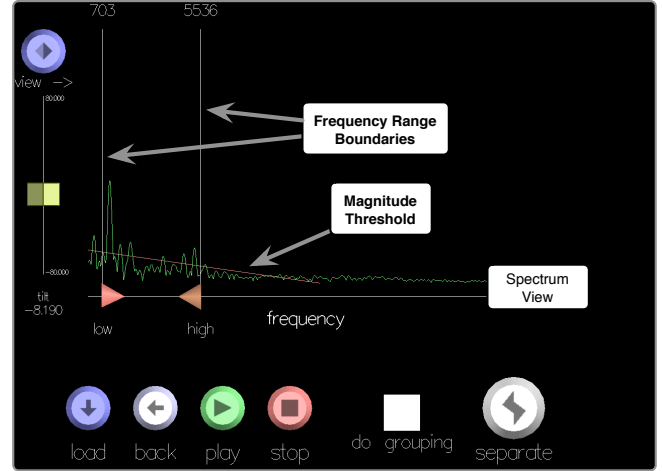


Figure 3: Spectrum view in analysis face.

onset/offset, to form deterministic events, which are essentially collections of related sinusoidal tracks. If the grouping option is not selected, each track is interpreted as a separate deterministic event. After the separation, the sinusoidal tracks found are marked on the spectrogram display. Each deterministic event can be individually played and saved as a template for use in the synthesis phase.

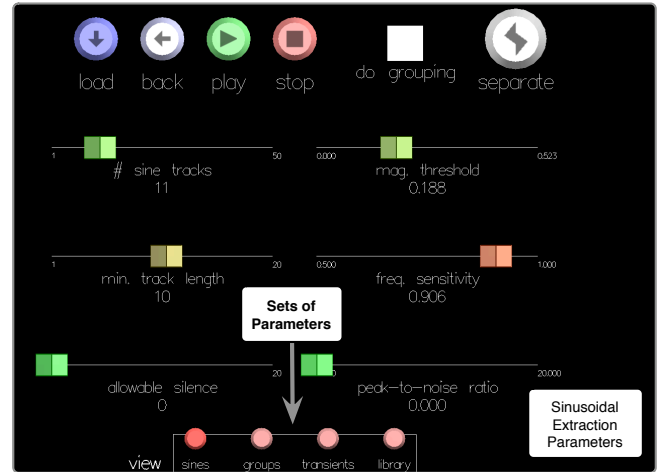


Figure 4: Sliders for sinusoidal analysis.

*Transient events* or brief noisy foreground events are usually detected in the time-domain by observing changes in signal energy over time (Verma and Meng 1998; Bello et al. 2005). TAPESTREA analyzes the recorded sound using a non-linear one-pole envelope follower filter with a sharp attack and slow decay and finds points where the derivative of the envelope is above a threshold. These points mark sudden increases in energy and are interpreted as transient on-

sets. A transient event is considered to last for up to half a second from its onset. The exact transient length, as well as the threshold, and filter parameters can all be modified in real-time via sliders (Figure 5). Detected transients can be individually replayed and saved as templates.

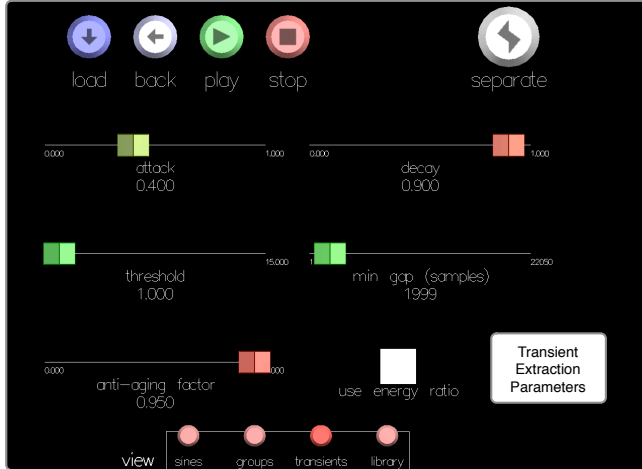


Figure 5: Transient analysis sliders.

The *stochastic background* represents parts of the recording that constitute background noise, and is obtained by removing the detected deterministic and transient events from the initial sound. Deterministic events are removed by eliminating the peaks of each sinusoidal track from the corresponding spectral frames; the magnitudes of the bins beneath the peak are smoothed down, while the phases in these bins are randomized (Figure 6). Transient events, in turn, are removed in the time-domain by applying wavelet tree learning (Dubnov et al. 2002) to generate a sound clip that resembles nearby transient-free segments of the recording. This synthesized “clean” background replaces the samples containing the transient event to be removed. Once separated, the stochastic background can be saved, played, or loaded into the interface for further iterative analysis.

Separating a sound into components in this way has several advantages. The distinction between foreground and background components is semantically clear to humans, who can therefore work within the framework with a concrete understanding of what each component represents. The different component types are also stored and processed separately according to their defining characteristics, thus allowing flexible transformations on individual components. Each transformed component can be saved as a template and later reloaded, reused, copied, further transformed, or otherwise treated as a single object. In addition, the act of separating a sound into smaller sounds makes it possible to “re-compose” them into a variety of pieces by combining templates in diverse ways.

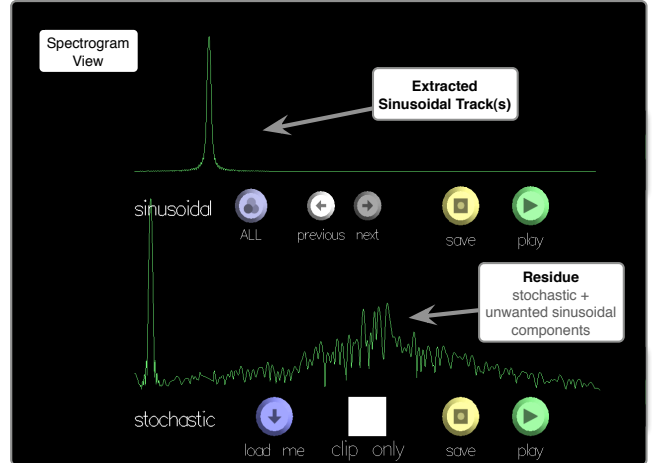


Figure 6: Spectrum of separated sinusoidal peaks (top) and stochastic residue (bottom).

## 4 Synthesis Phase

Once the components of a sound have been separated and saved as templates, TAPESTREA allows each template to be transformed and synthesized individually. The synthesis interface (Figure 7) provides access to the current library of saved templates, displayed as objects (Figure 8). Templates saved to file from prior sittings can be loaded into the library, too. Selecting any template in the library displays a set of transformation and synthesis parameters suited to the template type. A selected template can be synthesized to generate sound at any time, including while its transformation parameters are being modified. At this point, TAPESTREA also offers additional synthesis templates to control the placement or distribution of basic components in a composition. Thus, components can be manipulated individually and in groups, modeling both single sound and group characteristics. The transformation and synthesis options for the different template types are as follows:

### 4.1 Deterministic Events

Deterministic events are synthesized from their tracks via sinusoidal re-synthesis. Frequency and magnitude between consecutive frames in a track are linearly interpolated, and time-domain samples are computed from this information.

The track representation allows considerable flexibility in applying frequency and time transformations on a deterministic event. The event’s frequency can be linearly scaled before computing the time-domain samples, by multiplying the frequency at each point on its tracks by a specified factor. Similarly, the event can be stretched or shrunk in time by scaling the time values in the time-to-frequency trajectories of its



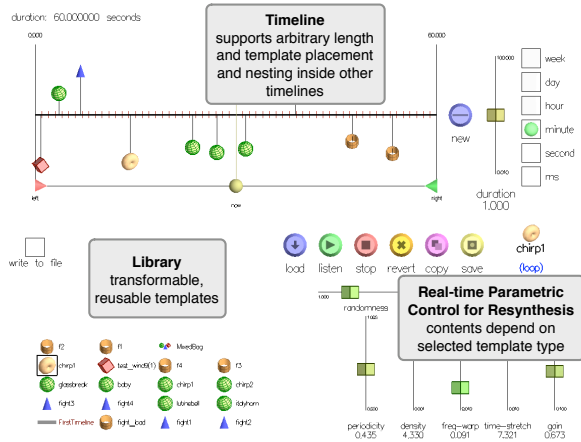


Figure 7: Screenshot of transformation + synthesis interface.

tracks. This works for almost any frequency or time scaling factor without producing artifacts. Frequency and time transformations can take place in real-time in TAPESTREA, allowing an event to be greatly stretched, shrunk or pitch shifted even as it is being synthesized.

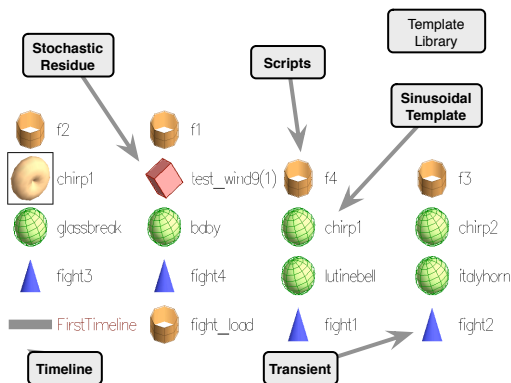


Figure 8: Library of saved templates.

## 4.2 Transient Events

Since transient events are brief by definition, TAPESTREA stores them directly as time-domain audio frames. Synthesizing a transient event without any transformations, therefore, involves playing back the samples in the audio frame.

In addition, TAPESTREA allows time-stretching and pitch-shifting in transient events as well. This is implemented using a phase vocoder (Dolson 1986), which limits the scaling factors to a range smaller and perhaps more reasonable than what is available for deterministic events, yet large enough to create noticeable effects.

Transient events by nature can also act as “grains” for traditional granular synthesis (Truax 1990; Roads 2002). The transformation tools for transients, along with the additional synthesis templates described in Sections 4.4 to 4.6, can thus provide an interactive “granular synthesis” interface.

## 4.3 Stochastic Background

The internal representation of a *stochastic background* template begins with a link to a sound file containing the related background component extracted in the analysis phase. However, merely looping through this sound file or randomly mixing segments of it does not produce a satisfactory background sound. Instead, our goal here is to generate ongoing background that sounds controllably similar to the original extracted stochastic background.

Therefore, the stochastic background is synthesized from the saved sound file using an extension of the wavelet tree learning algorithm (Dubnov et al. 2002). In the original algorithm, the saved background is decomposed into a wavelet tree where each node represents a coefficient, with depth corresponding to resolution. The wavelet coefficients are computed using the Daubechies wavelet with 5 vanishing moments. A new wavelet tree is then built, with each node selected based on the similarity of its ancestors and first  $k$  predecessors to corresponding sequences of nodes in the original tree. The learning algorithm also takes into account the amount of randomness desired. Finally, the new wavelet tree undergoes an inverse wavelet transform to provide the synthesized time-domain samples. This learning technique works best with the separated stochastic background as input, where the sinusoidal events it would otherwise chop up have been removed.

TAPESTREA uses a modified and optimized version of the algorithm, which follows the same basic steps but varies in details. For instance, the modified algorithm includes the option of incorporating randomness into the first level of learning, and also considers  $k$  as dependent on the depth of a node rather than being constant. More importantly, it optionally avoids learning the coefficients at the highest resolutions. These resolutions roughly correspond to high frequencies, and randomness at these levels does not significantly alter the results, while the learning involved takes the most time. Optionally stopping the learning at a lower level thus optimizes the algorithm and allows it to run in real-time.

Further, TAPESTREA offers interactive control over the learning parameters in the form of “randomness” and “similarity” parameters. The size of a sound segment to be analyzed as one unit can also be controlled, and results in a “smooth” synthesized background for larger sizes versus a more “chunky” background for smaller sizes. Creatively ma-

nipulating these parameters can, in fact, yield interesting musical compositions generated through “stochastic background” alone.

## 4.4 Event Loops

Event loops (Figure 9) are synthesis templates designed to facilitate the parametric repetition of a single event. Any deterministic or transient event template can be formed into a loop. When the loop is played, instances of the associated event are synthesized at the specified density and periodicity, and within a specified range of random transformations. These parameters can be modified while the loop is playing, to let the synthesized sound change gradually.

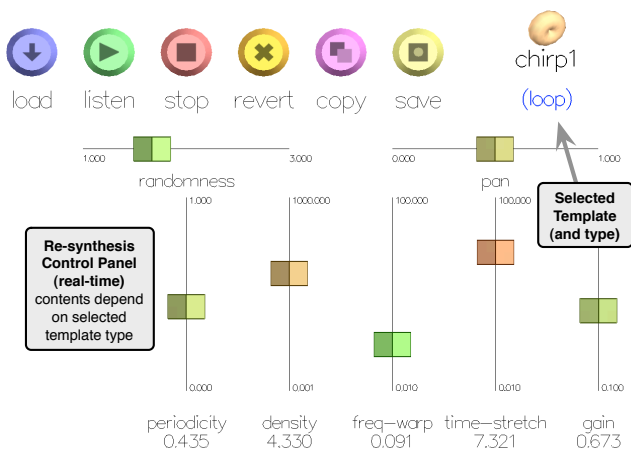


Figure 9: Sliders for controlling an event loop.

The density refers to how many times the event is repeated per second, and could be on the order of 0.001 to 1000. At the higher densities, and especially for transient events, the synthesized sound is often perceived as continuous, thus resembling granular synthesis.

The periodicity, ranging from 0 to 1, denotes how periodic the repetition is, with a periodicity of 1 meaning that the event is repeated at fixed time intervals. The interval between consecutive occurrences of an event is generally determined by feeding the desired periodicity and density into a Gaussian random number generator. It is straightforward to replace this generator with one that follows a Poisson or other user-specified probability distribution.

In addition to the parameters for specifying the temporal placement of events, TAPESTREA allows each instance of the recurring event to be randomly transformed within a range. The range is determined by selected average frequency and time-scale factors, and a randomness factor that dictates how far an individual transformation may vary from the average. Individual transformation parameters are uniformly se-

lected from within this range. Apart from frequency and time scaling, the gain and pan of event instances can also randomly vary in the same way.

## 4.5 Timelines

While a loop parametrically controls the repetition of a single event, with some amount of randomization, a timeline allows a template to be explicitly placed in time, in relation to other templates. Any number of existing templates can be added to a timeline, as well as deleted from it or re-positioned within it once they have been added.

A template’s location on the timeline indicates its onset time with respect to when the timeline starts playing. When a timeline is played, each template on it is synthesized at the appropriate onset time, and is played for its duration or till the end of the timeline is reached. The duration of the entire timeline can be on the order of milliseconds to weeks, and may be modified after the timeline’s creation.

TAPESTREA also allows the placement of timelines within timelines (or even within themselves). This allows for template placement to be controlled at multiple time-scales or levels, making for a “multiresolution synthesis.”

## 4.6 Mixed Bags

Another template for synthesis purposes is the mixed bag (Figure 10), which is designed to control the relative densities of multiple, possibly repeating, templates. Like a timeline, a mixed bag can contain any number of templates, but these are randomly placed in time and transformed, as in loops. The goal is to facilitate the synthesis of a composition with many repeating components, without specifying precisely when each event occurs. The real-time parameters for controlling this also enable the tone of a piece to change over time while using the same set of components, simply by synthesizing these components differently.

When a template is added to a mixed bag, it can be set to play either once or repeatedly. It also has a “likelihood” parameter, which determines the probability of that template’s being played in preference over any of the other templates in the bag. Finally, it has a “randomness” parameter, which controls the range for random transformations on that template, analogous to the randomness control in event loops.

Beyond these individual template parameters, each mixed bag has overall periodicity and density settings, which control the temporal distribution of repeating templates in the same way that an event loop does. However, while an event loop plays instances of a single event, a mixed bag randomly selects a repeating template from its list whenever it is time to synthesize a new instance. Templates with higher likelihood settings are more likely to be selected for synthesis.

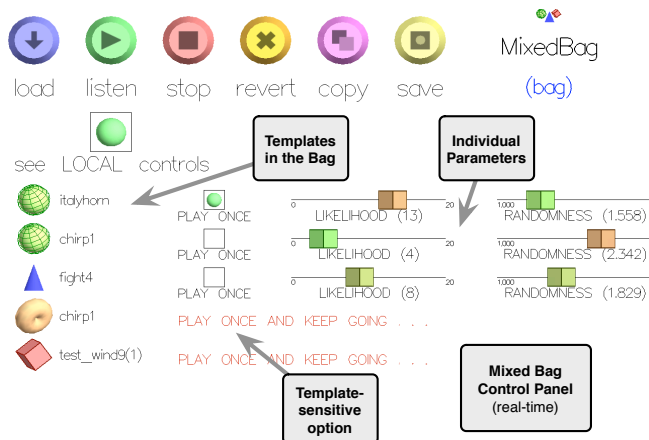


Figure 10: Sliders for controlling items in a mixed bag.

## 4.7 Pitch and Time Quantizations

While sliders control the synthesis parameters in a continuous way, more customized musical control can be exerted by quantizing pitches and times to user-specified values. Pitch and time tables can be loaded on-the-fly for each template.

The frequency scaling factor of a template is quantized to the nearest entry in its pitch table, if it has one. For event loops and mixed bags, this controls the possible frequency scaling during random transformations on the underlying events. The frequencies of individual templates on a timeline are scaled, in the order in which they are played, by successive entries on the timeline’s pitch table. This allows a user-defined musical scale to be applied to most templates.

Rhythm can be similarly specified by quantizing time to the nearest entry in a time table. In event loops and mixed bags, this quantizes the event density parameter as well as the intervals between consecutive events. On timelines, templates are positioned only at time points corresponding to table entries, if a table exists. Thus, templates can start synthesizing at particular beats.

## 4.8 Score Language

The manipulations described so far primarily occur through a visual interface. Even finer control over the synthesis can be obtained through the use of a score language. The audio programming language ChuckK (Wang and Cook 2003) is used here both for specifying precise parameter values and for controlling exactly how these values change over time. Since ChuckK allows the user to specify events and actions precisely and concurrently *in time*, it is straightforward to write scores to dynamically evolve a sound tapestry.

A ChuckK virtual machine is attached to TAPESTREA, which registers a set of API bindings with which ChuckK pro-

grams can access and control sound templates and automate tasks. Each script (called a *shred*) can be loaded as a sound template and be played or put on timelines. Scripts can run in parallel, synchronized to each other while controlling different parts of the synthesis. Also, scripting is an easy way to add “traditional” sound synthesis algorithms and real-time control via MIDI and Open Sound Control.

## 4.9 Other Controls

TAPESTREA also offers some generic synthesis and playback controls. The gain and stereo panning of templates can be controlled individually, or randomly set by event loops and mixed bags. A reverb effect adapted from STK (Cook and Scavone 1999) can also be added to the final synthesized sound.

The synthesis interface provides several ways to instantiate new templates. Any existing template can be copied, while deterministic and transient event templates can also be saved as event loops. New timelines and mixed bags can be freely created, and existing templates can be dragged onto or off these as needed. Templates can also be deleted from the library, provided they are not being used in a timeline or a mixed bag. Finally, while sound is generally synthesized in real-time, TAPESTREA offers the option of writing the synthesized sound to file.

## 5 Discussion

TAPESTREA makes it possible to create a wide range of *musical tapestries*. We describe one example recomposition here. The spectrogram (Figure 11) represents a 5 minute improvised piece called *Etude pour un Enfant Seul* (Study for a Child Alone). The source sound templates include the following: baby’s cry (1.5 sec; sinusoidal: 5 tracks), a clock chime (7 sec, sinusoidal: 25 tracks), glass breaking (.5 sec, sinusoidal: 4 tracks), car horn (.5 sec; sinusoidal: 10 tracks), bird chirp (.5 sec, sinusoidal: 4 tracks), firework pop (.2 sec, transient), boom (.4 sec, transient), bang (.3 sec, transient). These were extracted from BBC sound recordings. (Additional templates, including an ocean background with bird chirps removed, were extracted but not used here.)

We highlight some areas of interest in the recomposition (denoted by numbered diamonds in Figure 11). In area (1) are time/frequency-warped instances of the baby (7x time-stretch, 0.5x frequency-scaled), car horns (6x time, 0.2x and 0.28x freq), and glass (4x time, 0.5x freq). The percussion involving the pop/boom/bang templates begins around (2) and is dynamically coordinated by scripts. In (3), the percussion develops, punctuated by a solitary glass breaking sound. At (4), greatly modified bird chirps (.15x time; 0.4x freq) fade

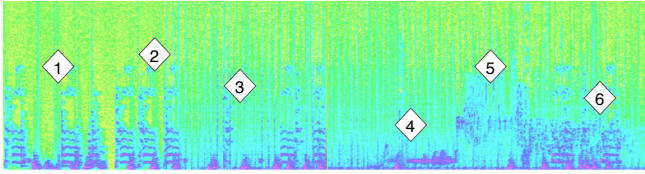


Figure 11: Example of a soundscape recomposition. Diamonds represent areas of significant shift in the piece.

in as part of a periodic loop, which is so dense that chirps are triggered at audio rates, forming a rich tone. As time-stretch, frequency-scale, and density are modified, the tone gradually morphs into a flock of birds and back. Combined with further modifications to periodicity and randomness, the flock reaches its peak at (5), modeling the sound of more than 30 birds spread out in time, frequency, volume, and pan—all from a single bird chirp template. The flock is then manipulated to sparser texture, and the child returns at (6) with three longer cries (baby cry; 9x time, 0.4x freq).

While this example makes good use of TAPESTREA, it is equally possible to create completely differently styled compositions using the same tool and even the same initial sounds.

## 6 Conclusion

TAPESTREA is a technique and system for “re-composing” recorded sounds by separating them into unique components and weaving these components into *musical tapestries*. The technique is applicable to musique concrète, soundscape composition and beyond, while the system combines algorithms and interfaces for implementing the concepts. Key contributions include: (1) an approach for recomposing natural sounds, defining semantically clear *sound template* types linked to specific processing techniques, (2) a system for extracting selected sound components into reusable templates, and for transforming and synthesizing these, (3) a class of user interfaces aimed to facilitate the process.

Creating *musical tapestries* with TAPESTREA is truly a multidimensional process. The interface simultaneously provides visual and audio information, while the system provides the means to interactively extract sound components, transform them radically while maintaining salient features, model them individually or in groups, and synthesize the final multi-level “recomposition” in any number of ways, ranging from a pre-set score to dynamically in real-time. Even with a modest set of original sounds, there is no end to the variety of *musical tapestries* one might weave.

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