

Week 8



**STEVENS**  
INSTITUTE *of* TECHNOLOGY  
THE INNOVATION UNIVERSITY®



# **An Introduction to Cyber Security – CS 573**

Instructor: Dr. Edward G. Amoroso  
[eamoroso@tag-cyber.com](mailto:eamoroso@tag-cyber.com)

## Required Week Eight Readings

1. "Blind Signatures for Untraceable Payments," David Chaum  
<https://sceweb.sce.uhcl.edu/yang/teaching/csci5234WebSecurityFall2011/Chaum-blind-signatures.PDF>
2. Finish *From CIA to APT: An Introduction to Cyber Security*, E. Amoroso & M. Amoroso

Twitter: @hashtag\_cyber  
LinkedIn: Edward Amoroso



Week 8

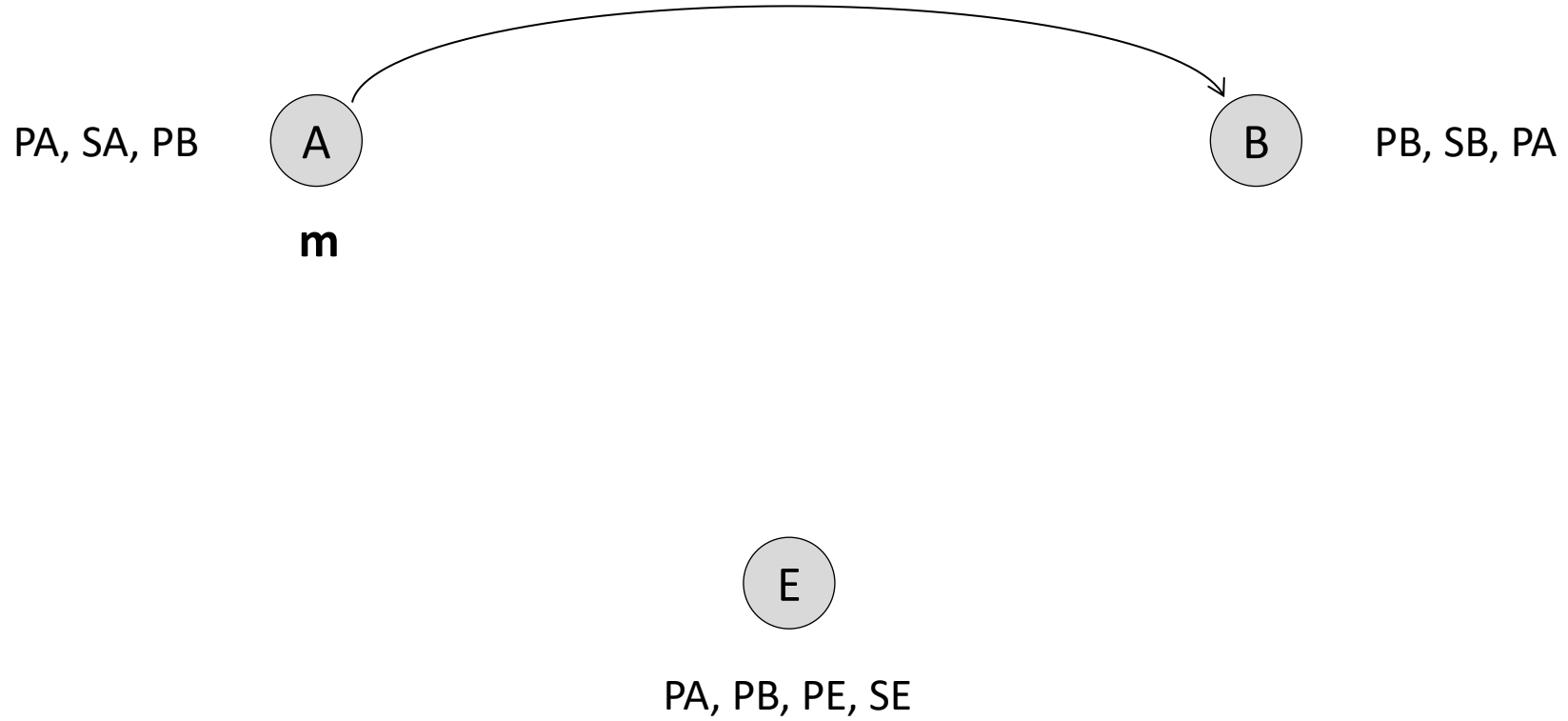


**Week 8: Key Distribution, Digital Signing, SSL, and Secure eCommerce**

What are the Basic Properties of  
Public Key Cryptography?  
(recap from last week's Zoom)

# Sending a Secret Message

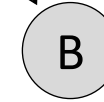
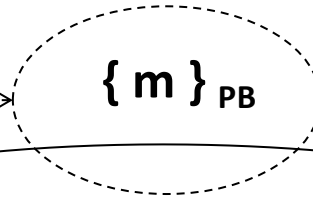
*Alice creates message  $m$  . . .*



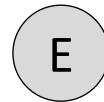
# Sending a Secret Message

*Alice creates message  $m$ ,  
encrypts using Bob's public key  
 $PB$ , and sends result to B*

PA, SA, PB

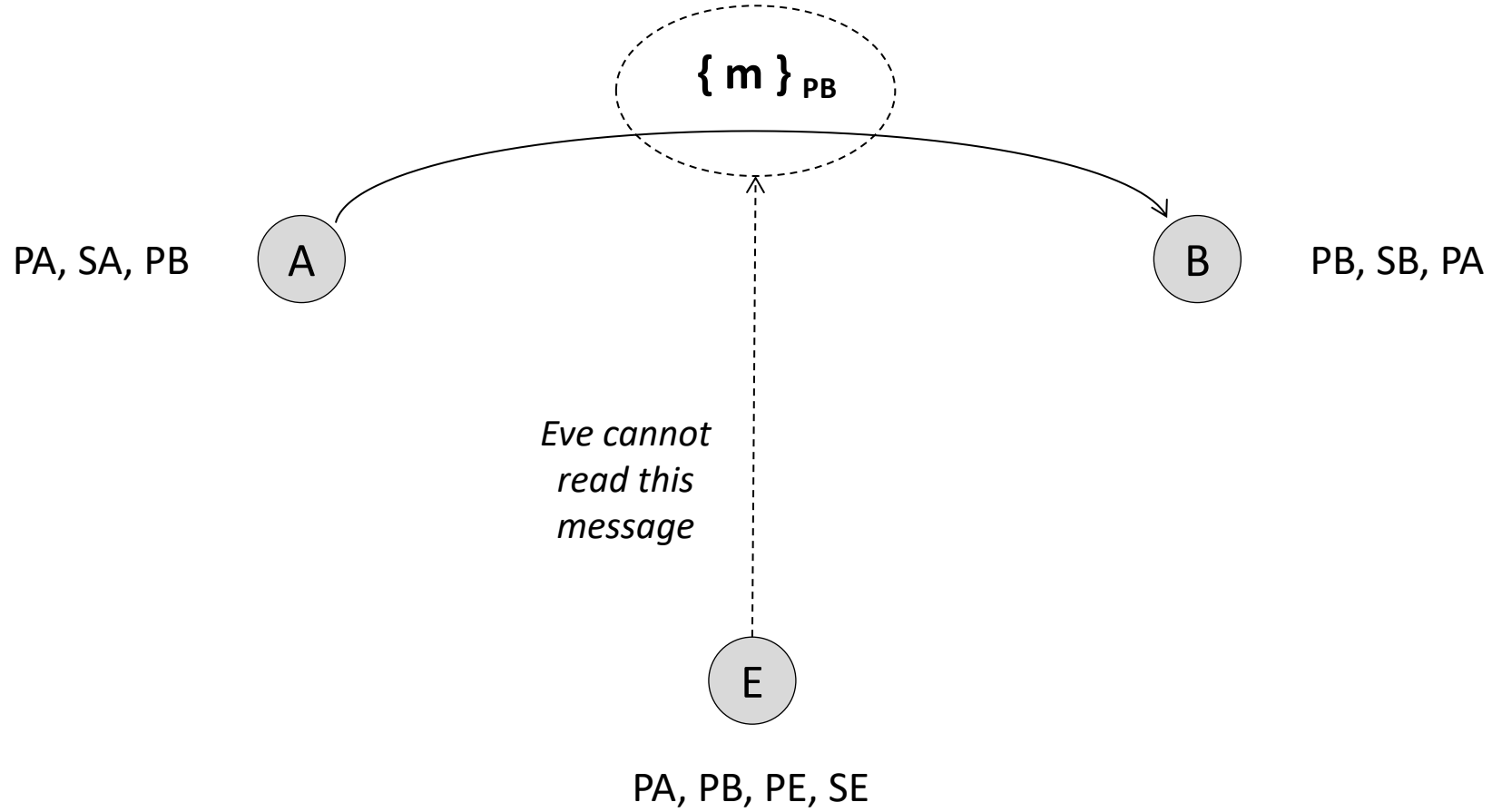


PB, SB, PA

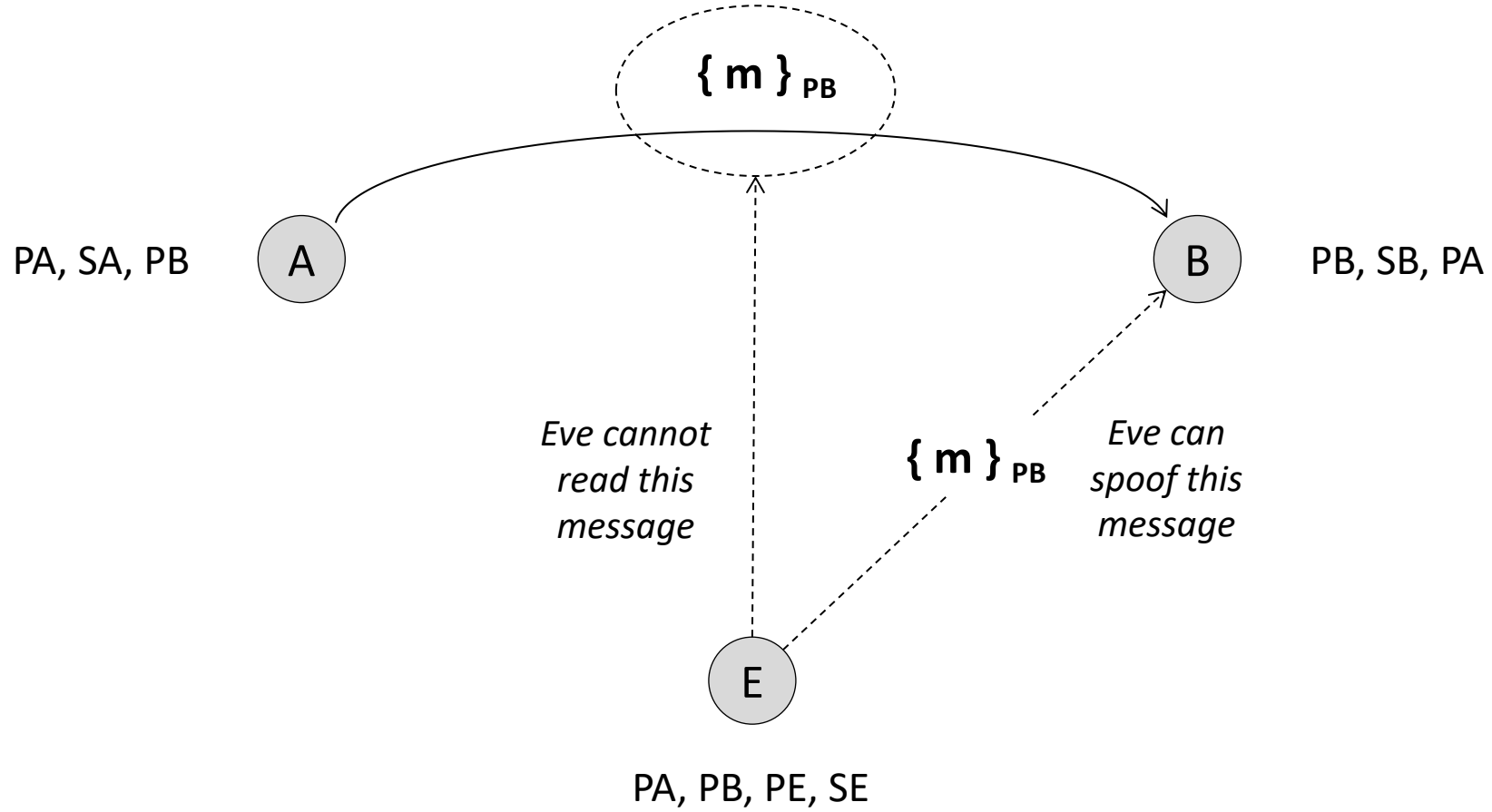


PA, PB, PE, SE

# Sending a Secret Message

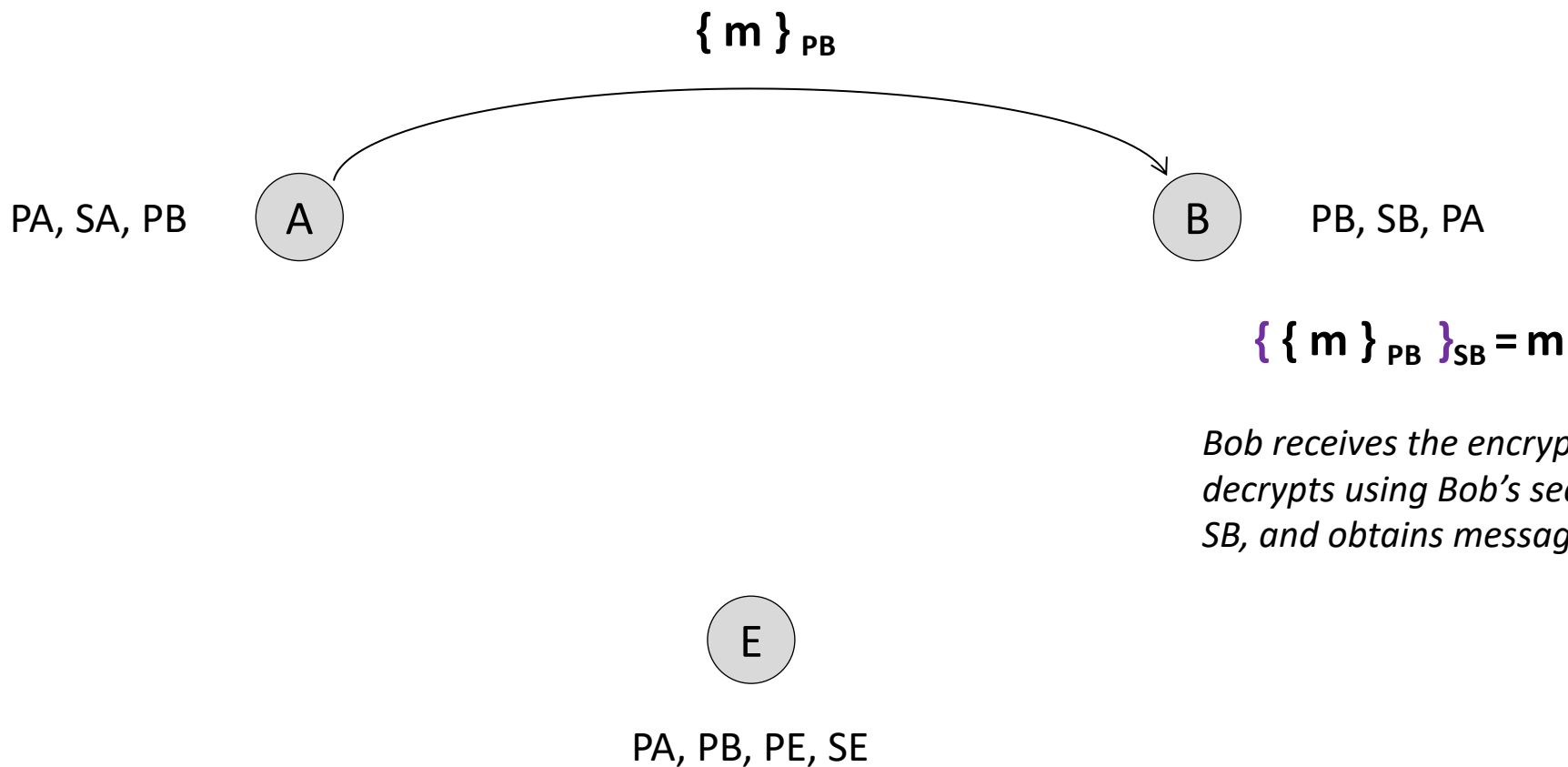


# Sending a Secret Message

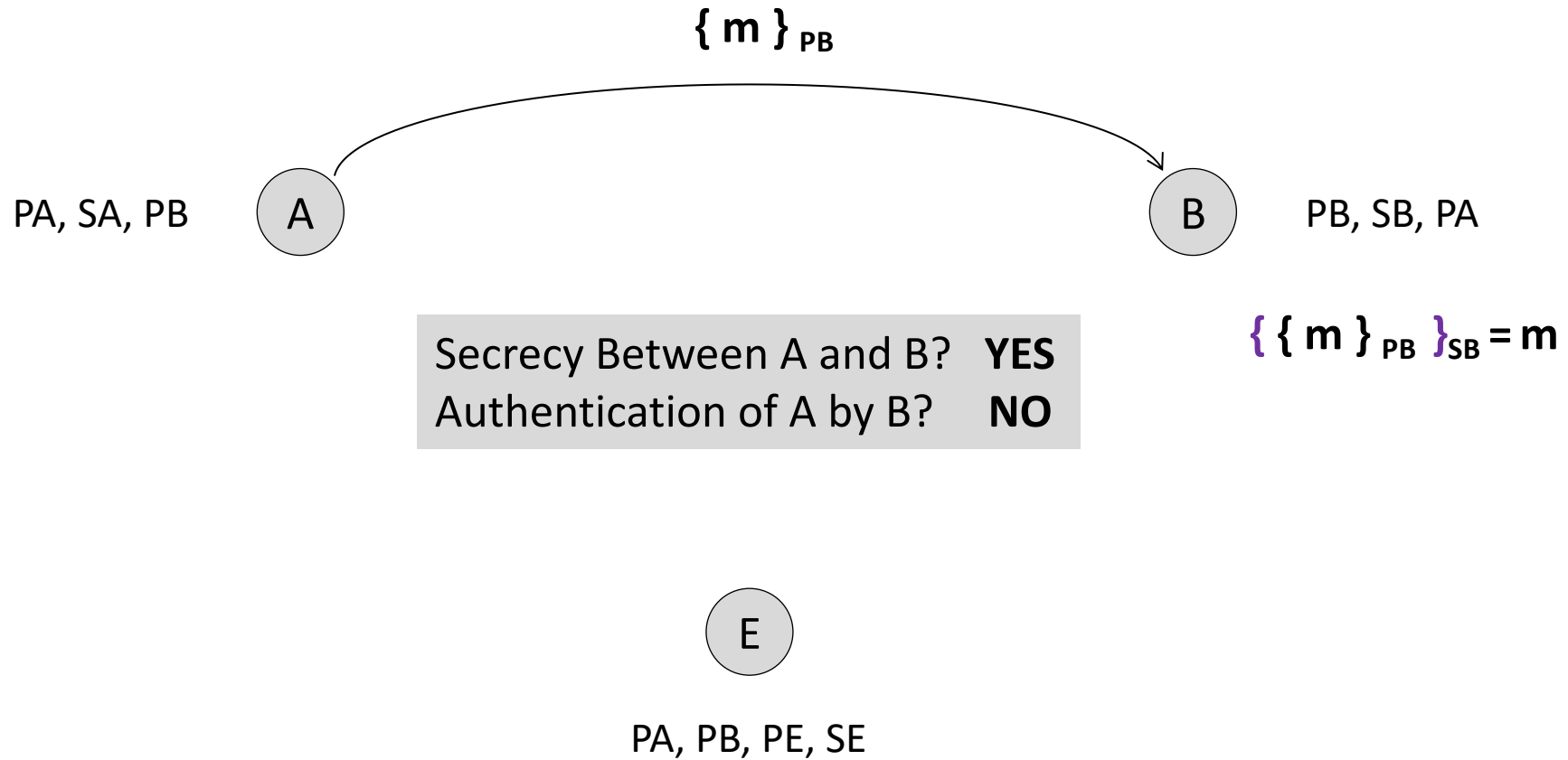




# Sending a Secret Message

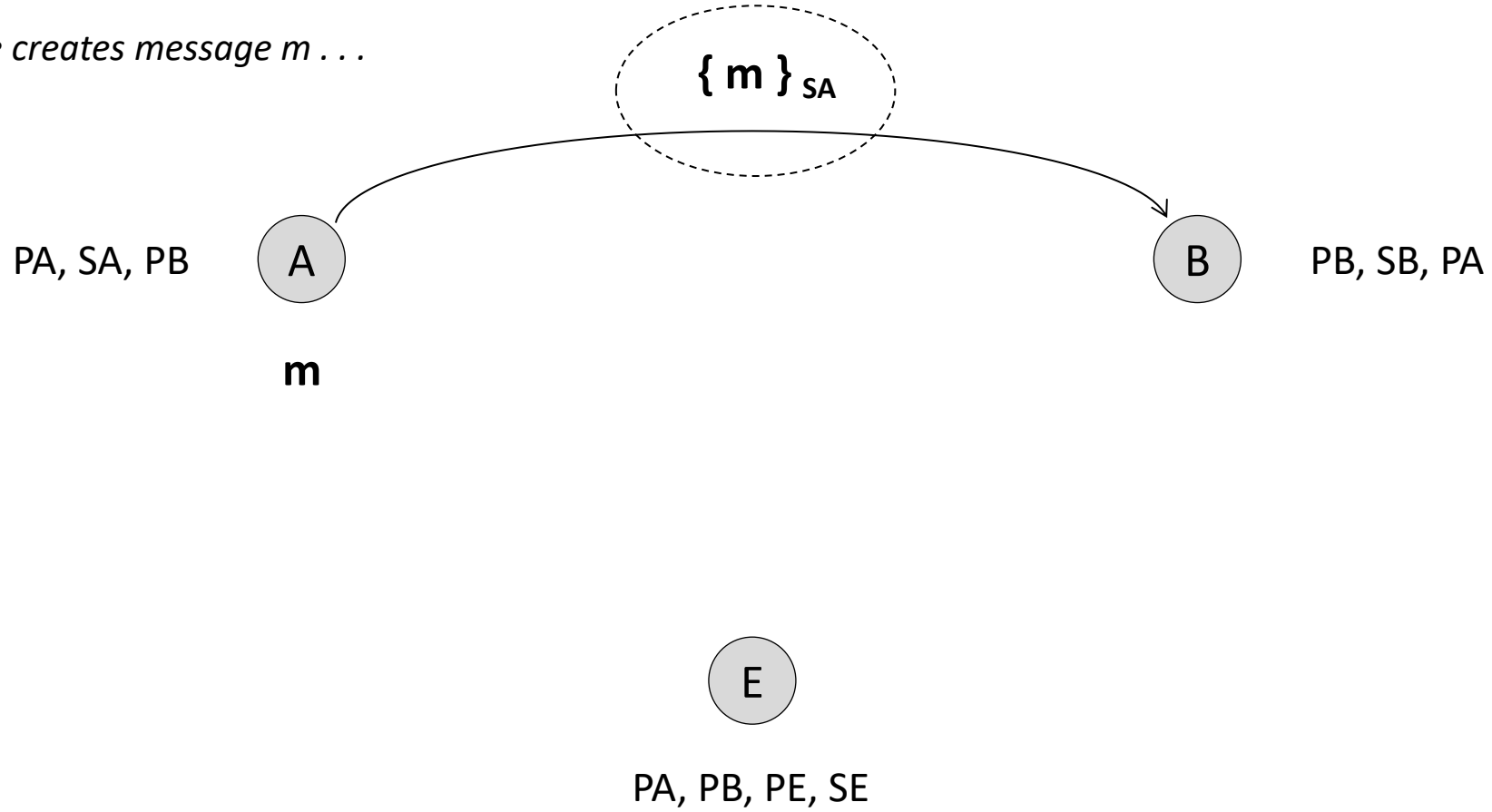


# Sending a Secret Message



# Sending a Signed Message

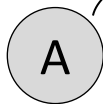
*Alice creates message  $m$  . . .*



# Sending a Signed Message

*Alice creates message  $m$ ,  
encrypts using Alice's secret key  
 $SA$ , and sends result to  $B$*

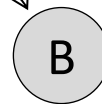
PA, SA, PB



$\{m\}_{SA}$

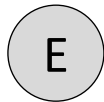
B

PB, SB, PA

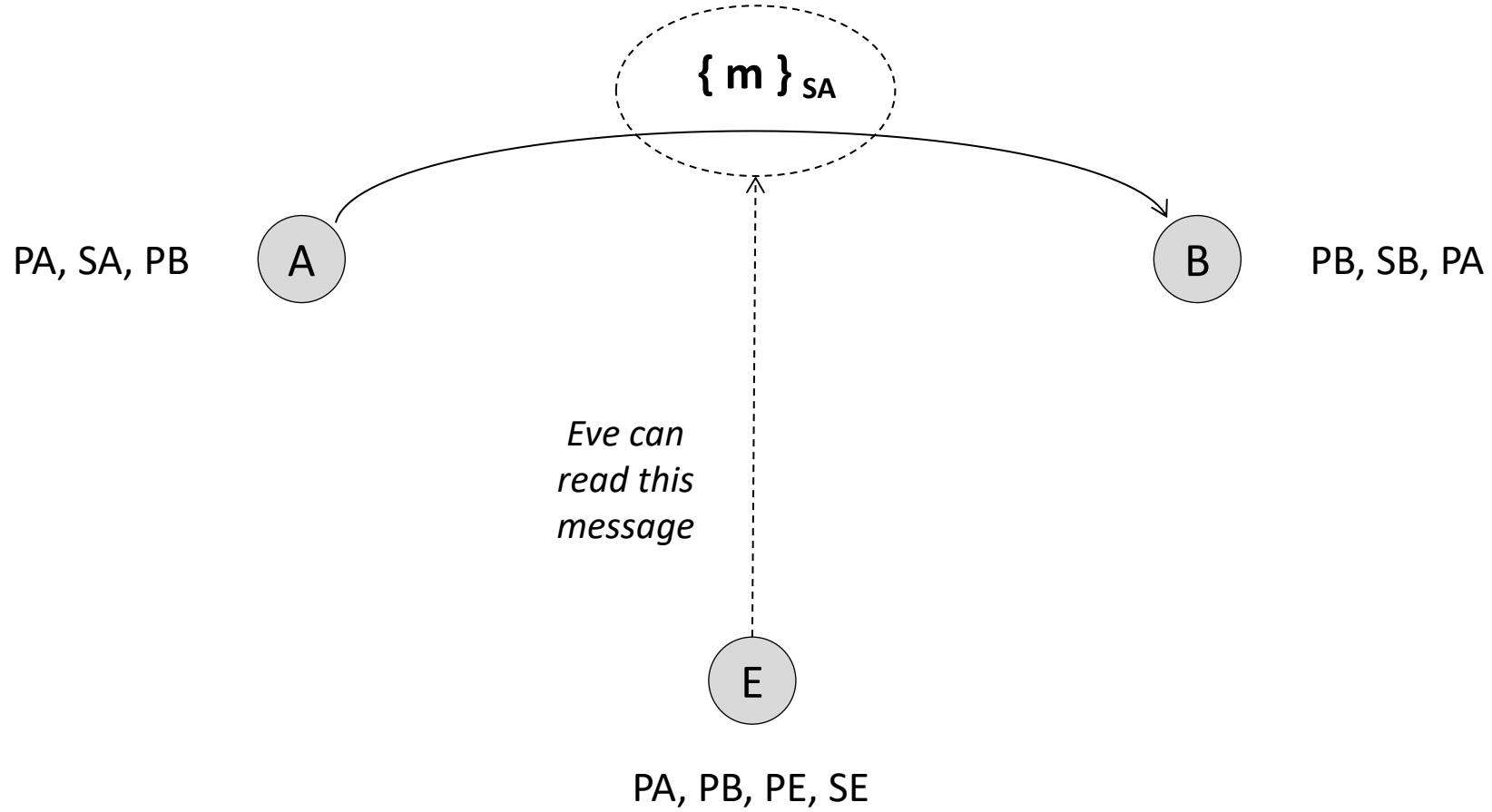


E

PA, PB, PE, SE

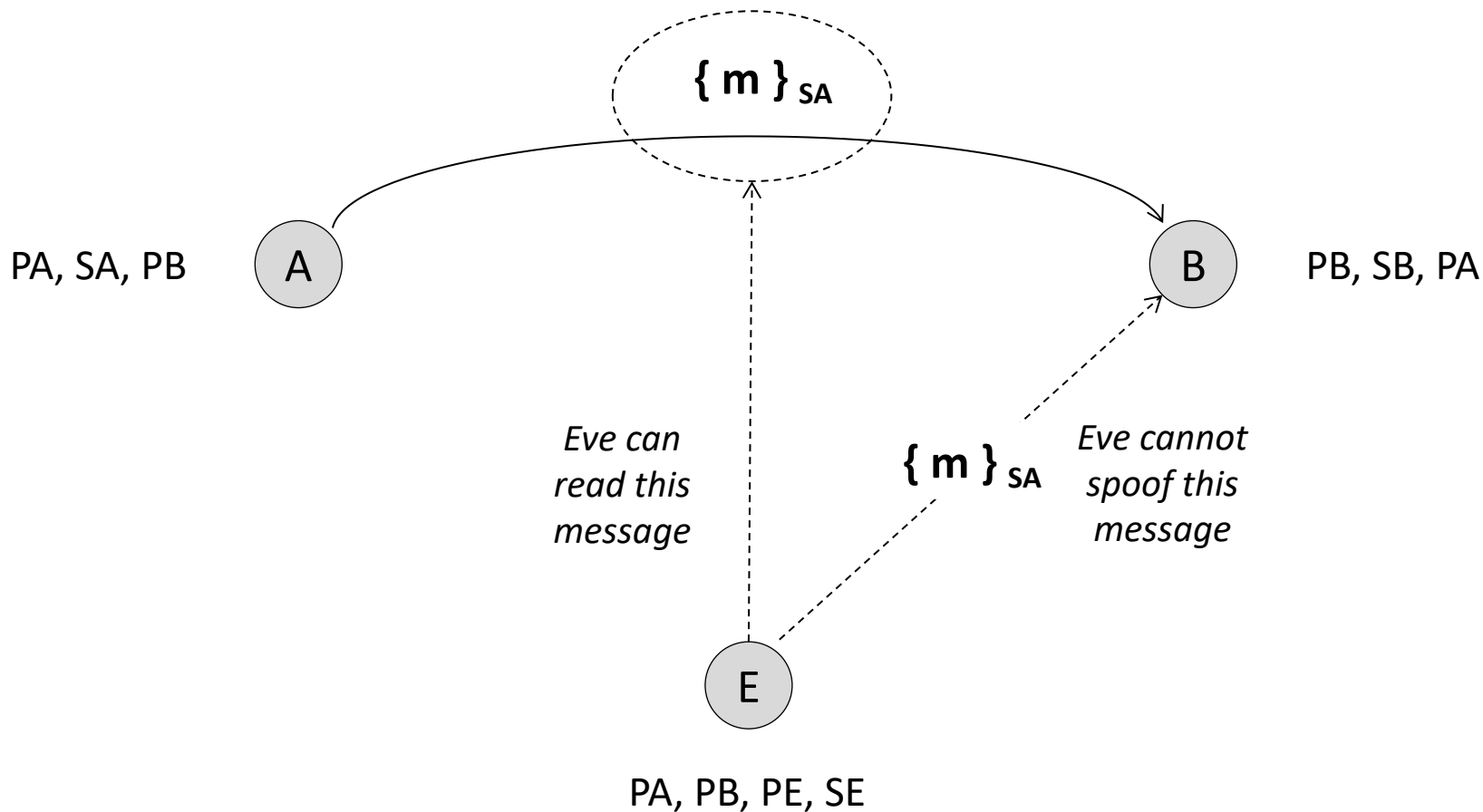


# Sending a Signed Message

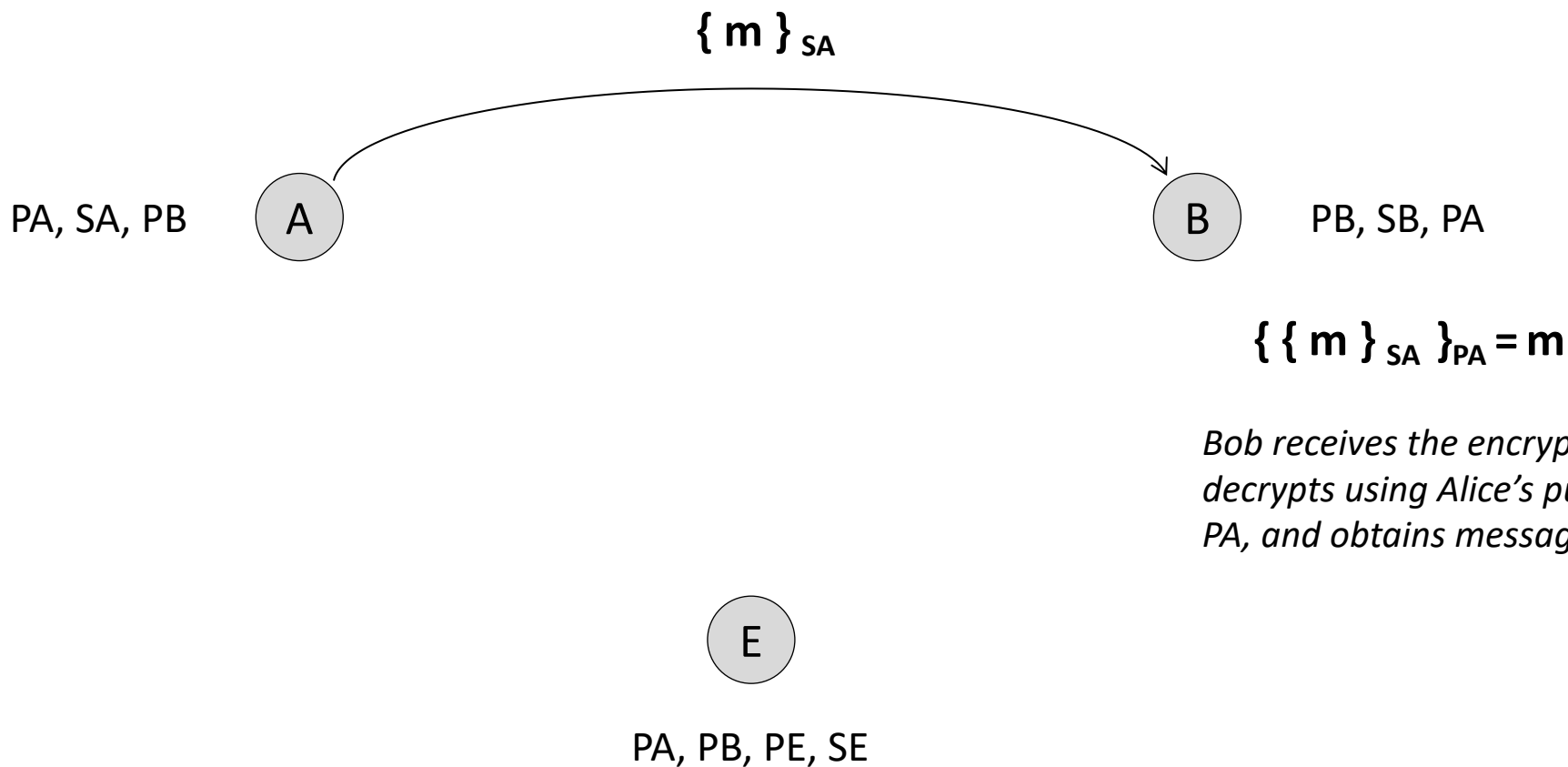




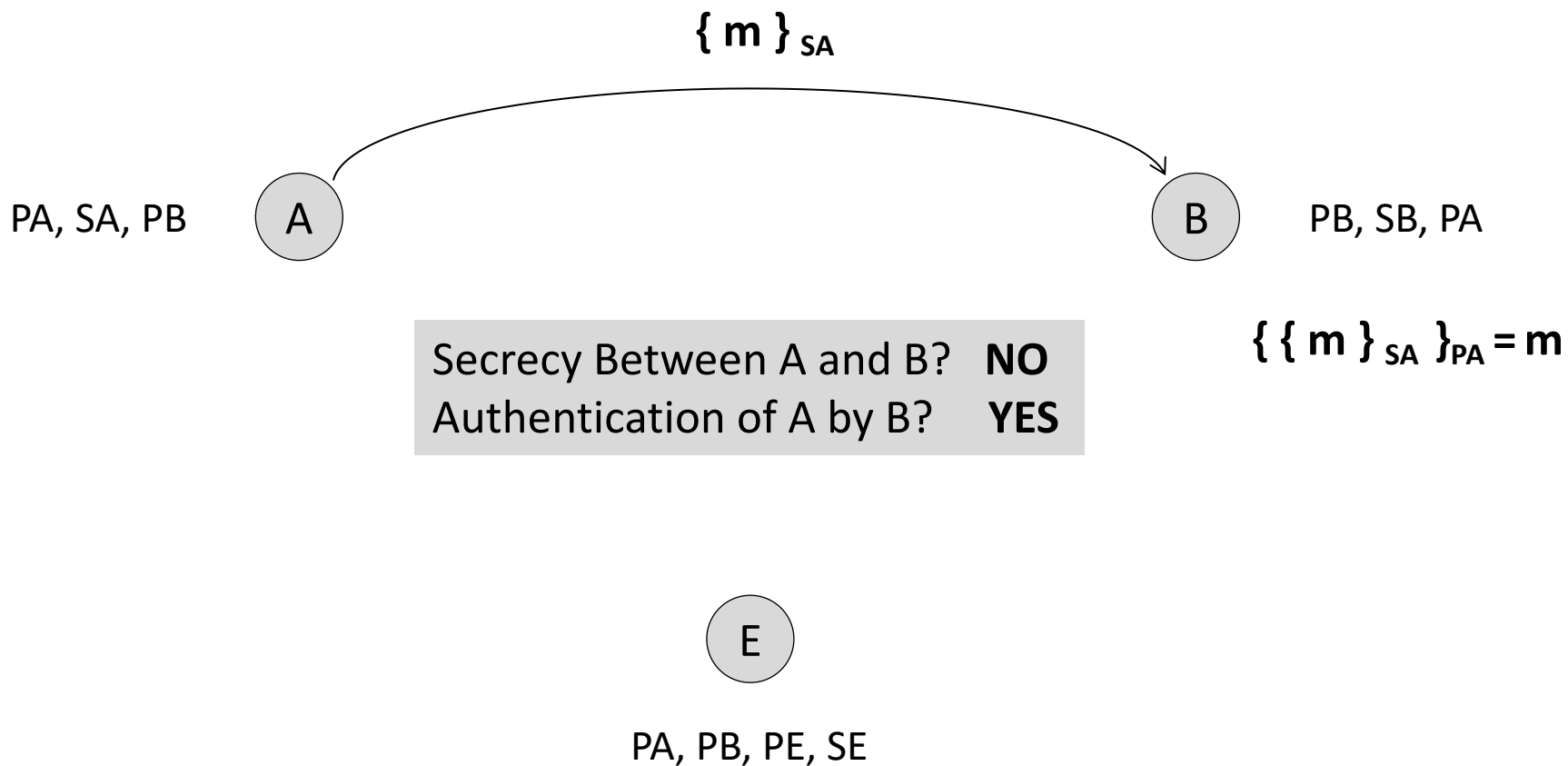
# Sending a Signed Message



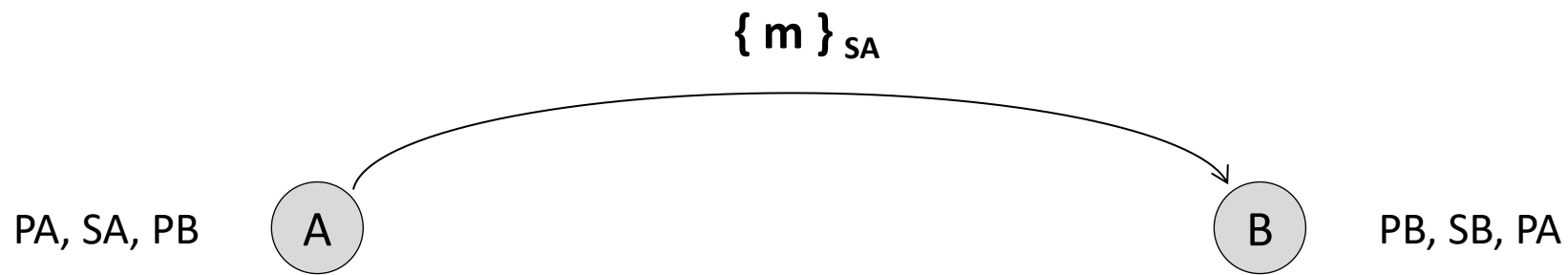
# Sending a Signed Message



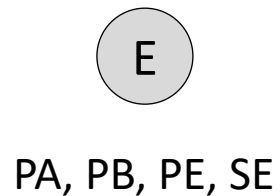
# Sending a Signed Message



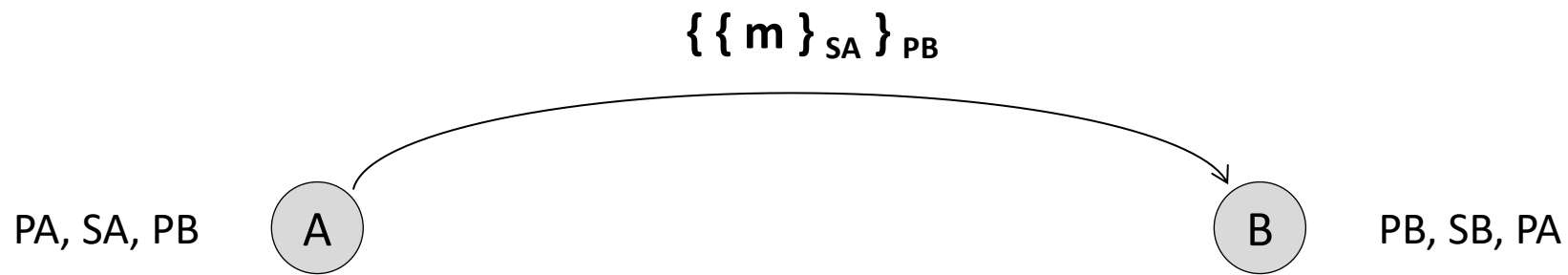
# Secure Message Exchange



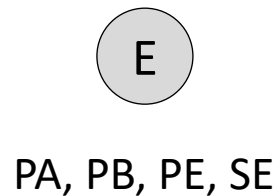
*Alice creates a message  $m$ ,  
encrypts it with a public key algorithm  
using her secret key  $SA$  . . .*



# Secure Message Exchange

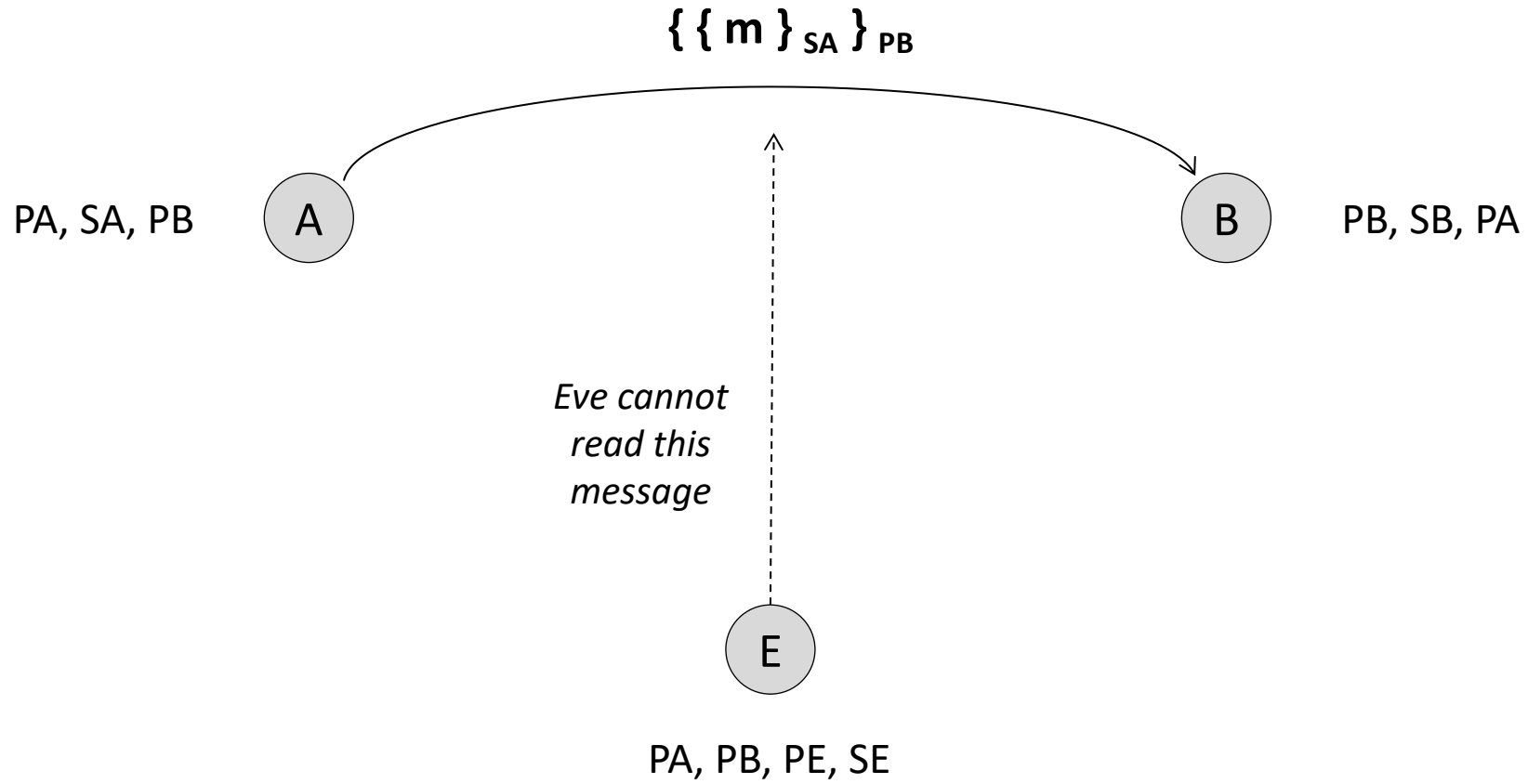


*Alice creates a message  $m$ ,  
encrypts it with a public key algorithm  
using her secret key  $SA$ , encrypts it again  
using a public key algorithm with Bob's  
public key  $PB$ , and sends the result to Bob*

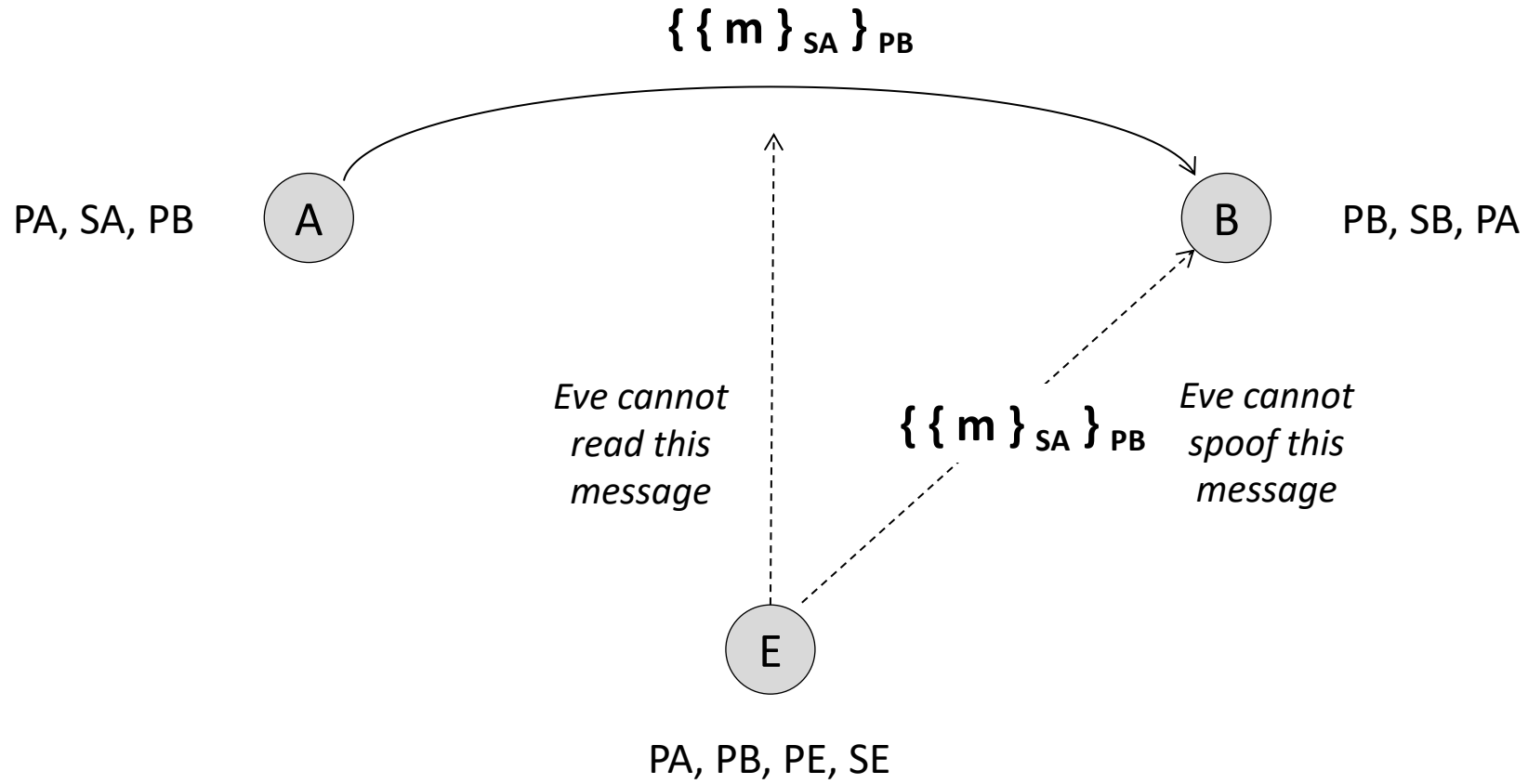




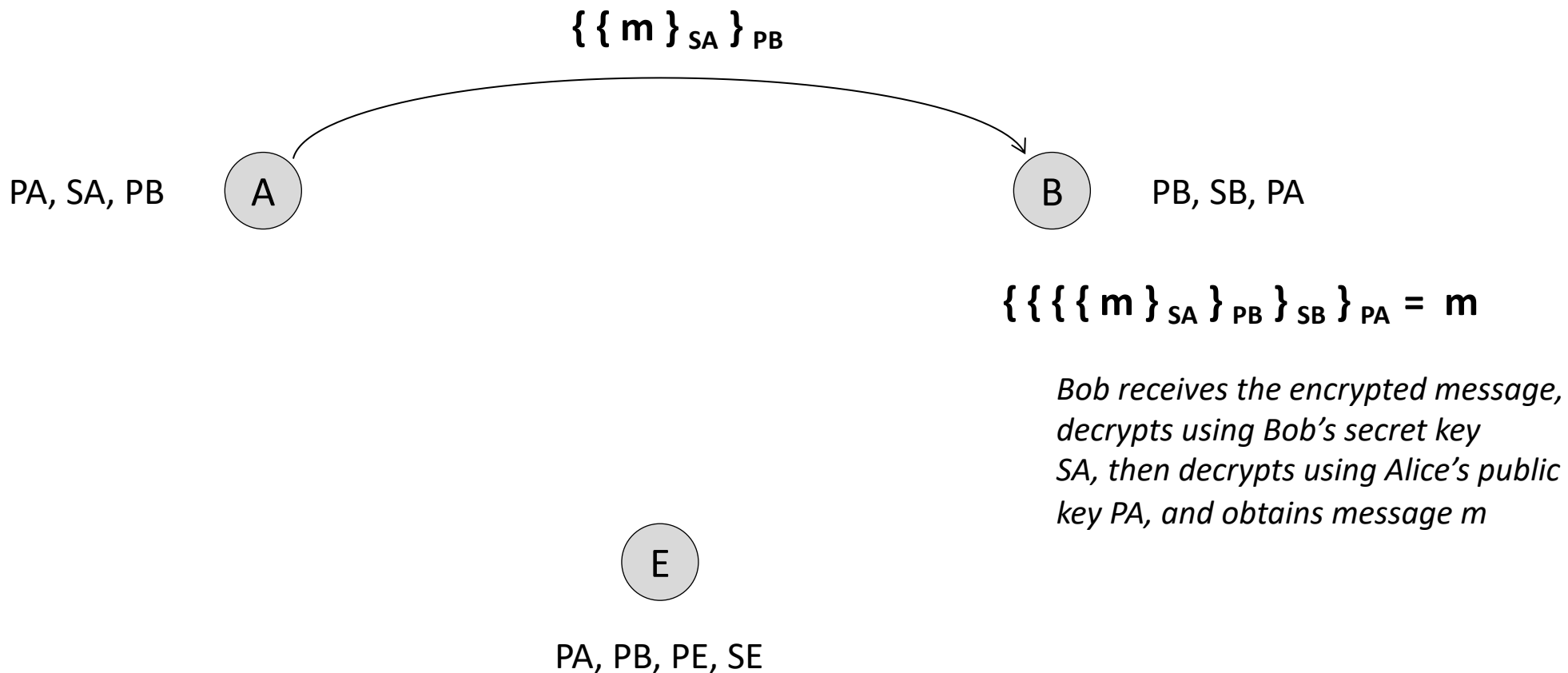
# Secure Message Exchange



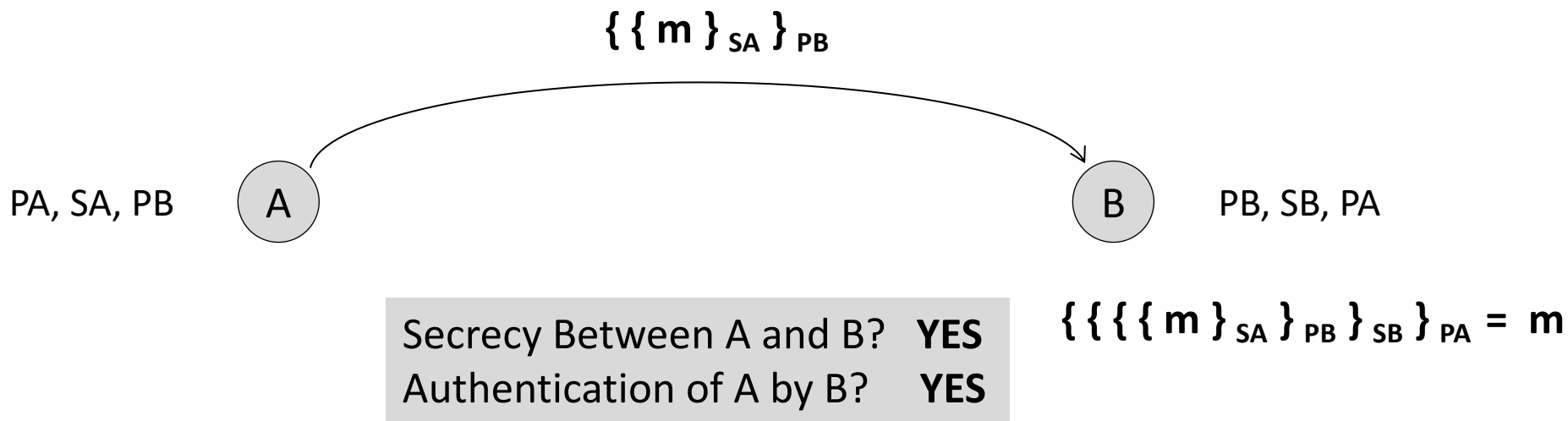
# Secure Message Exchange



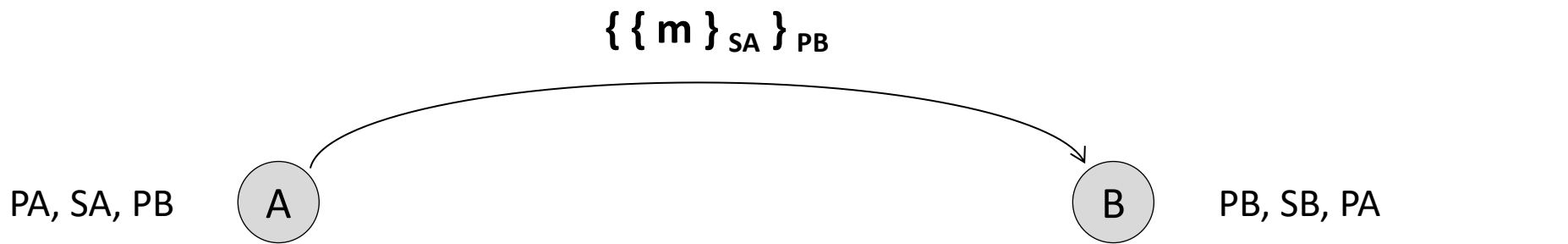
# Secure Message Exchange



# Secure Message Exchange



# Secure Message Exchange



Secrecy Between A and B? **YES**  
 Authentication of A by B? **YES**

$$\{\{\{\{m\}_{SA}\}_{PB}\}_{SB}\}_{PA} = m$$

Does this approach scale? **YES**



# Secure Message Exchange



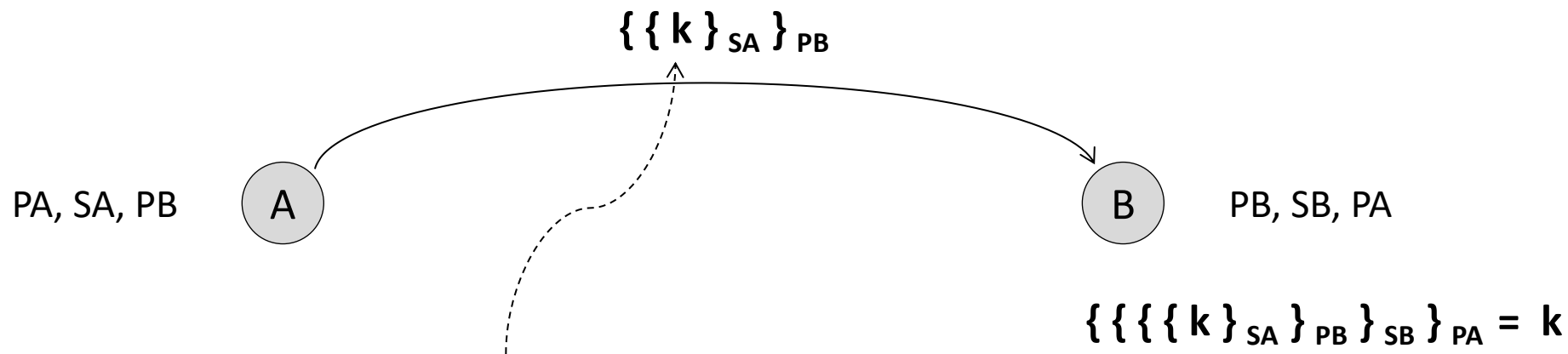
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Does this approach scale? **YES**

Is this approach efficient (cryptographically)? **NO**

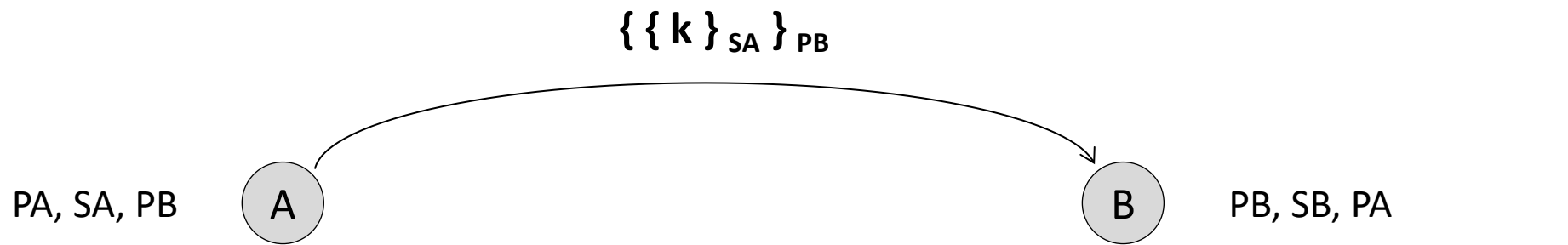
# Secure Key Exchange



*Alice generates a key  $k$  for some bulk encryption algorithm (like 3-DES) and provides this key to B using secure key exchange*

- Scalable
- Secret
- Authenticated

# Secure Key Exchange



Secrecy Between A and B? **YES**  
 Authentication of A by B? **YES**

$$\{\{\{\{k\}_{SA}\}_{PB}\}_{SB}\}_{PA} = k$$

Does this approach scale? **YES**

Is this approach efficient (cryptographically)? **YES**

How Does Diffie-Hellman Key Exchange Work?

# Diffie-Hellman Key Exchange

A

B

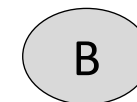
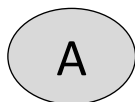
Goal:

*A and B share an encryption key  $k$   
with no KDC assistance*



# Diffie-Hellman Key Exchange

$p, g$



$p, g$

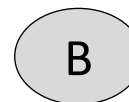
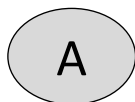
Assume Two Publicly Known Parameters:

$p$ : Large Prime – Typically 1024 Bits

$g$ : Primitive Element

# Diffie-Hellman Key Exchange

$p, g, a$



$p, g, b$

Step 1:

*A and B each locally generate  
private random values  $a$  and  $b$*

# Diffie-Hellman Key Exchange

$p, g, a$   
 $g^a \bmod p$

A

B

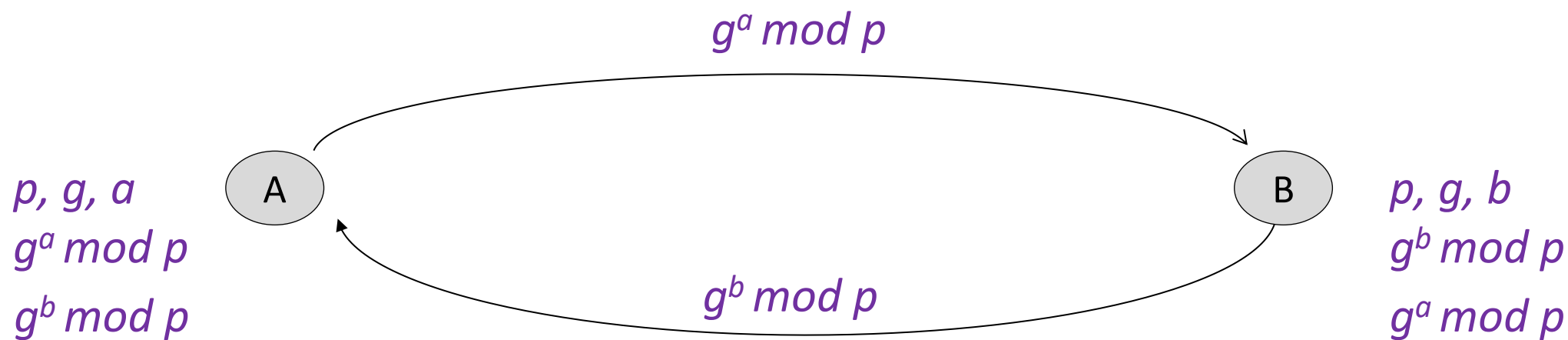
$p, g, b$   
 $g^b \bmod p$

Step 2:

A calculates  $g^a \bmod p$

B calculates  $g^b \bmod p$

# Diffie-Hellman Key Exchange

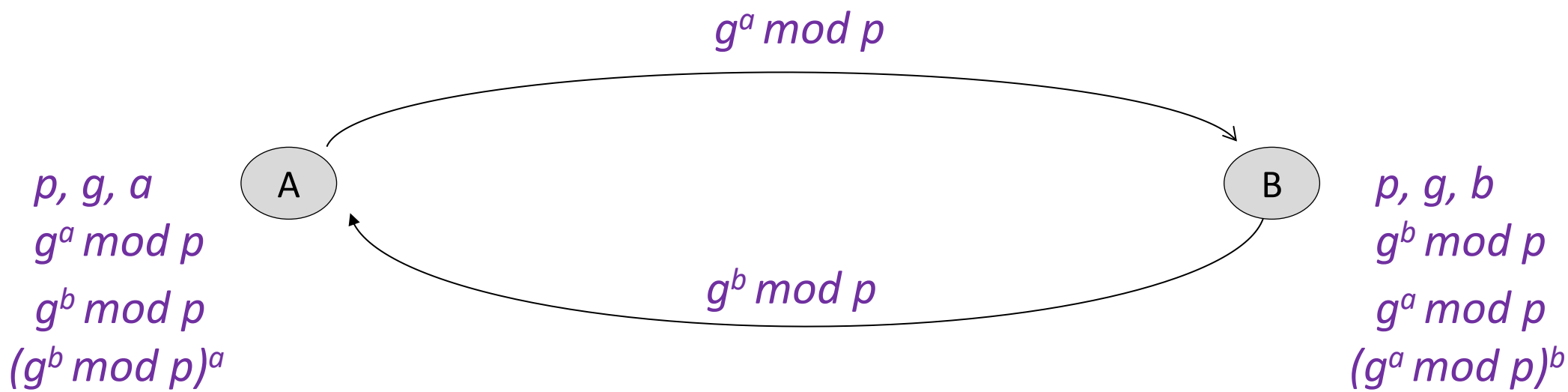


Step 3:

A sends  $g^a \bmod p$  to B

B send  $g^b \bmod p$  to A

# Diffie-Hellman Key Exchange

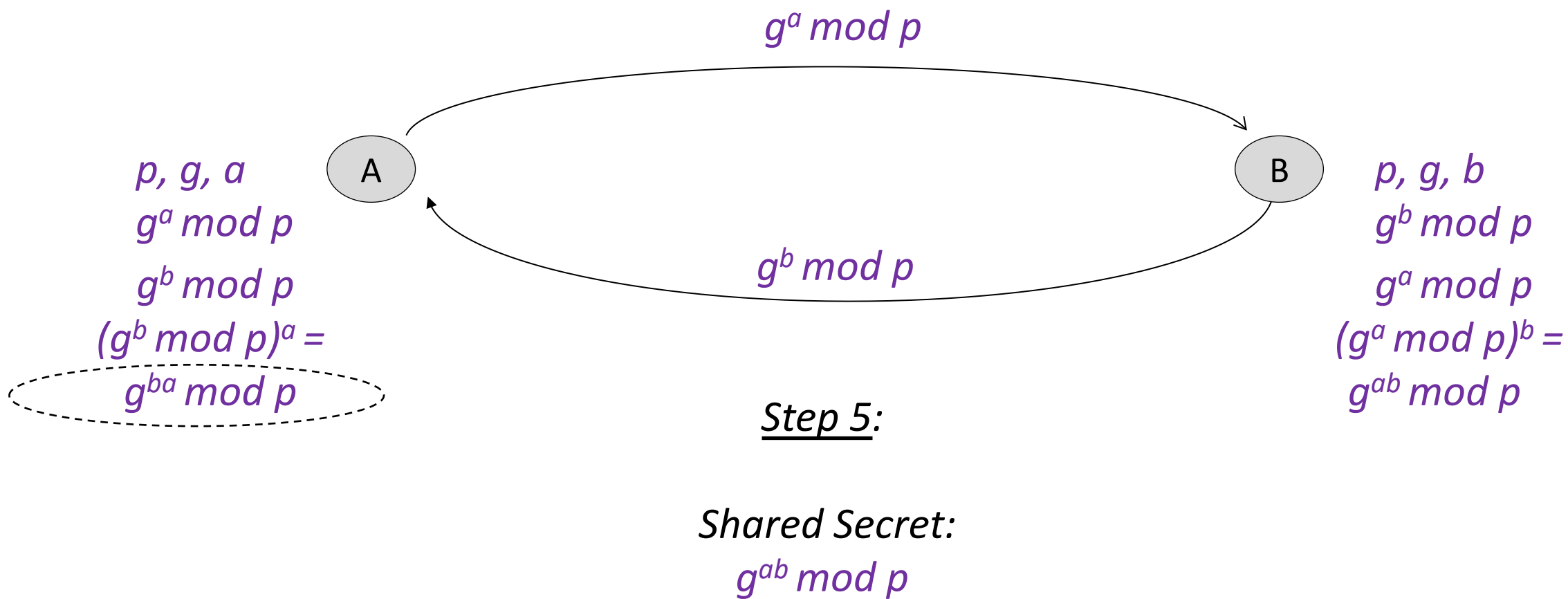


Step 4:

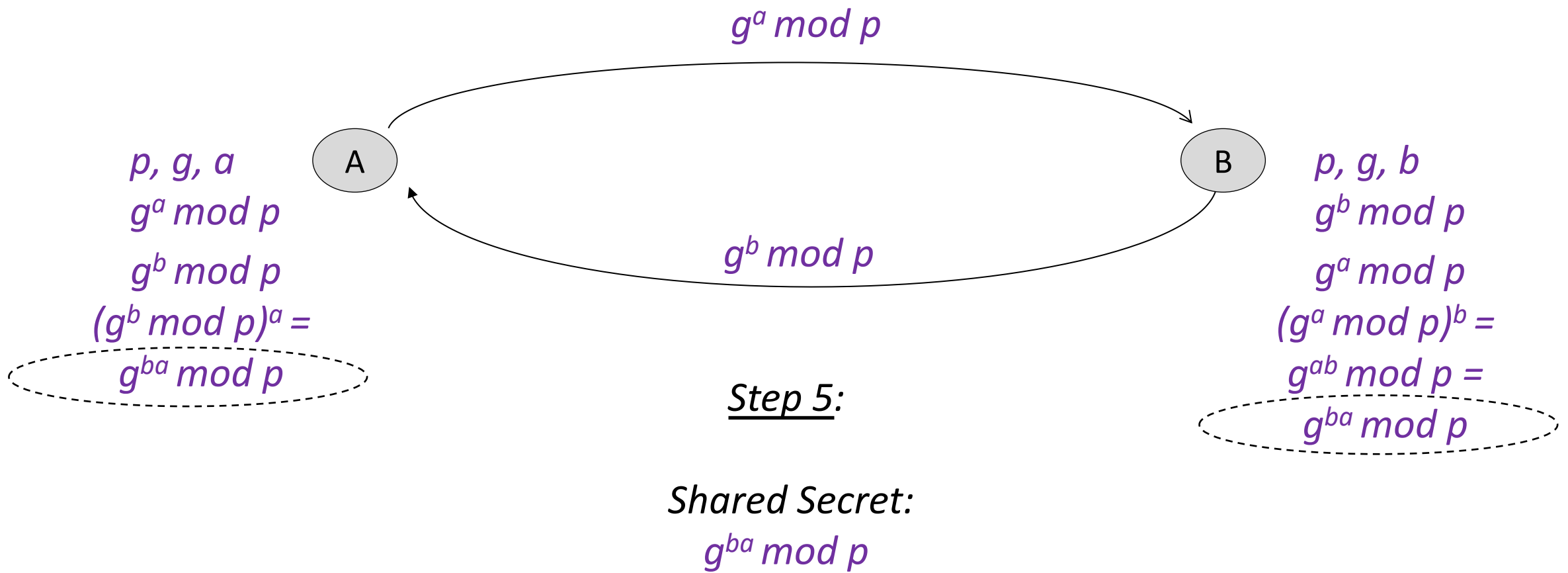
A computes  $(g^a \bmod p)^b$  to B

B computes  $(g^b \bmod p)^a$  to A

# Diffie-Hellman Key Exchange



# Diffie-Hellman Key Exchange



Week 8

# VICTOR DITTMER, WHITFIELD DIFFIE & MARTIN HELLMAN

Invented public-key  
cryptography



A.M.

**TURING**

A W A R D

2015



How Does the Original RSA Algorithm Work?

# RSA Algorithm

**Step 1:** Select two prime numbers  $p$  and  $q$ , each about 100 decimal digits in length



# RSA Algorithm

**Step 1:** Select two prime numbers  $p$  and  $q$ , each about 100 decimal digits in length

**Step 2:** Calculate  $n = pq$  and  $\psi = (p - 1)(q - 1)$

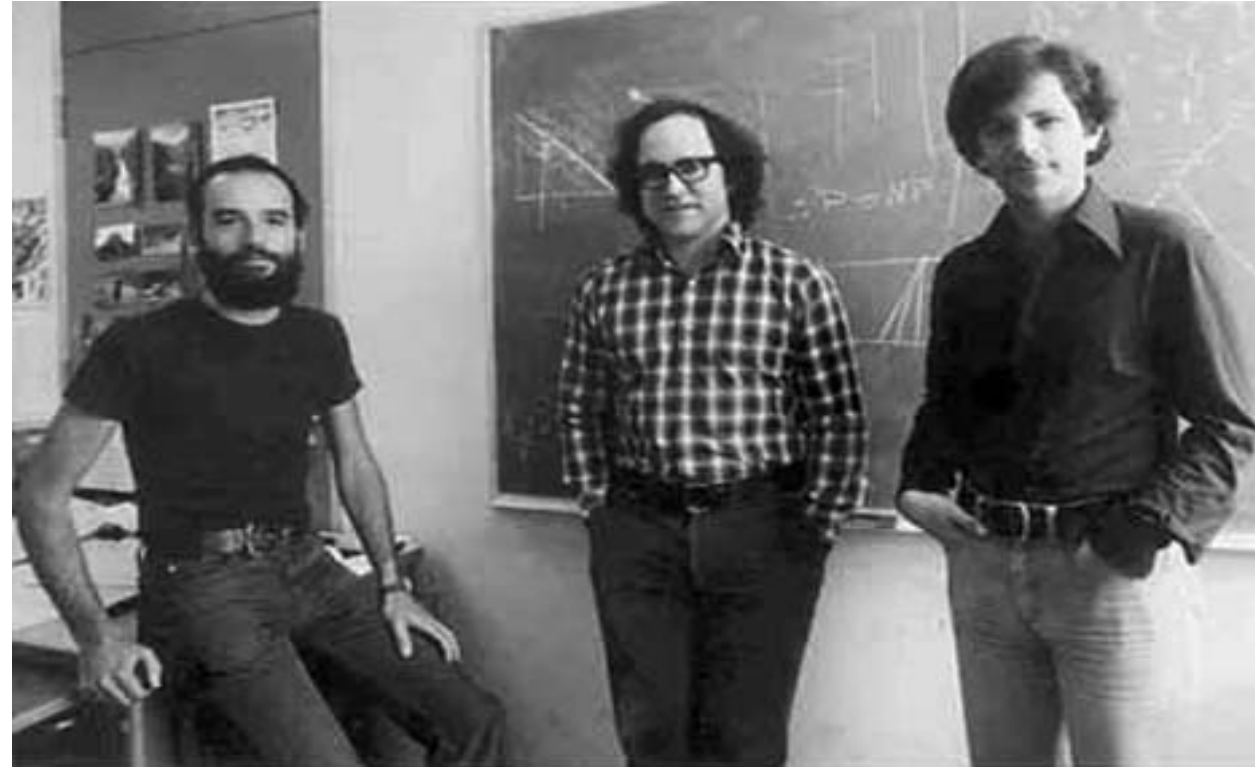


# RSA Algorithm

**Step 1:** Select two prime numbers  $p$  and  $q$ , each about 100 decimal digits in length

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**Step 3:** Select integer  $E$  between 3 and  $\Psi$ , which has no common factors with  $\Psi$



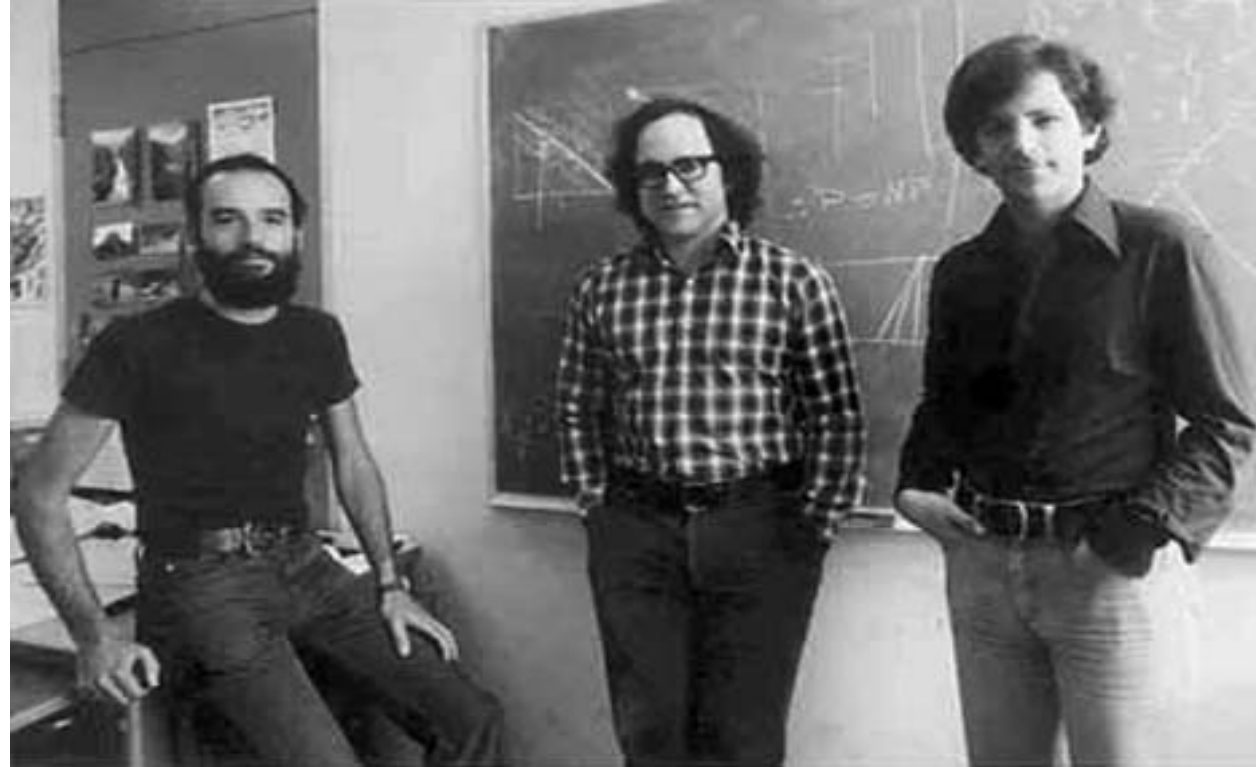
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**Step 4:** Select integer  $D$  such that  $DE$  differs by 1 from a multiple of  $\Psi$



# RSA Algorithm

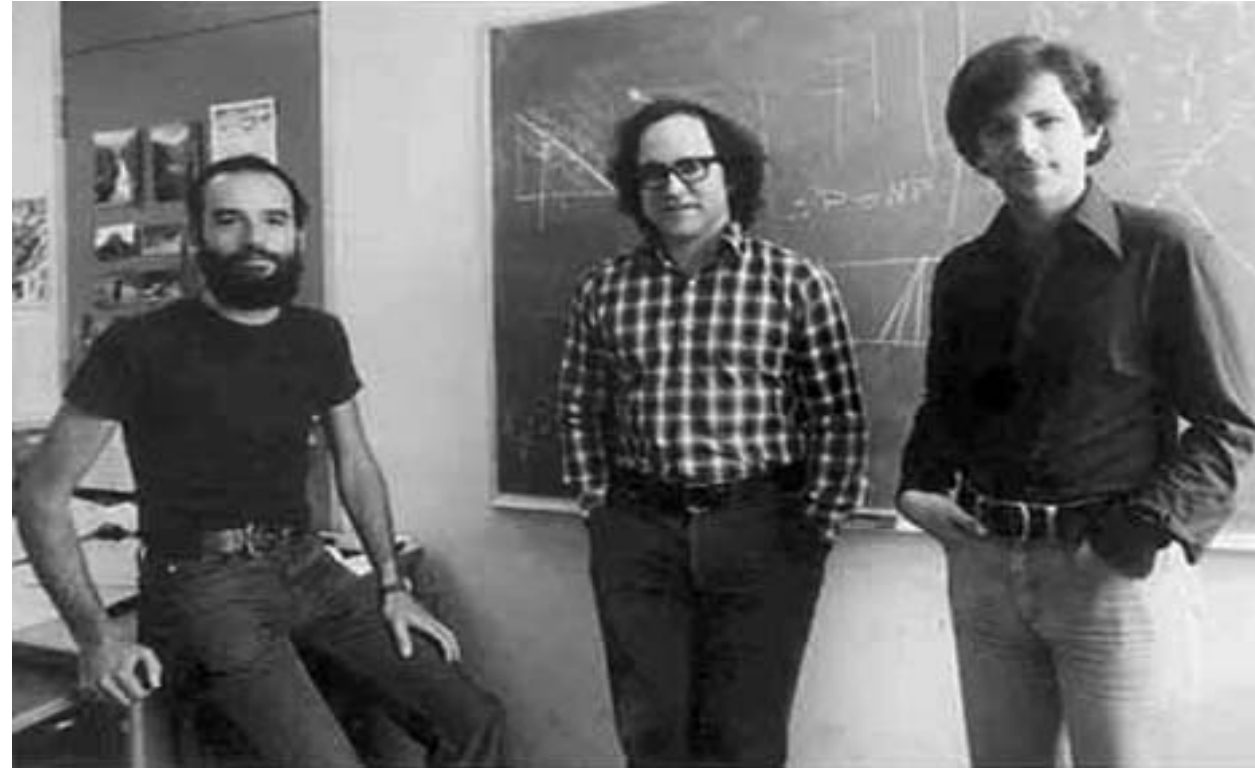
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**Step 5:** Make  $E$ ,  $n$  public, but keep  $p$ ,  $q$ ,  $D$  and  $\Psi$  secret



# RSA Algorithm

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**Encryption:**  $C = P^E \bmod n$

**Decryption:**  $P = C^D \bmod n$



# RSA Algorithm

**Step 1:** Select two prime numbers  $p$  and  $q$ , each about 100 decimal digits in length

**Step 2:** Calculate  $n = pq$  and  $\Psi = (p - 1)(q - 1)$

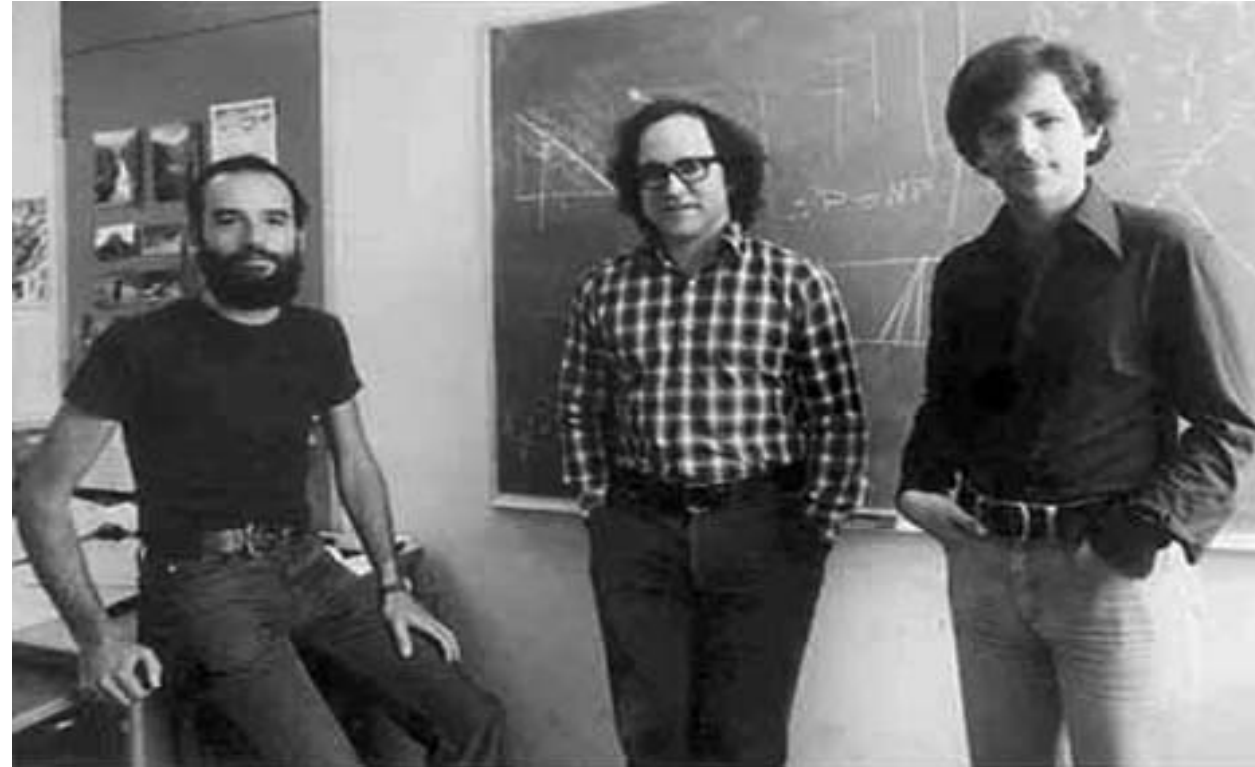
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**Encryption:**  $C = P^E \bmod n$

**Decryption:**  $P = C^D \bmod n$



**Example:**  $p = 3$ ,  $q = 5$ ,  $n = 15$ ,  $\Psi = 8$  Select  $E = 5$ ,  $D = 5$

Encrypt "2":  $2^5 \bmod 15 = 2$

Decrypt "2":  $2^5 \bmod 15 = 2$



Week 8

RON RIVEST, ADI SHAMIR & LEN ADLEMAN



A W A R D

2002



RSA public-key cryptography

A.M.  
**TURING**

Who Really Invented Public Key Technology?  
(Hint: UK)

# Public Key Cryptography – Original Paper By Diffie and Hellman

644

IEEE TRANSACTIONS ON INFORMATION THEORY, VOL. IT-22, NO. 6, NOVEMBER 1976

## New Directions in Cryptography

*Invited Paper*

WHITFIELD DIFFIE AND MARTIN E. HELLMAN, MEMBER, IEEE

**Abstract**—Two kinds of contemporary developments in cryptography are examined. Widening applications of teleprocessing have given rise to a need for new types of cryptographic systems, which minimize the need for secure key distribution channels and supply the equivalent of a written signature. This paper suggests ways to solve these currently open problems. It also discusses how the theories of communication and computation are beginning to provide the tools to solve cryptographic problems of long standing.

### I. INTRODUCTION

**W**E STAND TODAY on the brink of a revolution in cryptography. The development of cheap digital hardware has freed it from the design limitations of mechanical computing and brought the cost of high grade cryptographic devices down to where they can be used in such commercial applications as remote cash dispensers and computer terminals. In turn, such applications create a need for new types of cryptographic systems which minimize the necessity of secure key distribution channels

The best known cryptographic problem is that of privacy: preventing the unauthorized extraction of information from communications over an insecure channel. In order to use cryptography to insure privacy, however, it is currently necessary for the communicating parties to share a key which is known to no one else. This is done by sending the key in advance over some secure channel such as private courier or registered mail. A private conversation between two people with no prior acquaintance is a common occurrence in business, however, and it is unrealistic to expect initial business contacts to be postponed long enough for keys to be transmitted by some physical means. The cost and delay imposed by this key distribution problem is a major barrier to the transfer of business communications to large teleprocessing networks.

Section III proposes two approaches to transmitting keying information over public (i.e., insecure) channels without compromising the security of the system. In a *public key cryptosystem* enciphering and deciphering are governed by distinct keys,  $E$  and  $D$ , such that computing  $D$  from  $E$  is computationally infeasible (e.g., requiring

## James Ellis, Engineer at GCHQ – Circa 1969



## Bell Labs – Project C43 (1944)

<del>SECRET</del> 054 450						ATI- 29345
TITLE: Final Report - Part I - Speech Privacy Systems - Interception, Diagnosis, Decoding, Evaluation						REVISION (None)
AUTHOR(S): Koenig, W.						ORIG. AGENCY NO. (None)
ORIGINATING AGENCY: Bell Telephone Labs., Inc., New York, N. Y.						PUBLISHING AGENCY NO. 4573A
PUBLISHED BY: Office of Scientific Research and Development, NDRC, Div. 13						
DATE Oct '44	DOC. CLASS. Secr.	COUNTRY U.S.	LANGUAGE Eng.	PAGES 111	ILLUSTRATIONS photos, tables, diagrs	
<p><b>ABSTRACT:</b></p> <p>The results of three years' experience in diagnosing, decoding, and evaluating speech privacy systems are summarized. Speech privacy systems may be used in connection with radio telephone systems or wire systems, but radio interception problems only are discussed. The decoding techniques described apply to wire as well as to radio communications. The sound spectrograph is described including its history, method of operation, and capabilities. It analyzes speech in terms of its three basic dimensions, frequency, amplitude, and time; and portrays the analysis in the form of spectrograms. Basic speech scrambling methods are also explained in which the original speech is transmitted with its parts modified, displaced, or interchanged. Cryptanalysis and cryptography, which apply to telegraph types of communication, are also described.</p>						
<p><i>NTIS SOP memo 2 Aug 60</i></p> <p>DISTRIBUTION: Copies of this report obtainable from <del>the Communications Division, AT&amp;T, MCDND</del></p>						
DIVISION: Electronics (6)				SUBJECT HEADINGS: Communication systems, Secret (23992.87); Decoders (28877)		
SECTION: Communications (14, 5, 6)						
<b>AD-A800 206</b>				CAL INDEX <del>SECRET</del> Wright-Patterson Air Force Base Dayton, Ohio		



# GCHQ – Original and New Headquarters in Cheltenham, UK



# James Ellis' Paper 1970 – Classified for Three Decades

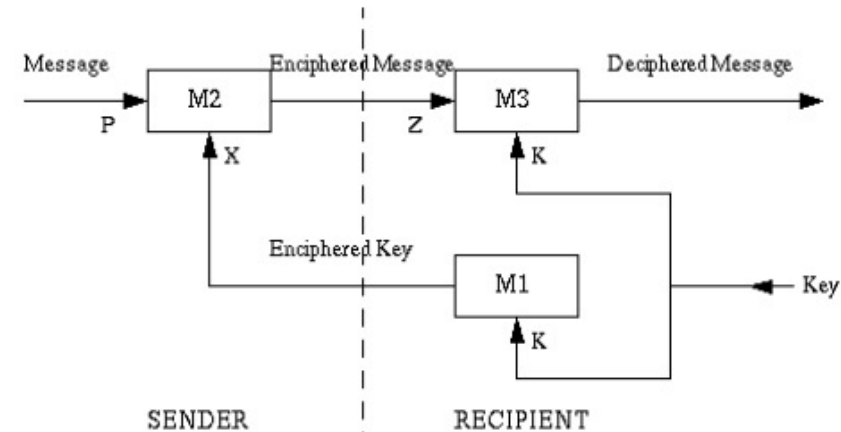
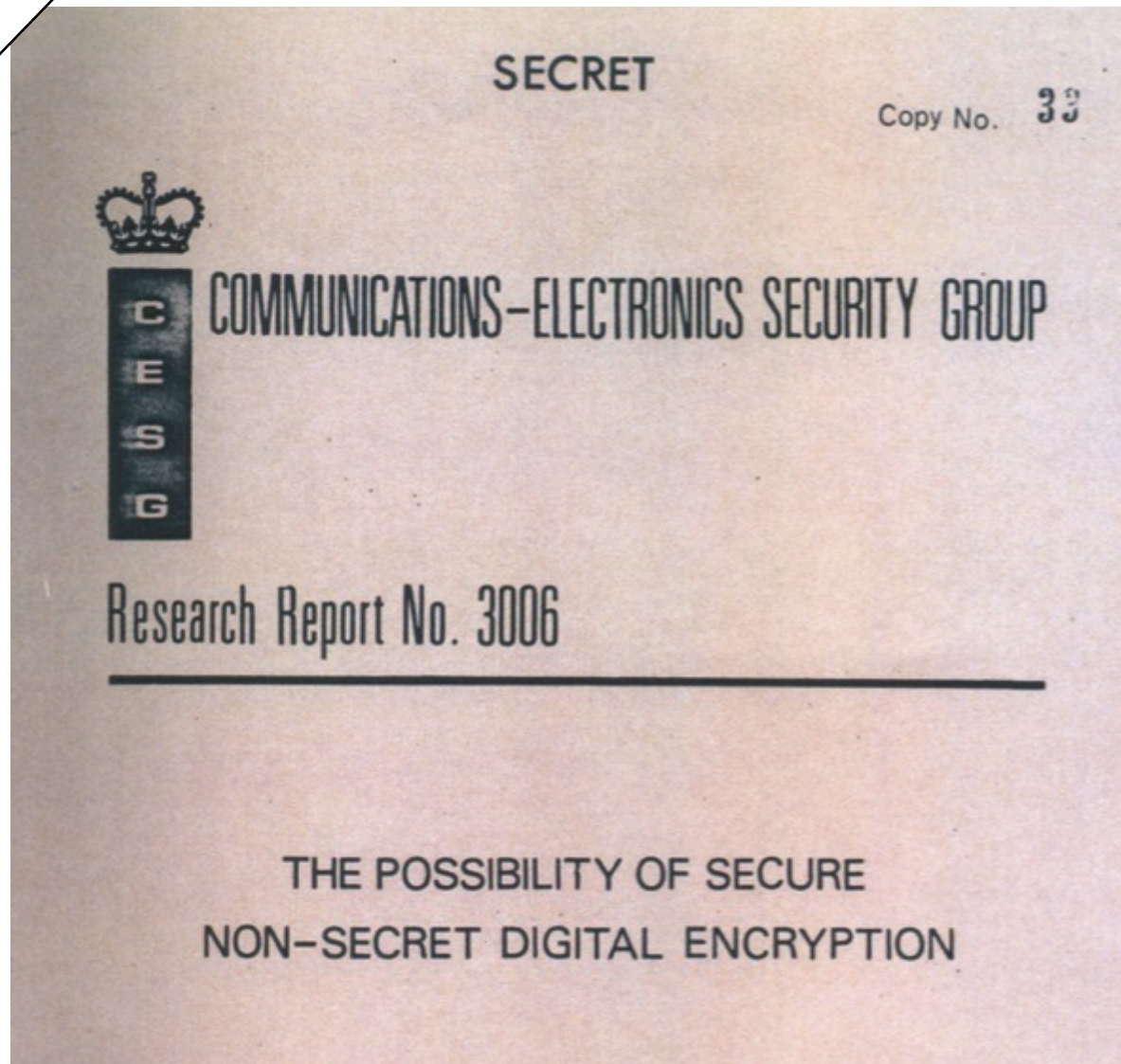


Fig. 1

13. The following properties are clearly essential. It must be impossible for the interceptor to obtain  $p$  from  $z$  without knowing  $k$  even though he knows  $x$ . Also, since a knowledge of  $k$  would enable him to decipher  $z$ , he must be unable to obtain  $k$  from  $x$ . Finally  $M3$  must have the property of being able to decipher  $z$ . To obtain these properties we specify the look-up tables corresponding to  $M1$ ,  $M2$  and  $M3$  in the following way: -
- Let  $k$  have  $n$  different possible values and  $p$  have  $m$  different possible values, for simplicity take them to be the integers 1 to  $n$  and 1 to  $m$  respectively. Let  $x$  have the same range of values as  $k$ , and  $z$  have the same range as  $p$ .
  - $M1$  can be defined as a linear look-up table of  $n$  entries whose contents are the numbers 1 to  $n$  in a random order, where "random" implies that the output is sufficiently uncorrelated with the input so that the position of a particular entry in the table cannot be found in a simpler way than by searching through the table.
  - $M2$  corresponds to an  $n$  by  $m$  rectangular table in which the entries for a fixed value of  $x$  consists of the numbers 1 to  $m$  in random order, and where the columns for the various values of  $x$  are suitable uncorrelated with one another.



# Clifford Cocks and Malcolm Williamson



SECRET

- 1 -

## Note on "Non-Secret Encryption"

In [1] J H Ellis describes a theoretical method of encryption which does not necessitate the sharing of secret information between the sender and receiver. The following describes a possible implementation of this.

a. The receiver picks 2 primes  $P, Q$  satisfying the conditions

i.  $P$  does not divide  $Q-1$ .

ii.  $Q$  does not divide  $P-1$ .

He then transmits  $N = PQ$  to the sender.

b. The sender has a message, consisting of numbers

$C_1, C_2, \dots, C_r$  with  $0 < C_i < N$

He sends each, encoded as  $D_i$  where

$$D_i = C_i^N \text{ reduced modulo } N.$$

c. To decode, the receiver finds, by Euclids Algorithm, numbers  $P', Q'$

satisfying  $P P' \equiv 1 \pmod{Q-1}$

$Q Q' \equiv 1 \pmod{P-1}$

Then  $C_i \equiv D_i^{P'} \pmod{Q}$

and  $C_i \equiv D_i^{Q'} \pmod{P}$

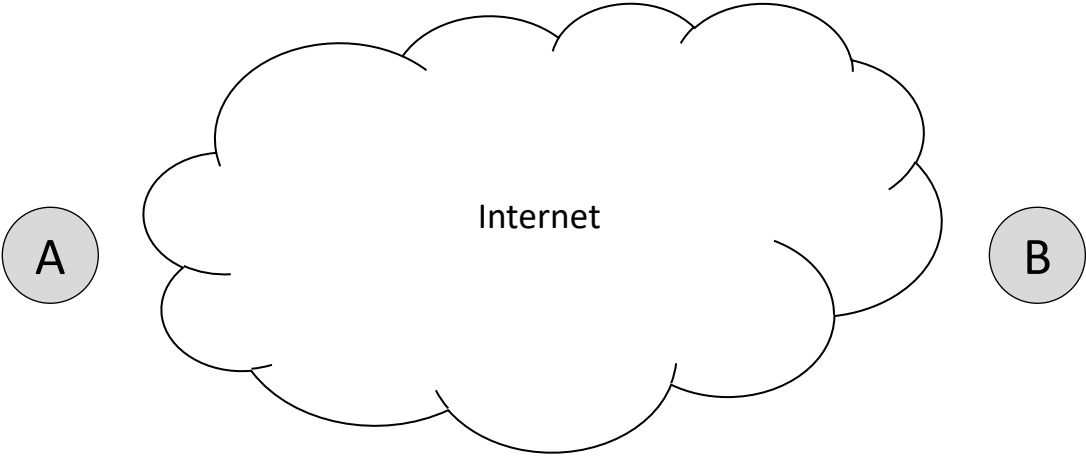


## Credit Where Credit is Due

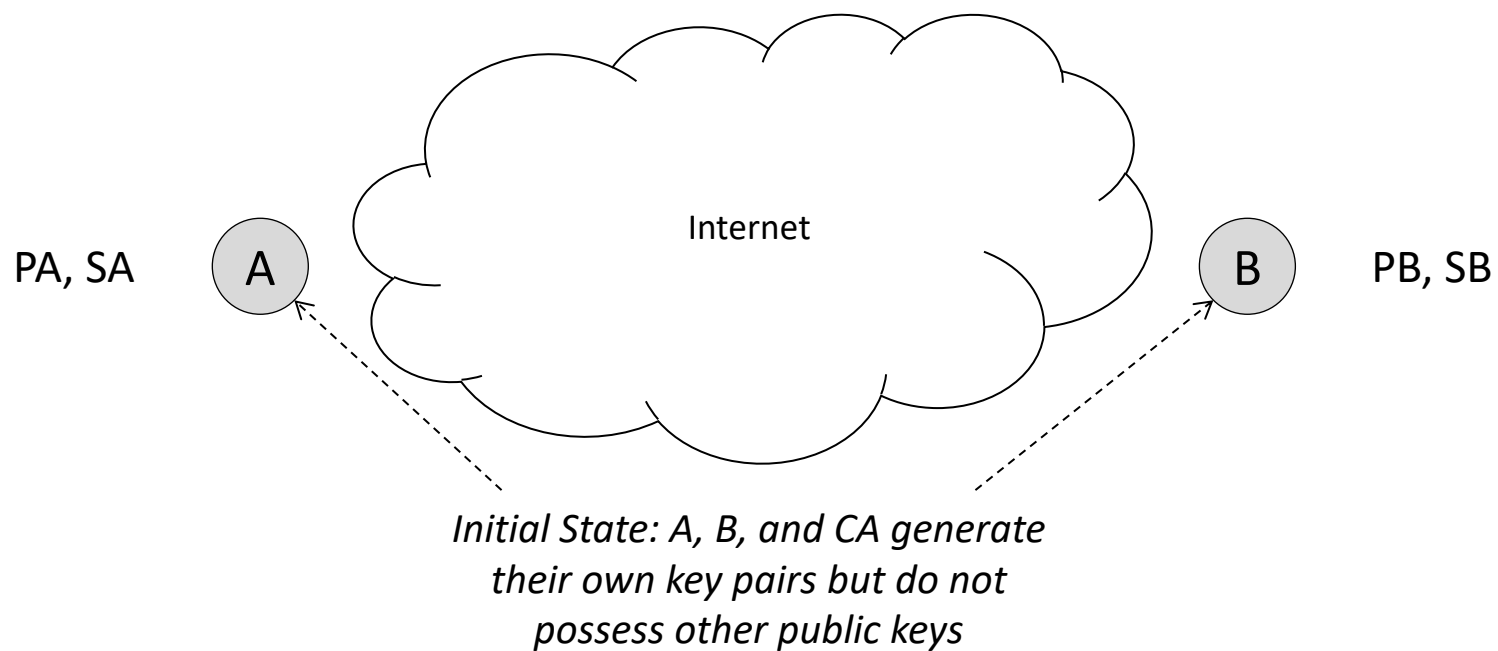


How are Keys Distributed?

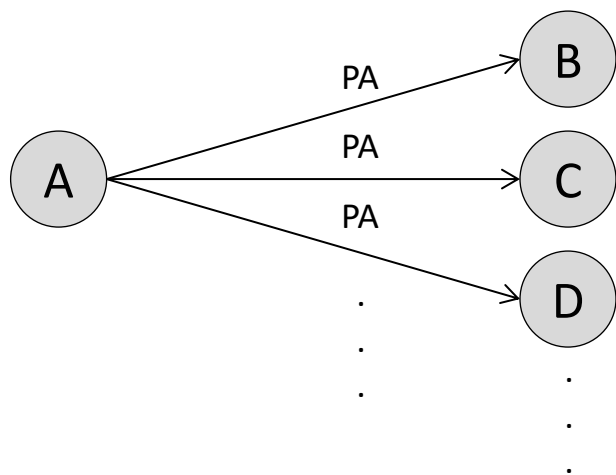
# Public Key Distribution



# Public Key Distribution

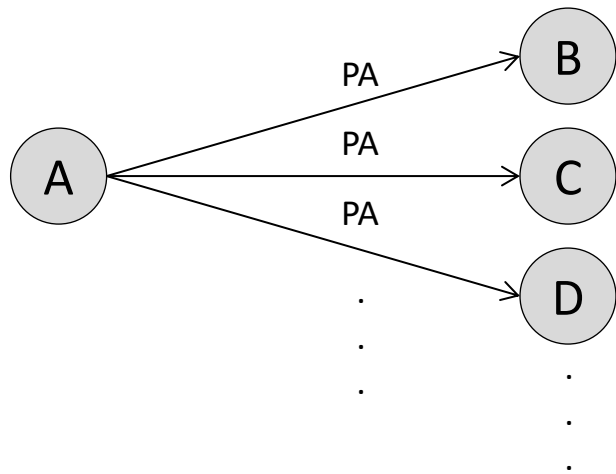


# Public Key Distribution – Manual Distribution

**Manual Distribution:**

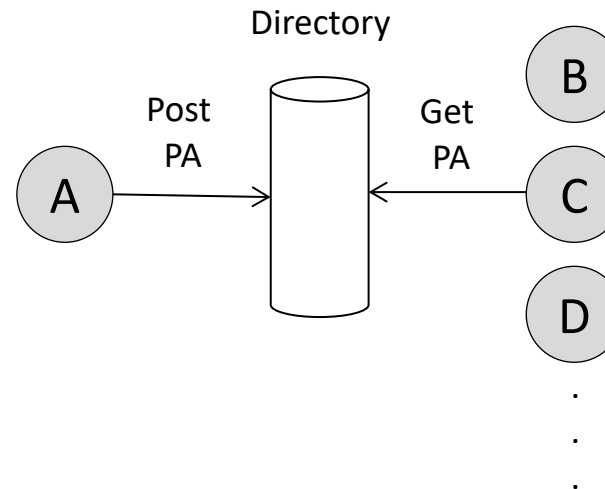
- Easy, attach to email, etc.
- Does not scale across large groups
- One new participant to group of size  $X$ , requires  $X$  key actions

# Public Key Distribution – Directory Post



## Manual Distribution:

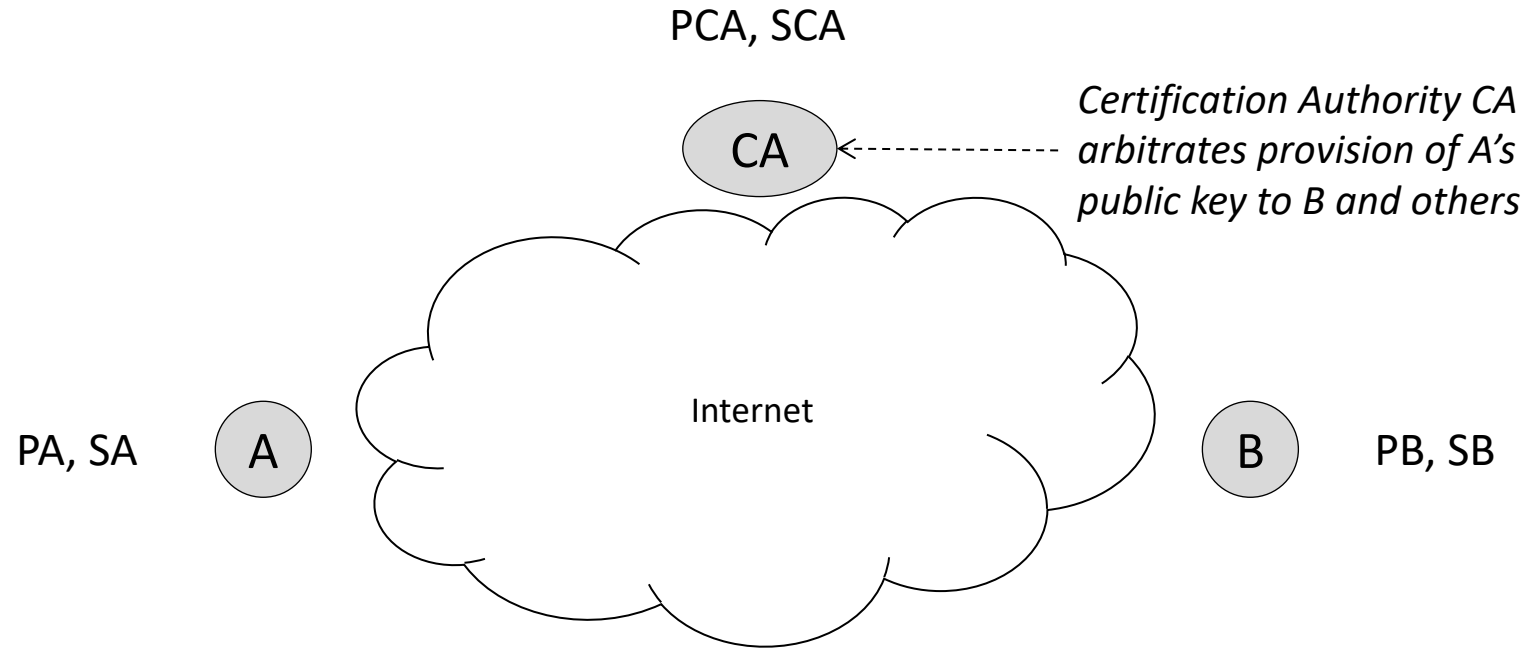
- Easy, attach to email, etc.
- Does not scale across large groups
- One new participant to group of size X, requires X key actions



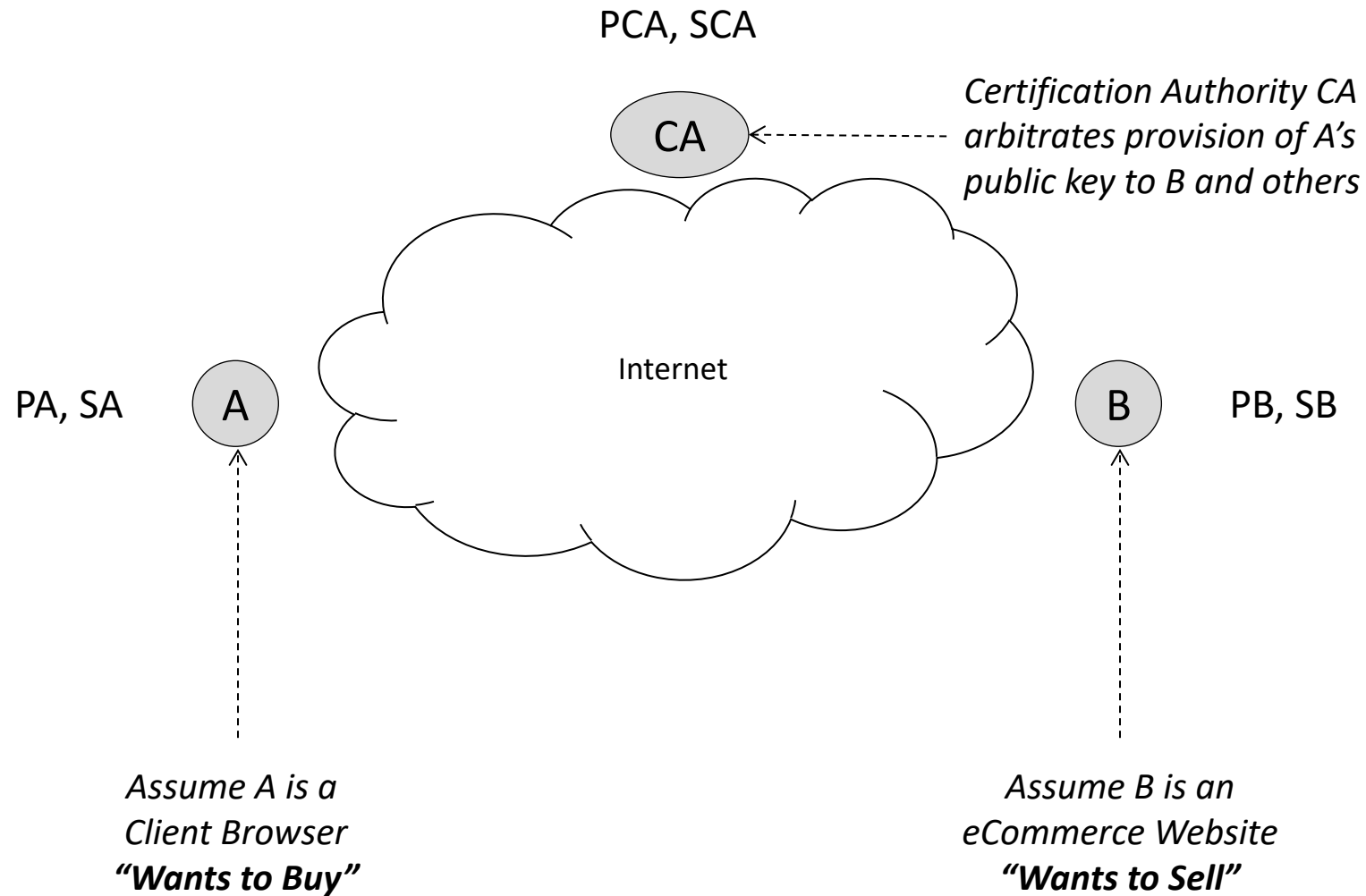
## Directory Post Distribution:

- Easy for enterprise directories
- Does not scale across large groups
- Vulnerable to outage – SPOF
- One new participant to group of size X, requires 1 post to directory

# Public Key Distribution – Certification Authority

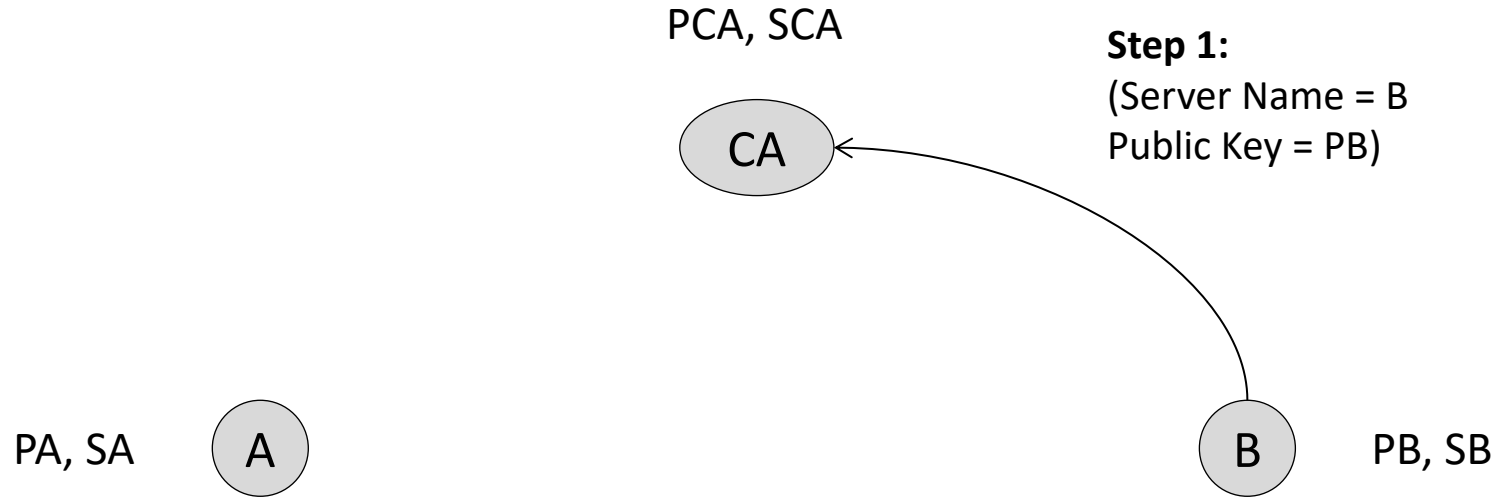


# Public Key Distribution – Certification Authority

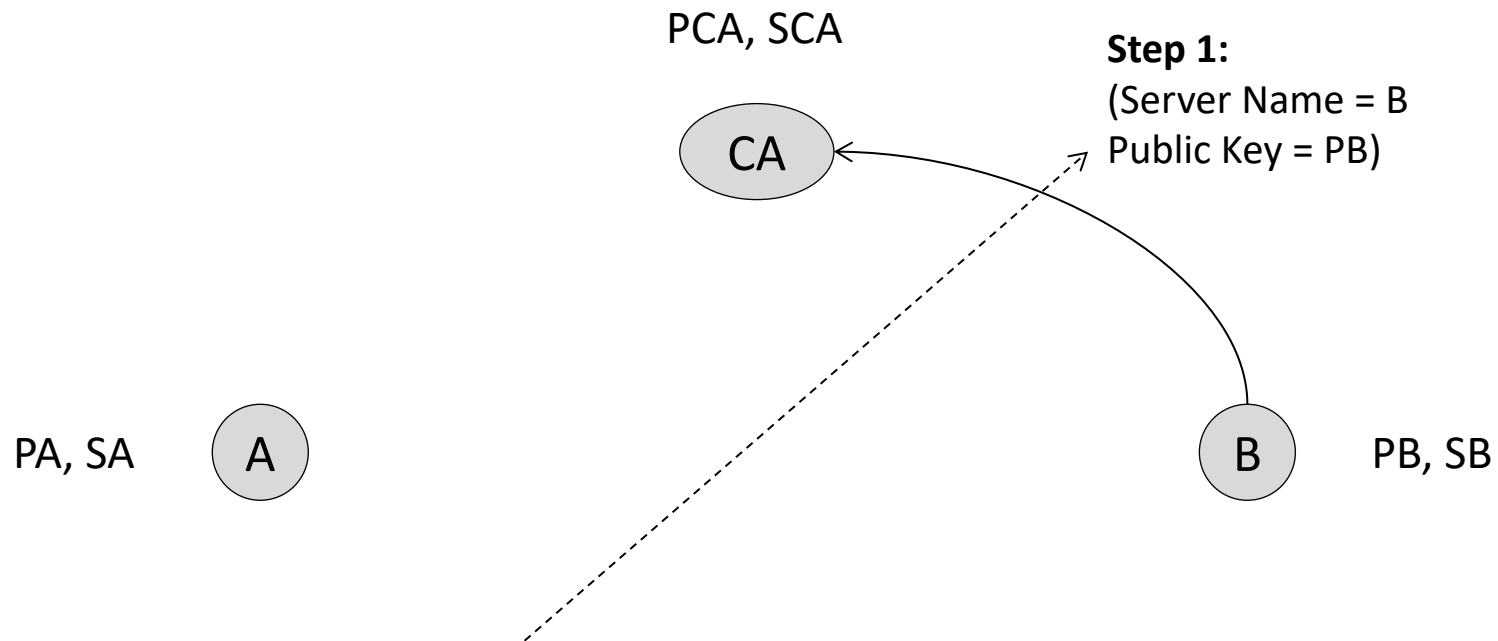




# Public Key Distribution – Certification Authority



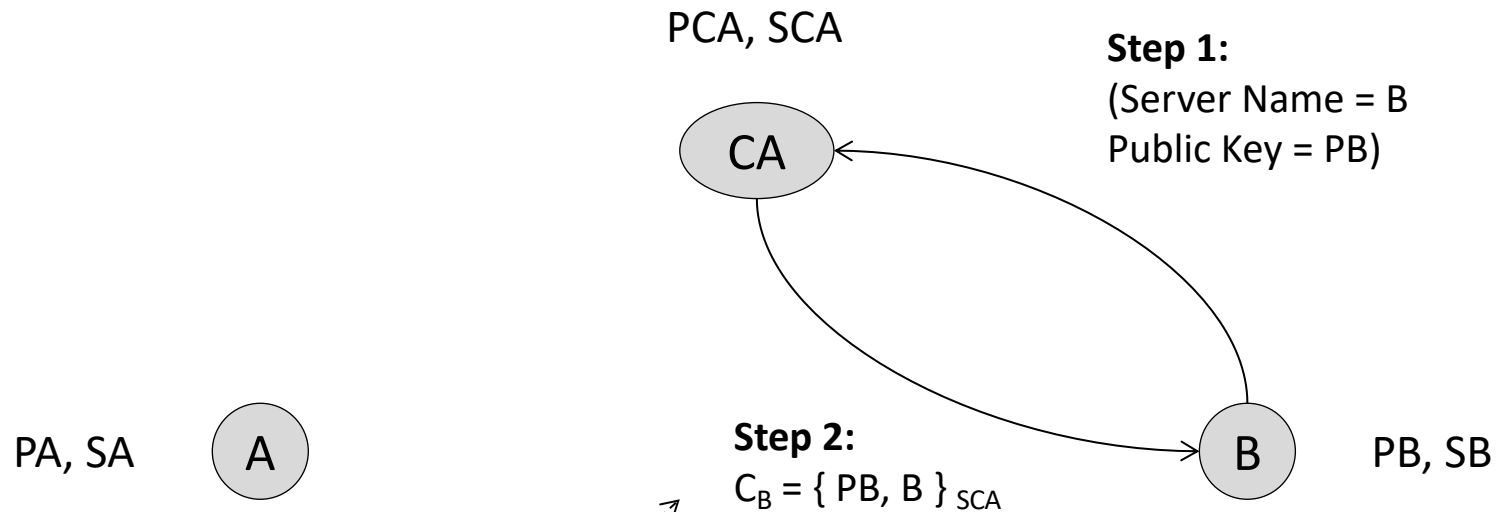
# Public Key Distribution – Certification Authority



## ***Three Potential Assurance Levels Between B and CA:***

- *Low*: Attributable Email from B's Server Admin to CA
- *Medium*: Out of Band Authentication of B's Server Admin by CA
- *High*: In-Person Authentication of B's Server Admin by CA

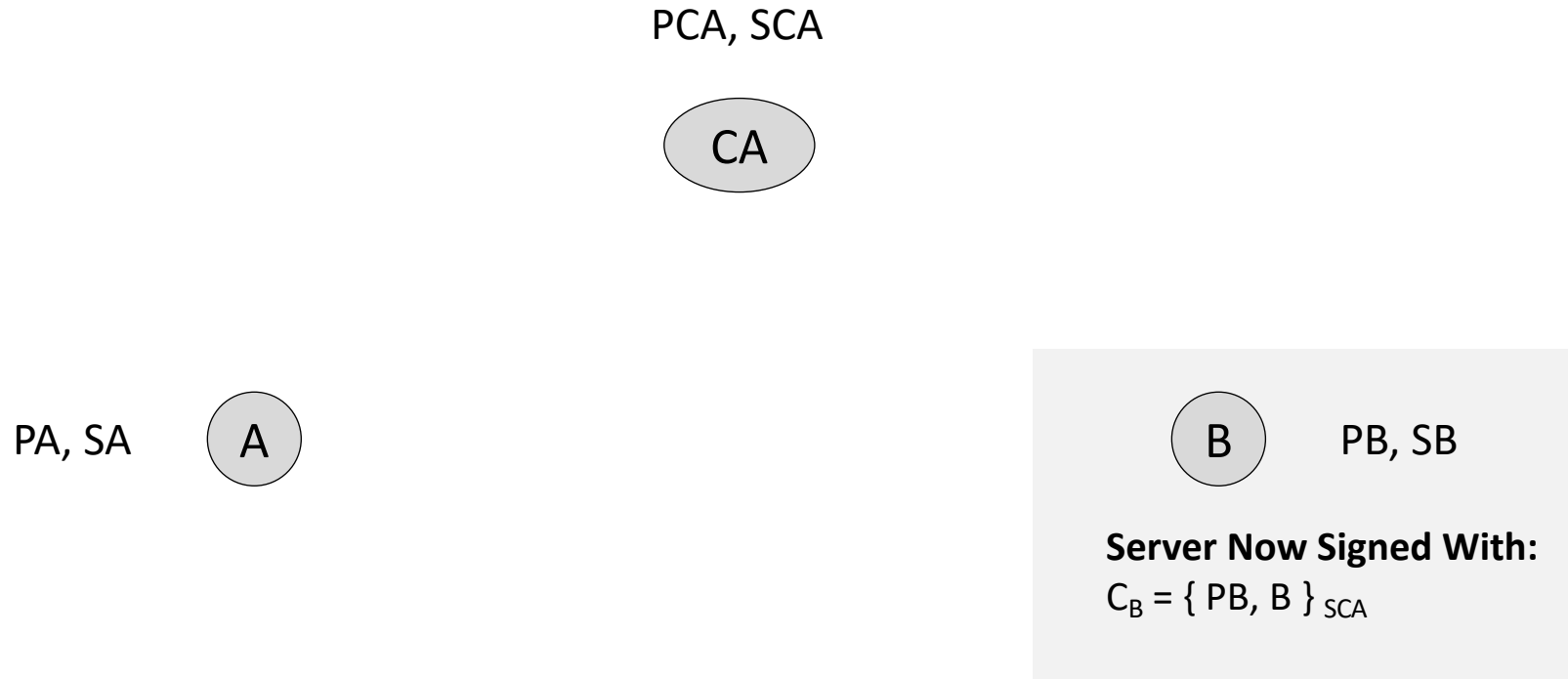
# Public Key Distribution – Certification Authority



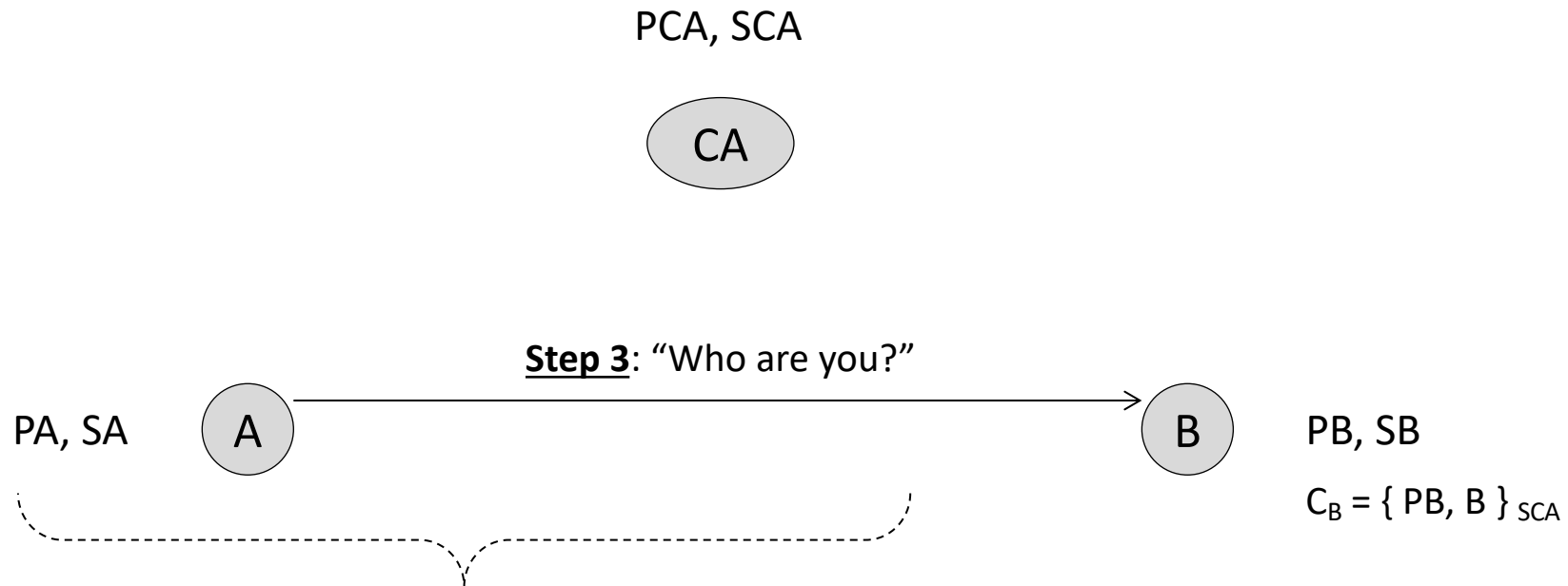
**CA Sign's the Server B with Certificate  $C_B$ :**

- Certificate follows X.509 v3 Standard
- Certificate encrypted with CA's Private Key SCA

# Public Key Distribution – Certification Authority



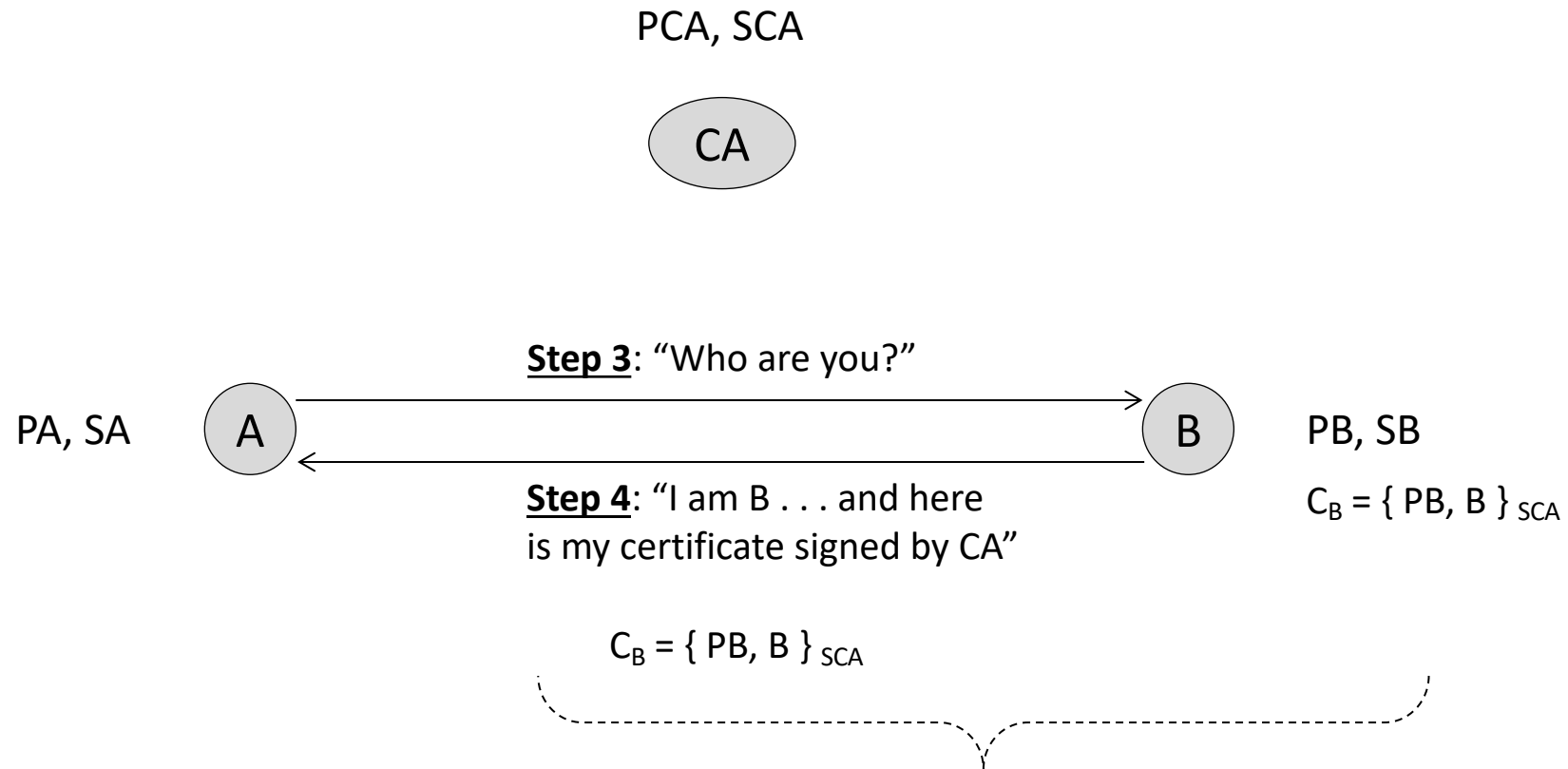
# Public Key Distribution – Certification Authority



*Server Authentication:*

A has a browser and presumably wants to buy something on B's Website

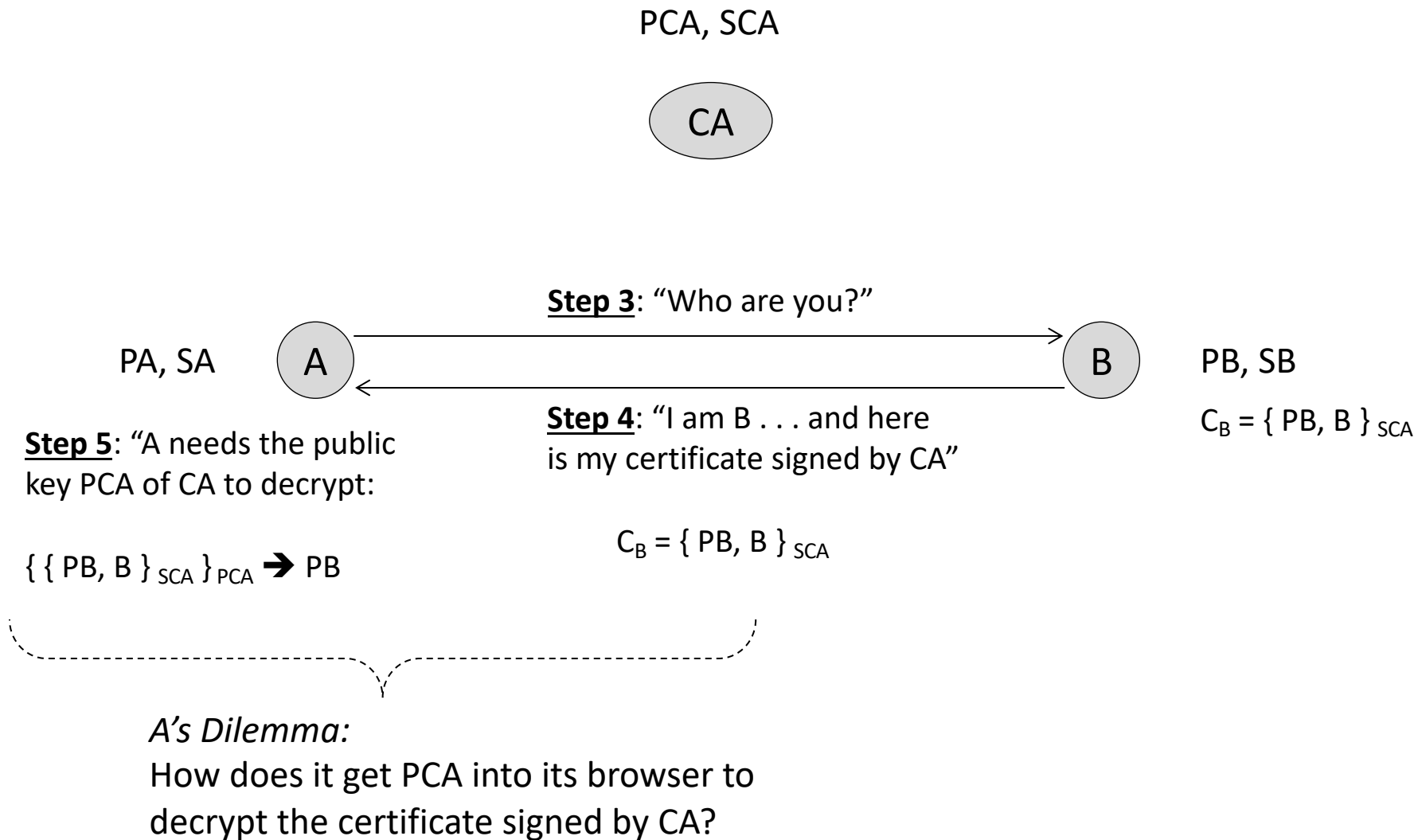
# Public Key Distribution – Certification Authority



*Server Response:*

B send its certificate to A in order to  
authenticate and send PB for encryption

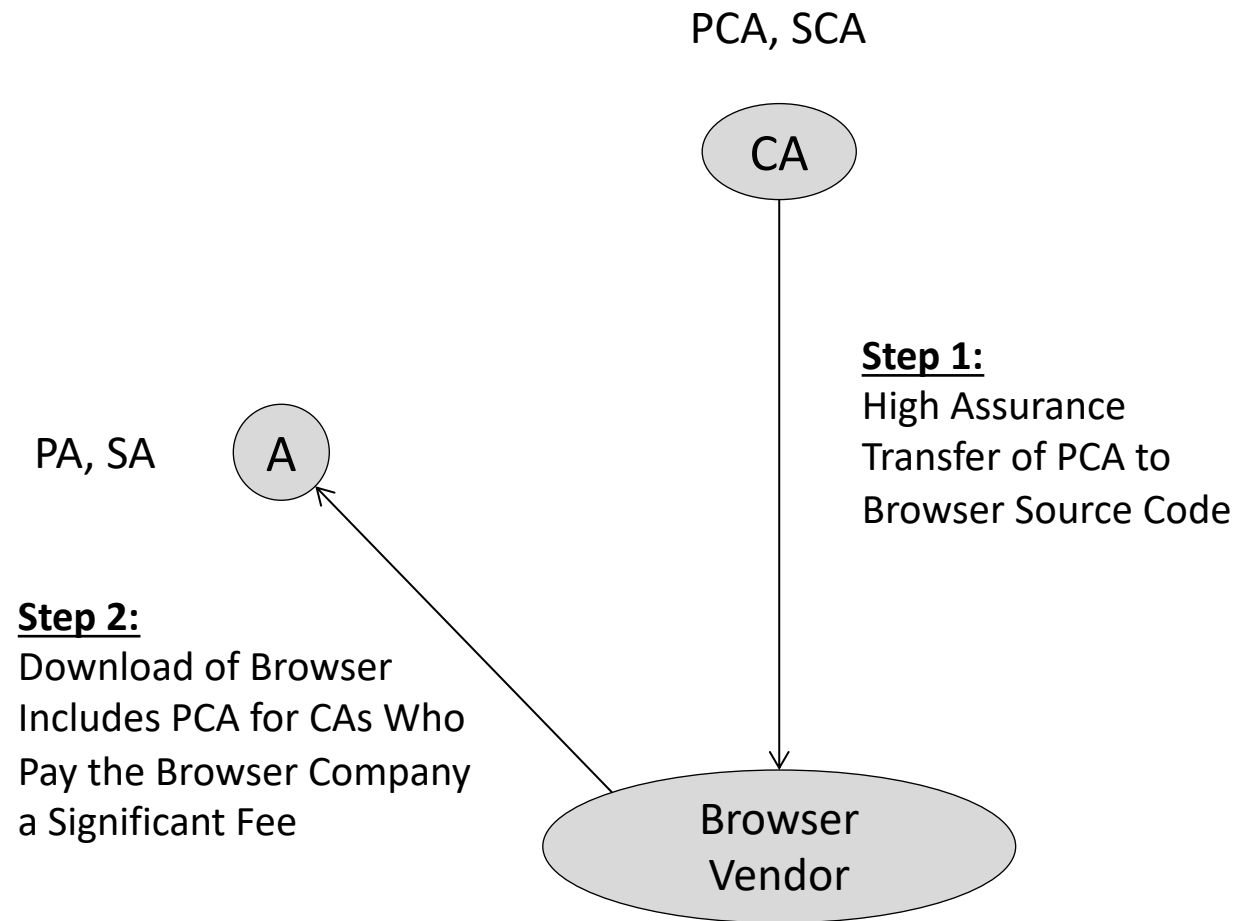
# Public Key Distribution – Certification Authority



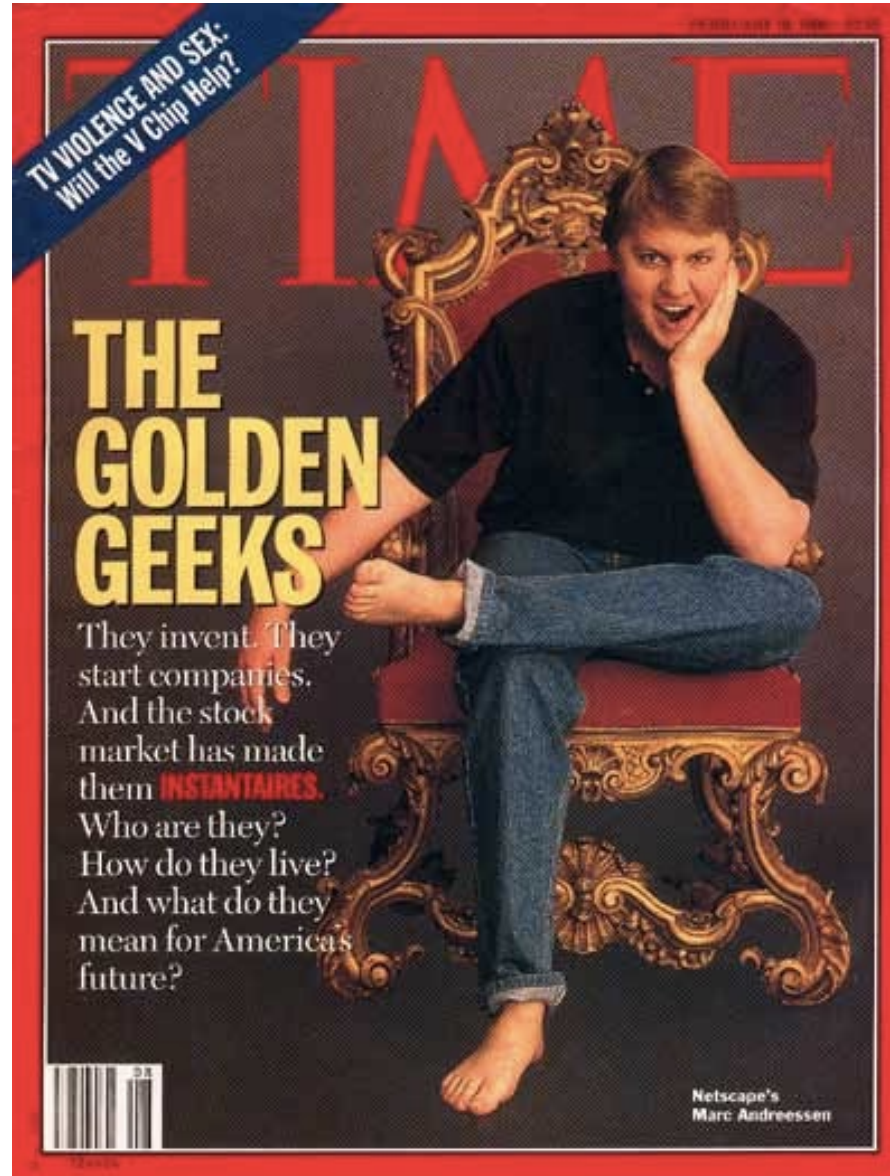
How Did Netscape Solve the CA Public Key Problem?



# Embedding Certificates in Browsers



## Resulting Protocol: Secure Sockets Layer (SSL)



Marc Andreessen  
*Netscape Browser  
Founder and Internet  
Billionaire Shown  
in Mid-1990's*

# Netscape's Historic IPO

## Actual Scenario – Post IPO

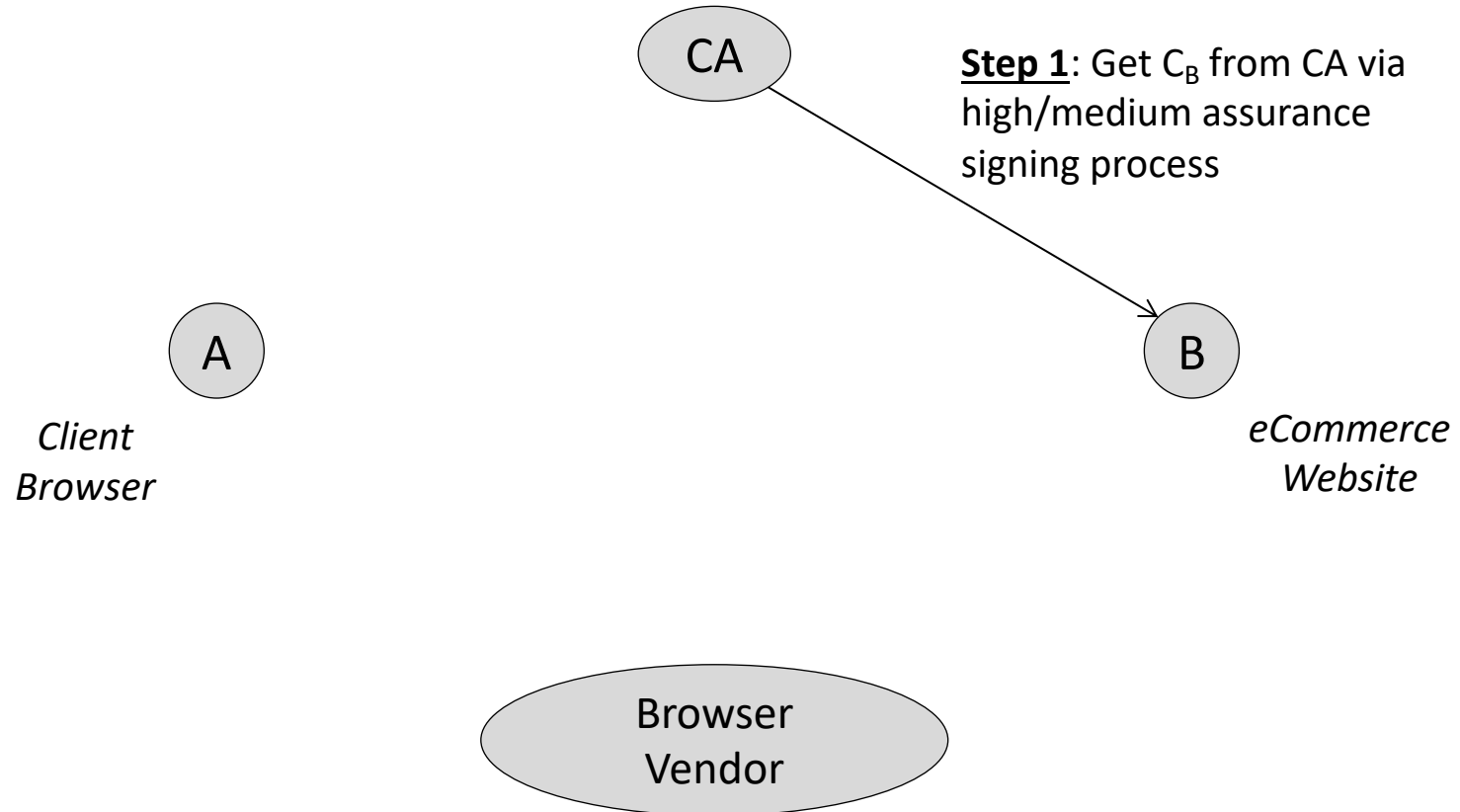
- Netscape shares opened at \$28.
- By the end of the trading day, they were going for \$75.
- The five-million-share IPO was oversubscribed by 100 million shares.
- Book Value of \$16 million was transformed into market value of a billion dollar.



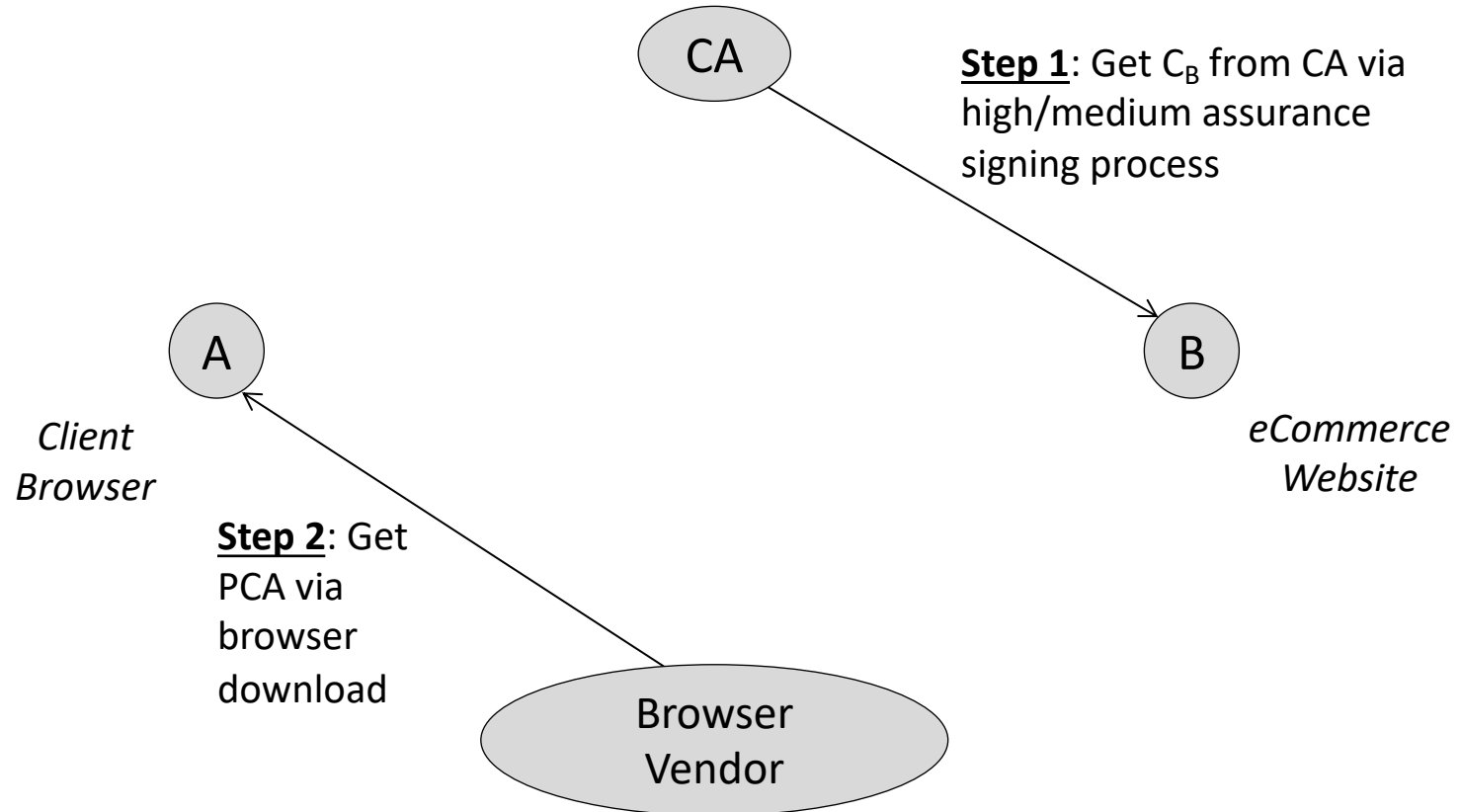
NETSCAPE



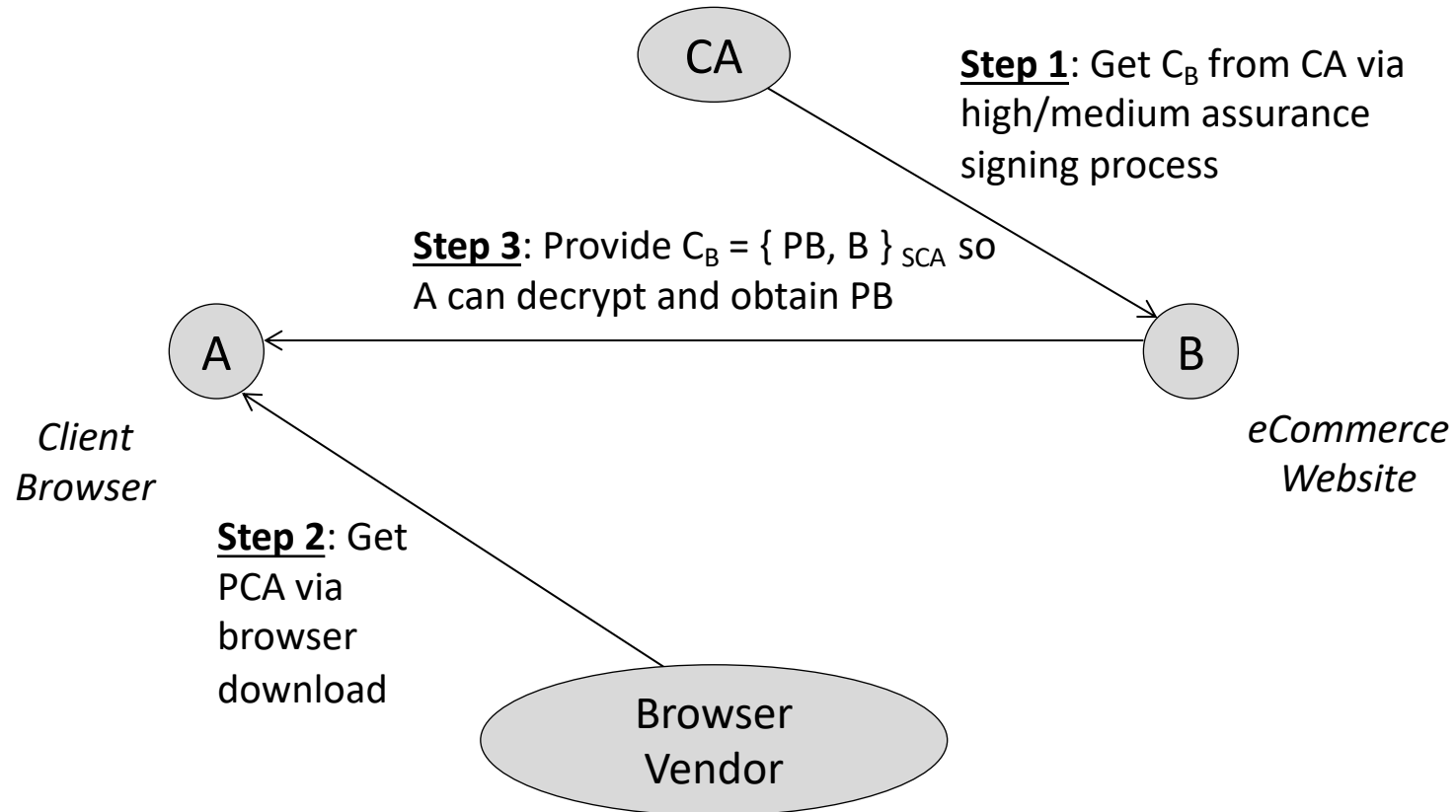
# SSL PKI/CA – Secure eCommerce



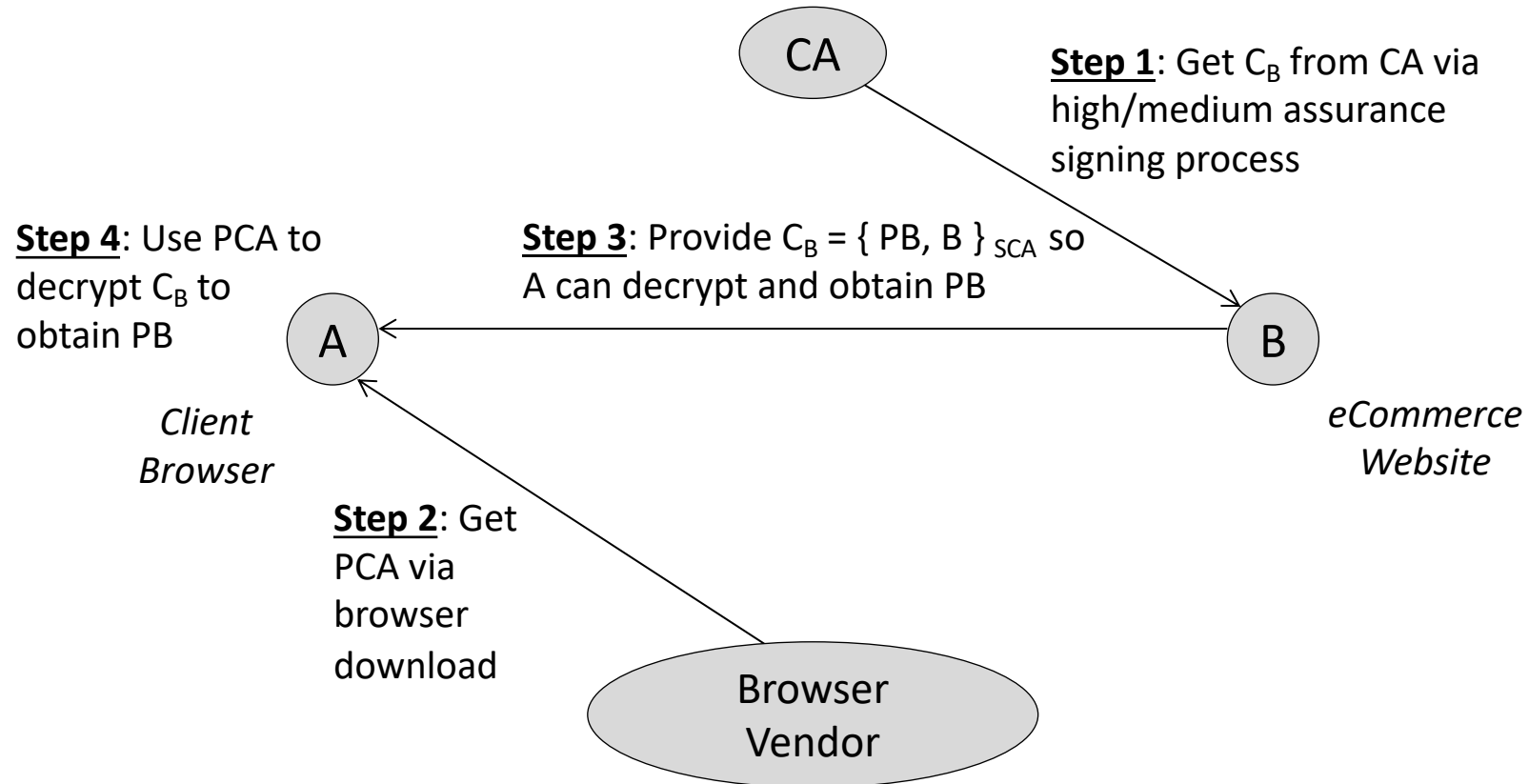
# SSL PKI/CA – Secure eCommerce



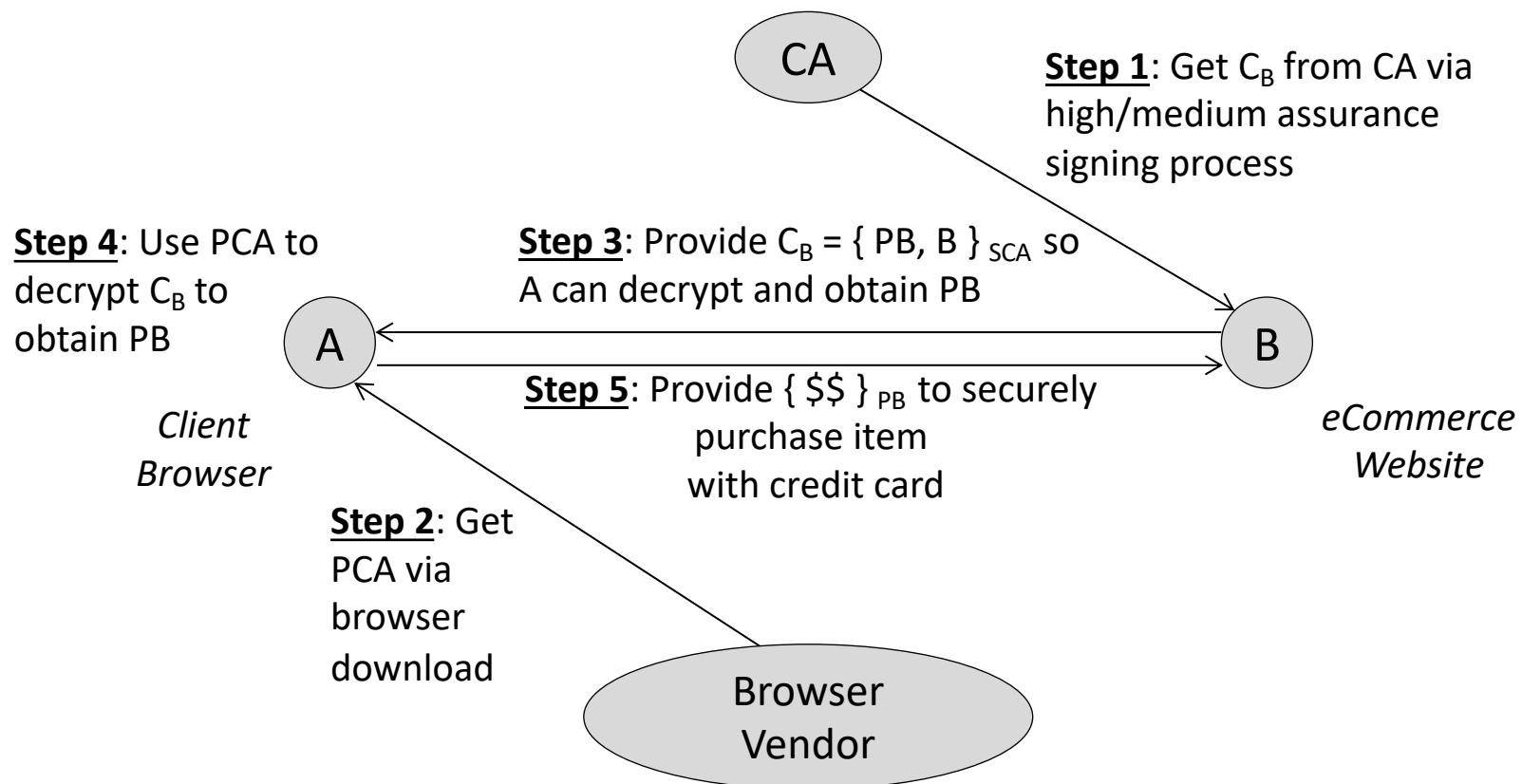
# SSL PKI/CA – Secure eCommerce



# SSL PKI/CA – Secure eCommerce



# SSL PKI/CA – Secure eCommerce





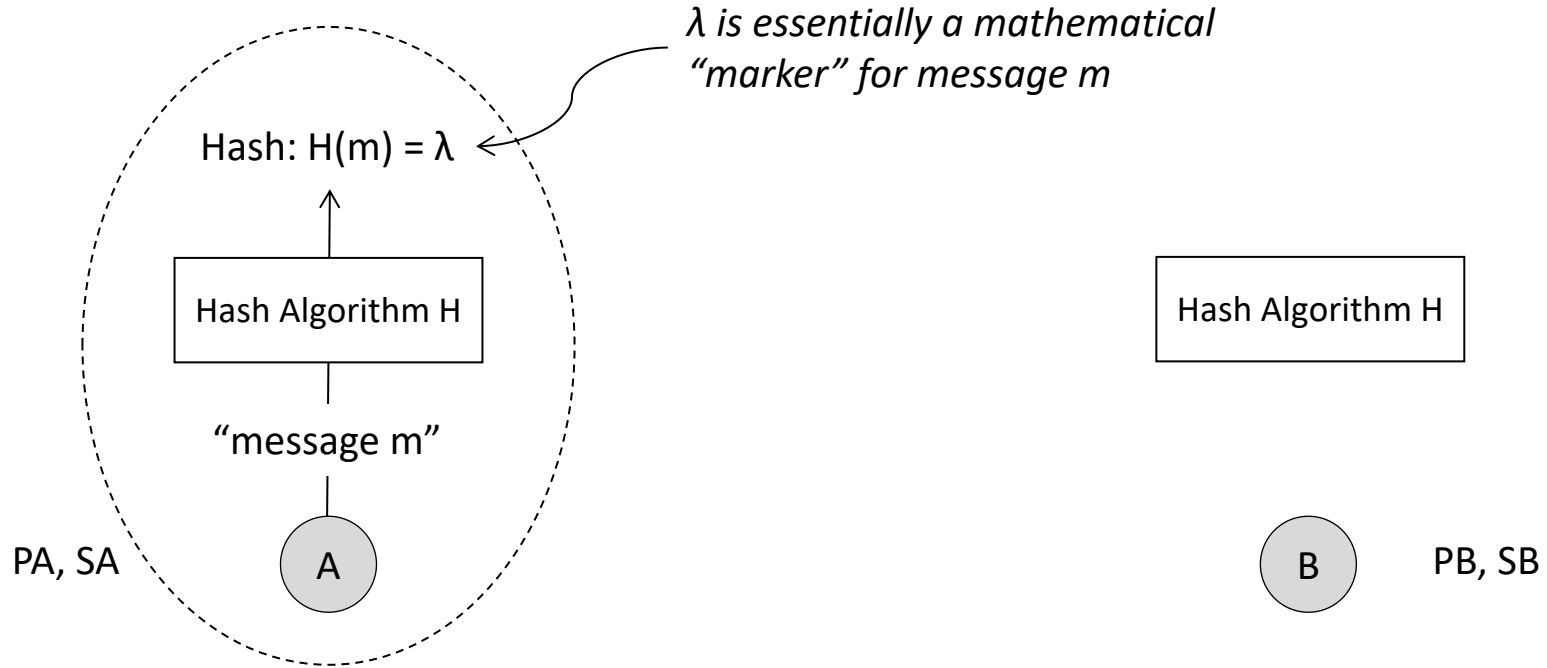
Week 8



**amazon.com**

# How Does Hashing Work?

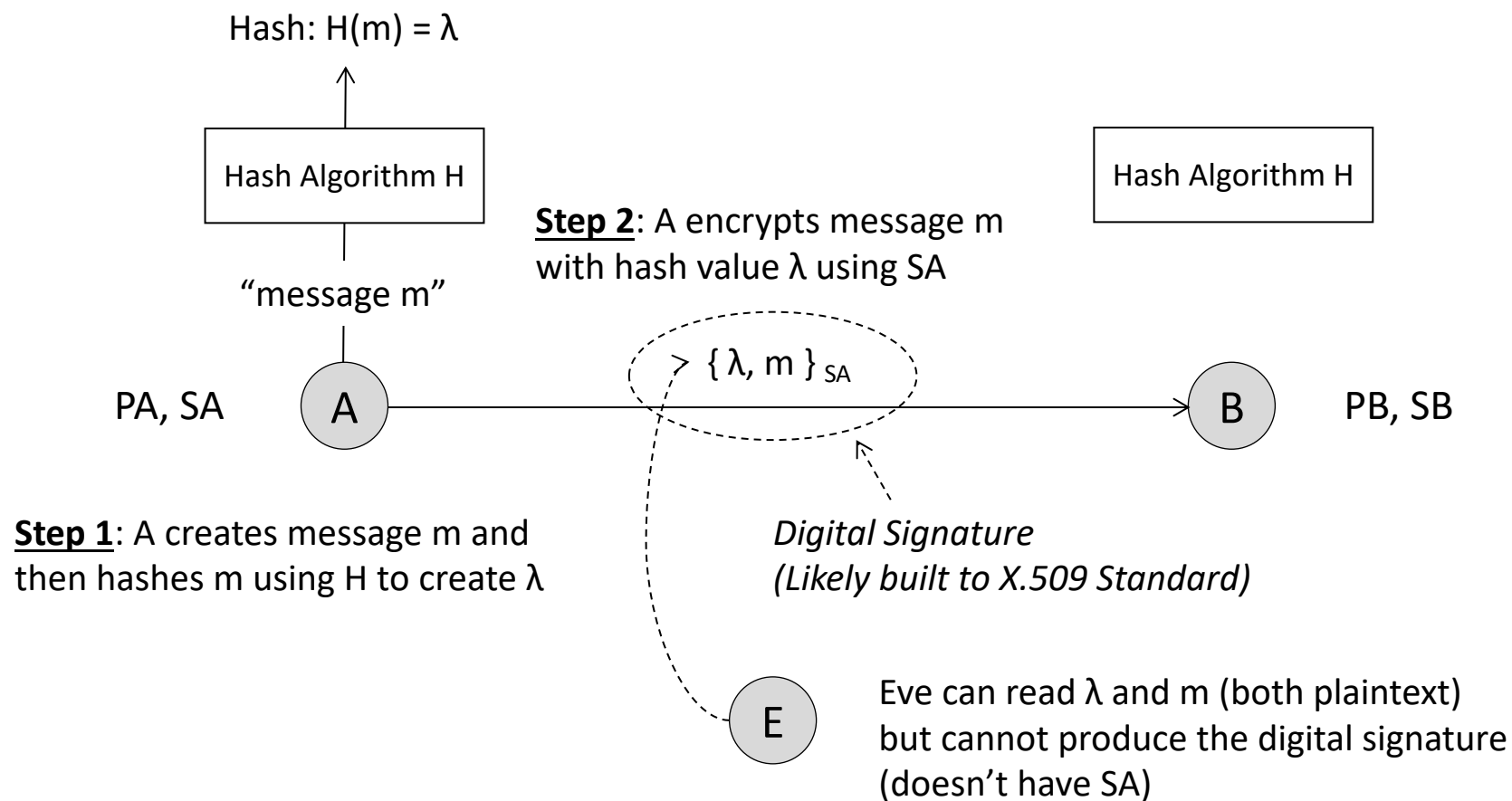
# Hashing for Digital Signature



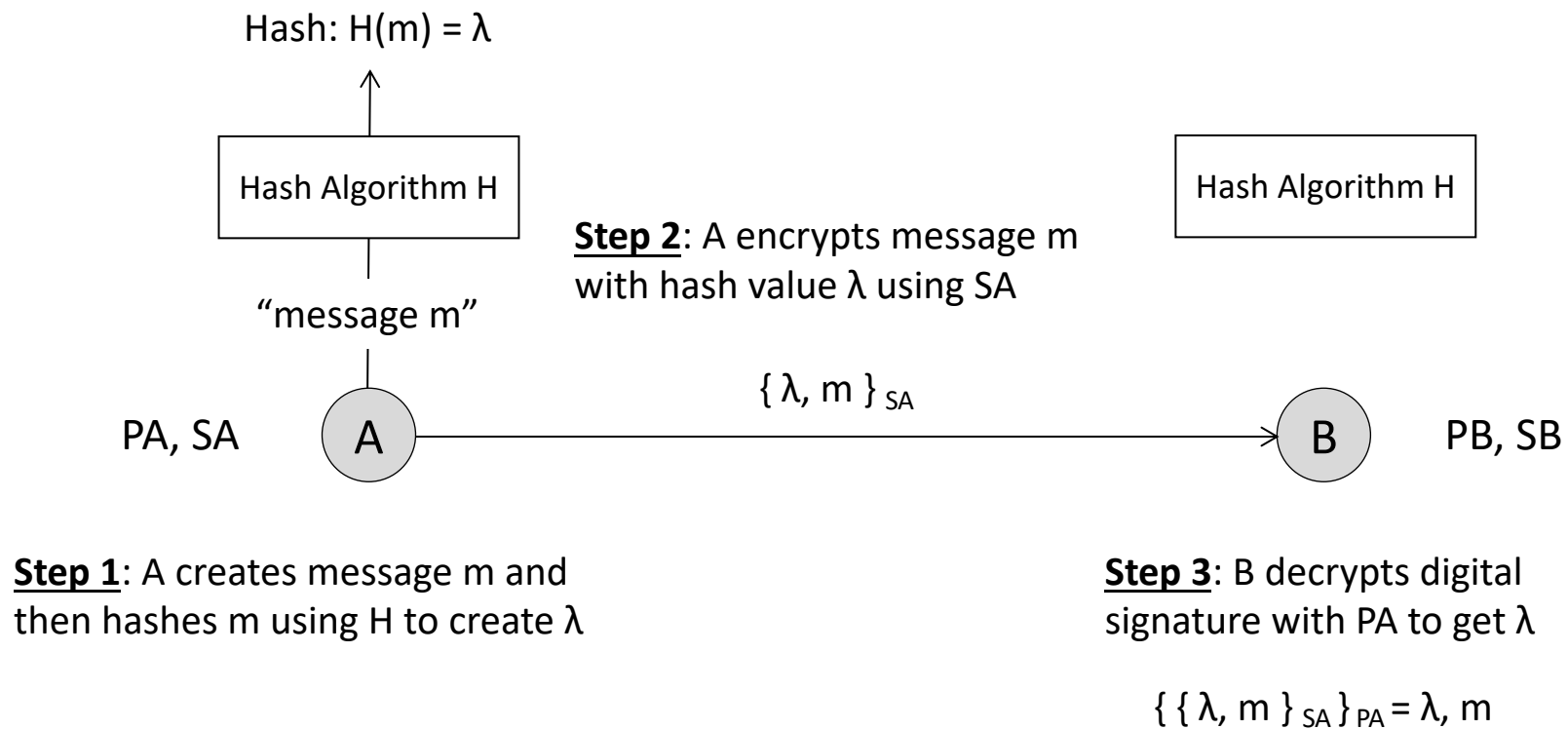
**Step 1:** A creates message  $m$  and then hashes  $m$  using  $H$  to create  $\lambda$

- *Hash Algorithm:* "Variable length input" (domain) to "fixed length output" (co-domain)
- *Hash Algorithm + Keys = Message Digest Algorithm*

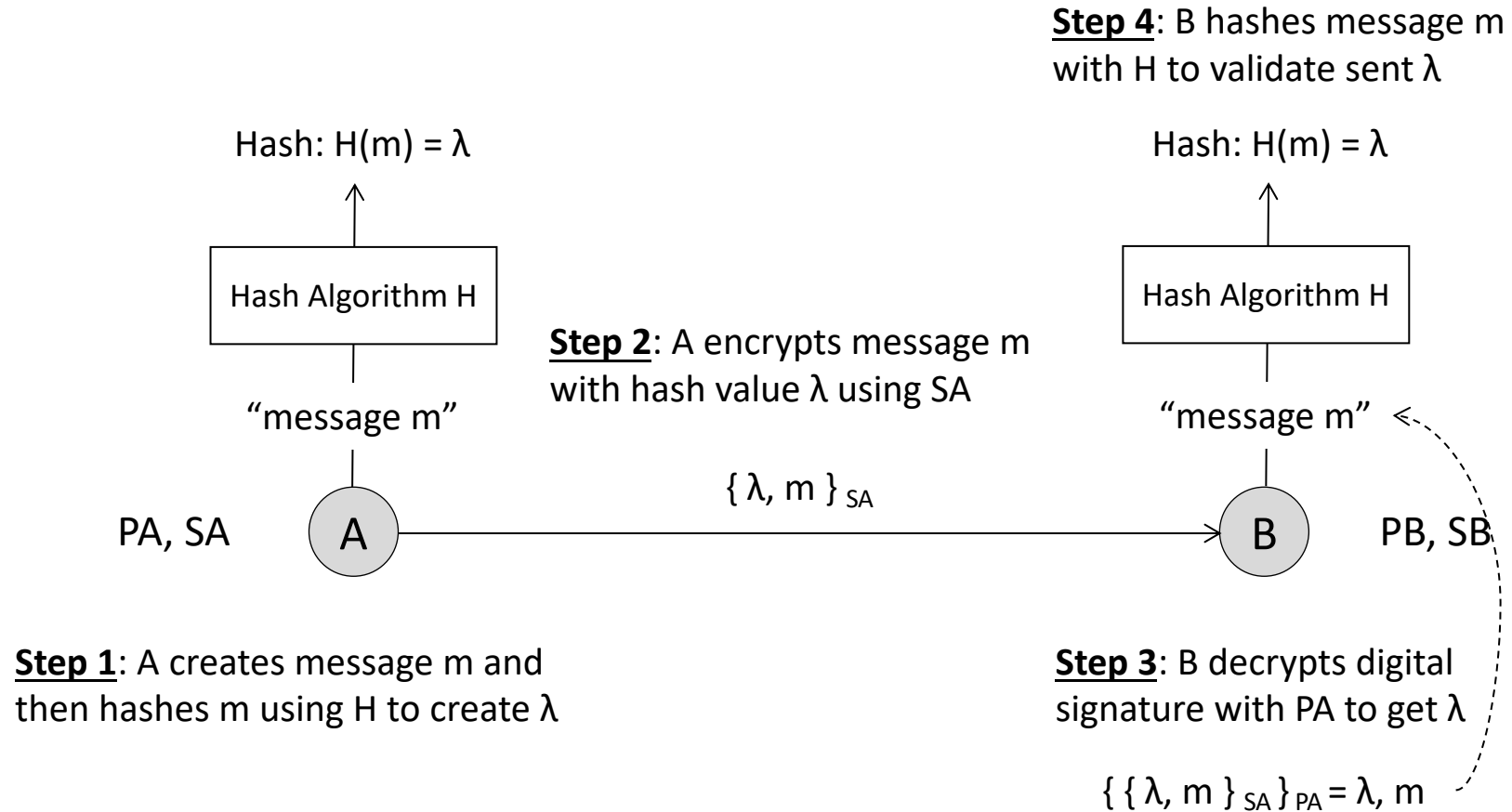
# Hashing for Digital Signature



# Hashing for Digital Signature



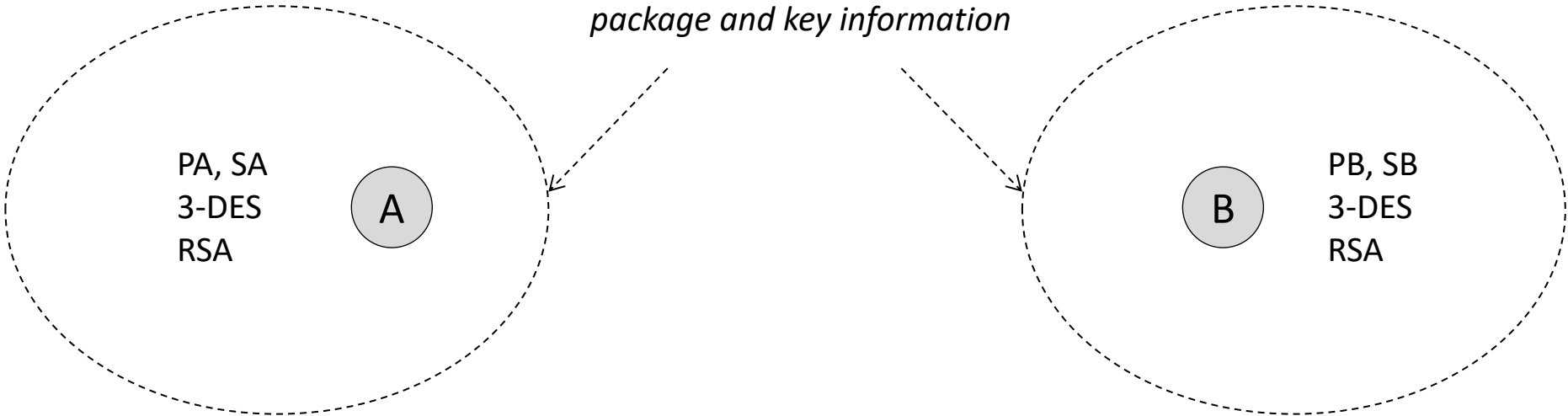
# Hashing for Digital Signature



How is Email Secured?

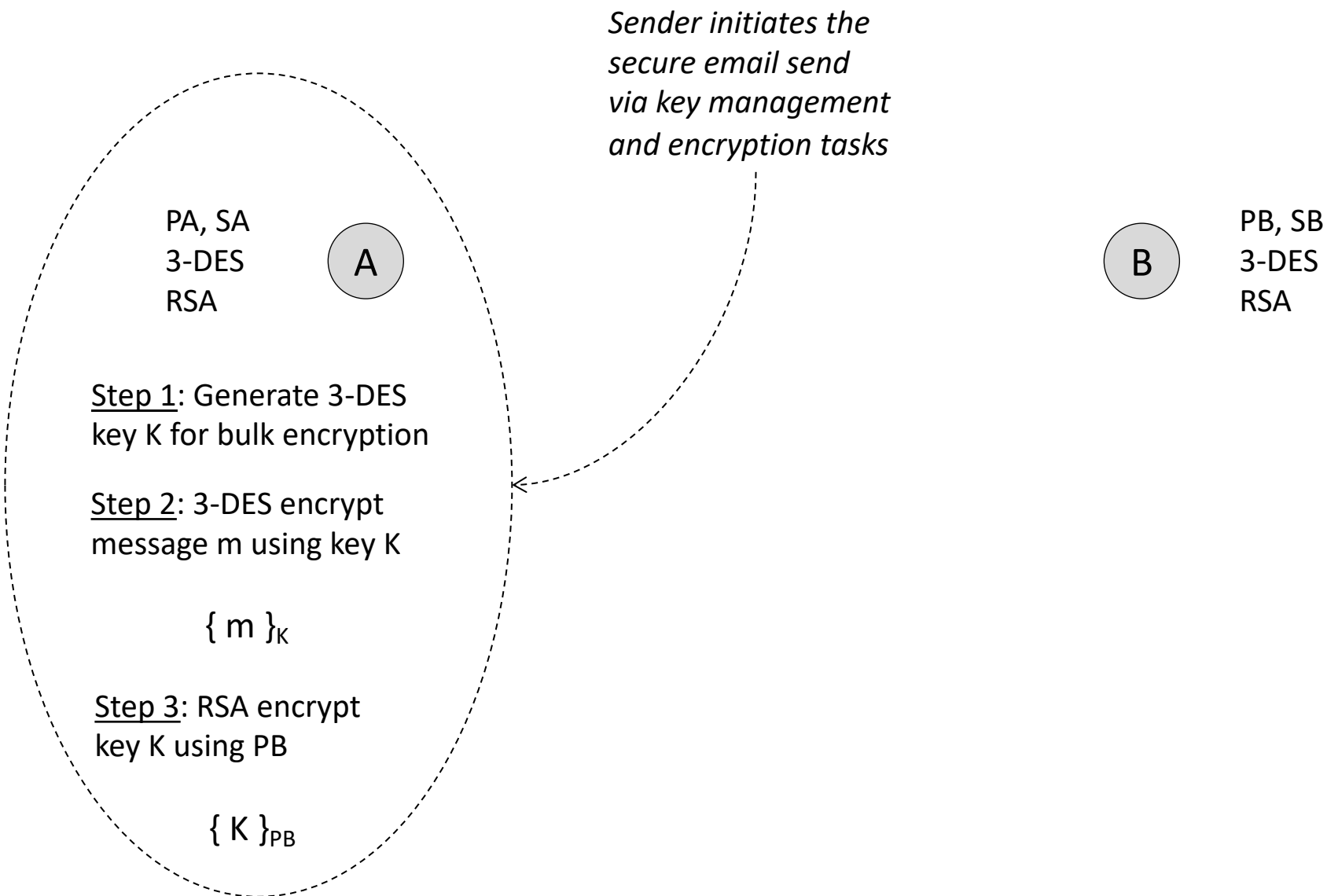
# Secret Email

*Sender and receiver must  
have the same email security  
package and key information*

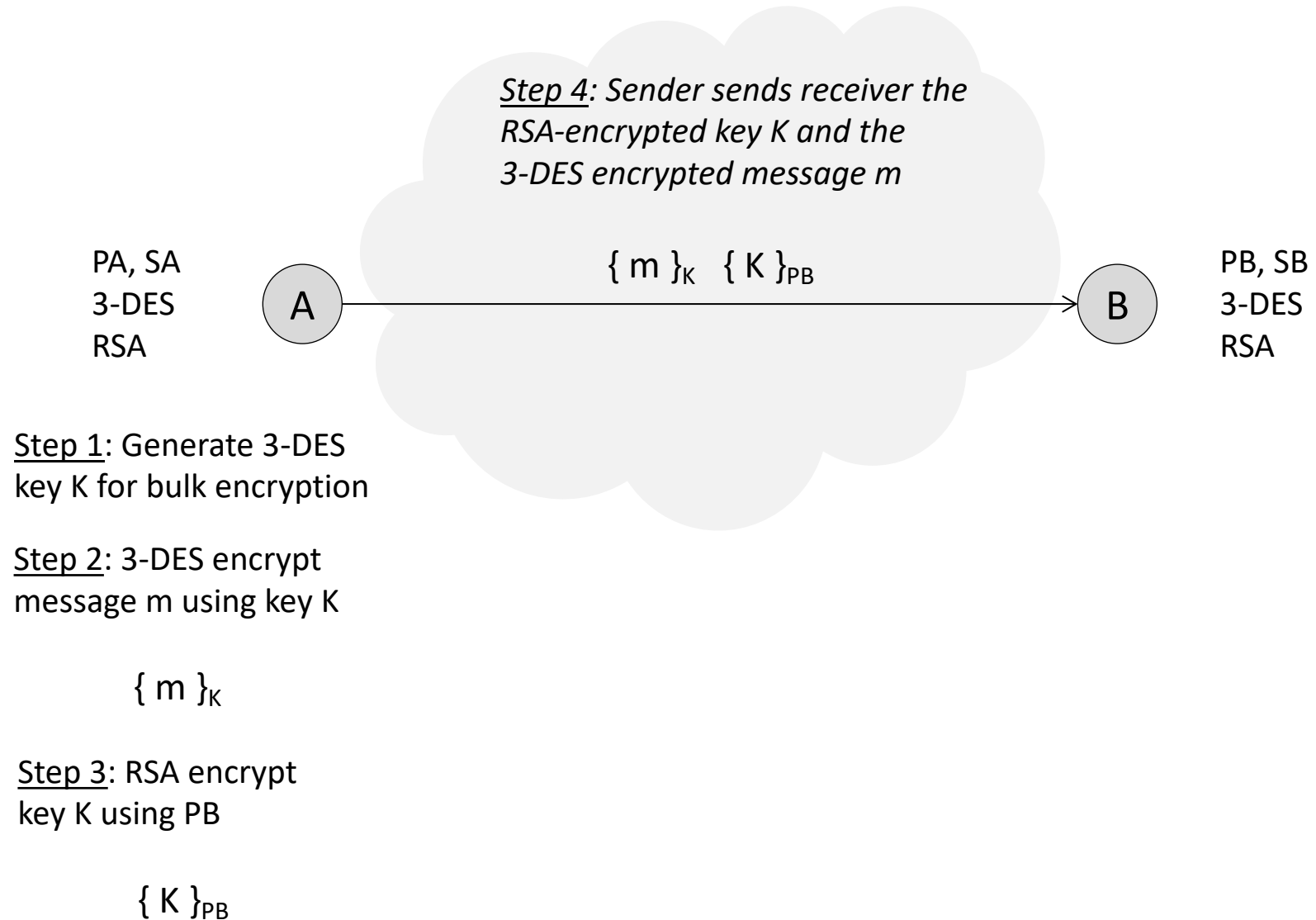




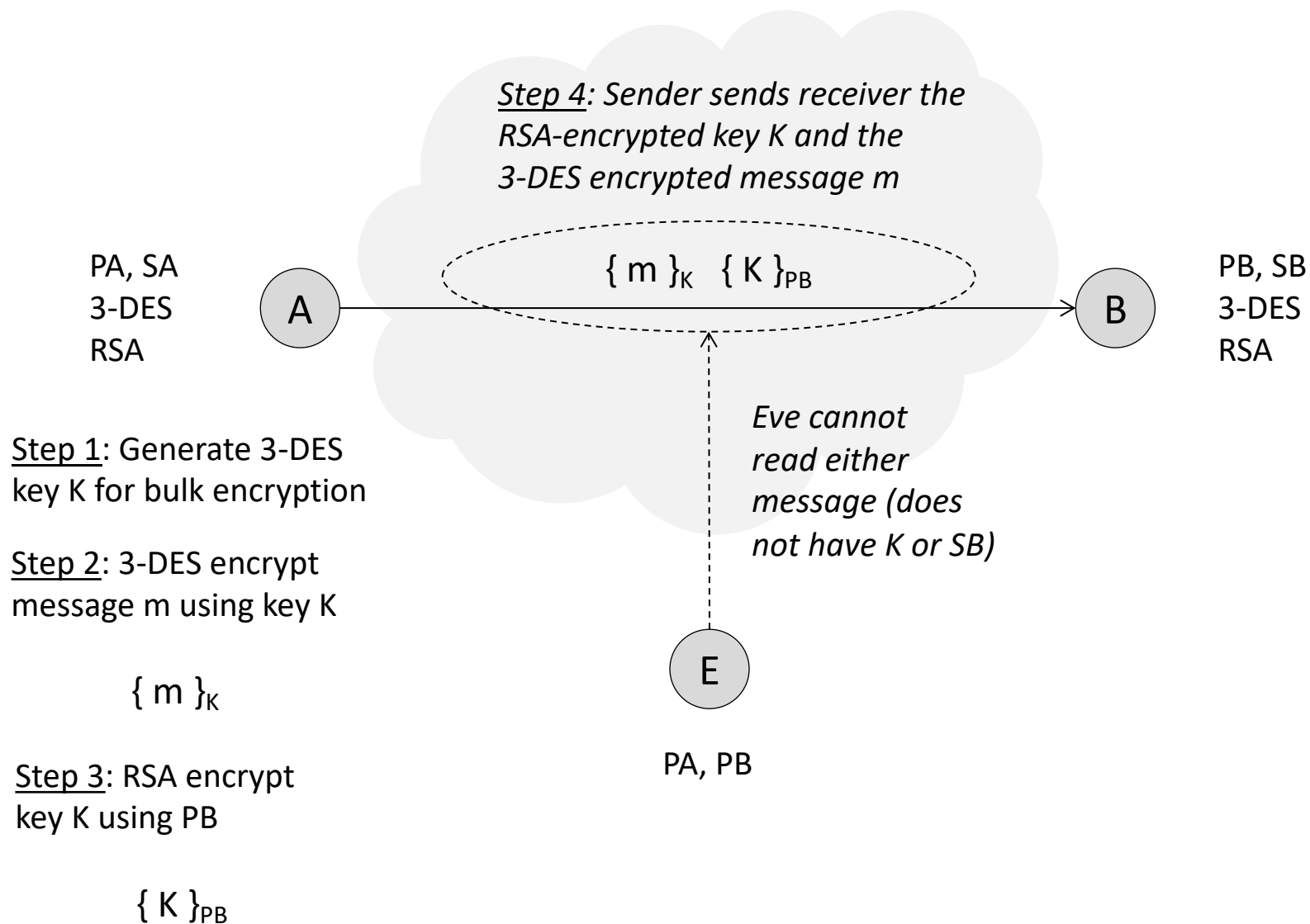
# Secret Email



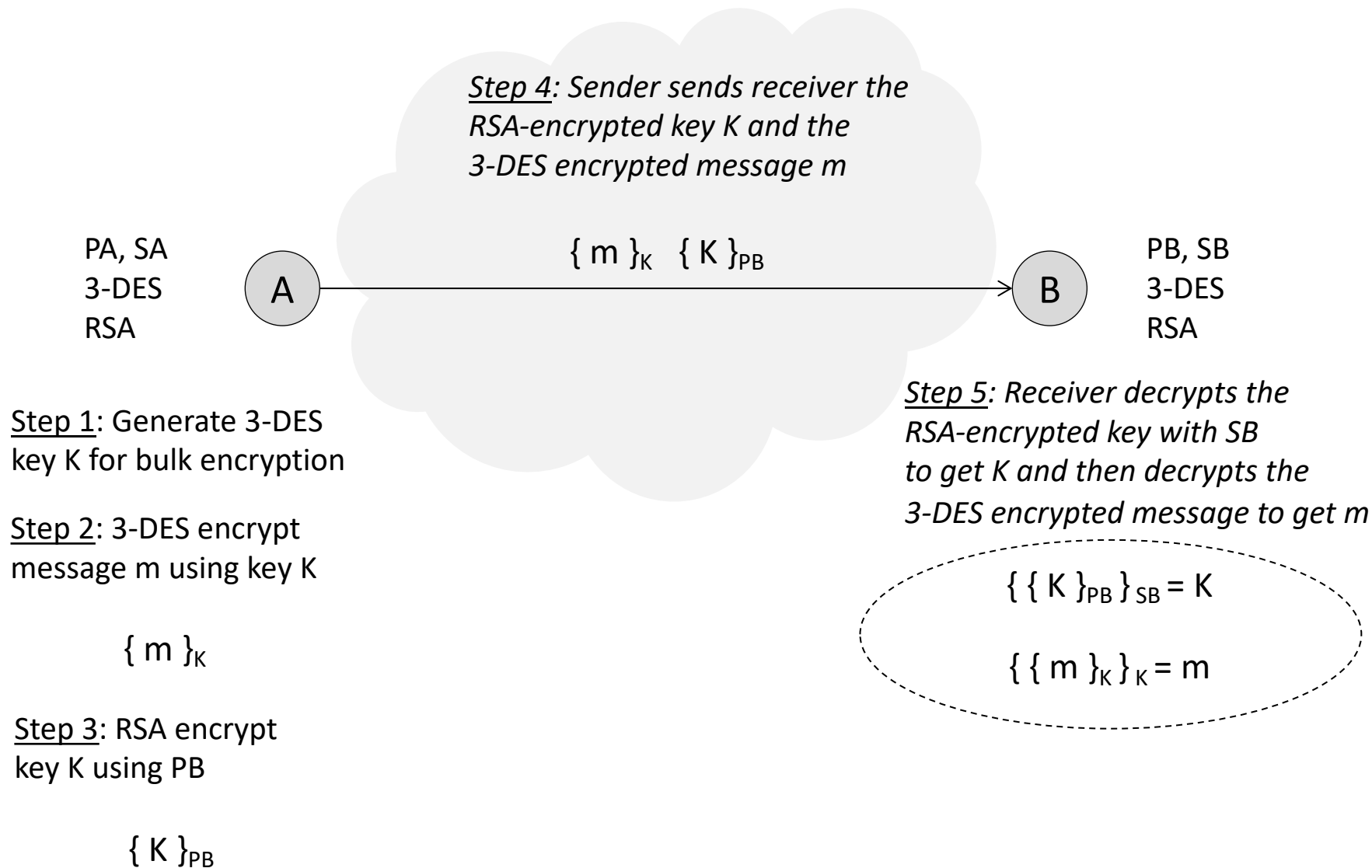
# Secret Email



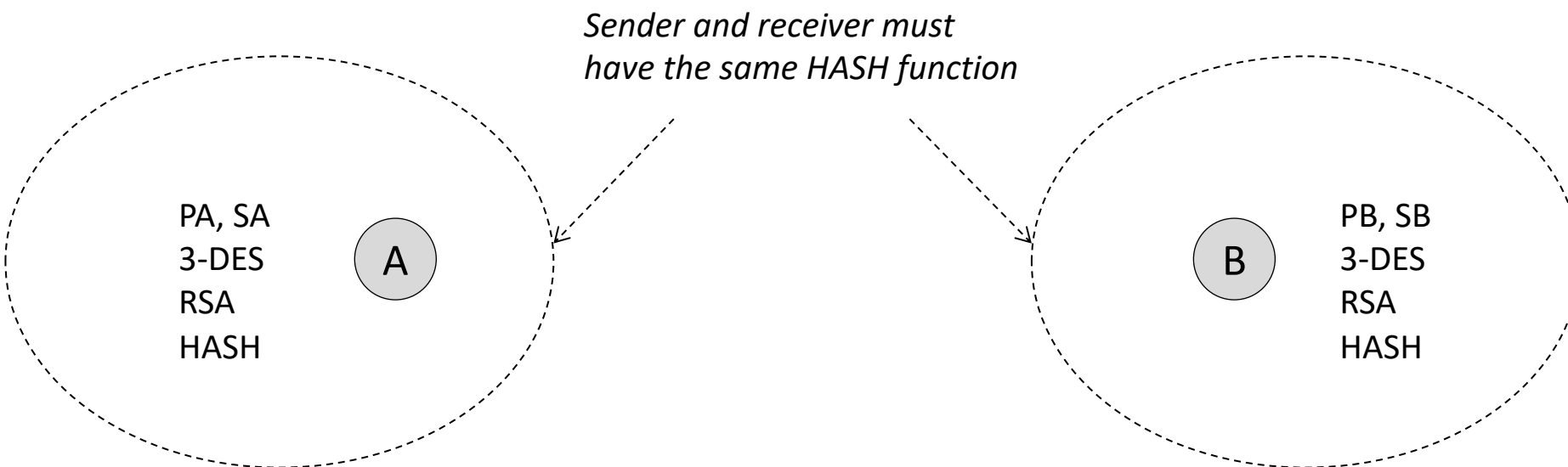
# Secret Email



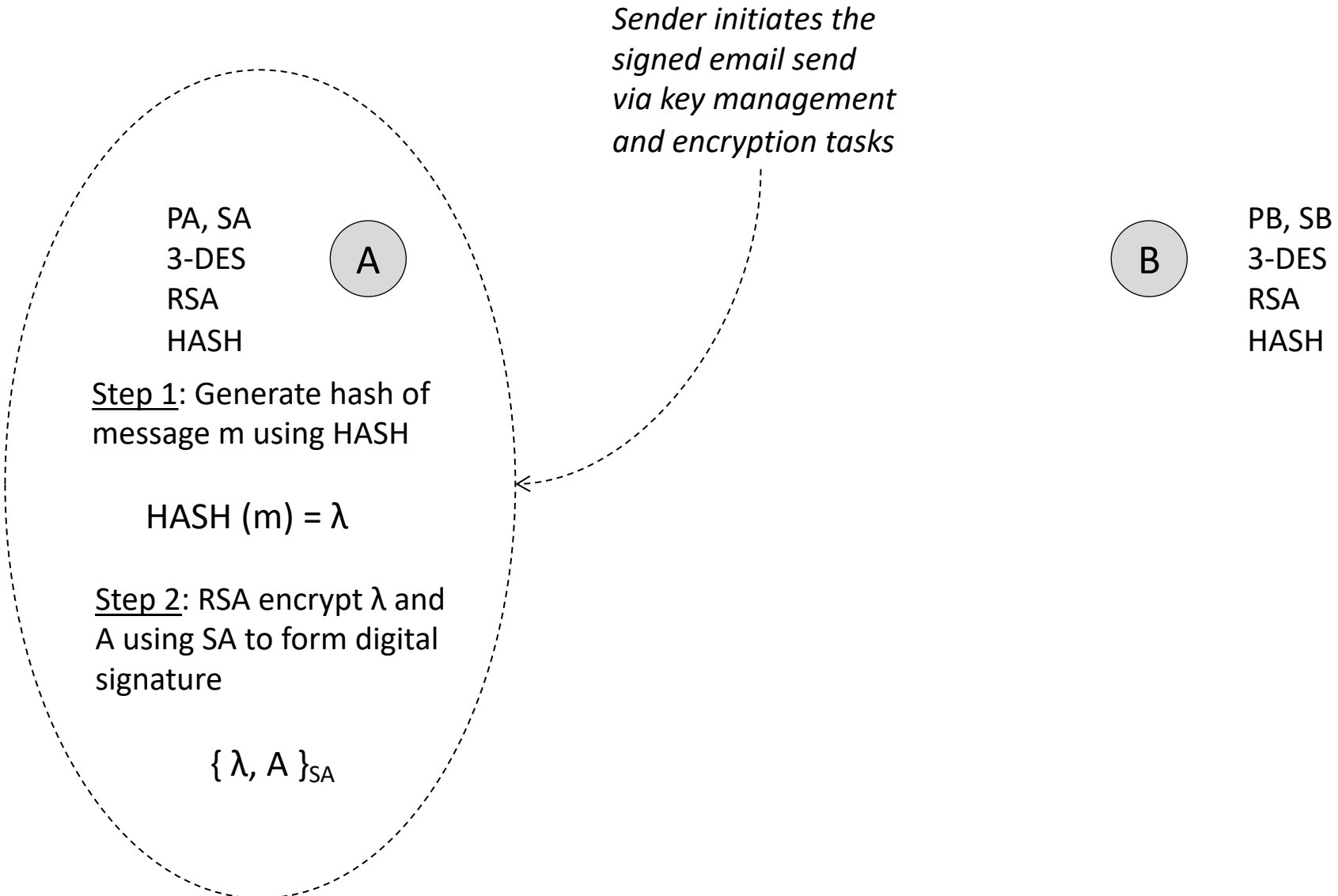
# Secret Email



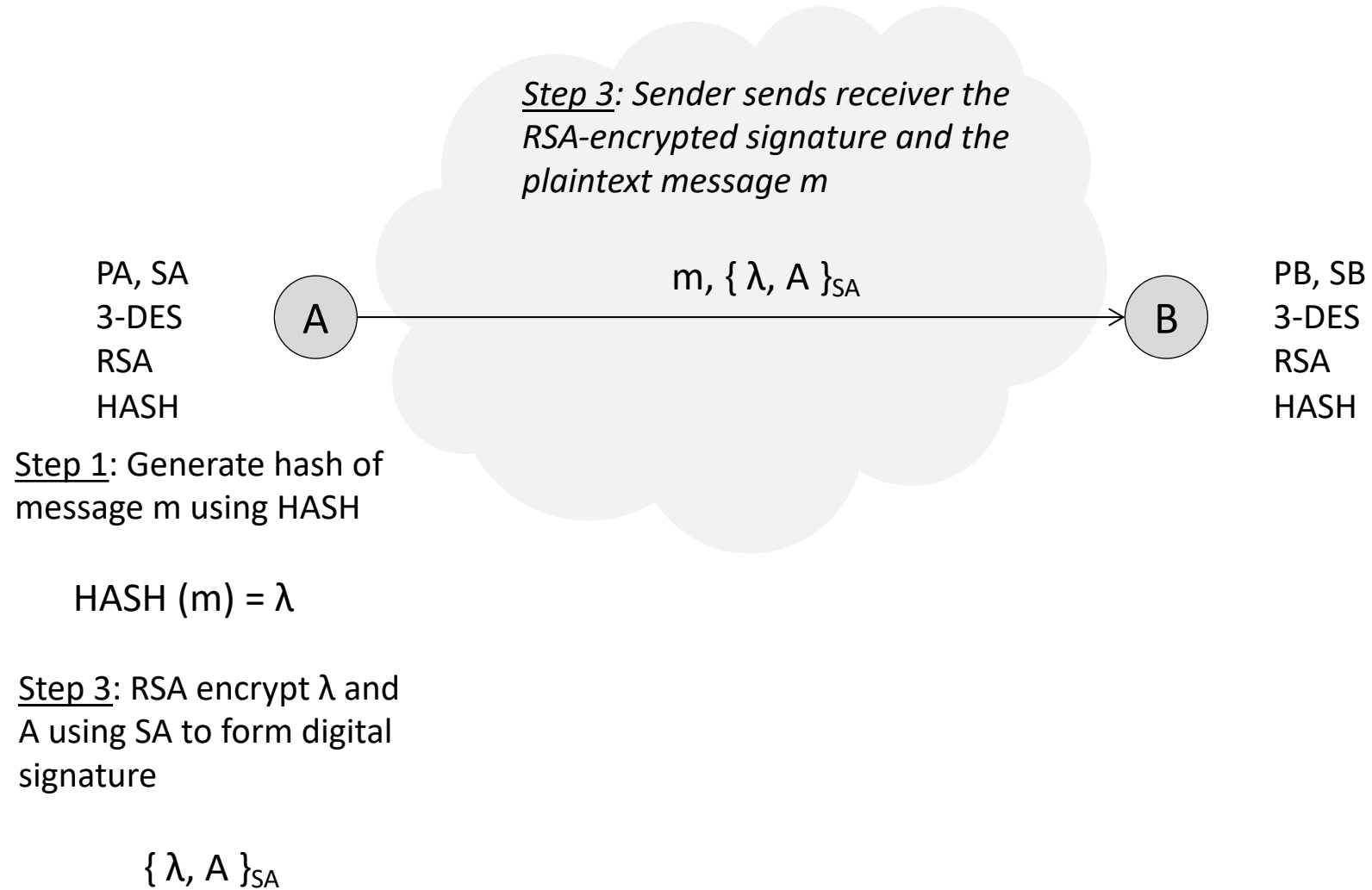
# Digitally Signed Email



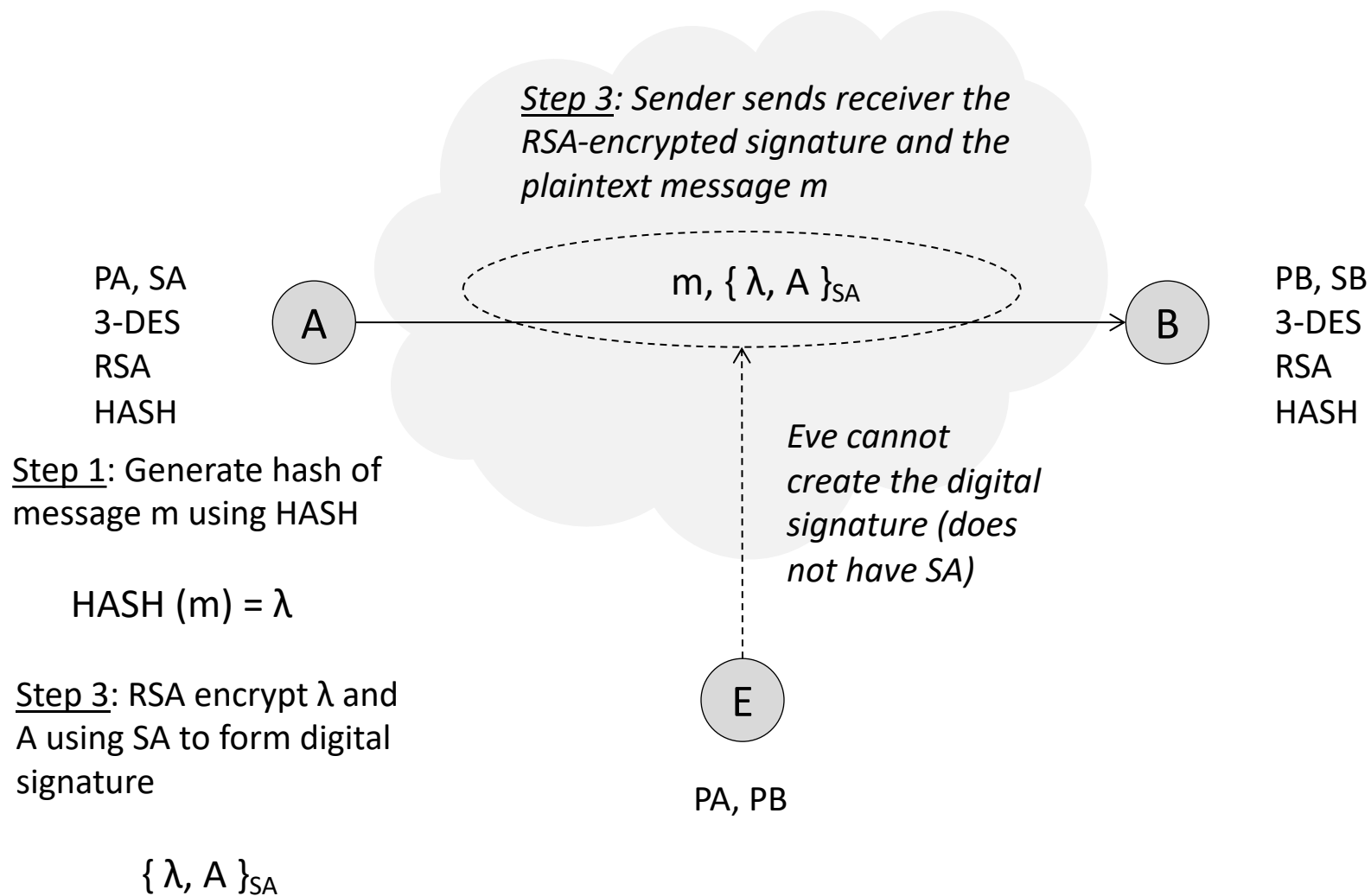
# Digitally Signed Email



# Digitally Signed Email

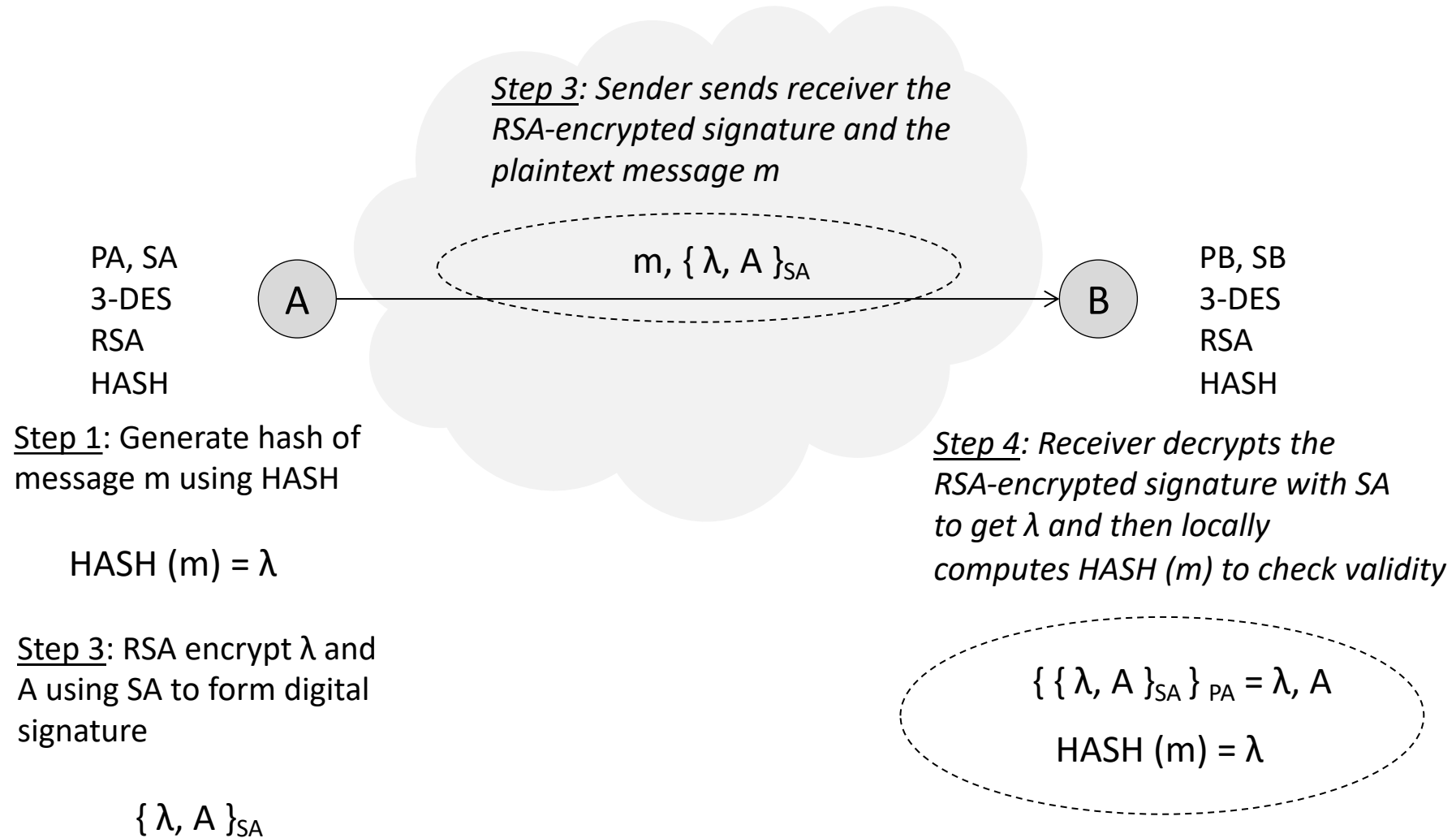


# Digitally Signed Email





# Digitally Signed Email

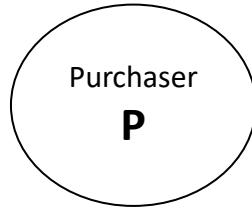


How Might Virtual Banking be Secured?

# Banking Security

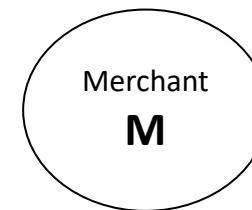
*“Wants to buy Teddy Bear  
On-line from M for \$10.00”*

PP, SP,  
PM, PB

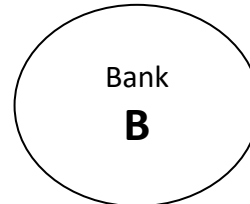


*“Selling Teddy Bears  
On-line for \$10.00”*

PM, SM  
PP, PB



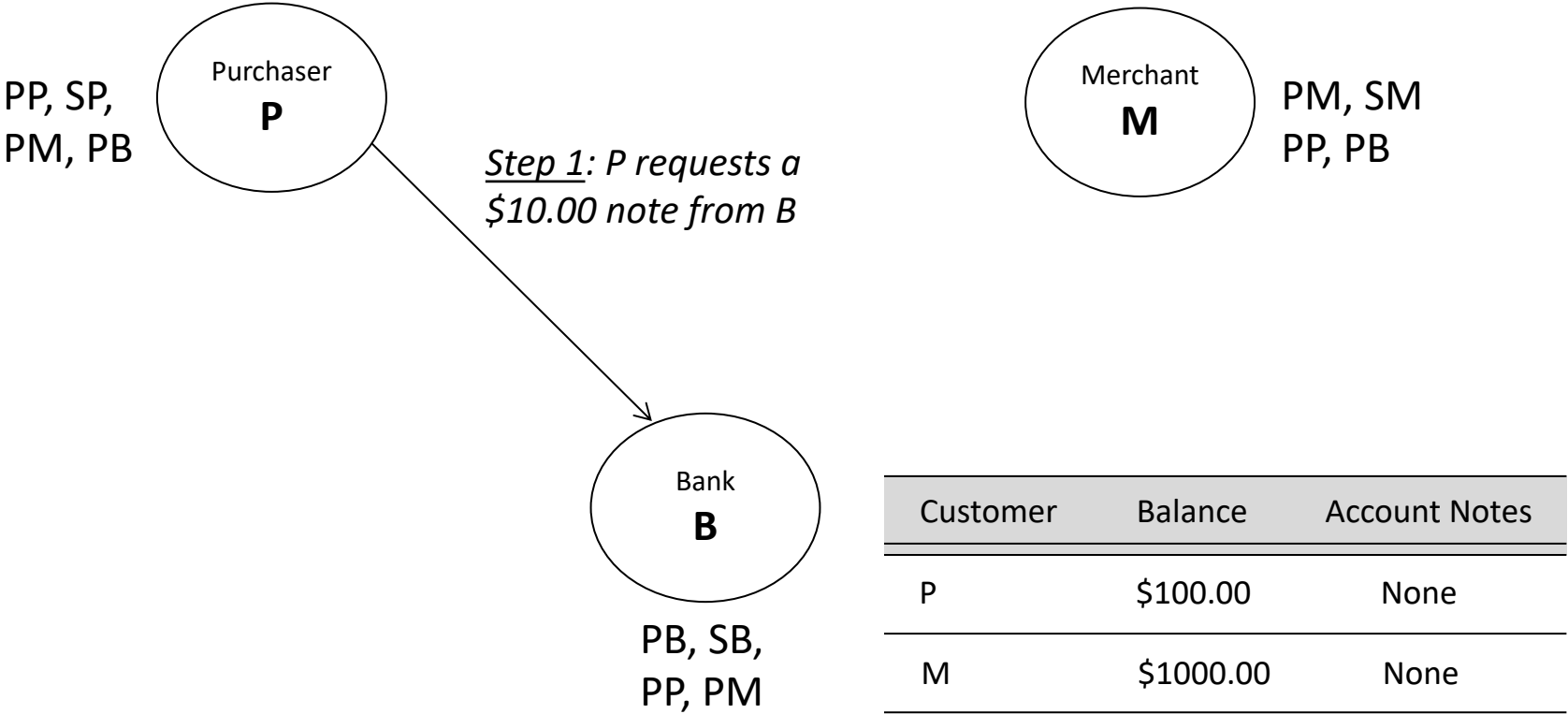
*“Maintains Bank Accounts for P  
and M with Real Money Balances”*



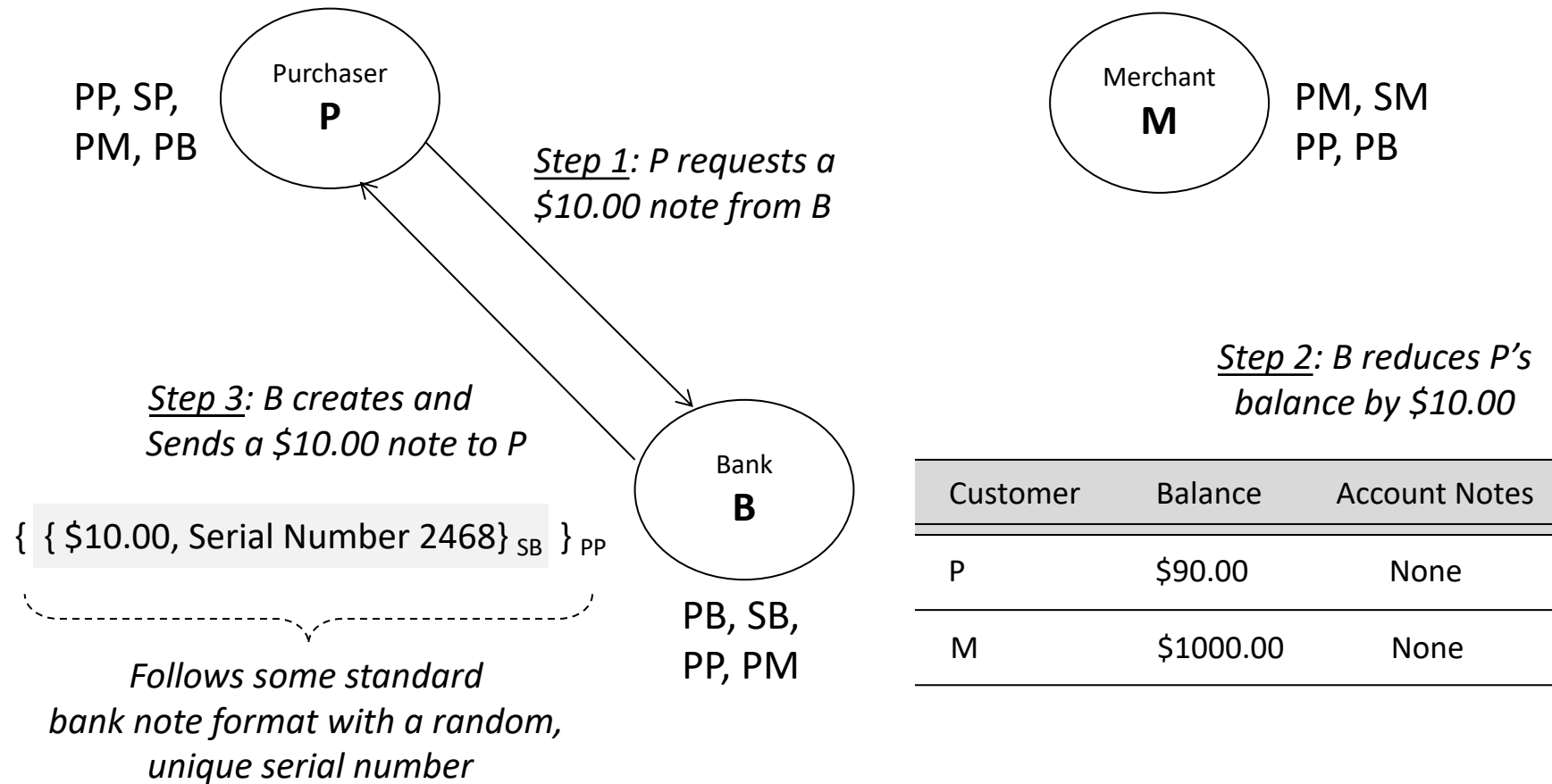
PB, SB,  
PP, PM

Customer	Balance	Account Notes
P	\$100.00	None
M	\$1000.00	None

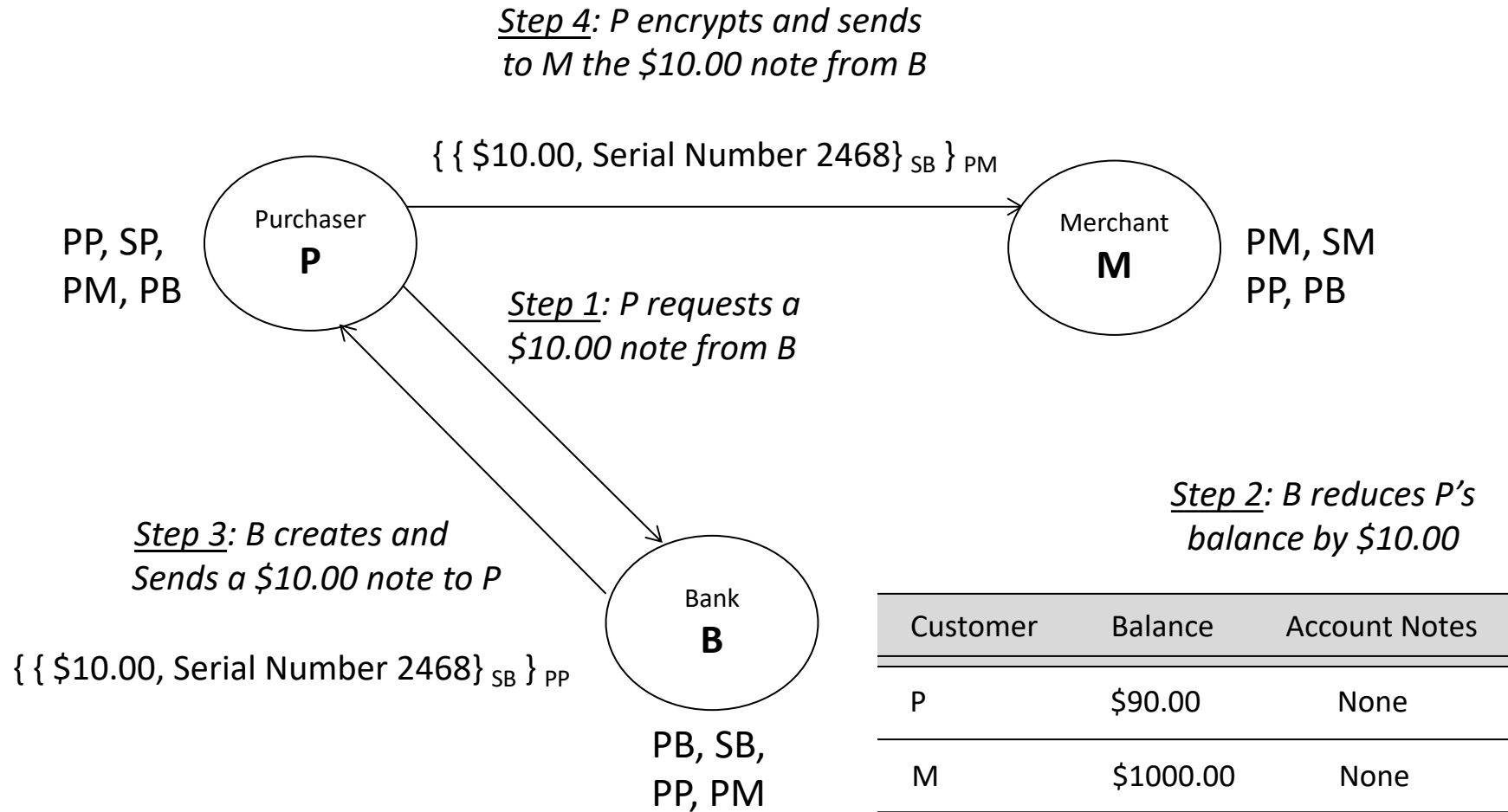
# Banking Security



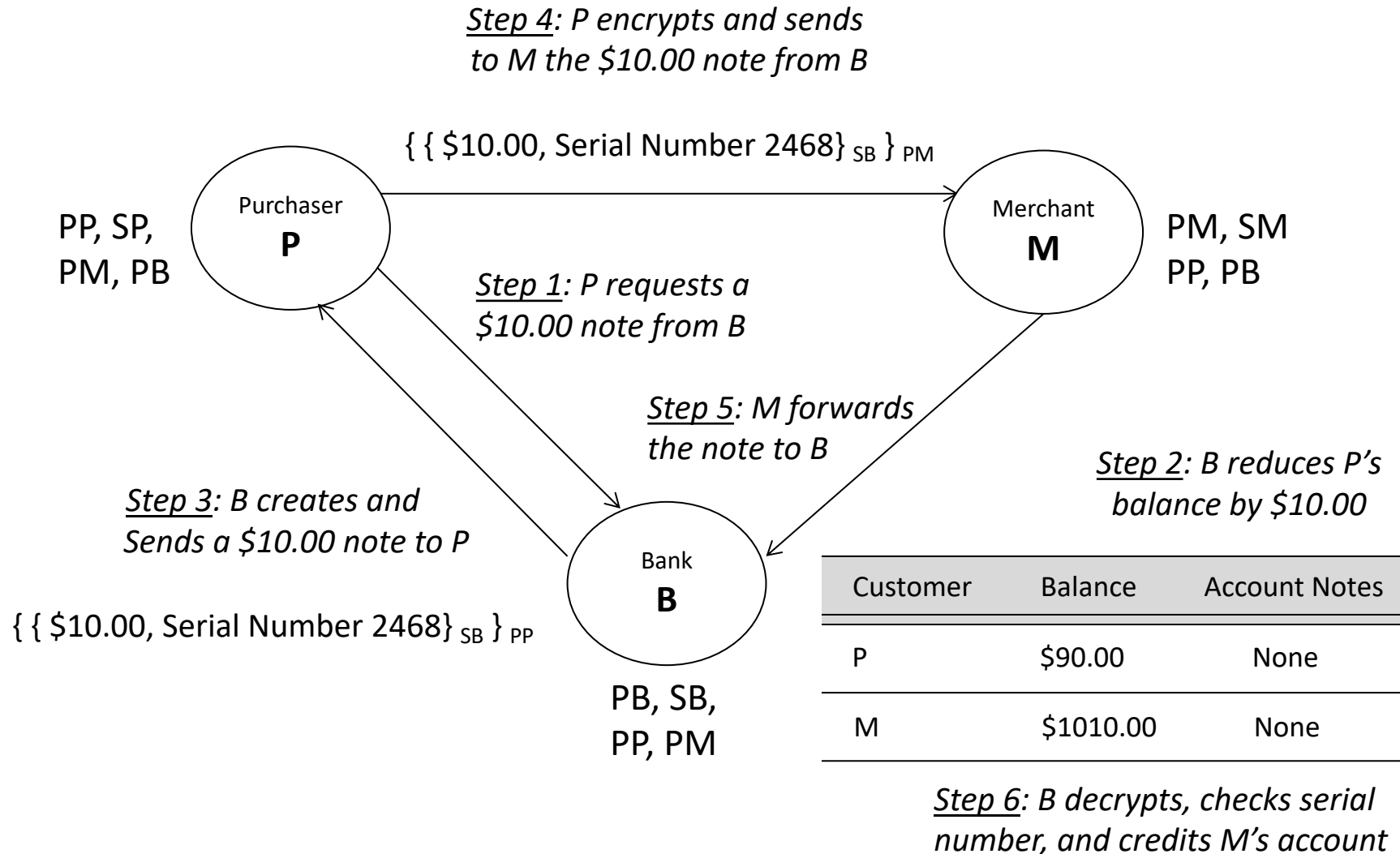
# Banking Security



# Banking Security



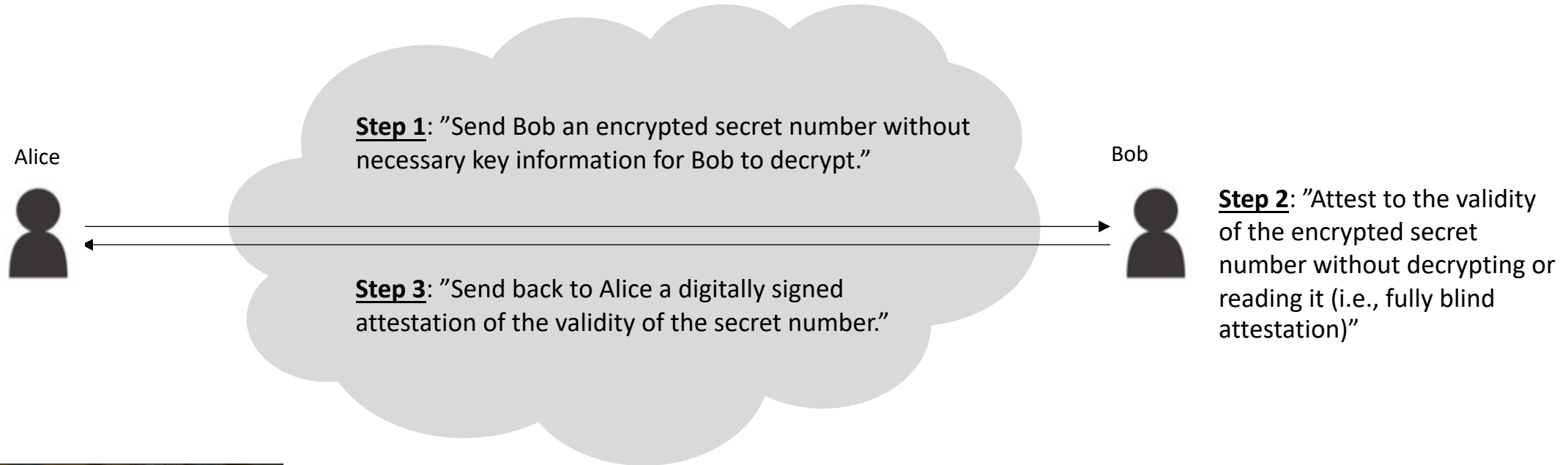
# Banking Security



What is a Blinding Protocol?



# Chaum's Blinding Protocol: Goal



*David Chaum  
University of California at Berkeley  
Founder DigiCash (defunct)*

# Chaum's Blinding Protocol: Goal

Alice (Client)

Network

Bob (Server)

**1. CREATE**

$\{\text{Serial \# 145167, \$2.00}\}_{K_1}$

**2. SEND**

$\{\text{Serial \# 145167, \$2.00}\}_{K_1}$

**3. SIGN**

$\{\{\text{Serial \# 145167, \$2.00}\}_{K_1}\}_{S_B}$

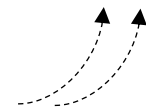
**4. RESPOND**

$\{\{\text{Serial \# 145167, \$2.00}\}_{K_1}\}_{S_B}$

**4. SIGNED CERTIFICATE**

$\{\{\text{Serial \# 145167, \$2.00}\}_{K_1}\}_{S_B}$

Verifiable with  $K_1$  and  $PB$



# Chaum's Blinding Protocol: Implementation

