

# PCA Steps

① Data of  $n$  observations

② No. of features =  $p$

③ Form a matrix of size  $n \times p$  with deviates from mean for each of the variables

④ Calculate covariance matrix ( $p \times p$ )

$$\text{cov}(x, y) = \frac{\sum_{i=1}^n (x_i - \bar{x})(y_i - \bar{y})}{(n-1)}$$

5 Calculate eigen values  
& eigenvectors of the  
covariance matrix

6 Choose principal components  
& form a <sup>new</sup> feature vec.

7 Derive the new data set

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Trace( $S$ ): The fraction of the  
total variance accounted for  
by the  $j$ th principal component  
is:  $\frac{\lambda_j}{\text{Trace}(S)}$

## PCA

Where  $\text{Trace}(\hat{S}) = \sum \lambda_j$

$$\begin{aligned}\text{Trace}(\hat{S}) &= 322.4 + 27.7 \\ &= 350.1\end{aligned}$$

Total variance accounted by  
1st principal component is:

$$\frac{\lambda_1}{\text{Trace}(\hat{S})} = \frac{322.3}{350.1} \approx 0.92$$

i.e. 92% of total system  
variance is captured  
by 1st PC

the remaining 8% is rejected  
by 2nd component.

Hence PC 2 is rejected &  
only PC 1 is considered.

From the 2 eigen vectors the  
feature vector is selected:

$$\begin{bmatrix} 0.801 \\ 0.599 \end{bmatrix}$$

Last step: multiply the der.  
cols with

the above selected feature  
vector: Der. vec 1 = 15 rows  
" 2 = 15 rows.

$$\therefore \text{der rank} = 15 \times 2$$

$$\text{feature set} = 2 \times 1$$

$$\therefore o/p = 15 \times 1$$

$$Z = X \cdot A$$

Multiply the matrix of  
deviations from mean  
with the eigen vectors  
to form a reduced  
vector.

This will be the reduced  
feature set.

## Imp of PCA

→ we have  $p$  independent  
vars.

→ we formulate ' $p$ ' principal  
components

→

$$y = f(x_1, x_2, \dots, x_p)$$

⇒ we select ' $p$ ' principal  
components

Each ' $p$ ' contributes to ~~the~~  
variance in  ~~$y$~~ .

Choose ' $q$ ' of ' $p$ ' principal  
components ( $q < p$ )

to be included in  
the Regression eqn.