

HW  
Q1  
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$$E = - \sum_{n=1}^N \sum_{k=1}^K t_{nk} \ln(y)$$

$$y = \frac{e^{a_k}}{\sum e^{a_i}}$$

$$\frac{dE}{dy} \cdot \frac{dy}{da} \rightarrow$$

$$\frac{dE}{dy} \Rightarrow \sum_n \sum_k \frac{-t_{nk} dy}{y_{nk}} \quad \text{sum over } n \Rightarrow \sum_k \frac{t_k}{y_k} dy$$

$$\frac{dy}{da} \Rightarrow \frac{e^{a_k}}{\sum e^{a_i}}$$

since  $t_{nk}$  0 or 1 - given  
&  $\sum_k t_{nk} = 1$  - given

$$\text{we can derive } \frac{dy}{da} \text{ to } \frac{e^{a_k}}{\sum e^{a_i}} \left( 1 - \frac{e^{a_k}}{\sum e^{a_i}} \right)$$

$$\text{now } \frac{dE}{dy} \cdot \frac{dy}{da} = \frac{-t_n}{y} \cdot \frac{e^{a_k}}{\sum e^{a_i}} \left( 1 - \frac{e^{a_k}}{\sum e^{a_i}} \right)$$

$$= \frac{-t}{y} \cdot y(1-y)$$

$$= -t + yt$$

$$= yt - t ?$$