

# Competitive Programming Notebook

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## 1 Graph

### 1.1 Prim MST

```
1 // take smallest edge that leads to vertex v
2 //
3 // Time: O(E log V)
4 // Space: O(V + E)
5 // Status: tested (UVA10048)
6
7 vector<vector<pair<int, int>> adj(M), mst(M);
8 vector<bool> taken(M, false);
9 int cost = 0;
10 using iii = pair<int, pair<int, int>>;
11 priority_queue<iii, vector<iii>, greater<iii> pq;
12
13 void process(int v) {
14     taken[v] = true;
15     for (auto &[w, u]: adj[v])
16         if (!taken[u])
17             pq.push({w, {v, u}});
18 }
19
20 void run(int n) {
21     process(0);
22     while (!pq.empty()) {
23         int w = pq.top().first,
24             v = pq.top().second.first,
25             u = pq.top().second.second;
26         pq.pop();
27         if (!taken[u]) {
28             mst_cost += w;
29             mst[u].push_back({w, v});
30             mst[v].push_back({v, w});
31             process(u);
32         }
33     }
34     for (int v = 1; v < n; ++v)
35         if (!taken[v]) {
36             process(v);
37             run(n);
38         }
39 }
```

### 1.2 Dijkstra SSSP

```
1 // Time: O((V+E) log V)
2 // Space: O(V^2)
3 //
4 // Status: tested (CF20C)
5
6 using ii = pair<int, int>;
7 const int inf = 0x3f3f3f3f;
8 vector<vector<ii>> adj(M);
9 vector<int> dist(M, inf), par(M, -1);
10
11 void dijkstra(int s) {
12     dist[s] = 0;
13     priority_queue<ii, vector<ii>,
14         greater<pair<int, int>>> pq;
15     pq.push(make_pair(0, s));
16     while (!pq.empty()) {
17         int w = pq.top().first;
```

```

17     int v = pq.top().second;
18     pq.pop();
19     if (w > dist[v]) continue;
20     for (auto &[d, u]: adj[v])
21         if (dist[v] != inf && dist[v]+d <
22             dist[u]) {
23             par[u] = v;
24             dist[u] = dist[v]+d;
25             pq.push(make_pair(dist[u], u));
26         }
27 }

```

## 1.3 Graph Check

```

1 // Check for tree edges, back edges and forward
  edges
2 //
3 // Usage: graphCheck(firstVertex, -1) (p stands
  for parent)
4 // Time: O(V + E)
5 // Space: O(V + E)
6
7 int UNVISITED = -1, EXPLORED = 0, VISITED = 1;
8 vector<vector<int>> adj(M);
9 vector<int> tin;
10
11 void graphCheck(int v, int p) { //vertex, parent
12     tin[v] = EXPLORED;
13     for (auto u: adj[v]) {
14         if (tin[u] == UNVISITED) { //tree edge
15             graphCheck(u, v);
16         } else if (tin[u] == EXPLORED) {
17             if (u == p)
18                 ; //two way edge u <-> v
19             else
20                 ; //back edge v -> u
21         } else if (tin[u] == VISITED) {
22             ; //forward/cross edge u-v
23         }
24     }
25     tin[v] = VISITED;
26 }

```

## 1.4 Articulations and Bridges

```

1 // Articulation point v: if you remove vertex v,
  then the connected component to which it
  belongs becomes disconnected
2 // Bridge u,v: if you remove the edge u->v, then
  you can't reach v from u
3 //
4 // Usage: dfs(source, -1)
5 //
6 // Time: O(V + E)
7 // Space: O(V + E)
8 // Status: not tested
9
10 int tk = 0;
11 vector<int> tin(M, -1);
12 vector<vector<int>> adj(M);
13
14 void dfs(int v, int p) {
15     tin[v] = low[v] = tk++;
16     int children = 0;
17     for (auto u: adj[v]) {
18         if (u == p) continue;
19         else if (tin[u] == -1) {
20             ++children;
21             dfs(u, v);
22             if (low[u] >= tin[v] && p != v)
23                 ; //articulation point
24             if (low[u] > tin[v])
25                 ; //bridge u-v
26             low[v] = min(low[v], low[u]);
27         } else {
28             low[v] = min(low[v], tin[u]);

```

```

29     }
30 }
31 }

```

## 1.5 Euler Tour

```

1 // Find the closest neighbor that has a path back
  to the current vertex to build an euler tour
2 //
3 // Euler path: visits each edge once
4 // Tour/cycle/circuit: euler path that starts and
  ends at same node
5 //
6 // Undirected and has path: every vertex has even
  degree or two have odd degree
7 // Undirected and has circuit: every vertex has
  even degree
8 // Directed and has path: indeg[i]-outdeg[i] == 1
  for at most one i, -1 for at most one i, 0 for
  all other i
9 // Directed and has circuit: indeg[i] == outdeg[i]
  for every i
10 //
11 // Usage: tour(cyc.begin(), start\_vertex)
12 // Time: O(E^2)
13 // Status: not tested
14 // Source: CP3 (pg. 205)
15
16 list<int> cyc;
17 vector<vector<int>> adj(M);
18 vector<vector<bool>> traversed(M, vector<bool>(M,
  false));
19
20 //euler tour (list for fast insertion)
21 void tour(list<int>::iterator i, int v) {
22     for (auto u: adj[v]) {
23         if (!traversed[v][u]) {
24             traversed[v][u] = true;
25             for (auto t: adj[u])
26                 if (t == v && !traversed[u][t]) {
27                     traversed[u][t] = true;
28                     break;
29                 }
30             tour(cyc.insert(i, v), u);
31         }
32     }
33 }

```

## 1.6 Kahn's topological sort

```

1 // particular order (alphabetical)
2 // Time: O(VE)
3 // Space: O(V+E)
4 // Status: tested (UVA11060)
5
6 vector<vector<int>> adj(M);
7 vector<int> sorted;
8
9 void kahn(int n) {
10     vector<int> indeg(n, 0);
11     vector<bool> valid(n, true);
12     priority_queue<int> pq;
13
14     for (int v = 0; v < n; ++v)
15         for (auto u: adj[v])
16             indeg[u]++;
17     for (int v = 0; v < n; ++v)
18         if (!indeg[v]) pq.push(v);
19
20     while (!pq.empty()) {
21         int v = pq.top(); pq.pop();
22         sorted.push_back(v);
23         valid[v] = false;
24         for (auto u: adj[v])
25             if (valid[u] && (--indeg[u]) == 0)
26                 pq.push(u);
27     }

```

```
28 }
```

## 1.7 Max Cardinality Bipartite Matching

```
1 // Jump from free to matched edges until you've
  used them all
2 //
3 // Time: O(VE)
4 // Status: not tested
5 // Source: CP3 (pg. 209)
6
7 vector<vector<int>> adj(M);
8 vector<int> match(M, -1);
9 vector<bool> visited(M);
10
11 bool augment(int left) { //match one on the left
  with one on the right
12     if (visited[left]) return false;
13     visited[left] = true;
14     for (auto right: adj[left])
15         if (match[right] == -1 ||
            augment(match[right])) {
16             match[right] = left;
17             return true;
18         }
19     return false;
20 }
21
22 //usage
23 //(mcbm = V iff there's at least one way to
  completely match both sides)
24 int mcbm = 0; //number of matched vertices
25 match.assign(M, -1);
26 for (int v = 0; v < ls; ++v) { //ls = size of the
  left set
27     visited.assign(ls, false);
28     mcbm += augment(v);
29 }
```

## 1.8 Lowest Common Ancestor

```
1 // Binary lift to binary search the LCA or euler
  path
2 //
3 // Time: O(N log N)
4 // Space: O(N log N)
5 // Status: not tested
6
7 ///--- binary lifting
8 int n, l = ceil(log2(n));
9 vector<vector<int>> adj;
10 int tk = 0;
11 vector<int> tin(n), tout(n);
12 vector<vector<int>> up(n, vector<int>(l+1)); //
  ancestor
13
14 void dfs(int v, int p) { // run dfs(root, root) to
  initialize
15     tin[v] = ++tk;
16     up[v][0] = p;
17     for (int i = 1; i <= l; ++i)
18         up[v][i] = up[up[v][i-1]][i-1];
19     for (int u : adj[v])
20         if (u != p)
21             dfs(u, v);
22     tout[v] = ++tk;
23 }
24
25 bool ancestor(int v, int u) { // v is ancestor of u
26     return tin[v] <= tin[u] && tout[v] >= tout[u];
27 }
28
29 int lca(int v, int u) {
30     if (ancestor(v, u)) return v;
31     if (ancestor(u, v)) return u;
```

```
32     for (int i = l; i >= 0; --i)
33         if (!ancestor(up[v][i], u))
34             v = up[v][i];
35     return up[v][0];
36 }
37
38 ///--- euler path
39 using ii = pair<int, int>;
40 vector<ii> t;
41 vector<int> idx(n);
42 int tk = 1;
43
44 void dfs(int v, int d) { // call with dfs(root, 0);
45     for (auto u : adj[v]) {
46         st.update(tk, {d, v});
47         tk++;
48         dfs(u, d+1);
49     }
50     idx[v] = tk;
51     st.update(tk, {d, v});
52     tk++;
53 }
54
55 int lca(int v, int u) {
56     int l = idx[v], r = idx[u];
57     return st.minquery(l, r).second; // .first is
  depth
58 }
```

## 1.9 Tarjan Strongly Connected Component

```
1 // A node can reach any other node in its own SCC
  (DFS+stack)
2 //
3 // Usage: Tarjan(N, adj)
4 // Time: O(V + E)
5 // Space: O(V + E)
6 // Status: tested (UVA247, UVA11838)
7
8 vector<int> tin(M, -1), low(M, -1);
9 vector<vector<int>> adj(M);
10 stack<int> S;
11 int tk = 0;
12
13 void dfs(int v) {
14     low[v] = tin[v] = tk++;
15     S.push(v);
16     visited[v] = true;
17     for (auto u: adj[v]) {
18         if (tin[u] == -1)
19             dfs(u);
20         if (visited[u])
21             low[v] = min(low[v], low[u]);
22     }
23     if (low[v] == tin[v])
24         while (true) {
25             int u = S.top(); S.pop(); visited[u] =
                false;
26             if (u == v) break;
27         }
28 }
```

## 1.10 Bellman-Ford SSSP

```
1 // Time: O(VE)
2 // Space: O(V + E)
3 // Status: tested (UVA1112, UVA10449)
4
5 const int inf = 0x3f3f3f3f;
6 vector<vector<pair<int, int>>> adj(M);
7 vector<int> dist(M, inf);
8
9 void bellmanFord(int n) {
10     for (int i = 0; i < n-1; ++i)
11         for (int v = 0; v < n; ++v)
```

```

12         for (auto &[u, w]: adj[v])
13             if (dist[v] != inf)
14                 dist[u] = min(dist[u],
15                             dist[v]+w);
16     }
17 //check if there are negative cycles
18 bool cycle(int n) {
19     bool ans = false;
20     for (int v = 0; v < n; ++v)
21         for (auto &[u, w]: v)
22             ans |= dist[v] != inf && dist[u] >
23                 dist[v]+w;
24 }

```

## 1.11 Kruskal MST

```

1 // order edges by increasing weight, then use a
  MUF to know if each edge is useful (if it
  connects two previously disconnected vertices)
2 //
3 // Min Span Subgraph: previously process fixed
  edges
4 //
5 // Min Span Forest: count number of sets on the MUF
6 //
7 // 2nd Best MST: run kruskal; for each chosen
  edge, flag it as unavailable and run it
  without using that edge ($O(VE)$)
8 //
9 // Minimax: max edge weight on the MST (maximin:
  min)
10 //
11 // Usage: Kruskal(V, E, edges) (weighted edges)
12 //
13 // Time:  $O(E \log V)$ 
14 // Space:  $O(V + E)$ 
15 // Status: tested (UVA1174)
16
17 using iii = pair<int, pair<int, int>>; //weight,
  two vertices
18 vector<iii> edges;
19 UnionFind muf;
20
21 int kruskal() {
22     int cost = 0;
23     sort(edges.begin(), edges.end());
24     for (auto a: edges) {
25         int w = a.first;
26         pair<int, int> e = a.second;
27         if (!muf.isSameSet(e.first, e.second)) {
28             cost += w;
29             muf.unionSet(e.first, e.second);
30         }
31     }
32     return cost;
33 }

```

## 1.12 Edmond Karp MaxFlow

```

1 // Ford-Fulkerson's method with BFS =  $O(VE)$  BFS
  calls,  $O(E)$  per BFS
2 //
3 // Vertex weights: if vertex V has a weight,
  create Vin (receives all in-edges of V and has
  an edge to Vout) and Vout(receives an edge
  from Vin and has all out-edges of V); Vin-Vout
  has the weight from V
4 //
5 // MinCut: run EdmondKarp, S-T sets are: all V
  that you can reach from the source with edges
  of positive residual capacity and all other V
6 //
7 // MultiSource/MultiSink: create a super source
  with infinite capacity pointing to all
  sources, analogous for sinks
8 //

```

```

9 // Max Cardinality Bipartite Matching: use
  capacity 1 on all edges and apply the
  multi-source and multi-sink strategies
10 //
11 // Time:  $O(VE^2)$ 
12 // Space:  $O(V + E)$ 
13 // Status: tested (CSES1694, CSES1695)
14
15 vector<vector<int>>> capacity(M, vector<int>(M,
  0)), adj(M);
16 vector<pair<int, int>> mc; //mincut edges
17
18 int bfs(int s, int t, vi &par) {
19     fill(all(par), -1);
20     par[s] = -2;
21     queue<pair<int, int>> q; q.push({s, inf});
22     while (!q.empty()) {
23         int v = q.front().first,
24             flow = q.front().second;
25         q.pop();
26         for (auto u: adj[v])
27             if (par[u] == -1 && capacity[v][u]) {
28                 par[u] = v;
29                 int new_flow = min(flow,
30                                     capacity[v][u]);
31                 if (u == t) return new_flow;
32                 q.push({u, new_flow});
33             }
34     }
35     return 0;
36 }
37
38 int maxflow(int s, int t) {
39     int flow = 0;
40     vi par(M);
41     int new_flow;
42     while ((new_flow = bfs(s, t, par))) {
43         flow += new_flow;
44         int v = t;
45         while (v != s) {
46             int p = par[v];
47             capacity[p][v] -= new_flow;
48             capacity[v][p] += new_flow;
49             v = p;
50         }
51     }
52     return flow;
53 }
54
55 void mincut(int s, int t) {
56     maxflow(s, t);
57     stack<int> st;
58     vector<bool> visited(n, false);
59     vector<pair<int, int>> ans;
60     st.push(0);
61     while (!st.empty()) {
62         int v = st.top(); st.pop();
63         if (visited[v]) continue;
64         visited[v] = true;
65         for (auto u: adj[v])
66             if (capacity[v][u] > 0)
67                 st.push(u);
68         else
69             ans.push_back({v, u});
70     }
71     mc.clear();
72     for (auto &[v, u] : ans)
73         if (!visited[u])
74             mc.push_back({v, u});
75 }

```

## 1.13 Floyd Warshall APSP

```

1 // Also works for SSSP ( $V \leq 400$ )
2 //
3 // Printing path: p[i][j] set to i (last node that
  appears before j on the path), then p[i][j] =
  p[k][j] on update.

```

```

4 //
5 // Transitive Closure: weight is boolean (init as
   1 if there's an edge), update with bitwise OR
6 //
7 // Minimax/Maximin: w[i][j] = min(w[i][j],
   max(w[i][k], w[k][j]))
8 //
9 // Finding negative/cheapest cycle: init w[i][i] =
   inf; run(); any w[i][i] != inf is a cycle and
   the smallest is the cheapest; any w[i][i] < 0
   is negative
10 //
11 // This can also be used for finding SCCs (check
   with transitive closure)
12 //
13 // Usage: FloydWarshall(n, edges)
14 // Time: O(V^3+E)
15 // Space: O(V^2+E)
16 // Status: tested (UVA821, UVA1056)
17
18 struct edge { int v, u, w; };
19 const int inf = 0x3f3f3f3f;
20 vector<vector<int>> weight(M, vector<int>(M, inf));
21 vector<edge> edges;
22
23 void floydWarshall(int n) {
24     for (auto e: edges)
25         weight[e.v][e.u] = e.w;
26     for (int k = 0; k < n; ++k)
27         for (int i = 0; i < n; ++i)
28             for (int j = 0; j < n; ++j)
29                 if (max(weight[i][k],
30                     weight[k][j]) < inf)
31                     weight[i][j] =
32                         min(weight[i][j],
33                             weight[i][k]+weight[k][j]);
34 }

```

## 2 Math

### 2.1 Sieve of Eratosthenes

```

1 // Time: O(n log log n)
2 // Space: O(n)
3 // Status: not tested
4
5 bitset<11234567> pr;
6 vector<int> factors(M, 0);
7 vector<int> primes;
8
9 void sieve(int n) {
10     pr.set();
11     for (int i = 2; i*i <= n; ++i)
12         if (pr[i]) { //factors[i] == 0
13             primes.push_back(i);
14             for (int p = i*i; p <= n; p += i) {
15                 pr[p] = false;
16                 factors[p]++;
17             }
18         }
19 }
20
21 // O(1) for small n, O(sieve_size) else
22 bool isPrime(int n) {
23     int sieve_size = 11234567;
24     if (n <= sieve_size) return pr[n];
25     for (auto p: primes) // only works if n <=
26         if (!(n%p)) return false;
27     return true;
28 }

```

### 2.2 Prime Factors w/ Optimized Trial Divisions

```

1 // Time: O(Pi(sqrt(n)))
2 // Space: O(n)
3 // Status: not tested
4 // Source: CP3 (pg. 238)
5
6 vector<int> primes;
7 vector<pair<int, int>> factors;
8
9 void pf(int n) {
10     for (auto p: primes) {
11         if (p*p > n) break;
12         int i = 0;
13         while (!(n%p)) {
14             n /= p;
15             i++;
16         }
17         factors.push_back({p, i});
18     }
19     if (n != 1) factors.push_back({n, 1});
20 }

```

### 2.3 Extended Euclid for solving Linear Diophantine Equations

```

1 // Time: O(log min(a, b))
2 // Status: not tested
3 // Source: CP3 (pg. 242)
4
5 int x, y, d;
6 void extendedEuclid(int a, int b) {
7     if (b == 0) { x = 1; y = 0; d = a; return; }
8     extendedEuclid(b, a%b);
9     int x1 = y;
10    int y1 = x - (a/b)*y;
11    x = x1;
12    y = y1;
13 }
14
15 void solve(int a, int b, int c, int i) { //i
16     solutions
17     extendedEuclid(a, b);
18     if (d%c) return;
19     x *= c/d;
20     y *= c/d;
21     do {
22         cout << x << ", " << y << '\n';
23         x += b/d;
24         y -= a/d;
25     } while (--i);
26 }

```

### 2.4 Floyd's algorithm cycle-finding

```

1 // Slow and fast (tortoise and hare)
2 //
3 // Time: O(V)
4 // Space: O(1)
5 // Status: not tested
6 // Source: CPHB (p. 156)
7
8 int findCycle(int x) {
9     int a, b;
10    a = succ(x);
11    b = succ(succ(x));
12    while (a != b) {
13        a = succ(a);
14        b = succ(succ(b));
15    }
16    a = x;
17    while (a != b) {
18        a = succ(a);
19        b = succ(b);
20    }
21    int first = a; // first element in cycle
22    b = succ(a);
23    int length = 1;

```

```

24     while (a != b) {
25         b = succ(b);
26         length++;
27     }
28 }

```

## 3 Paradigm

### 3.1 Coordinate Compression

```

1 // normalize vector access; can also be done with
  map/set but high constant
2 //
3 // Time: O(N log N)
4 // Status: not tested
5 // Source: GEMA ICMC (YouTube)
6
7 vector<int> v, vals, cv; // all of the same size,
  cv = compressed v
8 vals = v;
9 sort(vals.begin(), vals.end());
10 vals.erase(unique(vals.begin(), vals.end()),
  vals.end());
11 for (int i = 0; i < n; ++i) {
12     int idx = lower_bound(vals.begin(),
  vals.end(), v[i]) - vals.begin();
13     cv[i] = idx;
14 }

```

### 3.2 128 Bit Integers

```

1 // GCC extension; 2127 -1 ~ 1038
2 //
3 // Status: not tested
4 // Source: GEMA (YouTube)
5
6 // cout, cerr, etc; podedar over/underflow
7 ostream& operator<<(ostream& out, __int128 x) {
8     if (x == 0) return out << 0;
9     string s; bool sig = x < 0; x = x < 0 ? -x : x;
10    while(x > 0) s += x % 10 + '0', x /= 10;
11    if (sig) s += '-';
12    reverse(s.begin(), s.end());
13    return out << s;
14 }
15
16 // cin, etc; podedar over/underflow
17 istream& operator>>(istream& in, __int128& x) {
18     char c, neg = 0; while(isspace(c = in.get()));
19     if(!isdigit(c)) neg = (c == '-'), x = 0;
20     else x = c - '0';
21     while(isdigit(c = in.get())) x = (x << 3) + (x
  << 1) - '0' + c;
22     x = neg ? -x : x; return in;
23 }

```

### 3.3 Binary Search (but beautiful)

```

1 // binary steps
2 //
3 // Time: O(log N)
4 // Status: not tested
5 // Source: CPHB
6
7 // std
8 int l = 0, r = n-1;
9 while (l <= r) {
10     int m = l+(r-l)/2;
11     if (array[m] == x)
12         // found
13     if (array[m] > x) r = m-1;
14     else l = m+1;
15 }
16

```

```

17 // nice
18 int k = 0;
19 for (int b = n/2; b > 0; b /= 2)
20     while (k+b < n && array[k+b] <= x)
21         k += b;
22 if (array[k] == x)
23     // found

```

## 4 String

### 4.1 Prefix Function (KMP)

```

1 //
2 // to find occurrences of s in t, use the string
  s+%t, then look for pi[i] = s.length() on the
  "t side"
3 // Time: O(N)
4 // Status: not tested
5 // Source: CP-Algorithms
6
7 vector<int> prefix(string s) {
8     int n = s.length();
9     vector<int> pi(n, 0); // can be optimized if
  you know max prefix length
10    for (int i = 1; i < n; ++i) {
11        int j = pi[i-1];
12        while (j > 0 && s[i] != s[j])
13            j = pi[j-1];
14        if (s[i] == s[j])
15            j++;
16        pi[i] = j;
17    }
18    return pi;
19 }

```

## 5 Structure

### 5.1 Merge/Disjoint Union-Find

```

1 //
2 // Usage: UnionFind(N);
3 // Time: O(AM), ackerman * num_operations
4 // Space: O(N), elements
5 // Status: tested (UVA11503)
6
7 struct UnionFind {
8     int N;
9     vi par, rk, count;
10
11    UnionFind(int N) : N(N), par(N), rk(N, 0),
  count(N, 1) {
12        rep(i, 0, N) par[i] = i;
13    }
14
15    int findSet(int i) {
16        return par[i] == i ? i : (par[i] =
  findSet(par[i]));
17    }
18
19    int unionSet(int a, int b) {
20        int x = findSet(a), y = findSet(b);
21        if (x != y)
22            count[x] = count[y] =
  (count[x]+count[y]);
23        if (rk[x] < rk[y])
24            par[x] = y;
25        else {
26            par[y] = x;
27            if (rk[x] == rk[y])
28                rk[x]++;
29        }
30        return count[x];
31    }

```

```

32
33     bool isSameSet(int i, int j) {
34         return findSet(i) == findSet(j);
35     }
36 };

```

## 5.2 Bottom-Up Segment Tree

```

1 //
2 // Usage: SegTree(N);
3 //
4 // Source: CP Handbook
5 // Time: O(log N)
6 // Space: O(N), elements
7 // Status: not tested
8
9 struct SegTree {
10     unsigned int n;
11     vector<int> tree;
12
13     SegTree(vector<int> v) : n(v.size()), tree(2*n) {
14         for (int i = 0; i < n; ++i)
15             modify(i, v[i]);
16     }
17
18     int query(int a, int b) {
19         a += n, b += n;
20         int ans = 0;
21         while (a <= b) {
22             if (a%2 == 1) ans += tree[a++];
23             if (b%2 == 0) ans += tree[b--];
24             a >>= 1; b >>= 1;
25         }
26         return ans;
27     }
28
29     void modify(int k, int x) {
30         k += n;
31         tree[k] += x;
32         for (k /= 2; k >= 1; k /= 2)
33             tree[k] = tree[k<<1] + tree[(k<<1) + 1];
34     }
35 };

```

## 5.3 Segment Tree

```

1 //
2 // Usage: SegTree(N)
3
4 struct SegTree {
5     int N;
6     vi st, A;
7
8     SegTree(int N): N(N), st(4*n), A(n) {
9         init();
10    }
11
12    void init() { build(1, 0, n-1); }
13
14    int left(int i) { return i*2; }
15    int right(int i) { return i*2+1; }
16
17    //O(N)
18    void build(int v, int tl, int tr) {
19        if (tl == tr) st[v] = a[tl];
20        else {
21            int tm = (tl+tr)/2;
22            build(left(v), tl, tm);
23            build(right(v), tm+1, tr);
24            st[v] = max(st[left(v)], st[right(v)]);
25        }
26    }
27
28    //O(log n)
29    int maxquery(int v, int tl, int tr, int l, int
30                r) {
31        if (l > r) return -1;

```

```

31        if (l == tl && r == tr) return st[v];
32        int tm = (tl+tr)/2;
33        int q1 = maxquery(left(v), tl, tm, l,
34                          min(r, tm));
35        int q2 = maxquery(right(v), tm+1, tr,
36                          max(l, tm+1), r);
37        return max(q1, q2);
38    }
39
40    int maxquery(int l, int r) {
41        return maxquery(1, 0, n-1, l-1, r-1);
42    }
43
44    //O(log n)
45    void update(int v, int tl, int tr, int p, int
46               new_val) {
47        if (tl == tr) st[v] = new_val;
48        else {
49            int tm = (tl+tr)/2;
50            if (p <= tm)
51                update(left(v), tl, tm, p,
52                      new_val);
53            else
54                update(right(v), tm+1, tr, p,
55                      new_val);
56            st[v] = max(st[left(v)], st[right(v)]);
57        }
58    }
59
60    void update(int p, int new_val) {
61        update(1, 0, n-1, p-1, new_val);
62    }
63 };

```

## 6 Extra

### 6.1 Bashrc

```

1 xmodmap -e 'clear lock' -e 'keycode 66=Escape' #
2 caps -> esc
3
4 BASE_CP="/home/raul/cp2022"
5
6 alias c='g++ -Wall -Wconversion -Wfatal-errors -g
7 -O2 -std=gnu++17 -fsanitize=undefined,address'
8 alias c14='g++ -Wall -Wconversion -Wfatal-errors
9 -g -O2 -std=gnu++14
10 -fsanitize=undefined,address'
11 alias p3='py3 -m py_compile'
12
13 tp () {
14     [ -f "$1.cpp" ] && echo "$1.cpp already
15     exists";
16     [ ! -f "$1.cpp" ] && tail -n +2
17     $BASE_CP/code/extra/template.cpp > $1.cpp
18     && vim $1.cpp;
19 }
20
21 clip () {
22     if [ -f "$1" ];
23     then
24         cat $1 | clip.exe;
25     else
26         echo "$1 not found"
27     fi
28 }

```

### 6.2 Vim

```

1 set et ts=2 sw=2 ai si cindent sta
2 set is tm=50 nu noeb sm "cul
3 sy on

```

## 6.3 Generator

```
1 #include <bits/stdc++.h>
2 using namespace std;
3
4 int main(int argc, char *argv[]) {
5     cin.tie(0); ios_base::sync_with_stdio(0);
6     if (argc < 2) {
7         cout << "usage: " << argv[0] << " <seed>\n";
8         exit(1);
9     }
10    srand(atoi(argv[1]));
11    // use rand() for random value
12 }
```

## 6.4 C++ Template

```
1 #include <bits/stdc++.h>
2 using namespace std;
3 using ll = long long;
4
5 int main() {
6     ios_base::sync_with_stdio(0);
7     cin.tie(0);
8 }
```

## 6.5 Stress

```
1 for (( I=0; I < 5; I++ )); do
2     ./gen $I > a.in
3     ./brute < a.in > expected.txt
4     ./a.out < a.in > output.txt
5     if diff -u expected.txt output.txt; then : ; else
6         echo "--> input:"; cat a.in
7         echo "--> expected output:"; cat expected.txt
8         echo "--> received output:"; cat output.txt
9         break
10    fi
11    echo -n .
12 done
```