# Competitive Programming Notebook

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	1.1 Prim MST	1	
	1.2 Dijkstra SSSP	1	1 // Status: tested (UVA10048)
			<pre>3 vector &lt; vector &lt; pair &lt; int , int &gt;&gt; adj(M), mst(M);</pre>
	1.3 Graph Check	2	4 vector <bool> taken(M, false);</bool>
	1.4 Articulations and Bridges	2	5 int cost = 0;
	1.5 Euler Tour	2	<pre>6 using iii = pair<int, int="" pair<int,="">&gt;; 7 priority_queue<iii, greater<iii="" vector<iii,="">&gt; pq;</iii,></int,></pre>
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			13 pq.push({w, {v, u}}); 14 }
	1.10 Bellman-Ford SSSP	3	14 5
	1.11 Kruskal MST	3	16 void run(int n) {
	1.12 Edmond Karp MaxFlow	3	process(0); while (!pq.empty()) {
	1.13 Floyd Warshall APSP	4	int w = pq.top().first,
			v = pq.top().second.first,
<b>2</b>	Math	4	u = pq.top().second.second; pq.pop();
	2.1 Sieve of Eratosthenes	4	22 pq.pop(), 23 if (!taken[u]) {
	2.2 Prime Factors w/ Optimized Trial Di-	_	24 mst_cost += w;
	visions	4	25 mst[u].push_back({w, v}); 26 mst[v].push_back({v, w});
		4	27 process(u);
	2.3 Extended Euclid for solving Linear		28 }
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4	String	5	1 // Status: tested (CF20C)
	4.1 Prefix Function (KMP)	5	<pre>3 using ii = pair<int, int="">;</int,></pre>
			<pre>4 const int inf = 0x3f3f3f3f; 5 vector<vector<ii>&gt; adj(M);</vector<ii></pre>
5	Structure	<b>5</b>	6 vector < int > dist(M, inf), par(M, -1);
	5.1 Merge/Disjoint Union-Find	5	7
	5.2 Bottom-Up Segment Tree	6	<pre>8 void dijkstra(int s) { 9    dist[s] = 0;</pre>
	5.3 Segment Tree	6	priority_queue <ii, <ii="" vector="">,</ii,>
	5.5 Degment free	U	<pre>greater<pair<int, int="">&gt;&gt; pq;</pair<int,></pre>
6	Extra	6	11
U		-	int w = pq.top().first;
	6.1 Bashre	6	int v = pq.top().second;
	6.2 Vim	7	pq.pop(); if (w > dist[v]) continue;
	6.3 Generator	7	17 for (auto &[d, u]: adj[v])
	6.4 C++ Template	7	if (dist[v] != inf && dist[v]+d <
	C F CI	-	dist[u]) {

par[u] = v;

6.4 C++ Template . . . . . . . . . . . . . . . 

## 1.3 Graph Check

```
1 // Usage: graphCheck(firstVertex, -1) (p stands
      for parent)
3 int UNVISITED = -1, EXPLORED = 0, VISITED = 1;
4 vector < vector < int >> adj(M);
5 vector < int > tin;
7 void graphCheck(int v, int p) { //vertex, parent
      tin[v] = EXPLORED;
      for (auto u: adj[v]) {
          if (tin[u] == UNVISITED) { //tree edge
10
11
               graphCheck(u, v);
          } else if (tin[u] == EXPLORED) {
12
               if (u == p)
                   ; //two way edge u <-> v
15
                   ; //back edge v -> u
          } else if (tin[u] == VISITED) {
17
               ; //forward/cross edge u-v
18
19
20
      tin[v] = VISITED;
21
```

## 1.4 Articulations and Bridges

```
1 // Usage: dfs(source, -1)
2 // Status: not tested
4 int tk = 0;
5 vector < int > tin(M, -1);
6 vector < vector < int >> adj(M);
8 void dfs(int v, int p) {
      tin[v] = low[v] = tk++;
      int children = 0;
      for (auto u: adj[v]) {
11
           if (u == p) continue;
12
           else if (tin[u] == -1) {
               ++children;
               dfs(u, v);
               if (low[u] >= tin[v] && p != v)
16
                   ; //articulation point
17
               if (low[u] > tin[v])
                   : //bridge u-v
19
               low[v] = min(low[v], low[u]);
22
               low[v] = min(low[v], tin[u]);
24
25 }
```

### 1.5 Euler Tour

## 1.6 Kahn's topological sort

```
1 // Status: tested (UVA11060)
3 vector < vector < int >> adj(M);
4 vector < int > sorted;
6 void kahn(int n) {
      vector<int> indeg(n, 0);
      vector<bool> valid(n, true);
      priority_queue < int > pq;
10
      for (int v = 0; v < n; ++v)
11
          for (auto u: adj[v])
12
              indeg[u]++;
      for (int v = 0; v < n; ++v)
          if (!indeg[v]) pq.push(v);
15
      while (!pq.empty()) {
           int v = pq.top(); pq.pop();
18
           sorted.push_back(v);
           valid[v] = false;
20
           for (auto u: adj[v])
               if (valid[u] && !(--indeg[u]))
23
                   pq.push(u);
24
25 }
```

# 1.7 Max Cardinality Bipartite Matching

```
1 // Status: not tested
2 // Source: CP3 (pg. 209)
4 vector < vector < int >> adj(M);
5 vector < int > match(M, -1);
6 vector < bool > visited(M);
8 bool augment(int left) { //match one on the left
      with one on the right
      if (visited[left]) return false;
      visited[left] = true;
11
      for (auto right: adj[left])
           if (match[right] == -1 | |
12
               augment(match[right])) {
               match[right] = left;
13
14
               return true;
          }
      return false;
16
17 }
19 //usage
20 //(mcbm = V iff there's at least one way to
      completely match both sides)
21 int mcbm = 0; //number of matched vertices
22 match.assign(M, -1);
23 for (int v = 0; v < ls; ++v) {//ls = size of the
      left set
      visited.assign(ls, false);
      mcbm += augment(v);
26 }
```

#### 1.8 Lowest Common Ancestor

```
1 // Status: not tested
3 //--- binary lifting
4 int n, l = ceil(log2(n));
5 vector < vector < int >> adj;
6 \text{ int. } tk = 0:
7 vector < int > tin(n), tout(n);
8 vector < vector < int >> up(n, vector < int > (1+1)); //
10 void dfs(int v, int p) { // run dfs(root, root) to
      initialize
       tin[v] = ++tk;
11
      up[v][0] = p;
12
       for (int i = 1; i <= 1; ++i)
          up[v][i] = up[up[v][i-1]][i-1];
14
       for (int u : adj[v])
1.5
          if (u != p)
               dfs(u, v);
17
       tout[v] = ++tk;
18
19 }
20
21 bool ancestor(int v, int u) { // v is ancestor of u
      return tin[v] <= tin[u] && tout[v] >= tout[u];
23 }
25 int lca(int v, int u) {
       if (ancestor(v, u)) return v;
26
       if (ancestor(u, v)) return u;
       for (int i = 1; i >= 0; --i)
28
29
           if (!ancestor(up[v][i], u))
              v = up[v][i];
30
       return up[v][0];
31
32 }
33
34 //--- euler path
35 using ii = pair<int, int>;
36 vector<ii> t;
37 vector < int > idx(n);
38 int tk = 1:
39
40 void dfs(int v, int d) { // call with dfs(root, 0);
      for (auto u : adj[v]) {
41
42
           st.update(tk, {d, v});
           tk++;
43
           dfs(u, d+1);
44
45
46
       idx[v] = tk;
       st.update(tk, {d, v});
47
       tk++;
49 }
50
51 int lca(int v, int u) {
       int 1 = idx[v], r = idx[u];
52
       return st.minquery(1, r).second; // .first is
53
           depth
54 }
```

# 1.9 Tarjan Strongly Connected Component

```
1 // Usage: Tarjan(N, adj)
 _{2} // Status: tested (UVA247, UVA11838)
 4 vector \langle int \rangle tin(M, -1), low(M, -1);
 5 vector < vector < int > adj(M);
 6 stack < int > S;
 7 int tk = 0:
9 void dfs(int v) {
      low[v] = tin[v] = tk++;
       S.push(v);
11
       visited[v] = true;
12
       for (auto u: adj[v]) {
           if (tin[u] == -1)
14
15
                dfs(u):
           if (visited[u])
```

#### 1.10 Bellman-Ford SSSP

```
1 // Status: tested (UVA1112, UVA10449)
2 const int inf = 0x3f3f3f3f3f;
3 vector < vector < pair < int , int >>> adj(M);
4 vector<int> dist(M, inf);
6 void bellmanFord(int n) {
      for (int i = 0; i < n-1; ++i)
for (int v = 0; v < n; ++v)
                for (auto &[u, w]: adj[v])
                    if (dist[v] != inf)
                        dist[u] = min(dist[u],
                            dist[v]+w);
12 }
14 //check if there are negative cycles
15 bool cycle(int n) {
      bool ans = false;
       for (int v = 0; v < n; ++v)
           for (auto &[u, w]: v)
               ans |= dist[v] != inf && dist[u] >
                    dist[v]+w;
```

#### 1.11 Kruskal MST

```
1 // Usage: Kruskal(V, E, edges) (weighted edges)
2 // Status: tested (UVA1174)
4 using iii = pair<int, pair<int, int>>; //weight,
      two vertices
5 vector<iii> edges;
6 UnionFind muf;
8 int kruskal() {
      int cost = 0;
      sort(edges.begin(), edges.end());
10
      for (auto a: edges) {
          int w = a.first;
           pair < int , int > e = a.second;
           if (!muf.isSameSet(e.first, e.second)) {
               cost += w;
15
16
               muf.unionSet(e.first, e.second);
17
18
      return cost;
```

## 1.12 Edmond Karp MaxFlow

```
i // Status: tested (CSES1694, CSES1695)
3 vector < vector < int >> capacity(M, vector < int > (M,
      0)), adj(M);
4 vector <pair < int , int >> mc; //mincut edges
6 int bfs(int s, int t, vi &par) {
      fill(all(par), -1);
      par[s] = -2;
       queue <pair <int, int >> q; q.push({s, inf});
       while (!q.empty()) {
1.0
          int v = q.front().first,
                    flow = q.front().second;
12
13
           q.pop();
           for (auto u: adj[v])
```

```
if (par[u] == -1 && capacity[v][u]) {
                   par[u] = v;
                    int new_flow = min(flow,
17
                        capacity[v][u]);
                    if (u == t) return new_flow;
                    q.push({u, new_flow});
19
20
21
       return 0;
22
23 }
24
25 int maxflow(int s, int t) {
       int flow = 0;
26
       vi par(M);
27
       int new_flow;
       while ((new_flow = bfs(s, t, par))) {
29
           flow += new_flow;
30
           int v = t;
           while (v != s) {
32
               int p = par[v];
33
               capacity[p][v] -= new_flow;
               capacity[v][p] += new_flow;
35
36
37
      }
38
39
       return flow;
40 }
41
42 void mincut(int s, int t) {
      maxflow(s, t);
43
       stack < int > st;
45
       vector < bool > visited(n, false);
      vector<pair<int, int>> ans;
46
       st.push(0);
       while (!st.empty()) {
48
          int v = st.top(); st.pop();
49
           if (visited[v]) continue;
           visited[v] = true;
51
           for (auto u: adj[v])
52
               if (capacity[v][u] > 0)
54
                   st.push(u);
                   ans.push_back({v, u});
56
57
      mc.clear();
58
      for (auto &[v, u] : ans)
59
60
          if (!visited[u])
              mc.push_back({v, u});
61
62 }
```

# 1.13 Floyd Warshall APSP

```
1 // Usage: FloydWarshall(n, edges)
2 // Status: tested (UVA821, UVA1056)
4 struct edge { int v, u, w; };
5 const int inf = 0x3f3f3f3f;
6 vector<vector<int>> weight(M, vector<int>(M, inf));
7 vector < edge > edges;
9 void floydWarshall(int n) {
      for (auto e: edges)
10
11
          weight[e.v][e.u] = e.w;
12
       for (int k = 0; k < n; ++k)
           for (int i = 0; i < n; ++i)</pre>
13
               for (int j = 0; j < n; ++j)
                   if (max(weight[i][k],
15
                       weight[k][j]) < inf)
                       weight[i][j] =
                           min(weight[i][j],
                            weight[i][k]+weight[k][j]);
17 }
```

## 2 Math

### 2.1 Sieve of Eratosthenes

```
1 // Status: not tested
3 bitset <11234567> pr;
4 vector<int> factors(M, 0);
5 vector < int > primes;
7 void sieve(int n) {
      pr.set();
       for (int i = 2; i*i <= n; ++i)</pre>
            if (pr[i]) { //factors[i] == 0
10
                primes.push_back(i);
                for (int p = i*i; p <= n; p += i) {
    pr[p] = false;</pre>
                    factors[p]++;
14
                }
           }
17 }
19 // O(1) for small n, O(sieve_size) else
20 bool isPrime(int n) {
       int sieve_size = 11234567;
       if (n <= sieve_size) return pr[n];</pre>
22
       for (auto p: primes) // only works if n <=</pre>
           primes.back()^2
           if (!(n%p)) return false;
24
       return true;
```

# 2.2 Prime Factors w/ Optimized Trial Divisions

```
1 // Status: not tested
2 // Source: CP3 (pg. 238)
4 vector < int > primes;
5 vector < pair < int , int >> factors;
7 void pf(int n) {
       for (auto p: primes) {
           if (p*p > n) break;
           int i = 0;
10
           while (!(n%p)) {
               n /= p;
12
1.3
                i++;
           {\tt factors.push\_back(\{p,\ i\});}
15
16
       if (n != 1) factors.push_back({n, 1});
18 }
```

# 2.3 Extended Euclid for solving Linear Diophantine Equations

```
1 // Status: not tested
2 // Source: CP3 (pg. 242)
4 int x, y, d;
5 void extendedEuclid(int a, int b) {
      if (b == 0) { x = 1; y = 0; d = a; return; }
      extendedEuclid(b, a%b);
      int x1 = y;
      int y1 = x - (a/b)*y;
9
      x = x1;
      y = x1;
11
12 }
14 void solve(int a, int b, int c, int i) { //i
      solutions
      extendedEuclid(a, b);
```

```
if (d%c) return;
16
17
      x *= c/d;
      y *= c/d;
18
19
       do {
           cout << x << ", " << y << '\n';
20
           x += b/d;
21
           y = a/d;
22
       } while (--i);
23
24 }
```

## 2.4 Floyd's algorithm cycle-finding

```
1 // Status: not tested
2 // Source: CPHB (p. 156)
4 int findCycle(int x) {
      int a, b;
      a = succ(x);
      b = succ(succ(x));
      while (a != b) {
          a = succ(a):
           b = succ(succ(b));
      }
11
      a = x;
12
      while (a != b) {
          a = succ(a);
14
15
           b = succ(b);
16
      int first = a; // first element in cycle
17
      b = succ(a);
      int length = 1;
19
       while (a != b) {
20
21
           b = succ(b);
          length++;
22
23
```

# 3 Paradigm

# 3.1 Coordinate Compression

## 3.2 128 Bit Integers

```
1 // Status: not tested
2 // Source: GEMA (YouTube)
3
4 // cout, cerr, etc; pode dar over/underflow
5 ostream& operator<<(ostream& out, __int128 x) {
6    if (x == 0) return out << 0;
7    string s; bool sig = x < 0; x = x < 0 ? -x : x;
8    while(x > 0) s += x %, 10 + '0', x /= 10;
9    if (sig) s += '-';
10    reverse(s.begin(), s.end());
11    return out << s;
12 }
13
14 // cin, etc; pode dar over/underflow
15 istream& operator>>(istream& in, __int128& x) {
16    char c, neg = 0; while(isspace(c = in.get()));
```

## 3.3 Binary Search (but beautiful)

```
1 // Status: not tested
2 // Source: CPHB
4 // std
5 int 1 = 0, r = n-1;
6 while (1 <= r) {
      int m = 1+(r-1)/2;
      if (array[m] == x)
          // found
      if (array[m] > x) r = m-1;
      else 1 = m+1;
11
12 }
14 // nice - binary steps
15 int k = 0;
16 for (int b = n/2; b > 0; b /= 2)
      while (k+b < n && array[k+b] <= x)
       k += b;
18
19 if (array[k] == x)
      // found
```

# 4 String

# 4.1 Prefix Function (KMP)

```
i // Status: not tested
2 // Source: CP-Algorithms
4 vector<int> prefix(string s) {
      int n = s.length();
      vector < int > pi(n, 0); // can be optimized if
           you know max prefix length
      for (int i = 1; i < n; ++i) {
          int j = pi[i-1];
           while (j > 0 && s[i] != s[j])
              j = pi[j-1];
           if (s[i] == s[j])
               j++;
           pi[i] = j;
13
      }
15
      return pi;
16 }
```

# 5 Structure

# 5.1 Merge/Disjoint Union-Find

```
15
16
       int unionSet(int a, int b) {
           int x = findSet(a), y = findSet(b);
17
18
           if (x != y)
               count[x] = count[y] =
19
                    (count[x]+count[y]);
           if (rk[x] < rk[y])</pre>
20
               par[x] = y;
21
           else {
22
               par[y] = x;
               if (rk[x] == rk[y])
24
25
                    rk[x]++;
26
           return count[x]:
27
       }
28
29
       bool isSameSet(int i, int j) {
30
           return findSet(i) == findSet(j);
32
33 }:
```

## 5.2 Bottom-Up Segment Tree

```
1 // Usage: SegTree(N);
2 // Source: CP Handbook
3 // Status: not tested
5 struct SegTree {
    unsigned int n;
     vector < int > tree;
    SegTree(vector<int> v) : n(v.size()), tree(2*n) {
10
       for (int i = 0; i < n; ++i)</pre>
         modify(i, v[i]);
11
12
13
     int query(int a, int b) {
14
      a += n, b += n;
       int ans = 0;
16
       while (a <= b) {
17
         if (a%2 == 1) ans += tree[a++];
18
         if (b%2 == 0) ans += tree[b--];
19
         a >>= 1; b >>= 1;
20
      }
21
22
       return ans;
23
24
25
    void modify(int k, int x) {
26
      k += n;
       tree[k] += x;
27
       for (k /= 2; k >= 1; k /= 2)
28
         tree[k] = tree[k<<1] + tree[(k<<1) + 1];
29
30
31 };
```

# 5.3 Segment Tree

```
1 // Usage: SegTree(N)
3 struct SegTree {
      int N;
      vi st, A;
      SegTree(int N): N(N), st(4*n), A(n) {
           init();
9
10
      void init() { build(1, 0, n-1); }
11
12
      int left(int i) { return i*2; }
13
      int right(int i) { return i*2+1; }
15
      //n(N)
16
       void build(int v, int tl, int tr) {
          if (tl == tr) st[v] = a[tl];
18
19
           else {
               int tm = (tl+tr)/2;
```

```
build(left(v), tl, tm);
               build(right(v), tm+1, tr);
               st[v] = max(st[left(v)], st[right(v)]);
23
          }
24
26
27
       //0(log n)
       int maxquery(int v, int tl, int tr, int l, int
          r) {
           if (1 > r) return -1;
           if (1 == tl && r == tr) return st[v];
30
31
           int tm = (tl+tr)/2;
           int q1 = maxquery(left(v), tl, tm, l,
              min(r, tm)):
           int q2 = maxquery(right(v), tm+1, tr,
              max(1, tm+1), r);
           return max(q1, q2);
34
36
       int maxquery(int 1, int r) {
37
          return maxquery(1, 0, n-1, 1-1, r-1);
39
40
      //0(log n)
      void update(int v, int tl, int tr, int p, int
42
          new_val) {
           if (tl == tr) st[v] = new_val;
43
           else {
45
               int tm = (tl+tr)/2;
               if (p <= tm)
46
                   update(left(v), tl, tm, p,
                       new_val);
                   update(right(v), tm+1, tr, p,
                       new val):
               st[v] = max(st[left(v)], st[right(v)]);
50
           }
      }
52
53
       void update(int p, int new_val) {
           update(1, 0, n-1, p-1, new_val);
55
57 };
```

### 6 Extra

### 6.1 Bashrc

```
1 xmodmap -e 'clear lock' -e 'keycode 66=Escape' #
      caps -> esc
2 alias e=vim
4 BASE_CP="/home/raul/cp2022"
6 alias c='g++ -Wall -Wconversion -Wfatal-errors -g
      -02 -std=gnu++17 -fsanitize=undefined, address;
7 alias c14='g++ -Wall -Wconversion -Wfatal-errors
      -g -02 -std=gnu++14
      -fsanitize=undefined, address'
8 alias p3='pypy3 -m py_compile'
10 tp () {
      [ -f "$1.cpp" ] && echo "$1.cpp already
          exists";
      [ ! -f "$1.cpp" ] && tail -n +2
          $BASE_CP/code/extra/template.cpp > $1.cpp
          && vim $1.cpp;
13 }
15 clip () {
      if [ -f "$1" ];
16
17
      then
         cat $1 | clip.exe;
19
      else
          echo "$1 not found"
20
```

```
22 }
```

### 6.2 Vim

```
1 set et ts=2 sw=2 ai si cindent sta
2 set is tm=50 nu noeb sm "cul
3 sy on
```

## 6.3 Generator

```
1 #include <bits/stdc++.h>
2 using namepsace std;
3
4 int main(int argc, char *argv[]) {
5    cin.tie(0); ios_base::sync_with_stdio(0);
6    if (argc < 2) {
7       cout << "usage: " << argv[0] << " <seed>\n";
8       exit(1);
9    }
10    srand(atoi(argv[1]));
11    // use rand() for random value
12 }
```

# 6.4 C++ Template

```
1 #include <bits/stdc++.h>
2 using namespace std;
3 using ll = long long;
4
5 int main() {
6    ios_base::sync_with_stdio(0);
7    cin.tie(0);
8 }
```

## 6.5 Stress

```
1 for (( I=0; I < 5; I++ )); do
2    ./gen $I > a.in
3    ./brute < a.in > expected.txt
4    ./a.out < a.in > output.txt
5    if diff -u expected.txt output.txt; then : ; else
6    echo "--> input:"; cat a.in
7    echo "--> expected output:"; cat expected.txt
8    echo "--> received output:"; cat output.txt
9    break
10    fi
11    echo -n .
12 done
```