Competitive Programming Notebook

Raul Almeida¹

$^1{\rm Universidade}$ Federal do Paraná

October 9, 2023

C	ontents		6		9
1	Theory 1.1 Relevant comparisons	2 2 2 2	_	6.2 128 Bit Integers	9 9 9
	1.4 Series Identities 1.5 Binomial Identities 1.6 Lucas' Theorem 1.7 Fermat Theorems 1.8 Modulo @ exponent 1.9 Heron's Formula 1.10 Some Primes 1.11 Catalan Numbers	2 3 3 3 3 3 3 3	8	7.1 Rolling hash (linear)	0
2	1.12 Binomial	3 4 4 4 4 4 4	9	8.3 Segment Tree	1 1 1 1
3	Geometry 3.1 Points 3.2 Convex Hull (Monotone)	4 4 5		9.7 Stress	
4	Graph 4.1 Prim MST 4.2 Dijkstra SSSP 4.3 Graph Check 4.4 Articulations and Bridges 4.5 Euler Tour 4.6 FFEK MaxFlow 4.7 Heavy-Light Decomposition 4.8 Kahn's topological sort 4.9 MCBM (Kunh Matching) 4.10 LCA - Binary lifting 4.11 Tarjan Strongly Connected Component 4.12 LCA - Euler Path 4.13 Kosaraju SCC 4.14 Bellman-Ford SSSP 4.15 Kruskal MST 4.16 Floyd Warshall APSP	5 5 5 5 5 6 6 6 7 7 7 7 7 8 8			
5	Math 5.1 Sieve of Eratosthenes	8 8 8 8			

\overline{n}	not-TLE algorithm	Example
$\leq [1011]$	$\mathcal{O}(n!),\mathcal{O}(n^6)$	Enumerate permutations
$\leq [1518]$	$\mathcal{O}(2^n n^2)$	TSP with DP
$\leq [1822]$	$\mathcal{O}(2^n n)$	Bitmask DP
≤ 100	$\mathcal{O}(n^4)$	3D DP with $\mathcal{O}(n)$ loop
≤ 400	$\mathcal{O}(n^3)$	Floyd-Warshall
$\leq 2 \cdot 10^3$	$\mathcal{O}(n^2 \lg n)$	2 nested loops + tree query
$\leq 5 \cdot 10^4$	$\mathcal{O}(n^2)$	Bubble/Selection/Insertion Sort
$\leq 10^{5}$	$\mathcal{O}(n \lg^2 n) = \mathcal{O}((\lg n)(\lg n))$	Build suffix array
$\leq 10^{6}$	$\mathcal{O}(n \lg n)$	MergeSort, build SegTree
$\leq 10^{7}$	$\mathcal{O}(n \lg \lg n)$	Sieve, totient function
$\leq 10^{8}$	$\mathcal{O}(n),\mathcal{O}(\lg n),\mathcal{O}(1)$	Mathy solution often with IO bottleneck $(n \le 10^9)$

 10^8 ops/second

1 Theory

1.1 Relevant comparisons

lg 10 (1E1)	2.3
$\lg 100 \; (1E1)$	4.6
$\lg 1000 \; (1E2)$	6.9
$\lg 10000 \text{ (1E3)}$	9.2
$\lg 100000$ (1E4)	11.5
lg 1000000 (1E5)	13.8
lg 10000000 (1E6)	16.1
lg 100000000 (1E7)	18.4
$\lg 1000000000$ (1E8)	20.7
$\lg 10000000000$ (1E9)	23.0
$\lg 1000000000000$ (1E10)	25.3
lg 1000000000000 (1E11)	27.6
lg 10000000000000 (1E12)	29.9
2^{10}	$\approx 10^3$
2^{20}	$\approx 10^6$

Sign	Type	Bits	Max	Digits
±	char	8	127	2
+	unsigned char	8	255	2
\pm	short	16	32767	4
+	unsigned short	16	65535	4
\pm	int/long	32	$\approx 2 \cdot 10^9$	9
+	unsigned int/long	32	$\approx 4 \cdot 10^9$	9
\pm	long long	64	$\approx 9 \cdot 10^{18}$	18
+	unsigned long long	64	$\approx 18 \cdot 10^{18}$	19
\pm	int128	128	$\approx 17 \cdot 10^{37}$	38
+	unsignedint128	128	$\approx 3 \cdot 10^{38}$	38

1.2 Prime counting function - pi(x)

Asymptotic to $\frac{x}{\log x}$ by the prime number theorem.

1.3 Progressions

$$a_n = a_k + r(n - k)$$
$$a_n = a_k q^{(n-k)}$$

- r, q: Ratio
- k: Known term

Algorithm	Time	Space
ArticBridges	$\mathcal{O}(V+E)$	$\mathcal{O}(V+E)$
Bellman-Ford	$\mathcal{O}(VE)$	$\mathcal{O}(V+E)$
Dijksta	$\mathcal{O}((V+E)\log V)$	$\mathcal{O}(V^2)$
Edmond Karp	$\mathcal{O}(VE^2)$	$\mathcal{O}(V+E)$
Euler Tour	$\mathcal{O}(E^2)$	
Floyd Warshall	$\mathcal{O}(V^3 + E)$	$\mathcal{O}(V^2 + E)$
Graph Check	$\mathcal{O}(V+E)$	$\mathcal{O}(V+E)$
Kahn	$\mathcal{O}(VE)$	$\mathcal{O}(V+E)$
Kruskal	$\mathcal{O}(E \log V)$	$\mathcal{O}(V+E)$
LCA	$\mathcal{O}(N \log N)$	$\mathcal{O}(N \log N)$
MCBM	$\mathcal{O}(VE)$	
Prim	$\mathcal{O}(E \log V)$	$\mathcal{O}(V+E)$
Tarjan	$\mathcal{O}(V+E)$	$\mathcal{O}(V+E)$
Extended Euclid	$\mathcal{O}(\log \min(a,b))$	$\mathcal{O}(1)$
Floyd (cycle)	$\mathcal{O}(V)$	$\mathcal{O}(1)$
PrimeFac + OptTrialDiv	$\mathcal{O}(\pi(\sqrt{n}))$	$\mathcal{O}(n)$
Sieve of Eratosthenes	$\mathcal{O}(n\log\log n)$	$\mathcal{O}(n)$
Binary Search	$\mathcal{O}(\log N)$	
Coordinate Compression	$\mathcal{O}(N \log N)$	
KMP	$\mathcal{O}(N)$	
MUF	$\mathcal{O}(AM)$	$\mathcal{O}(N)$
Bottom-Up SegTree	$\mathcal{O}(\log N)$	$\mathcal{O}(N)$

X	10	10^{2}	10^{3}	10^{4}
$\pi(x)$	4	25	168	1 229
X	10^{5}	10^{6}	10^{7}	10^{8}
$\pi(x)$	9592	78498	664579	5761455

• n: Term you want

$$S_n = \frac{n(a_1 + a_n)}{2}$$
$$S_n = \frac{a_1(q^n - 1)}{q - 1}$$

1.4 Series Identities

$$\sum_{i=1}^{n} i^2 = \frac{n(n+1)(2n+1)}{6} \qquad \sum_{i=1}^{n} i^3 = \frac{n^2(n+1)^2}{4} = \left(\sum_{i=1}^{n} i\right)^2$$

$$g_k(n) = \sum_{i=1}^n i^k = \frac{1}{k+1} \left(n^{k+1} + \sum_{j=1}^k \binom{k+1}{j+1} (-1)^{j+1} g_{k-j}(n) \right)$$

$$\sum_{i=0}^{n} ic^{i} = \frac{nc^{n+2} - (n+1)c^{n+1} + c}{(c-1)^{2}}, \quad c \neq 1$$

$$\sum_{i=0}^{\infty} ic^{i} = \frac{c}{(1-c)^{2}}, \quad |c| < 1$$

$$l + (l+1) + \dots + r = \frac{(l+r) \cdot (r-l+1)}{2}$$

Binomial Identities

$$\binom{n}{k} = \frac{n}{k} \binom{n-1}{k-1}$$

$$\binom{n-1}{k} - \binom{n-1}{k-1} = \frac{n-2k}{k} \binom{n}{k}$$

$$\binom{n}{k} \binom{n-h}{k} = \binom{n}{k} \binom{n-k}{h}$$

$$\binom{n}{k} = \frac{n+1-k}{k} \binom{n}{k-1}$$

$$\sum_{k=0}^{n} k \binom{n}{k} = n2^{n-1}$$

$$\sum_{k=0}^{n} k^{2} \binom{n}{k} = (n+n^{2})2^{n-2}$$

$$\sum_{j=0}^{k} \binom{m}{j} \binom{n-m}{k-j} = \binom{n}{k}$$

$$\sum_{j=0}^{m} \binom{m}{j}^{2} = \binom{2m}{m}$$

$$\sum_{m=0}^{n} \binom{m}{j} \binom{n-m}{k-j} = \binom{n+1}{k+1}$$

$$\sum_{m=k}^{n} \binom{m}{k} = \binom{n+1}{k+1}$$

$$\sum_{k=0}^{n} \binom{n+r}{k} = \binom{n+m+1}{m}$$

$$\binom{n-k}{k} = \text{Fib}(n+1)$$

$$(x+y)^{n} = \sum_{k=0}^{n} \binom{n}{k} x^{n-k} y^{k}$$

$$(1+x)^{n} = \sum_{k=0}^{n} \binom{n}{k} x^{k}$$

$$2\sum_{k=0}^{n} \binom{n}{k} - \binom{n}{k} = \sum_{k=0}^{n} \binom{n}{k} x^{k}$$

$$2\sum_{k=0}^{n} \binom{n}{k} - \binom{n}{k} = \sum_{k=0}^{n} \binom{n}{k} x^{k}$$

Lucas' Theorem 1.6

$$\binom{n}{m} = \prod_{i=0}^k \binom{n_i}{m_i} \pmod{p}$$

For prime p, n_i and m_i are coefficients of the representations of n and m in base p.

Fermat Theorems

p is prime

$$a^{p} = a \pmod{p}$$

$$a^{p-1} = 1 \pmod{p}$$

$$(a+b)^{p} = a^{p} + b^{p} \pmod{p}$$

$$a^{-1} = a^{p-2} \pmod{p}$$

Modulo @ exponent

For coprime a, m:

$$a^n \equiv a^{n \bmod \varphi(m)} \pmod{m}$$

Generally, if $n \geq \log_2 m$, then

$$a^n \equiv a^{\varphi(m)+[n \mod \varphi(m)]} \pmod{m}$$

1.9 Heron's Formula

Area of a triangle $(s = \frac{a+b+c}{2})$

$$A = \sqrt{s(s-a)(s-b)(s-c)}$$

1.10 Some Primes

- $10^6 + 69$
- 1000000007

• $10^9 + 7$

1000000009

• $10^9 + 9$

- 1000000021
- $10^{18} 11$ • $10^{18} + 3$
- 1000000033

• $10^{18} - 11$

 $2^{61}-1$

- 1000696969
- $10^{18} + 3$
- 998244353
- 2305843009213693951 =
- 999999937
- $2^{61} 1$

1.11 Catalan Numbers

1, 1, 2, 5, 14, 42, 132, 429, 1430, 4862, 16796, 58786, 208012, 742900, 2674440, 9694845, 35357670, 129644790, 477638700, 1767263190, 6564120420, 24466267020, 91482563640, 343059613650, 1289904147324, 4861946401452, 18367353072152, 69533550916004, 263747951750360, 1002242216651368.

$$C_n = \frac{1}{n+1} {2n \choose n} = \frac{(2n)!}{(n+1)!n!} = \prod_{k=2}^n \frac{n+k}{k}, n \ge 0.$$

- The number of valid parenthesis strings with n paren-
- The number of complete binary trees with n+1 leaves
- How many times a n + 2-sided convex polygon can be cut in triangles conecting its vertices with straight lines

1.12Binomial

X is the number of successes in a sequence of n independent experiments. $P(X = k) = \binom{n}{k} p^k (1-p)^{n-k}$, and E[X] = npand Var(X) = np(1-p).

1.13 Trigonometry

$$\sin^2 \theta + \cos^2 \theta = 1$$
, $\sin = \frac{opo}{hip}$, $\cos = \frac{adj}{hip}$, $\tan = \frac{opo}{adj}$. $\sin \theta = x \rightarrow \arcsin x = \theta$.
 α degrees to x rd: $\alpha = \frac{180x}{\pi}$

1.14 Multiples of gcd

Multiples of gcd(A, B) that are $\in [0, A)$ Let A, B > 0, g = GCD(A, B), A = ag and B = bg. a integers $(0 \times B)\%A$, $(1 \times B)\%A$, $(2 \times B)\%A \dots ((a - B)\%A)$ 1) $\times B$ % A correspond to each multiple of q between 0 and A-1 (inclusive): note that they are all unique.

Mod value range

$$A < B \implies A\%B = A, A > B \implies A\%B < A/2$$

Expected Value 1.16

Avg value of event. For each event, add to the sum the probability of an event times the value of X in that event $\mathbb{E}(X) = \sum_{\omega \in \Omega} (P(\omega) \times X(\omega))$ Another way of looking at it: $\mathbb{E}(X) = \sum_{i=1}^{M} (i \times P(X=i))$

$$\mathbb{E}(X) = \sum_{i=1}^{M} (i \times P(X=i))$$

Since in the expanded version of this sum P(X = i) will appear i times, you're also calculating for each i the probability that $X \geq i$ (P(x = M) will appear M times, once for each i; P(x = 1) will appear exactly once, for i = 1; and so

$$\mathbb{E}(X) = \sum_{i=1}^{M} (i \times P(X=i)) = \sum_{i=1}^{M} P(X \ge i)$$

1.17Combination

A combination ${}_{n}C_{k} = \binom{n}{k}$ (n chooses k) refers to selecting k objects from a collection of n where the order of choice doesn't matter.

Without repetition: can't choose an element twice.

 $\binom{n}{k} = \frac{n!}{r!(n-k)!}$ With repetition: elements may be chosen more than once. $\binom{n}{k} = \frac{(k+n-1)!}{k!(n-1)!}$

1.18 Permutation

A permutation ${}_{n}P_{k}$ refers to selecting k objects from a collection of n where the order of choice matters.

With repetition: elements may be chosen more than once. ${}_{n}P_{k}=n^{k}$

Without repetition: can't choose an element twice. $_{n}P_{k} = \frac{n!}{(n-k)!}$

2 **Emergency**

Pre-submit

Write a few simple test cases if sample is not enough.

Are time limits close? If so, generate max cases.

Is the memory usage fine?

Could anything overflow?

Make sure to submit the right file (check the filename you're editing).

Wrong answer

Print your solution and debug output!

Are you clearing all data structures between test cases?

Can your algorithm handle the whole range of input?

Read the full problem statement again.

Do you handle all corner cases correctly?

Have you understood the problem correctly?

Any uninitialized variables?

Any overflows?

Confusing N and M, i and j, etc.?

Are you sure your algorithm works?

What special cases have you not thought of?

Are you sure the STL functions you use work as you think?

Add some assertions, maybe resubmit.

Create some testcases to run your algorithm on.

Go through the algorithm for a simple case.

Go through this list again.

Explain your algorithm to a teammate.

Ask the teammate to look at your code.

Go for a small walk, e.g. to the toilet.

Is your output format correct? (including whitespace)

Rewrite your solution from the start or let a teammate do it.

Runtime error

Have you tested all corner cases locally?

Any uninitialized variables?

Are you reading or writing outside the range of any vector?

Any assertions that might fail?

Any possible division by 0? (mod 0 for example)

Any possible infinite recursion?

Invalidated pointers or iterators?

Are you using too much memory?

Debug with resubmits (e.g. remapped signals, see Various).

Time limit exceeded

Do you have any possible infinite loops?

What is the complexity of your algorithm?

Are you copying a lot of unnecessary data? (use references)

How big is the input and output? (consider scanf and printf)

Avoid vector, map. (use array/unordered_map)

What do your teammates think about your algorithm?

Memory limit exceeded

What is the max amount of memory your algorithm should

Are you clearing all data structures between test cases?

Geometry

3.1 Points

```
1 using pt = complex<double>;
2 #define px real()
3 #define py imag()
5 double dot(pt a, pt b) { return (conj(a)*b).px; }
6 double cross(pt a, pt b) { return (conj(a)*b).py; }
7 pt vec(pt a, pt b) { return b-a; }
8 int sgn(double \nu) { return (\nu > -EPS) - (\nu < EPS); }
9 int seg_ornt(pt a, pt b, pt c) {
   return sgn(cross(vec(a, b), vec(a, c)));
10
11 }
12 int ccw(pt a, pt b, pt c, bool col) {
   int o = seg_ornt(a, b, c);
13
   return (o == 1) || (o == 0 && col);
15 }
16 const double PI = acos(-1);
17 double angle(pt a, pt b, pt c) {
18
    return abs(remainder(arg(a-b) - arg(c-b), 2.0*PI));
```

3.2 Convex Hull (Monotone)

```
\mathcal{O}(n \log n), and is vector of point indexes
```

```
1 using pti = pair<pt, int>;
 2 #define fi first
 3 #define se second
 4 vi convex_hull(vector<pti>& ps, bool col = false) {
    int k = 0, n = ps.size(); vi ans (2*n);
 6
     sort(all(ps), [](pti a, pti b) {
      return make_pair(a.fi.px, a.fi.py) < make_pair(b.fi.px,</pre>
 7
           b.fi.py);
 8
     for (int i = 0; i < n; i++) {</pre>
 9
      while (k >= 2 && !ccw( /* lower hull */
10
          ps[ans[k-2]].fi, ps[ans[k-1]].fi, ps[i].fi, col)) {
11
               k--; }
12
       ans[k++] = i;
13
     if (k == n) {
14
15
      ans.resize(n);
16
      for (auto &i : ans) i = ps[i].second;
17
      return ans; }
     for (int i = n-2, t = k+1; i >= 0; i--) {
      while (k >= t && !ccw( /* upper hull */
19
20
          ps[ans[k-2]].fi, ps[ans[k-1]].fi, ps[i].fi, col)) {
               k--; }
      ans[k++] = i;
21
22
23
     ans.resize(k-1);
     for (auto &i : ans) i = ps[i].second;
24
25
     return ans;
26 }
```

Graph

Prim MST 4.1

Time Space
$\mathcal{O}(E \log V) \mathcal{O}(V + E)$
1 vi par(N, -1);
2 vector <ll> d(N, oo);</ll>
<pre>3 vector<vector<wv>>> mst(N);</vector<wv></pre>
4
5 ll prim(int s) {
6 ll sum = 0;
<pre>7 priority_queue<wv, vector<wv="">, greater<wv>>> Q;</wv></wv,></pre>
8 auto add = [&](int v, ll x, int p) {
9 if $(x < d[v])$ {
10 Q.emplace($d[v]=x, v$);
11 par[v] = u;
12 }};
13 add(s, 0, s);
14 while (Q.size()) {
15
<pre>16 if (vis[u]) continue;</pre>
<pre>17 vis[u] = true;</pre>
18 if (par[u] != -1) {
19
<pre>20 mst[v].emplace_back(w, u);</pre>
<pre>21 mst[u].emplace_back(w, ν);</pre>
22 }
23 sum += w ;
24 for (auto [c, u] : g[v])
25 if (!vis[u])
26 add(u, c, v);
27 }
28 return sum;
29 }

4.2 Dijkstra SSSP

Time	Space
$\mathcal{O}((V+E)\log V)$	$\mathcal{O}(V^2)$

```
1 vi d(MAXN, oo);
3 void dijkstra(int s) {
    priority_queue<wv, vector<wv>, greater<wv>>> pq;
    pq.emplace(d[s] = 0, s);
    add(s, 0);
    while (!pq.empty()) {
      auto [w, v] = pq.top(); pq.pop();
8
9
      if (w > dist[v]) continue;
      for (auto [x, u] : g[v])
10
        if (w+x < d[u])
11
12
          pq.emplace(d[u]=w+x, u);
13
    }
14 }
```

4.3 Graph Check

```
Time/Space
                  Usage
 \mathcal{O}(V+E)
                  graphCheck(firstVertex, -1)
 1 int UNVISITED = -1, EXPLORED = 0, VISITED = 1;
 2 vector<vi> adj(M);
 3 vi tin;
 5 void graphCheck(int v, int p) { //vertex, parent
    tin[v] = EXPLORED;
    for (auto u: adj[v]) {
      if (tin[u] == UNVISITED) { //tree edge
9
        graphCheck(u, v);
      } else if (tin[u] == EXPLORED) {
10
11
        if (u == p)
12
          ; //two way edge u <-> v
13
        else
14
          ; //back edge v -> u
15
      } else if (tin[u] == VISITED) {
16
        ; //forward/cross edge u-v
17
18
    }
19
    tin[v] = VISITED;
```

Articulations and Bridges

```
Time/Space
                   Usage
 \mathcal{O}(V+E)
                   dfs(src, -1)
 2 int tk = 0;
 3 vi tin(M, -1);
 4 vector<vi> adj(M);
6 void dfs(int ν, int p) {
     tin[v] = low[v] = tk++;
     int children = 0;
9
     for (auto u: adj[v]) {
10
      if (u == p) continue;
      else if (tin[u] == -1) {
11
12
        ++children;
13
        dfs(u, v);
        if (low[u] >= tin[v] && p != v)
14
15
          ; //articulation point
16
        if (low[u] > tin[v])
          ; //bridge u-v
17
        low[v] = min(low[v], low[u]);
19
      } else {
20
        low[v] = min(low[v], tin[u]);
22
    }
23 }
```

4.5 **Euler Tour**

Time	Usage	
$\mathcal{O}(E^2)$	tour(cyc.begin(),	start_vertex)

```
1 list<int> cyc;
 2 vector<vi> adj(M);
 3 vector<vector<bool>> traversed(M, vector<bool>(M, false));
5 //euler tour (list for fast insertion)
6 void tour(list<int>::iterator i, int ν) {
    for (auto u: adj[v]) {
      if (!traversed[v][u]) {
8
9
        traversed[v][u] = true;
10
        for (auto t: adj[u])
          if (t == v \&\& !traversed[u][t]) {
11
12
            traversed[u][t] = true;
13
            break:
14
15
        tour(cyc.insert(i, v), u);
16
17
    }
18 }
```

4.6 FFEK MaxFlow

Space

O(V+E)

Time

39 }

41 void mincut(int s, int t) {

while (!st.empty()) {

visited[v] = true;

st.push(u);

else

for (auto u: adj[v])

vector<bool> visited(n, false);

int v = st.top(); st.pop();

if (visited[v]) continue;

if (capacity[v][u] > 0)

st.push(s); // changed from 0 to s

maxflow(s, t);

stack<int> st;

vector<ii> ans;

40

42

43

44

45

46

47

48

49

50

51

52

53

54

 $\mathcal{O}(VE^2)$

1	
2	<pre>vector<vi> capacity(M, vi(M, 0)), adj(M);</vi></pre>
3	<pre>vector<ii> mc; //mincut edges</ii></pre>
4	
5	
6	fill(all(par), -1);
7	par[s] = -2;
8	queue <ii> q; q.push({s, inf});</ii>
9	
10	<pre>int v = q.front().first,</pre>
11	flow = q.front().second;
12	q.pop();
13	<pre>for (auto u: adj[v])</pre>
14	if (par[u] == -1 && capacity[v][u]) {
15	par[u] = ν;
16	<pre>int new_flow = min(flow, capacity[v][u]);</pre>
17	· · · · · · · · · · · · · · · · · · ·
18	q.push({u, new_flow});
19	}
20	}
21	return 0;
22	}
23	
24	<pre>int maxflow(int s, int t) {</pre>
25	<pre>int flow = 0;</pre>
26	vi par(M);
27	-
28	
വ	** = * * * * * * * * * * * * * * * * *
29	flow += new_flow;
30	flow += new_flow; int v = t;
30 31	flow += new_flow; int v = t; while (v != s) {
30 31 32	<pre>flow += new_flow; int v = t; while (v != s) { int p = par[v];</pre>
30 31 32 33	<pre>flow += new_flow; int v = t; while (v != s) { int p = par[v]; capacity[p][v] -= new_flow;</pre>
30 31 32 33 34	<pre>flow += new_flow; int v = t; while (v != s) { int p = par[v]; capacity[p][v] -= new_flow; capacity[v][p] += new_flow;</pre>
30 31 32 33 34 35	<pre>flow += new_flow; int v = t; while (v != s) { int p = par[v]; capacity[p][v] -= new_flow; capacity[v][p] += new_flow; v = p;</pre>
30 31 32 33 34 35 36	<pre>flow += new_flow; int v = t; while (v != s) { int p = par[v]; capacity[p][v] -= new_flow; capacity[v][p] += new_flow; v = p; }</pre>
30 31 32 33 34 35	<pre>flow += new_flow; int v = t; while (v != s) { int p = par[v]; capacity[p][v] -= new_flow; capacity[v][p] += new_flow; v = p;</pre>

```
55          ans.push_back({v, u});
56    }
57    mc.clear();
58    for (auto &[v, u] : ans)
59         if (!visited[u])
60         mc.push_back({v, u});
61 }
```

4.7 Heavy-Light Decomposition

```
Update
 Query
              Setup
 \mathcal{O}(\log^2 n)
              define oper(a,b) for query
                                              rmq.upd(pos[x],v)
Queries on edges: assign values of edges to child node, then
change pos[x] to pos[x]+1 in query (see !!!)
 1 vi g[MAXN];
 2 int wg[MAXN],par[MAXN],h[MAXN]; // subtree
        size, father, height
 3 void dfs1(int x){
     wg[x]=1;
     for(int y:g[x])if(y!=par[x]){
       par[y]=x;h[y]=h[x]+1;dfs1(y);
 7
       wg[x]+=wg[y];
 8
    }
 9 }
10 int curpos,pos[MAXN],head[MAXN]; // head = representante
11 void hld(int x, int c){
    if(c<0)c=x;
12
13
     pos[x]=curpos++;head[x]=c;
     int mx=-1;
     for(int y:g[x])if(y!=par[x]&&(mx<0||wg[mx]<wg[y]))mx=y;</pre>
15
     if(mx>=0)hld(mx,c);
16
17
     for(int y:g[x])if(y!=mx&&y!=par[x])hld(y,-1);
18 }
19 void
        hld_init(){par[0]=-1;h[0]=0;dfs1(0);curpos=0;hld(0,-1);}
20 int query(int x, int y, stree% rmq){
21
     int r=NEUT;
     while(head[x]!=head[y]){
23
       if(h[head[x]]>h[head[y]])swap(x,y);
24
       r=oper(r,rmq.query(pos[head[y]],pos[y]+1));
25
       y=par[head[y]];
26
     }
27
     if(h[x]>h[y])swap(x,y); // now x is lca
    r=oper(r,rmq.query(pos[x],pos[y]+1)); // !!!
29
     return r;
30 }
```

4.8 Kahn's topological sort

```
Time
            Space
 \mathcal{O}(VE)
            \mathcal{O}(V+E)
2 vector<vi> adj(M);
3 vi sorted;
5 void kahn(int n) {
    vi indeg(n, 0);
    vector<bool> valid(n, true);
    priority_queue<int> pq;
10
    for (int v = 0; v < n; ++v)
11
      for (auto u: adj[v])
        indeg[u]++;
12
13
    for (int v = 0; v < n; ++v)
14
      if (!indeg[v]) pq.push(v);
15
16
    while (!pq.empty()) {
17
       int v = pq.top(); pq.pop();
18
       sorted.push_back(v);
19
       valid[v] = false;
20
       for (auto u: adj[v])
21
        if (valid[u] && !(--indeg[u]))
22
          pq.push(u);
```

```
23 }
24 }
```

4.9 MCBM (Kunh Matching)

```
\mathcal{O}(VE) time
   Max Cardinality Bipartite Matching
   g: arcos do lado esquerdo pro lado direito do grafo
 1 vi mat:
 2 vector<bool> vis;
 3
 4 bool match(int ν) {
     if (vis[v]) return false;
     vis[v] = true;
     for (int u: g[v])
       if (mat[u] < 0 || match(mat[u])) {</pre>
        mat[u] = v;
 9
10
         return true;
11
12
     return false;
13 }
14
15 \text{ mat.assign(n, -1);}
16 int mcbm = 0; // num matched vertices
17 for (int i = 0; i < n; ++i) {
    vis.assign(n, false);
19
    mcbm += try_kuhn(i);
20 }
21 // match: mat[i] -> i (i é do lado direito)
```

4.10 LCA - Binary lifting

```
\mathcal{O}(n \log n) time \mathcal{O}(n \log n) space
1 int L = //log2(n)
3 void dfs(int v, int p) { // uso: dfs(raiz, raiz)
4
    up[v][0] = p;
    for (int l = 1; l <= L; ++l)
6
      up[v][l] = up[up[v][l-1]][l-1];
    for (int u : g[v])
      if (u != p) dfs(u, v);
9 }
10
11 int lca(int a, int b) {
    if (dep[b] >= dep[a]) { swap(a, b); }
12
    int diff = dep[a] - dep[b];
    for (int l = L; l >= 0; l--) if (diff & (1 << l))
14
15
      a = up[a][l];
    if (a == b) { return a; }
    for (int l = L; l >= 0; l--) if (up[a][l] != up[b][l])
17
      a = up[a][l], b = up[b][l];
     return up[a][0];
19
20 }
```

4.11 Tarjan Strongly Connected Component

	, -	_	
\mathcal{C}	O(V+E)	Tarjan(n,	adj)
1			
	vi tin(M, -1),	low(M, -1);	
3	vector <bool> vi</bool>	Ls(M);	
4	vector <vi> adj(</vi>	(M);	
5	stack <int> S;</int>		
	int tk = 0;		
7			
8	void dfs(int v)) {	
9	low[v] = tin[[v] = tk++;	
10	, , , ,		
11		•	
	for (auto u:	•	
13	<pre>if (tin[u]</pre>	== -1)	
14	dfs(u);		

Usage

Time/Space

```
15    if (vis[u])
16     low[v] = min(low[v], low[u]);
17    }
18    if (low[v] == tin[v])
19    while (true) {
20      int u = S.top(); S.pop(); vis[u] = false;
21     if (u == v) break;
22    }
23 }
```

4.12 LCA - Euler Path

```
\mathcal{O}(n \log n) time
                     \mathcal{O}(n) space
 1 vi idx(n):
 2 int tk = 1;
 4 void dfs(int ν, int d) { // call with dfs(root, 0);
     for (auto u : adj[v]) {
       st.update(tk, {d, v});
       tk++;
 8
       dfs(u, d+1);
     }
 9
10
     idx[v] = tk;
11
     st.update(tk, {d, v});
12
     tk++;
13 }
14
15 int lca(int ν, int u) {
16 int l = idx[v], r = idx[u];
    return st.minquery(l, r).second; // .first is depth
17
18 }
```

4.13 Kosaraju SCC

```
Time/Space
                  Usage
 \mathcal{O}(V+E)
                  kosaraju()
   rep: representante do componente de cada vtx
   scc: 2a dfs, processa os vtx do componente c
 1 vi S, rep(MAXN);
 3 void dfs(int v) {
 4
    vis[v] = true;
    for (int u: g[v])
      if (!vis[u]) dfs(u);
 7
    S.push_back(v);
 8 }
10 void scc(int v, int c) {
11
    vis[v] = true;
    rep[v] = c;
12
    for (int u: gi[v])
14
      if (!vis[u]) scc(u, c);
15 }
16
17 void kosaraju() {
    for (int i = 0; i < n; ++i)</pre>
18
      if (!vis[i]) dfs(i);
19
20
    vis.assign(n, false);
21
     reverse(all(S));
    for (int v: order)
23
      if (!vis[v]) scc(v, v);
```

4.14 Bellman-Ford SSSP

${f Time}$	Space
$\mathcal{O}(VE)$	$\mathcal{O}(V+E)$
1	

```
5 void bellmanFord(int n) {
    for (int i = 0; i < n-1; ++i)</pre>
      for (int v = 0; v < n; ++v)
        for (auto &[u, w]: adj[v])
9
          if (dist[v] != inf)
            dist[u] = min(dist[u], dist[v]+w);
10
11 }
12
13 //check if there are negative cycles
14 bool cycle(int n) {
   bool ans = false;
15
    for (int v = 0; v < n; ++v)
16
      for (auto &[u, w]: ν)
17
        ans |= dist[v] != inf && dist[u] > dist[v]+\omega;
18
19 }
```

4.15 Kruskal MST

Space

Time

$\mathcal{O}(E \log V) \mathcal{O}(V + E)$
1 using edge = tuple <ll, int="" int,="">; // peso, u, v</ll,>
<pre>2 vector<edge> edges;</edge></pre>
3 UnionFind muf;
4
<pre>5 pair<ll, vector<edge="">> kruskal(int n) { // n = #vertices</ll,></pre>
<pre>6 vector<edge> mst;</edge></pre>
<pre>7 ll cost = 0; sort(all(edges));</pre>
8 for (auto [w, u, v] : edges)
9 if (!muf.isSameSet(u, v)) {
<pre>10 mst.emplace_back(w, u, v);</pre>
11 cost += w;
<pre>12 muf.unionSet(u, v);</pre>
13 }
<pre>14 return {cost, mst};</pre>
15 }

4.16 Floyd Warshall APSP

Time	Space	\cup sage		
$\mathcal{O}(V^3+E)$	$\mathcal{O}(V^2 + E)$	FloydWarshall(n,	edges)	
1 vector <vi> w(MAXN, vi(MAXN, oo));</vi>				
<pre>2 void fw(int</pre>	<pre>2 void fw(int n) {</pre>			
<pre>3 for (int m = 0; m < n; ++m)</pre>				
4 for (int u = 0; u < n; ++u)				
5 for (int $v = 0$; $v < n$; ++ v)				
6 if (max(w[u][m], w[m][v]) < oo)				
7 w[i	u][v] = min(w[u	i][ν], w[u][m]+w[m][ν]));	
8 }			•	

5 Math

Time

5.1 Sieve of Eratosthenes

$\mathcal{O}(n\log\log n)$ $\mathcal{O}(n)$
1
<pre>2 bitset<11234567> pr;</pre>
3 vi factors(M, 0);
4 vi primes;
5
<pre>6 void sieve(int n) {</pre>
<pre>7 pr.set();</pre>
8
9
<pre>10 primes.push_back(i);</pre>
11 for (int p = i*i; p <= n; p += i) {
12 pr[p] = false ;
<pre>factors[p]++;</pre>
14 }
15 }

Space

```
16 }
17
18 // O(1) for small n, O(sieve_size) else
19 bool isPrime(int n) {
20   int sieve_size = 11234567;
21   if (n <= sieve_size) return pr[n];
22   for (auto p: primes) // only works if n <= primes.back()^2
23   if (!(n%p)) return false;
24   return true;
25 }</pre>
```

5.2 Prime Factors w/ Optimized Trial Divisions

Time

Space

```
\overline{\mathcal{O}(\pi(\sqrt{n}))}
                 \mathcal{O}(n)
 2 vi primes;
 3 vector<ii> factors;
 5 void pf(int n) {
     for (auto p: primes) {
       if (p*p > n) break;
 8
       int i = 0;
       while (!(n%p)) {
         n /= p;
10
11
         i++;
12
13
      factors.push_back({p, i});
15
     if (n != 1) factors.push_back({n, 1});
16 }
```

5.3 Extended Euclid for Linear Diophantines

```
Time
                     Usage for a,b
 \mathcal{O}(\log \min(a, b))
                     int x, y; gcd(a, b, x, y);
 1 int gcd(int a, int b, int& x, int& y) {
    if (!b) {
3
      x = 1;
      y = 0;
4
      return a;
6
    }
     int x1, y1;
    int d = gcd(b, a % b, x1, y1);
    x = y1;

y = x1 - y1 * (a / b);
10
11
    return d;
12 }
```

5.4 Floyd's algorithm cycle-finding

```
\mathcal{O}(V) time
 1 int findCycle(int x) {
    int a, b;
     a = succ(x);
    b = succ(succ(x));
     while (a != b) {
      a = succ(a);
 6
 7
       b = succ(succ(b));
 8
    }
 9
     a = x;
10
    while (a != b) {
      a = succ(a);
11
12
      b = succ(b);
13
     int first = a; // first element in cycle
14
15
     b = succ(a);
16
    int length = 1;
     while (a != b) {
17
18
      b = succ(b);
```

```
\begin{array}{ccc} 19 & & \texttt{length++;} \\ 20 & \texttt{;} \\ 21 & \texttt{;} \end{array}
```

6 Paradigm

6.1 Coordinate Compression

Normalize vector access; can also be done with map/set but high constant. $\mathcal{O}(n \log n)$ time

```
1 vi v, vals, cv; // all same size, cv = compressed v
2 vals = v;
3 sort(all(vals));
4 vals.erase(unique(all(vals)), vals.end());
5 for (int i = 0; i < n; ++i)
6 cv[i] = lower_bound(all(vals), v[i]) - vals.begin();</pre>
```

6.2 128 Bit Integers

```
1 // cout, cerr, etc; may over/underflow
 2 ostream& operator<<(ostream& out, __int128 x) {</pre>
 3
       if (x == 0) return out << 0;</pre>
       string s; bool sig = x < 0; x = x < 0? -x : x; while (x > 0) s += x % 10 + '0', x /= 10;
 5
       if (sig) s += '-';
 6
 7
       reverse(all(s));
 8
       return out << s;
 9 }
10 // cin, etc; may over/underflow
11 istream& operator>>(istream& in, __int128& x) {
12
       char c, neg = 0; while(isspace(c = in.get()));
       if(!isdigit(c)) neg = (c == '-'), x = 0;
13
14
       else x = c - '0';
15
       while(isdigit(c = in.get())) x = (x << 3) + (x << 1) -
            '0' + c;
       x = neg ? -x : x; return in;
17 }
```

6.3 Prefix AND

 $\mathcal{O}(\log N)$ bitwise and on array, $\mathcal{O}(N \log N)$ build

```
1 vector<vi> ps(n, vi(32));
 2 const int L = 32; // teto(log2(max(v[i])))
 3
 4 void build(vi &v) {
     int n = v.size();
     for (int i = 0; i < n; ++i) // build</pre>
 6
       for (int b = 0; b < L; ++b) {
        if (i > 0) ps[i][b] = ps[i-1][b];
        if (v[i] & (1ll << b)) ps[i][b]++;</pre>
 9
       }
10
11 }
12
13 int qry(int l, int r) {
    int num = 0;
14
15
     for (int b = 0; b < L; ++b)
       // ligado em todos
16
       if (ps[r][b] - (l ? ps[l-1][b] : 0) == r-l+1)
17
18
        num |= (1ll << b);
19
     return num;
20 }
```

6.4 Binary Search

```
1 // std
2 int l = 0, r = n-1;
3 while (l <= r) {
4   int m = l+(r-l)/2;
5   if (array[m] == x) // found
6   if (array[m] > x) r = m-1;
7   else l = m+1;
8 }
```

```
9 // nice - binary steps
10 int k = 0;
11 for (int b = n/2; b > 0; b /= 2)
12 while (k+b < n && array[k+b] <= x)
13     k += b;
14 if (array[k] == x) // found</pre>
```

7 String

7.1 Rolling hash (linear)

```
\mathcal{O}(n) time
Let h_{i..j} = \text{hash}(s_{i..j}).
```

 $h_{i...j} \times p^i = h_{0...j} - h_{0...i-1}$. Instead of finding the multiplicative inverse of p^i , you can multiply this term by p^{n-i} (so every hash is compared multiplied by p^n).

```
1 ll hash(string const& s) {
    const int p = 31; // ~alphabet size (31 for lowercase, 53
         for uppercase)
3
    const int M = 1e9 + 9;
4
    ll h = 0;
    ll p_pow = 1; // precompute for performance
5
    for (char c : s) {
     h = (h + (c - 'a' + 1)*p_pow) % M;
      p_{pow} = (p_{pow} * p) % M;
    }
9
10
    return h;
11 }
```

7.2 Prefix Function (KMP)

 $\mathcal{O}(n)$ time

To find ocurrences of s in t, use the string s+%+t, then look for pi[i] = s.length() on the "t side"

```
1 vi prefix(string s) {
     int n = s.length();
 3
     vi pi(n, 0); // can be optimized if you know max prefix
          length
     for (int i = 1; i < n; ++i) {
      int j = pi[i-1];
5
 6
      while (j > 0 \&\& s[i] != s[j])
 7
        j = pi[j-1];
      if (s[i] == s[j])
 8
9
         j++;
      pi[i] = j;
10
11
    }
12
     return pi;
13 }
```

7.3 Suffix Array

Build	Query
$\mathcal{O}(n \log n)$	$\mathcal{O}(\log n)$

To find whether p is a substring of s (and where this ocurrence starts), you can build the suffix array A of s. Since A is sorted, you can binary search for p as a prefix of all suffixes of s. Complexity (besides construction): $\mathcal{O}(|p|\log(|s|))$.

```
1 //  sort p by the values in c (stable) (O(|alphabet| + n))
 2 void count_sort(vi &p, vi &c) {
    int n = p.size();
     int alphabet = 256; // ascii range
     vi cnt(max(alphabet, n));
     for (auto x : c)
6
      cnt[x]++;
8
     vi pos(max(alphabet, n));
9
10
     pos[0] = 0;
11
     for (int i = 1; i < max(alphabet, n); ++i)</pre>
12
      pos[i] = pos[i-1] + cnt[i-1];
13
```

```
14 vi p_sorted(n);
15
     for (auto x : p) {
16
      p_sorted[pos[c[x]]++] = x;
17
18
19
     p = p_sorted;
20 }
21
22 // build suffix array
23 vi suffix_array(string s) {
    s += "$";
25
     int n = s.size();
    // at k = 2^0, sort strings of length 1
     vi p(n), c(n); // suffix start position, equivalence class
27
     for (int i = 0; i < n; ++i) {</pre>
29
      p[i] = i;
30
      c[i] = s[i];
31
     // at first c is just a hack to sort p, it's not really
32
          equiv. class
     count_sort(p, c);
// but then it is
33
34
     c[p[0]] = 0;
     for (int i = 1; i < n; ++i) {</pre>
36
37
       c[p[i]] = c[p[i-1]];
       if (s[p[i]] != s[p[i-1]])
38
39
         c[p[i]]++;
40
41
     int k = 1;
42
     while (k < n) {
       // transition from k to k+1
43
       for (int i = 0; i < n; ++i)</pre>
44
        p[i] = (p[i] - k + n) % n;
45
46
       count_sort(p, c);
       // recalculate equiv.
47
48
       vi c_upd(n);
       c_upd[p[0]] = 0;
for (int i = 1; i < n; ++i) {</pre>
49
50
         ii prev = \{c[p[i-1]], c[(p[i-1] + k)%n]\};
         ii curr = \{c[p[i]], c[(p[i] + k)%n]\};
52
         c_{upd}[p[i]] = c_{upd}[p[i-1]];
53
         if (curr != prev)
54
           c_upd[p[i]]++;
55
56
57
       c = c_upd;
58
       k <<= 1;
59
     }
60
     return p;
61 }
```

8 Structure

Time

8.1 Merge/Disjoint Union-Find

Space

$\mathcal{O}(A imes n)$ $\mathcal{O}(n)$ muf(n)
1 struct MUF {
2 int N;
3 vi par, rk, count;
4
<pre>5 MUF(int N) : N(N), par(N), rk(N, 0), count(N, 1) {</pre>
6 rep(i,0,N)
7
8 }
9
10 int find(int i) {
11
12 }
13
14 int merge(int a, int b) {
15
16 if (x != y)
17 count[x] = count[y] = (count[x]+count[y]);
18 if (rk[x] < rk[y])
19 $par[x] = y;$

Usage

```
20
      else {
21
        par[y] = x;
22
         if (rk[x] == rk[y])
23
          rk[x]++;
24
25
      return count[x];
26
27
28
     bool same(int i, int j) {
     return find(i) == find(j);
30
31 };
```

Build Ouery

8.2 Bottom-Up Segment Tree

Bulla	Query	Opdate	\cup sage		
$\mathcal{O}(n)$	$\mathcal{O}(\log n)$	$\mathcal{O}(\log n)$	seg(n)		
Uses 1	less space t	han top-dov	vn 4n seg	tree $(2n)$	here)
1 struct	seg {				
2 int 1	n;				
3 vit	;				
4					
5 seg(νi ν) : n(ν.	size()), t(2	*n) {		
6 for	r (int $i = 0$; i < n; ++i)		
7 u	upd(i, v[i])	;			
8 }	,	,			
9 seg(int sz) : n(sz), t(2*n)	{}		
10					
11 int (query(<mark>int</mark> a,	<pre>int b) {</pre>			
12 int	ans = 0;				
13 for	r (a += n, b	+= n; a <=	b; ++a /= 2	2,b /=	2) {
14 i	f (a%2 == 1) ans += t[a]];		
15 i	f (b%2 == 0)) ans += t[b]];		
16 }					
17 ret	turn ans;				
18 }					
19					
20 void	upd(int p,	<pre>int x) {</pre>			
	p += n] = x;				
22 whi	ile (p /= 2)	t[p] = t[p<	<1] + t[(p-	<<1)+1];	
23 }					
24 };					

Undate Usage

8.3 Segment Tree

Build	Query	Modify	Usage
$\mathcal{O}(n\log n)$	$\mathcal{O}(\log n)$	$\mathcal{O}(\log n)$	stree(n)

```
1 struct stree {
     int n;
3
     vi st, v;
     stree(vi v): n(v.size()), st(4*n), v(v) {
5
      build(1, 0, n-1); }
6
7
8
     int left(int i) { return i<<1; }</pre>
9
     int right(int i) { return (i<<1)+1; }</pre>
10
11
12
     void build(int p, int pl, int pr) {
      if (pl == pr) {
13
14
        st[p] = v[pl];
15
        return;
16
17
       int m = (pl+pr)/2;
       build(left(p), pl, m);
18
19
       build(right(p), m+1, pr);
20
       st[p] = min(st[left(p)], st[right(p)]);
21
22
23
     int query(int p, int pl, int pr, int ql, int qr) {
24
       \ensuremath{//} same params as update, except [ql..qr] is the query
            range
       if (qr < pl || ql > pr) return inf;
```

```
26
       if (ql <= pl && pr <= qr) return st[p];</pre>
                                                                        4 int main(int argc, char *argv[]) {
27
       int m = (pl+pr)/2;
                                                                        5
28
       int query_left = query(left(p), pl, m, ql, qr);
                                                                        6
                                                                            if (argc < 2) {
29
       int query_right = query(right(p), m+1, pr, ql, qr);
30
       return min(query_left, query_right);
                                                                        8
                                                                              exit(1);
                                                                           }
31
                                                                        9
32
                                                                          srand(atoi(argv[1]));
     int query(int ql, int qr) { return query(1, 0, n-1, ql,
33
                                                                       11
                                                                       12 }
34
                                                                            Makefile
     void update(int p, int pl, int pr, int i, int x) {
                                                                      9.5
35
       // p = st idx, corresponds to range [pl..pr]
if (i < pl || i > pr) return;
36
37
                                                                        1 # p3: pypy3 -m py_compile
       if (pl == pr) {
38
                                                                        2 \text{ CXX} = g++
39
         st[p] = x;
40
         return;
41
       }
42
       int m = (pl+pr)/2;
       update(left(p), pl, m, i, x);
43
       update(right(p), m+1, pr, i, x);
44
                                                                      9.6 C++ Template
45
       st[p] = min(st[left(p)], st[right(p)]);
46
                                                                        1 #include <bits/stdc++.h>
                                                                        2 using namespace std;
48
     void update(int i, int x) { update(1, 0, n-1, i, x); }
                                                                        3 #define fi first
49 };
                                                                        4 #define se second
9
     Extra
                                                                        7 #define endl '\n'
                                                                        8 #define int long long
                                                                        9 using vi = vector<int>;
9.1 C++ structs
                                                                       10 using ll = long long;
                                                                       11 using ii = pair<int, int>;
12 using wv = pair<ll, int>;
 1 struct st {
 2 via;
                                                                       13
     vector<bool> b = vector<bool>(5); // default value
 3
                                                                       14 // PBDS ----
 4
     st(int _i) : a(_i), i(_i) {};
                                                                       16 using namespace __gnu_pbds;
     bool operator< (st& e) const { return i < e.i; }</pre>
 7 };
                                                                       19 // ---
 8
                                                                       20
 9 \text{ st e} = \text{st(3)}; \text{ st f(3)};
```

```
10
11 struct matrix {
12 vector<vi> m;
     matrix(int n) m(n, vi(n)) {};
matrix operator * (const matrix &b) {
13
14
       matrix c = matrix();
15
       for (int i = 0; i < m.size(); ++i)</pre>
16
         for (int j = 0; j < m.size(); ++j)</pre>
17
            for (int k = 0; k < m.size(); ++k)</pre>
             c.m[i][j] = c.m[i][j] + 1LL*m[i][k]*b.m[k][j];
19
20
       return c;
21
22 };.
```

9.2 cmp

```
1 // upper bound: 1st > x, lower bound: 1st >= x
2 // last <= x: up-1, first >= x: lo
3 priority_queue<int, vector<int>, greater<int>> pq;
4 struct {
5
   bool operator()(const int& a, const int& b) const {
6
      return a < b;
    }
8 } cmp;
9 priority_queue<int, vector<int>, cmp> pq2;
10 sort(all(v), cmp);
```

9.3 Vim

1 set et ts=2 sw=2 ai si cindent sta is tm=50 nu noeb sm "cul 2 sy on

9.4 Generator

```
1 #include <bits/stdc++.h>
2 using namespace std;
3
```

```
cin.tie(0); ios_base::sync_with_stdio(0);
  cout << "usage: " << argv[0] << " <seed>\n";
// use rand() for random value
```

```
3 CXXFLAGS = -Wall -Wconversion -Wfatal-errors -g -02
4 -std=gnu++20 -fsanitize=address,undefined -Wshadow
5 -fno-omit-frame-pointer -Wno-unused-result
6 -Wno-sign-compare -Wno-char-subscripts #-fuse-ld=gold
```

```
5 #define rep(i,a,b) for (int i = (a); i < (b); ++i)
6 #define all(x) begin(x), end(x)
15 #include <ext/pb_ds/assoc_container.hpp>
17 typedef tree<int,null_type,less<int>,rb_tree_tag,
18 tree_order_statistics_node_update> indexed_set;
21 signed main() {
22 cin.tie(0)->sync_with_stdio(0);
23 }
```

9.7 Stress

```
1 for (( I=0; I < 5; I++ )); do
    ./gen $I > z.in
 3
      ./brute < z.in > expected.txt
 4
      ./prog < z.in > output.txt
     if diff -u expected.txt output.txt; then : ; else
       echo "--> input (z.in):"; cat z.in
 6
       echo "--> expected output:"; cat expected.txt
echo "--> received output:"; cat output.txt
 q
       break
10
     fi
     echo -n .
11
12 done
```