Competitive Programming Notebook

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\overline{n}	not-TLE algorithm	Example
$\leq [1011]$	$\mathcal{O}(n!),\mathcal{O}(n^6)$	Enumerate permutations
$\leq [1518]$	$\mathcal{O}(2^n n^2)$	TSP with DP
$\leq [1822]$	$\mathcal{O}(2^n n)$	Bitmask DP
≤ 100	$\mathcal{O}(n^4)$	3D DP with $\mathcal{O}(n)$ loop
≤ 400	$\mathcal{O}(n^3)$	Floyd-Warshall
$\leq 2 \cdot 10^3$	$\mathcal{O}(n^2 \lg n)$	2 nested loops + tree query
$\leq 5 \cdot 10^4$	$\mathcal{O}(n^2)$	Bubble/Selection/Insertion Sort
$\leq 10^{5}$	$\mathcal{O}(n \lg^2 n) = \mathcal{O}((\lg n)(\lg n))$	Build suffix array
$\leq 10^{6}$	$\mathcal{O}(n \lg n)$	MergeSort, build SegTree
$\leq 10^{7}$	$\mathcal{O}(n \lg \lg n)$	Sieve, totient function
$\leq 10^{8}$	$\mathcal{O}(n), \mathcal{O}(\lg n), \mathcal{O}(1)$	Mathy solution often with IO bottleneck $(n \le 10^9)$

 10^8 ops/second

1 Theory

1.1 Relevant comparisons

lg 10 (1E1)	2.3
$\lg 100 \; (1E1)$	4.6
$\lg 1000 \; (1E2)$	6.9
$\lg 10000 \text{ (1E3)}$	9.2
$\lg 100000$ (1E4)	11.5
lg 1000000 (1E5)	13.8
lg 10000000 (1E6)	16.1
lg 100000000 (1E7)	18.4
$\lg 1000000000$ (1E8)	20.7
$\lg 100000000000$ (1E9)	23.0
$\lg 1000000000000$ (1E10)	25.3
$\lg 10000000000000$ (1E11)	27.6
lg 10000000000000 (1E12)	29.9
2^{10}	$\approx 10^3$
2^{20}	$\approx 10^6$

Sign	Type	Bits	Max	Digits
±	char	8	127	2
+	unsigned char	8	255	2
\pm	short	16	32767	4
+	unsigned short	16	65535	4
\pm	int/long	32	$\approx 2 \cdot 10^9$	9
+	unsigned int/long	32	$\approx 4 \cdot 10^9$	9
\pm	long long	64	$\approx 9 \cdot 10^{18}$	18
+	unsigned long long	64	$\approx 18 \cdot 10^{18}$	19
\pm	int128	128	$\approx 17 \cdot 10^{37}$	38
+	unsignedint128	128	$\approx 3 \cdot 10^{38}$	38

1.2 Prime counting function - pi(x)

Asymptotic to $\frac{x}{\log x}$ by the prime number theorem.

1.3 Progressions

$$a_n = a_k + r(n - k)$$
$$a_n = a_k q^{(n-k)}$$

- r, q: Ratio
- k: Known term

Algorithm	Time	Space
ArticBridges	$\mathcal{O}(V+E)$	$\mathcal{O}(V+E)$
Bellman-Ford	$\mathcal{O}(VE)$	$\mathcal{O}(V+E)$
Dijksta	$\mathcal{O}((V+E)\log V)$	$\mathcal{O}(V^2)$
Edmond Karp	$\mathcal{O}(VE^2)$	$\mathcal{O}(V+E)$
Euler Tour	$\mathcal{O}(E^2)$	
Floyd Warshall	$\mathcal{O}(V^3 + E)$	$\mathcal{O}(V^2 + E)$
Graph Check	$\mathcal{O}(V+E)$	$\mathcal{O}(V+E)$
Kahn	$\mathcal{O}(VE)$	$\mathcal{O}(V+E)$
Kruskal	$\mathcal{O}(E \log V)$	$\mathcal{O}(V+E)$
LCA	$\mathcal{O}(N \log N)$	$\mathcal{O}(N \log N)$
MCBM	$\mathcal{O}(VE)$	
Prim	$\mathcal{O}(E \log V)$	$\mathcal{O}(V+E)$
Tarjan	$\mathcal{O}(V+E)$	$\mathcal{O}(V+E)$
Extended Euclid	$\mathcal{O}(\log \min(a, b))$	$\mathcal{O}(1)$
Floyd (cycle)	$\mathcal{O}(V)$	$\mathcal{O}(1)$
PrimeFac + OptTrialDiv	$\mathcal{O}(\pi(\sqrt{n}))$	$\mathcal{O}(n)$
Sieve of Eratosthenes	$\mathcal{O}(n\log\log n)$	$\mathcal{O}(n)$
Binary Search	$\mathcal{O}(\log N)$	
Coordinate Compression	$\mathcal{O}(N \log N)$	
KMP	$\mathcal{O}(N)$	
MUF	$\mathcal{O}(AM)$	$\mathcal{O}(N)$
Bottom-Up SegTree	$\mathcal{O}(\log N)$	$\mathcal{O}(N)$

X	10	10^{2}	10^{3}	10^{4}
$\pi(x)$	4	25	168	1 229
X	10^{5}	10^{6}	10^{7}	10^{8}
$\pi(x)$	9592	78498	664579	5761455

• n: Term you want

$$S_n = \frac{n(a_1 + a_n)}{2}$$
$$S_n = \frac{a_1(q^n - 1)}{q - 1}$$

1.4 Series Identities

$$\sum_{i=1}^{n} i^2 = \frac{n(n+1)(2n+1)}{6} \qquad \sum_{i=1}^{n} i^3 = \frac{n^2(n+1)^2}{4} = \left(\sum_{i=1}^{n} i\right)^2$$

$$g_k(n) = \sum_{i=1}^n i^k = \frac{1}{k+1} \left(n^{k+1} + \sum_{j=1}^k \binom{k+1}{j+1} (-1)^{j+1} g_{k-j}(n) \right)$$

$$\sum_{i=0}^{n} ic^{i} = \frac{nc^{n+2} - (n+1)c^{n+1} + c}{(c-1)^{2}}, \quad c \neq 1$$

$$\sum_{i=0}^{\infty} ic^{i} = \frac{c}{(1-c)^{2}}, \quad |c| < 1$$

Binomial Identities 1.5

$$\binom{n}{k} = \frac{n}{k} \binom{n-1}{k-1}$$

$$\binom{n-1}{k} - \binom{n-1}{k-1} = \frac{n-2k}{k} \binom{n}{k}$$

$$\binom{n}{h} \binom{n-h}{k} = \binom{n}{k} \binom{n-k}{h}$$

$$\binom{n}{k} = \frac{n+1-k}{k} \binom{n}{k-1}$$

$$\sum_{k=0}^{n} k \binom{n}{k} = n2^{n-1}$$

$$\sum_{k=0}^{n} k^2 \binom{n}{k} = (n+n^2)2^{n-2}$$

$$\sum_{j=0}^{k} \binom{m}{j} \binom{n-m}{k-j} = \binom{n}{k}$$

$$\sum_{j=0}^{m} \binom{m}{j}^2 = \binom{2m}{m}$$

$$\sum_{m=0}^{n} \binom{m}{j} \binom{n-m}{k-j} = \binom{n+1}{k+1}$$

$$\sum_{m=k}^{n} \binom{m}{k} = \binom{n+1}{k+1}$$

$$\sum_{k=0}^{m} \binom{n+r}{k} = \binom{n+m+1}{m}$$

$$(x+y)^n = \sum_{k=0}^{n} \binom{n}{k} x^{n-k} y^k$$

$$(1+x)^n = \sum_{k=0}^{n} \binom{n}{k} x^k$$

$$2\sum_{k=0}^{n} \binom{n}{k} - \binom{n}{k} = \sum_{k=0}^{n} \binom{n+1}{k} x^k$$

Lucas' Theorem

$$\binom{n}{m} = \prod_{i=0}^k \binom{n_i}{m_i} \pmod{p}$$

For prime p, n_i and m_i are coefficients of the representations of n and m in base p.

Fermat Theorems

p is prime

$$a^{p} = a \pmod{p}$$

$$a^{p-1} = 1 \pmod{p}$$

$$(a+b)^{p} = a^{p} + b^{p} \pmod{p}$$

$$a^{-1} = a^{p-2} \pmod{p}$$

Modulo @ exponent

For coprime a, m:

$$a^n \equiv a^{n \bmod \varphi(m)} \pmod{m}$$

Generally, if $n \geq \log_2 m$, then

$$a^n \equiv a^{\varphi(m) + [n \mod \varphi(m)]} \pmod{m}$$

1.9 Heron's Formula

Area of a triangle $(s = \frac{a+b+c}{2})$

$$A = \sqrt{s(s-a)(s-b)(s-c)}$$

1.10 Some Primes

- $10^6 + 69$
- 1000000007

• $10^9 + 7$

1000000009

• $10^9 + 9$

- 1000000021
- $10^{18} 11$ • $10^{18} + 3$
- 1000000033

• $10^{18} - 11$

 $2^{61} - 1$

- 1000696969
- $10^{18} + 3$
- 998244353
- 2305843009213693951 =
- 999999937
- $2^{61} 1$

1.11 Catalan Numbers

1, 1, 2, 5, 14, 42, 132, 429, 1430, 4862, 16796, 58786, 208012, 742900, 2674440, 9694845, 35357670, 129644790, 477638700, 1767263190, 6564120420, 24466267020, 91482563640, 343059613650, 1289904147324, 4861946401452, 18367353072152, 69533550916004, 263747951750360, 1002242216651368.

$$C_n = \frac{1}{n+1} {2n \choose n} = \frac{(2n)!}{(n+1)!n!} = \prod_{k=2}^n \frac{n+k}{k}, n \ge 0.$$

- The number of valid parenthesis strings with n paren-
- The number of complete binary trees with n+1 leaves
- How many times a n + 2-sided convex polygon can be cut in triangles conecting its vertices with straight lines

1.12Binomial

X is the number of successes in a sequence of n independent experiments. $P(X = k) = \binom{n}{k} p^k (1-p)^{n-k}$, and E[X] = npand Var(X) = np(1-p).

1.13 Trigonometry

$$\sin^2 \theta + \cos^2 \theta = 1$$
, $\sin = \frac{opo}{hip}$, $\cos = \frac{adj}{hip}$, $\tan = \frac{opo}{adj}$. $\sin \theta = x \rightarrow \arcsin x = \theta$.

 α degrees to x rd: $\alpha = \frac{180x}{\pi}$

1.14 Multiples of gcd

Multiples of gcd(A, B) that are $\in [0, A)$

Let
$$A, B > 0$$
, $g = GCD(A, B)$, $A = ag$ and $B = bg$.
 a integers $(0 \times B)\%A$, $(1 \times B)\%A$, $(2 \times B)\%A$... $((a - 1) \times B)\%A$ correspond to each multiple of g between 0 and $A - 1$ (inclusive); note that they are all unique.

Expected Value

Avg value of event. For each event, add to the sum the probability of an event times the value of X in that event $\mathbb{E}(X) = \sum_{\omega \in \Omega} (P(\omega) \times X(\omega))$

Another way of looking at it: $\mathbb{E}(X) = \sum_{i=1}^{M} (i \times P(X=i))$

$$\mathbb{E}(X) = \sum_{i=1}^{M} (i \times P(X = i))$$

Since in the expanded version of this sum P(X = i) will appear i times, you're also calculating for each i the probability that $X \geq i$ (P(x = M) will appear M times, once for each i; P(x = 1) will appear exactly once, for i = 1; and so on). So

$$\mathbb{E}(X) = \sum_{i=1}^{M} (i \times P(X=i)) = \sum_{i=1}^{M} P(X \ge i)$$

Combination 1.16

A combination ${}_{n}C_{k} = \binom{n}{k}$ (n chooses k) refers to selecting k objects from a collection of n where the order of choice doesn't matter.

Without repetition: can't choose an element twice.

 $\binom{n}{k} = \frac{n!}{r!(n-k)!}$ With repetition: elements may be chosen more than once. $\binom{n}{k} = \frac{(k+n-1)!}{k!(n-1)!}$

1.17 Permutation

A permutation ${}_{n}P_{k}$ refers to selecting k objects from a collection of n where the order of choice matters.

With repetition: elements may be chosen more than once. ${}_{n}P_{k}=n^{k}$

Without repetition: can't choose an element twice. $_{n}P_{k} = \frac{n!}{(n-k)!}$

Paradigm

Bounds in C++

• Last element ≤ x: upper_bound - 1

First element ≥ x: lower_bound

• upper_bound: first element > x

• lower_bound: first element >= x

2.2Coordinate Compression

Normalize vector access; can also be done with map/set but high constant

String

3.1 **Suffix Array**

To find whether p is a substring of s (and where this occurrence starts), you can build the suffix array A of s. Since A is sorted, you can binary search for p as a prefix of all suffixes of s. Complexity (besides construction): $\mathcal{O}(|p|\log(|s|))$.

3.2 Prefix Function (KMP)

To find ocurrences of s in t, use the string s+%+t, then look for pi[i] = s.length() on the "t side"

3.3 Hash

Let $h_{i...j} = \text{hash}(s_{i...j})$.

 $h_{i..j} \times p^i = h_{0..j} - h_{0..i-1}$. Instead of finding the multiplicative inverse of p^i , you can multiply this term by p^{n-i} (so every hash is compared multiplied by p^n).

Emergency 4

Pre-submit

Write a few simple test cases if sample is not enough.

Are time limits close? If so, generate max cases.

Is the memory usage fine?

Could anything overflow?

Make sure to submit the right file (check the filename you're editing).

Wrong answer

Print your solution and debug output!

Are you clearing all data structures between test cases?

Can your algorithm handle the whole range of input?

Read the full problem statement again.

Do you handle all corner cases correctly?

Have you understood the problem correctly?

Any uninitialized variables?

Any overflows?

Confusing N and M, i and j, etc.?

Are you sure your algorithm works?

What special cases have you not thought of?

Are you sure the STL functions you use work as you think? Add some assertions, maybe resubmit.

Create some testcases to run your algorithm on.

Go through the algorithm for a simple case.

Go through this list again.

Explain your algorithm to a teammate.

Ask the teammate to look at your code.

Go for a small walk, e.g. to the toilet.

Is your output format correct? (including whitespace)

Rewrite your solution from the start or let a teammate do it.

Runtime error

Have you tested all corner cases locally?

Any uninitialized variables?

Are you reading or writing outside the range of any vector?

Any assertions that might fail?

Any possible division by 0? (mod 0 for example)

Any possible infinite recursion?

Invalidated pointers or iterators?

Are you using too much memory?

Debug with resubmits (e.g. remapped signals, see Various).

Time limit exceeded

Do you have any possible infinite loops?

What is the complexity of your algorithm?

Are you copying a lot of unnecessary data? (use references) How big is the input and output? (consider scanf and printf)

Avoid vector, map. (use array/unordered map)

What do your teammates think about your algorithm?

Memory limit exceeded

What is the max amount of memory your algorithm should need?

Are you clearing all data structures between test cases?

5 To do

Agora é só juntar tudo isso com os códigos e permitir latex no início do código // nome da seção /* latex coisas em latex etal */ codigo em c++

6 Geometry

6.1 Points

```
1 using pt = complex<double>;
2 #define px real()
3 #define py imag()
5 double dot(pt a, pt b) { return (conj(a)*b).px; }
6 double cross(pt a, pt b) { return (conj(a)*b).py; }
7 pt vec(pt a, pt b) { return b-a; }
 8 int sgn(double \nu) { return (\nu > -EPS) - (\nu < EPS); }
9 int seg_ornt(pt a, pt b, pt c) {
10
    return sgn(cross(vec(a, b), vec(a, c)));
11 }
12 int ccw(pt a, pt b, pt c, bool col) {
13
    int o = seg_ornt(a, b, c);
     return (0 == 1) || (0 == 0 && col);
15 }
16 const double PI = acos(-1);
17 double angle(pt a, pt b, pt c) {
     return abs(remainder(arg(a-b) - arg(c-b), 2.0*PI));
18
19 }
```

6.2 Convex Hull (Monotone)

```
1 vector<pt> convex hull(vector<pt>& ps, bool col = false) {
    int k = 0, n = ps.size(); vector<pt> ans (2*n);
3
     sort(ps.begin(), ps.end(), [](pt a, pt b) {
      return make_pair(a.px, a.py) < make_pair(b.px, b.py);</pre>
4
5
6
     for (int i = 0; i < n; i++) {</pre>
      while (k >= 2 && !ccw( /* lower hull */
7
8
          ans[k-2], ans[k-1], ps[i], col)) { k--; }
      ans[k++] = ps[i];
9
10
     if (k == n) { ans.resize(n); return ans; }
11
     for (int i = n-2, t = k+1; i >= 0; i--) {
12
13
      while (k >= t && !ccw( /* upper hull */
14
          ans[k-2], ans[k-1], ps[i], col)) { k--; }
15
      ans[k++] = ps[i];
16
    ans.resize(k-1); return ans;
17
18 }
19
20 // with answer as idx of points
21 using pti = pair<pt, int>;
22 #define fi first
23 #define se second
24 vector<int> convex_hull(vector<pti>& ps, bool col = false) {
    int k = 0, n = ps.size(); vector<int> ans (2*n);
26
     sort(ps.begin(), ps.end(), [](pti a, pti b) {
27
      return make_pair(a.fi.px, a.fi.py) < make_pair(b.fi.px,</pre>
           b.fi.py);
28
    });
```

```
29
    for (int i = 0; i < n; i++) {
30
      while (k >= 2 && !ccw( /* lower hull */
31
          ps[ans[k-2]].fi, ps[ans[k-1]].fi, ps[i].fi, col)) {
32
      ans[k++] = i;
33
    }
    if (k == n) {
34
      ans.resize(n);
35
36
      for (auto &i : ans) i = ps[i].second;
37
      return ans; }
38
     for (int i = n-2, t = k+1; i >= 0; i--) {
39
      while (k >= t && !ccw( /* upper hull */
          ps[ans[k-2]].fi, ps[ans[k-1]].fi, ps[i].fi, col)) {
40
               k--; }
41
      ans[k++] = i;
    }
42
43
    ans.resize(k-1);
     for (auto &i : ans) i = ps[i].second;
44
45
     return ans;
46 }
```

7 Graph

7.1 Prim MST

```
1 // Status: tested (UVA10048)
 2 // O(E log V) time, O(V+E) space
3
 4 vector<vector<pair<int, int>> adj(M), mst(M);
 5 vector<bool> taken(M, false);
 6 int cost = 0;
 7 using iii = pair<int, pair<int, int>>;
 8 priority_queue<iii, vector<iii, greater<iii> pq;
9
10 void process(int v) {
     taken[v] = true;
11
12
     for (auto &[w, u]: adj[v])
13
       if (!taken[u])
14
         pq.push({w, {v, u}});
15 }
16
17 void run(int n) {
18
     process(0);
     while (!pq.empty()) {
19
20
       int w = pq.top().first,
21
          v = pq.top().second.first,
22
          u = pq.top().second.second;
23
       pq.pop();
24
       if (!taken[u]) {
25
        mst_cost += w;
26
        mst[u].push_back({w, v});
27
        mst[v].push\_back(\{v, w\});
28
        process(u);
29
      }
     }
30
31
     for (int v = 1; v < n; ++v)
32
       if (!taken[v]) {
33
        process(v);
34
        run(n);
35
       }
36 }
```

7.2 Dijkstra SSSP

```
1 // Status: tested (CF20C)
2 // O((V+E) log V) time, O(V^2) space
3
4 using ii = pair<int, int>;
5 const int inf = 0x3f3f3f3f;
6 vector<vector<ii>> adj(M);
7 vector<int> dist(M, inf), par(M, -1);
8
9 void dijkstra(int s) {
10 dist[s] = 0;
11 priority_queue<ii, vector<ii>>, greater<pair<int, int>>> pq;
12 pq.push(make_pair(0, s));
13 while (!pq.empty()) {
```

```
14
       int w = pq.top().first;
15
       int v = pq.top().second;
16
       pq.pop();
       if (w > dist[v]) continue;
17
       for (auto \{d, u\}: adj[v])
18
        if (dist[v] != inf && dist[v]+d < dist[u]) {</pre>
19
20
          par[u] = v;
21
          dist[u] = dist[v]+d;
22
          pq.push(make_pair(dist[u], u));
23
24
25 }
```

7.3 Graph Check

```
1 // Usage: graphCheck(firstVertex, -1) (p stands for parent)
 2 // O(V+E) time & space
 4 int UNVISITED = -1, EXPLORED = 0, VISITED = 1;
 5 vector<vector<int>> adj(M);
 6 vector<int> tin:
 8 void graphCheck(int v, int p) { //vertex, parent
    tin[v] = EXPLORED;
10
     for (auto u: adj[v]) {
11
       if (tin[u] == UNVISITED) { //tree edge
        graphCheck(u, v);
12
       } else if (tin[u] == EXPLORED) {
        if (u == p)
14
15
          ; //two way edge u <-> v
16
17
          ; //back edge \nu -> u
18
      } else if (tin[u] == VISITED) {
        ; //forward/cross edge u-v
19
      }
20
21
     tin[v] = VISITED;
23 }
```

7.4 Articulations and Bridges

```
1 // Usage: dfs(source, -1)
2 // Status: not tested
 3 // O(V+E) time & space
5 int tk = 0;
 6 vector<int> tin(M, -1);
7 vector<vector<int>> adj(M);
9 void dfs(int ν, int p) {
10 tin[v] = low[v] = tk++;
    int children = 0;
    for (auto u: adj[v]) {
12
13
      if (u == p) continue;
      else if (tin[u] == -1) {
        ++children;
15
16
        dfs(u, v);
        if (low[u] >= tin[v] \&\& p != v)
17
18
          ; //articulation point
19
        if (low[u] > tin[v])
          : //bridge u-v
20
21
        low[v] = min(low[v], low[u]);
22
      } else {
        low[v] = min(low[v], tin[u]);
23
24
25
26 }
```

7.5 Euler Tour

```
1 // Usage: tour(cyc.begin(), start\_vertex)
2 // Status: not tested
3 // Source: CP3 (pg. 205)
4 // O(E^2) time
5
6 list<int> cyc;
7 vector<vector<int>> adj(M);
8 vector<vector<bool>> traversed(M, vector<bool>(M, false));
```

```
10 //euler tour (list for fast insertion)
11 void tour(list<int>::iterator i, int v) {
    for (auto u: adj[v]) {
      if (!traversed[v][u]) {
        traversed[v][u] = true;
14
15
         for (auto t: adj[u])
          if (t == v \&\& !traversed[u][t]) {
16
17
            traversed[u][t] = true;
18
19
20
         tour(cyc.insert(i, v), u);
21
22
    }
23 }
```

7.6 Heavy-Light Decomposition

```
Update
 Query
              Setup
 \mathcal{O}(\log^2 n)
              define oper(a,b) for query
                                              rmq.upd(pos[x],v)
Queries on edges: assign values of edges to child node, then
change pos[x] to pos[x]+1 in query (see !!!)
 1 vector<int> g[MAXN];
 2 int wg[MAXN],par[MAXN],h[MAXN]; // subtree
        size, father, height
 3 void dfs1(int x){
 4
     wg[x]=1;
     for(int y:g[x])if(y!=par[x]){
 6
       par[y]=x;h[y]=h[x]+1;dfs1(y);
 7
       wg[x] += wg[y];
 8
    }
 9 }
10 int curpos,pos[MAXN],head[MAXN]; // head = representante
11 void hld(int x, int c){
    if(c<0)c=x;
12
13
     pos[x]=curpos++;head[x]=c;
14
     int mx=-1;
     for(int y:g[x])if(y!=par[x]&&(mx<0||wg[mx]<wg[y]))mx=y;</pre>
     if(mx>=0)hld(mx,c);
16
17
     for(int y:g[x])if(y!=mx&&y!=par[x])hld(y,-1);
18 }
19 void
        hld_init(){par[0]=-1;h[0]=0;dfs1(0);curpos=0;hld(0,-1);}
20 int query(int x, int y, stree& rmq){
     int r=NEUT;
     while(head[x]!=head[y]){
       if(h[head[x]]>h[head[y]])swap(x,y);
24
       r=oper(r,rmq.query(pos[head[y]],pos[y]+1));
25
       y=par[head[y]];
26
27
     if(h[x]>h[y])swap(x,y); // now x is lca
28
     r=oper(r,rmq.query(pos[x],pos[y]+1)); // !!!
29
     return r;
30 }
```

7.7 Kahn's topological sort

```
1 // Status: tested (UVA11060)
 2 // O(VE) time, O(V+E) space
 4 vector<vector<int>> adj(M);
5 vector<int> sorted;
6
7 void kahn(int n) {
     vector<int> indeg(n, 0);
9
     vector<bool> valid(n, true);
10
     priority_queue<int> pq;
11
12
     for (int v = 0; v < n; ++v)
     for (auto u: adj[v])
13
14
        indeg[u]++;
15
     for (int v = 0; v < n; ++v)
16
      if (!indeg[v]) pq.push(v);
17
18
     while (!pq.empty()) {
19
      int v = pq.top(); pq.pop();
20
       sorted.push_back(v);
```

7.8 Max Cardinality Bipartite Matching

```
1 // Status: not tested
 2 // Source: CP3 (pg. 209)
 3 // O(VE) time
5 vector<vector<int>> adj(M);
 6 vector<int> match(M, -1);
7 vector<bool> visited(M);
9 bool augment(int left) { //match one on the left with one
        on the right
    if (visited[left]) return false;
    visited[left] = true;
11
     for (auto right: adj[left])
13
      if (match[right] == -1 || augment(match[right])) {
        match[right] = left;
14
15
        return true;
16
      }
17
    return false;
18 }
19
20 //usage
21 //(mcbm = V iff there's at least one way to completely
        match both sides)
22 int mcbm = 0; //number of matched vertices
23 match.assign(M, -1);
24 for (int \nu = 0; \nu < ls; ++\nu) {//ls = size of the left set
   visited.assign(ls, false);
   mcbm += augment(v);
27 }
```

7.9 LCA - Binary lifting

```
\mathcal{O}(n \log n) time \mid \mathcal{O}(n \log n) space
1 int n, l = ceil(log2(n));
2 vector<vector<int>> adj;
 3 int tk = 0;
4 vector<int> tin(n), tout(n);
5 vector<vector<int>> up(n, vector<int>(l+1)); // ancestor
6
7 void dfs(int v, int p) { // run dfs(root, root) to
        initialize
     tin[v] = ++tk;
8
     up[v][0] = p;
9
10
     for (int i = 1; i <= l; ++i)</pre>
      up[v][i] = up[up[v][i-1]][i-1];
11
12
     for (int u : adj[v])
      if (u != p)
13
        dfs(u, v);
14
     tout[v] = ++tk;
15
16 }
17
18 bool ancestor(int \nu, int u) { // \nu is ancestor of u
    return tin[v] <= tin[u] && tout[v] >= tout[u];
19
20 }
21
22 int lca(int \nu, int u) {
23
    if (ancestor(v, u)) return v;
    if (ancestor(u, v)) return u;
25
     for (int i = l; i >= 0; --i)
       if (!ancestor(up[v][i], u))
26
        v = up[v][i];
28
     return up[v][0];
29 }
```

7.10 Tarjan Strongly Connected Component

```
1 // Usage: Tarjan(N, adj)
2 // Status: tested (UVA247, UVA11838)
```

```
3 // O(V+E) time & space
5 vector<int> tin(M, -1), low(M, -1);
 6 vector<bool> vis(M);
 7 vector<vector<int> adj(M);
8 stack<int> S;
9 int tk = 0;
10
11 void dfs(int ν) {
12
    low[v] = tin[v] = tk++;
13
     S.push(v);
14
     vis[v] = true;
15
     for (auto u: adj[v]) {
16
      if (tin[u] == -1)
17
        dfs(u);
18
      if (vis[u])
19
        low[v] = min(low[v], low[u]);
20
     if (low[v] == tin[v])
21
22
       while (true) {
23
        int u = S.top(); S.pop(); vis[u] = false;
24
         if (u == v) break;
25
26 }
```

7.11 LCA - Euler Path

```
\mathcal{O}(n \log n) time \mid \mathcal{O}(n) space
 1 using ii = pair<int, int>;
 2 vector<int> idx(n);
 3 int tk = 1;
   void dfs(int ν, int d) { // call with dfs(root, 0);
 5
     for (auto u : adj[v]) {
       st.update(tk, \{d, v\});
       tk++;
9
       dfs(u, d+1);
10
    }
11
     idx[v] = tk;
    st.update(tk, {d, v});
12
13
14 }
15
16 int lca(int v, int u) {
    int l = idx[v], r = idx[u];
17
    return st.minquery(l, r).second; // .first is depth
18
```

7.12 Kosaraju SCC

```
1 // run kosaraju()
 2 // tested: cf103931M
4 // O(V+E) time & space (2 dfs calls)
6 int n; // number of vertices
7 vector<vector<int>> adj(n), adj_rev(n);
8 vector<bool> used(n):
9 vector<int> order, component;
10
11 void dfs1(int ν) {
12
    used[v] = true;
    for (auto u: adj[v])
13
14
      if (!used[u])
15
        dfs1(u);
16
    order.push_back(v);
17 }
18
19 void dfs2(int \nu) {
    used[v] = true;
    component.push\_back(v);
21
22
    for (auto u: adj_rev[v])
      if (!used[u])
24
        dfs2(u):
25 }
27 void kosaraju() {
```

```
28
    for (int i = 0; i < n; ++i)
29
      if (!used[i]) dfs1(i);
30
    used.assign(n, false);
31
32
    reverse(order.begin(), order.end());
33
     for (auto v: order)
34
      if (!used[v]) {
35
36
        dfs2(v);
37
        // ...process vertices in component
38
        component.clear();
39
40 }
7.13 Bellman-Ford SSSP
```

```
1 // Status: tested (UVA1112, UVA10449)
 2 // O(VE) time, O(V+E) space
3 const int inf = 0x3f3f3f3f;
 4 vector<vector<pair<int, int>>> adj(M);
5 vector<int> dist(M, inf);
7 void bellmanFord(int n) {
   for (int i = 0; i < n-1; ++i)</pre>
9
      for (int v = 0; v < n; ++v)
        for (auto &[u, w]: adj[v])
10
          if (dist[v] != inf)
11
            dist[u] = min(dist[u], dist[v]+w);
12
13 }
14
15 //check if there are negative cycles
16 bool cycle(int n) {
17
   bool ans = false;
    for (int v = 0; v < n; ++v)
     for (auto &[u, w]: ν)
19
20
        ans \mid= dist[v] != inf && dist[u] > dist[v]+w;
21 }
```

7.14 Kruskal MST

```
1 // Usage: Kruskal(V, E, edges) (weighted edges)
 2 // Status: tested (UVA1174)
3 // O(E log V) time, O(V+E) space \,
5 using iii = pair<int, pair<int, int>>; //weight, two
        vertices
 6 vector<iii> edges;
7 UnionFind muf;
9 int kruskal() {
10 int cost = 0;
     sort(edges.begin(), edges.end());
    for (auto a: edges) {
12
     int w = a.first;
13
      pair<int, int> e = a.second;
      if (!muf.isSameSet(e.first, e.second)) {
15
16
        cost += w;
17
        muf.unionSet(e.first, e.second);
18
      }
19
    return cost;
20
```

7.15 Edmond Karp MaxFlow

```
1 // Status: tested (CSES1694, CSES1695)
2 // O(VE^2) time, O(V+E) space
3
4 vector<vector<int>> capacity(M, vector<int>(M, 0)), adj(M);
5 vector<pair<int, int>> mc; //mincut edges
6
7 int bfs(int s, int t, vi &par) {
8 fill(all(par), -1);
9 par[s] = -2;
10 queue<pair<int, int>> q; q.push({s, inf});
11 while (!q.empty()) {
12 int v = q.front().first,
13 flow = q.front().second;
14 q.pop();
```

```
15
      for (auto u: adj[v])
16
        if (par[u] == -1 && capacity[v][u]) {
17
          par[u] = v;
          int new_flow = min(flow, capacity[v][u]);
18
19
          if (u == t) return new_flow;
          q.push({u, new_flow});
20
21
22
    }
23
     return 0;
24 }
25
26 int maxflow(int s, int t) {
    int flow = 0;
28
     vi par(M);
29
     int new_flow;
     while ((new_flow = bfs(s, t, par))) {
30
31
      flow += new_flow;
32
       int v = t;
33
      while (\nu != s) {
34
        int p = par[v];
35
        capacity[p][v] -= new_flow;
36
        capacity[v][p] += new_flow;
37
        v = p;
38
      }
    }
39
    return flow;
41 }
42
43 void mincut(int s, int t) {
44
     maxflow(s, t);
     stack<int> st;
45
     vector<bool> visited(n, false);
46
47
     vector<pair<int, int>> ans;
48
     st.push(s); // changed from 0 to s
49
     while (!st.empty()) {
50
      int v = st.top(); st.pop();
51
      if (visited[v]) continue;
      visited[v] = true;
52
       for (auto u: adj[v])
53
54
        if (capacity[v][u] > 0)
55
          st.push(u);
56
57
          ans.push_back({v, u});
58
     }
59
     mc.clear();
     for (auto &[v, u] : ans)
60
61
      if (!visited[u])
62
        mc.push_back({v, u});
63 }
```

7.16 Floyd Warshall APSP

```
1 // Usage: FloydWarshall(n, edges)
 2 // Status: tested (UVA821, UVA1056)
 3 // O(V^3 + E) time, O(V^2 + E) space
5 struct edge { int v, u, w; };
6 const int inf = 0x3f3f3f3f;
7 vector<vector<int>> weight(M, vector<int>(M, inf));
8 vector<edge> edges;
9
10 void floydWarshall(int n) {
   for (auto e: edges)
11
12
      weight[e.v][e.u] = e.w;
13
     for (int k = 0; k < n; ++k)
      for (int i = 0; i < n; ++i)</pre>
14
         for (int j = 0; j < n; ++j)
  if (max(weight[i][k], weight[k][j]) < inf)</pre>
15
16
             weight[i][j] = min(weight[i][j],
17
                  weight[i][k]+weight[k][j]);
18 }
```

8 Math

8.1 Sieve of Eratosthenes

```
1 // Status: not tested
2 // O(n log log n) time, O(n) space
```

```
3
 4 bitset<11234567> pr;
 5 vector<int> factors(M, 0);
 6 vector<int> primes;
 8 void sieve(int n) {
    pr.set();
     for (int i = 2; i*i <= n; ++i)
  if (pr[i]) { //factors[i] == 0</pre>
10
11
12
         primes.push_back(i);
         for (int p = i*i; p <= n; p += i) {</pre>
13
           pr[p] = false;
14
15
           factors[p]++;
         }
16
17
       }
18 }
19
20 // O(1) for small n, O(sieve_size) else
21 bool isPrime(int n) {
22   int sieve_size = 11234567;
     if (n <= sieve_size) return pr[n];</pre>
    for (auto p: primes) // only works if n <= primes.back()^2</pre>
      if (!(n%p)) return false;
26
    return true;
27 }
```

8.2 Prime Factors w/ Optimized Trial Divisions

```
1 // Status: not tested
2 // Source: CP3 (pg. 238)
3 // O(pi(sqrt(n))) time, O(n) space
5 vector<int> primes;
6 vector<pair<int, int>> factors;
8 void pf(int n) {
9
   for (auto p: primes) {
10
      if (p*p > n) break;
      int i = 0;
11
      while (!(n%p)) {
12
       n /= p;
13
14
        i++;
15
16
      factors.push_back({p, i});
17
18
    if (n != 1) factors.push_back({n, 1});
19 }
```

8.3 Extended Euclid for solving Linear Diophantine Equations

```
1 // Status: not tested
 2 // Source: cp-algorithms
 3 // O(log min(a, b)) time
 5 int gcd(int a, int b, int& x, int& y) {
    if (!b) {
 7
      x = 1;
      y = 0;
 9
      return a;
10
    int x1, y1;
11
    int d = gcd(b, a % b, x1, y1);
12
    x = y1;
    y = x1 - y1 * (a / b);
14
15
    return d;
16 }
17
18 int gcd(int a, int b) {
    int x, y;
19
20
    return gcd(a, b, x, y);
```

8.4 Floyd's algorithm cycle-finding

```
1 // Status: not tested 2 // Source: CPHB (p. 156)
```

```
3 // O(V) time
5 int findCycle(int x) {
    int a, b;
    a = succ(x);
   b = succ(succ(x));
   while (a != b) {
10
      a = succ(a);
11
      b = succ(succ(b));
   }
12
    a = x;
13
    while (a != b) {
14
15
     a = succ(a);
16
      b = succ(b);
17
    }
    int first = a; // first element in cycle
18
19
    b = succ(a);
20
    int length = 1;
    while (a != b) {
21
22
      b = succ(b);
23
      length++;
    }
24
25 }
```

9 Paradigm

9.1 Coordinate Compression

9.2 128 Bit Integers

```
1 // Status: not tested
2 // Source: GEMA (YouTube)
 3
 4 // cout, cerr, etc; pode dar over/underflow
 5 ostream& operator<<(ostream& out, __int128 x) {</pre>
       if (x == 0) return out << 0;</pre>
       string s; bool sig = x < 0; x = x < 0 ? -x : x;
       while(x > 0) s += x % 10 + '0', x /= 10;
       if (sig) s += '-';
9
10
       reverse(s.begin(), s.end());
       return out << s;</pre>
11
12 }
13
14 // cin, etc; pode dar over/underflow
15 istream& operator>>(istream& in, __int128& x) {
16
       char c, neg = 0; while(isspace(c = in.get()));
       if(!isdigit(c)) neg = (c == '-'), x = 0;
17
       else x = c - '0';
18
       while(isdigit(c = in.get())) x = (x << 3) + (x << 1) -
19
           '0' + c;
       x = neg ? -x : x; return in;
21 }
```

9.3 Binary Search (but beautiful)

```
1 // Status: not tested
2 // Source: CPHB
3 // O(log N) time
4
5 // std
6 int l = 0, r = n-1;
7 while (l <= r) {
8 int m = l+(r-l)/2;</pre>
```

```
if (array[m] == x)
9
10
      // found
11
    if (array[m] > x) r = m-1;
    else l = m+1;
13 }
14
15 // nice - binary steps
16 \text{ int } k = 0;
17 for (int b = n/2; b > 0; b /= 2)
18 while (k+b < n && array[k+b] <= x)
      k += b:
20 \text{ if } (array[k] == x)
    // found
```

10 String

10.1 Rolling hash (O(N))

```
1 // Status: not tested
 2 // Source: CP-Algorithms
 3 // O(N) time
 4
 5 ll hash(string const& s) {
    const int p = 31; // ~alphabet size (31 for lowercase, 53
         for uppercase)
    const int M = 1e9 + 9;
    ll h = 0;
 8
 9
    ll p_pow = 1; // precompute for performance
10
    for (char c : s) {
      h = (h + (c - 'a' + 1)*p_pow) % M;
11
      p_pow = (p_pow * p) % M;
13
    }
14
    return h;
15 }
```

10.2 Prefix Function (KMP)

```
1 // Status: not tested
 2 // Source: CP-Algorithms
 3 // O(N) time
4
5 vector<int> prefix(string s) {
   int n = s.length();
    vector < int > pi(n, 0); // can be optimized if you know max
          prefix length
     for (int i = 1; i < n; ++i) {</pre>
8
q
      int j = pi[i-1];
10
      while (j > 0 && s[i] != s[j])
        j = pi[j-1];
11
      if (s[i] == s[j])
12
13
        j++;
14
      pi[i] = j;
    }
```

10.3 Suffix Array

return pi;

16

17 }

```
1 // Status: tested (ITMO course)
 2 // Source: ITMO @ CF Edu, CP-Algorithms
3 // O(nlogn) construction
4
5 // sort p by the values in c (stable) (0(|alphabet| + n))
6 void count_sort(vector<int> &p, vector<int> &c) {
    int n = p.size();
    int alphabet = 256; // ascii range
    vector<int> cnt(max(alphabet, n));
9
    for (auto x : c)
      cnt[x]++;
11
12
13
    vector<int> pos(max(alphabet, n));
    pos[0] = 0;
14
     for (int i = 1; i < max(alphabet, n); ++i)</pre>
15
      pos[i] = pos[i-1] + cnt[i-1];
16
17
18
     vector<int> p_sorted(n);
19
    for (auto x : p) {
```

```
24 }
25
26 // build suffix array
27 vector<int> suffix_array(string s) {
28
    s += "$";
    int n = s.size();
30
    // at k = 2^0, sort strings of length 1
     vector<int> p(n), c(n); // suffix start position,
31
          equivalence class
    for (int i = 0; i < n; ++i) {</pre>
32
33
      p[i] = i;
      c[i] = s[i];
34
    }
35
36
    // at first c is just a hack to sort p, it's not really
          equiv. class
37
     count_sort(p, c);
38
     // but then it is
39
     c[p[0]] = 0;
     for (int i = 1; i < n; ++i) {</pre>
      c[p[i]] = c[p[i-1]];
41
42
       if (s[p[i]] != s[p[i-1]])
43
        c[p[i]]++;
44
    }
45
     int k = 1;
46
     while (k < n) {
47
       // transition from k to k+1
48
       for (int i = 0; i < n; ++i)</pre>
        p[i] = (p[i] - k + n) % n;
49
50
       count_sort(p, c);
51
       // recalculate equiv.
       vector<int> c_upd(n);
52
53
       c_{p[0]} = 0;
54
       for (int i = 1; i < n; ++i) {</pre>
        pair<int, int> prev = {c[p[i-1]], c[(p[i-1] + k)%n]};
55
        pair<int, int> curr = {c[p[i]], c[(p[i] + k)%n]};
56
57
        c_upd[p[i]] = c_upd[p[i-1]];
58
        if (curr != prev)
          c_upd[p[i]]++;
59
60
61
       c = c_upd;
62
      k <<= 1;
    }
63
64
     return p;
65 }
```

11 Structure

20

21

22

23

p_sorted[pos[c[x]]++] = x;

p = p_sorted;

11.1 Merge/Disjoint Union-Find

```
1 // Usage: muf(N);
 2 // Status: tested (UVA11503)
 3 // O(Ackermann * N) time, O(N) space
4
5 struct muf {
6
    int N:
7
     vector<int> par, rk, count;
     muf(int N) : N(N), par(N), rk(N, 0), count(N, 1) {
9
      for (int i = 0; i < N; ++i)</pre>
10
11
        par[i] = i;
     }
12
13
14
     int findSet(int i) {
      return par[i] == i ? i : (par[i] = findSet(par[i]));
15
16
17
18
     int unionSet(int a, int b) {
19
      int x = findSet(a), y = findSet(b);
      if (x != y)
20
21
        count[x] = count[y] = (count[x]+count[y]);
       if (rk[x] < rk[y])
22
23
        par[x] = y;
24
       else {
        par[y] = x;
25
```

```
26     if (rk[x] == rk[y])
27     rk[x]++;
28     }
29     return count[x];
30     }
31
32     bool isSameSet(int i, int j) {
33         return findSet(i) == findSet(j);
34     }
35 };
```

11.2 Bottom-Up Segment Tree

```
1 // Usage: stree(N);
 2 // Source: CP Handbook
 3 // Status: not tested
 4 // Complexity:
 5 // build: O(n)
 6 // query: O(log n)
 7 // modify: 0(log n)
 8 // + uses less space than top-down 4n segtree (2n here)
10 struct stree {
11
    unsigned int n;
12
     vector<int> tree;
13
     stree(vector<int> v) : n(v.size()), tree(2*n) {
14
      for (int i = 0; i < n; ++i)</pre>
15
        modify(i, v[i]);
16
17
18
19
     int query(int a, int b) {
20
      a += n, b += n;
      int ans = 0:
21
22
      while (a <= b) {
23
        if (a\%2 == 1) ans += tree[a++];
        if (b\%2 == 0) ans += tree[b--];
24
25
        a >>= 1; b >>= 1;
26
27
       return ans;
28
29
30
     void modify(int k, int x) {
31
      k += n;
      tree[k] += x;
32
       for (k /= 2; k >= 1; k /= 2)
33
        tree[k] = tree[k<<1] + tree[(k<<1) + 1];
34
35
36 };
```

11.3 Segment Tree

```
1 // Usage: stree(N)
 2 // Complexity:
 3 // build: O(nlogn)
 4 // query: 0(logn)
 5 // modify: O(logn)
 6
 7 struct stree {
    int n;
 9
     vector<int> st, ν;
10
11
     stree(vector<int> v): n(v.size()), st(4*n), v(v) {
12
      build(1, 0, n-1); }
13
14
15
     int left(int i) { return i<<1; }</pre>
     int right(int i) { return (i<<1)+1; }</pre>
16
18
     void build(int p, int pl, int pr) {
19
       if (pl == pr) {
20
        st[p] = v[pl];
21
        return;
22
23
       int m = (pl+pr)/2;
       build(left(p), pl, m);
24
25
       build(right(p), m+1, pr);
26
       st[p] = min(st[left(p)], st[right(p)]);
27
```

```
28
29
     int query(int p, int pl, int pr, int ql, int qr) {
30
       // same params as update, except [ql..qr] is the query
31
       if (qr < pl || ql > pr) return inf;
       if (ql <= pl && pr <= qr) return st[p];</pre>
32
       int m = (pl+pr)/2;
       int query_left = query(left(p), pl, m, ql, qr);
34
35
       int query_right = query(right(p), m+1, pr, ql, qr);
       return min(query_left, query_right);
36
37
38
39
     int query(int ql, int qr) { return query(1, 0, n-1, ql,
          qr); }
40
     void update(int p, int pl, int pr, int i, int x) {
41
       // p = st idx, corresponds to range [pl..pr]
if (i < pl || i > pr) return;
42
43
       if (pl == pr) {
44
45
         st[p] = x;
46
        return;
       }
47
48
       int m = (pl+pr)/2;
       update(left(p), pl, m, i, x);
49
       update(right(p), m+1, pr, i, x);
50
51
       st[p] = min(st[left(p)], st[right(p)]);
52
53
     void update(int i, int x) { update(1, 0, n-1, i, x); }
54
55 };
```

12 Extra

12.1 C++ structs

```
1 struct st {
     vector<int> a;
     vector<bool> b = vector<bool>(5); // default value
    int i:
     st(int _i) : a(_i), i(_i) {};
6
     bool operator< (st& e) const { return i < e.i; }</pre>
7 };
9 \text{ st e} = \text{st}(3); \text{ st f}(3);
10
11 struct matrix {
12
    vector<vector<int>> m;
13
     matrix(int n) m(n, vector<int>(n)) {};
     matrix operator * (const matrix &b) {
14
15
       matrix c = matrix();
16
       for (int i = 0; i < m.size(); ++i)</pre>
         for (int j = 0; j < m.size(); ++j)</pre>
17
18
           for (int k = 0; k < m.size(); ++k)</pre>
19
            c.m[i][j] = c.m[i][j] + 1LL*m[i][k]*b.m[k][j];
20
       return c;
21
    }
22 };.
```

12.2 Shell

12.3 cmp

```
1 priority_queue<int, vector<int>, greater<int>> pq;
2 struct {
3   bool operator()(const int& a, const int& b) const {
4     return a < b;
5   }
6 } cmp;
7 priority_queue<int, vector<int>, cmp> pq2;
8 sort(v.begin(), v.end(), cmp);
```

12.4 Vim

```
1\, set et ts=2 sw=2 ai si cindent sta is tm=50 nu noeb sm "cul 2\, sy on
```

12.5 Generator

```
1 #include <bits/stdc++.h>
2 using namespace std;
3
4 int main(int argc, char *argv[]) {
5 cin.tie(0); ios_base::sync_with_stdio(0);
6 if (argc < 2) {
7 cout << "usage: " << argv[0] << " <seed>\n";
8 exit(1);
9 }
10 srand(atoi(argv[1]));
11 // use rand() for random value
12 }
```

12.6 C++ Template

```
1 #include <bits/stdc++.h>
2 using namespace std;
3
4 int32_t main() {
5  ios_base::sync_with_stdio(0); cin.tie(0);
6 }
```

12.7 Stress

```
1 for (( I=0; I < 5; I++ )); do
2    ./gen $I > z.in
3    ./brute < z.in > expected.txt
4    ./prog < z.in > output.txt
5    if diff -u expected.txt output.txt; then : ; else
6    echo "--> input (z.in):"; cat z.in
7    echo "--> expected output:"; cat expected.txt
8    echo "--> received output:"; cat output.txt
9    break
10    fi
11    echo -n .
12    done
```