## LAPORAN PEMROSESAN PARALEL

(Numerik Python Menggunakan MPI Secara Paralel)



# Disusun Oleh:

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#### 1. Master dan Worker

Menentukan master dan worker dengan melihat spesifikasi masing masing device

• Khairunnisa Junaidi sebagai master



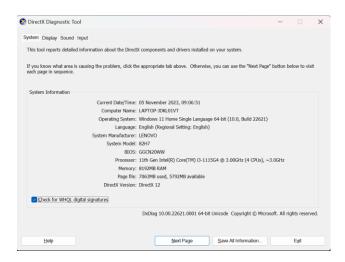
• Eka Ratna Anindita sebagai worker1



• Almirah Callysta Aurelie sebagai worker2



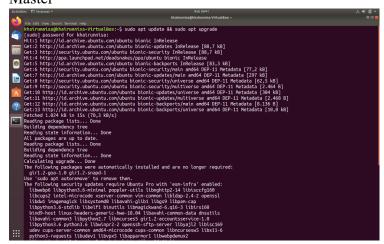
• Nabilla Suci Febriani sebagai worker3



# 2. Upgrade OS

Menggunakan command 'sudo apt update && sudo apt upgrade' untuk memperbarui OS pada setiap device

• Master



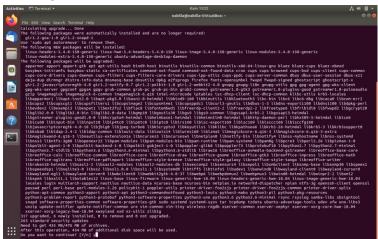
• Worker1

```
### See as a see a
```

• Worker2

```
root@almirah-VirtualBox:/home/almirah# sudo apt update && apt upgrade
Hit:1 http://id.archive.ubuntu.com/ubuntu bionic InRelease
Get:2 http://id.archive.ubuntu.com/ubuntu bionic-updates InRelease [88,7 kB]
Get:3 http://id.archive.ubuntu.com/ubuntu bionic-backports InRelease [83,3 kB]
Hit:4 http://security.ubuntu.com/ubuntu bionic-security InRelease
Hit:5 http://ppa.launchpad.net/deadsnakes/ppa/ubuntu bionic InRelease
Get:6 http://d.archive.ubuntu.com/ubuntu bionic-updates/main amd64 DEP-11 Meta
daRhythmbox B1
Ret: http://pd.tarchive.ubuntu.com/ubuntu bionic-updates/main amd64 DEP-11 Meta daRhythmbox B]
Get:7 http://id.archive.ubuntu.com/ubuntu bionic-updates/universe amd64 DEP-11 Metadata [303 kB]
Get:8 http://id.archive.ubuntu.com/ubuntu bionic-updates/multiverse amd64 DEP-11 Metadata [2.468 B]
Get:9 http://id.archive.ubuntu.com/ubuntu bionic-backports/main amd64 DEP-11 Metadata [8.144 B]
Get:10 http://id.archive.ubuntu.com/ubuntu bionic-backports/main amd64 DEP-11 Metadata [8.148 B]
Fetched 793 kB in 7s (118 kB/s)
Reading package lists... Done
Building dependency tree
Reading state information... Done
All packages are up to date.
Reading package lists... Done
Building dependency tree
Reading state information... Done
Calculating upgrade... Done
The following packages were automatically installed and are no longer required:
oir1.2-goa-1.0 gir1.2-snapd-1
```

Worker3



#### 3. Install net-tools

Melakukan penginstalan net-tools dengan menggunakan command 'sudo apt install net-tools vim' untuk cek IP, vim sebagai teks editor

```
m'untuk cek IP, vim sebagai teks editor

root@almirah-VirtualBox:/home/almirah# sudo apt install net-tools vim
Reading package lists... Done
Building dependency tree
Reading state information... Done
The following packages were automatically installed and are no longer required:
    gir1.2-goa-1.0 gir1.2-snapd-1
    Use 'sudo apt autoremove' to remove them.
The following additional packages will be installed:
    vim-runtime
Suggested packages:
    ctags vim-doc vim-scripts
The following NEW packages will be installed:
    net-tools vim vim-runtime
0 upgraded, 3 newly installed, 0 to remove and 0 not upgraded.
Need to get 6.790 kB of archives.
After this operation, 32,8 MB of additional disk space will be used.
Do you want to continue? [Y/n] y
Get:1 http://id.archive.ubuntu.com/ubuntu bionic/main amd64 net-tools amd64 1.6
0+git20161116.90da8a0-lubuntu1 [194 kB]
Get:2 http://id.archive.ubuntu.com/ubuntu bionic-updates/main amd64 vim-runtime
    all 2:8.0.1453-lubuntu1.13 [5.439 kB]
Get:3 http://id.archive.ubuntu.com/ubuntu bionic-updates/main amd64 vim amd64 2
:8.0.1453-lubuntu1.13 [1.156 kB]
Fetched 6.790 kB in 12s (544 kB/s)
Selecting previously unselected package net-tools.
(Reading database ... 16477 files and directortes currently installed.)
Preparing to unpack .../net-tools_1.60+git20161116.90da8a0-1ubuntu1] ...
```

#### 4. Konfigurasi file

Membuka file /etc/hosts menggunakan command 'sudo nano /etc/hosts'

khairunnisa@khairunnisa-VirtualBox:~\$ sudo nano /etc/hosts

Lalu mengedit file dengan menambahkan IP dan peran.

```
dina@worker2: ~
File Edit View Search Terminal Help
 GNU nano 2.9.3
                                      /etc/hosts
               worker2 localhost
10.1.40.26
127.0.1.1
               almirah-VirtualBox
::1 ip6-localhost ip6-loopback
fe00::0 ip6-localnet
ff00::0 ip6-mcastprefix
ff02::1 ip6-allnodes
ff02::2 ip6-allrouters
10.1.40.16
                master
10.1.42.182
               worker1
10.1.43.181
                worker3
```

#### 5. Konfigurasi SSH

Melakukan konfigurasi SSH, SSH(Secure Shell) digunakan untuk otentikasi dan pertukaran data aman antara node dalam cluster MPI.

#### > Install SSH

Melakukan penginstallan SSH dengan command 'sudo apt install openssh-server'

```
dina@almirah-VirtualBox:/home/almirah$ sudo apt install openssh-server
[sudo] password for dina:
Reading package lists... Done
Building dependency tree
Reading state information... Done
The following packages were automatically installed and are no longer required:
    gir1.2-goa-1.0 gir1.2-snapd-1
Use 'sudo apt autoremove' to remove them.
The following additional packages will be installed:
    ncurses-term openssh-sftp-server ssh-import-id
Suggested packages:
    molly-guard monkeysphere rssh ssh-asknass
            molly-guard monkeysphere rssh ssh-askpass
    The following NEW packages will be installed:
 The following NEW packages will be installed:
    ncurses-term openssh-server openssh-sftp-server ssh-import-id
0 upgraded, 4 newly installed, 0 to remove and 0 not upgraded.
Need to get 637 kB of archives.
After this operation, 5.320 kB of additional disk space will be used.
Do you want to continue? [Y/n] y
Get:1 http://id.archive.ubuntu.com/ubuntu bionic-updates/main amd64 ncurses-ter
m all 6.1-1ubuntu1.18.04.1 [248 kB]
Get:2 http://id.archive.ubuntu.com/ubuntu bionic-updates/main amd64 openssh-sft
D-server amd64 1:7.6p1-4ubuntu0.7 [45.5 kB]
```

Dapat dilakukan pengecekan SSH untuk menghubungkan master ke klien, dengan command 'ssh <nama user>@<host>'

```
dina@ekaratna-VirtualBox:~$ ssh dina@master
The authenticity of host 'master (192.168.100.142)' can't be established.
ECDSA key fingerprint is SHAZ56:Lmn8CRORCOUPYqONnBUvxTJ4eQxhxy6BrkQurtwAx1I.
Are you sure you want to continue connecting (yes/no)? y
Please type 'yes' or 'no': yes
Warning: Permanently added 'master,192.168.100.142' (ECDSA) to the list of known hosts.
dina@master's pastword'.
dina@master's password:
Welcome to Ubuntu 18.04.6 LTS (GNU/Linux 5.4.0-150-generic x86_64)
  * Documentation: https://help.ubuntu.com

* Management: https://landscape.canonical.com

* Support: https://ubuntu.com/advantage
Expanded Security Maintenance for Infrastructure is not enabled.
0 updates can be applied immediately.
130 additional security updates can be applied with ESM Infra.
Learn more about enabling ESM Infra service for Ubuntu 18.04 at
https://ubuntu.com/18-04
New release '20.04.6 LTS' available.
Run 'do-release-upgrade' to upgrade to it.
Your Hardware Enablement Stack (HWE) is supported until April 2023.
Last login: Thu Nov 2 16:02:39 2023 from 192.168.100.145
To run a command as administrator (user "root"), use "sudo <command>".
See "man sudo_root" for details.
dina@khairunnisa-VirtualBox:~$
```

#### > Generate keygen

Dilakukan di master, menggunakan command 'ssh-keygen -t rsa'

#### Input key publik ke klient

Dilakukan di master, membuat isi dari file *id\_rsa.pub* disalin ke file *authorized\_keys* menggunakan command 'cd.ssh'

dina@khairunnisa-VirtualBox:~\$ cd .ssh

#### • Master - worker1

```
dina@khairunnisa-VirtualBox:~/.ssh$ cat id_rsa.pub | ssh dina@worker1 " cat>> .ssh/authorized_keys"

dina@ekaratna-VirtualBox:~$ ls .ssh
authorized_keys known_hosts
```

#### Master – worker2

```
dina@khairunnisa-VirtualBox:~/.ssh$ cat id_rsa.pub | ssh dina@worker2 " cat>> .ssh/authorized_keys"
dina@almirah-VirtualBox:~$ ls .ssh
authorized_keys known_hosts
```

#### • Master – worker3

```
dina@khairunnisa-VirtualBox:~/.ssh$ cat id_rsa.pub | ssh dina@worker3 " cat>> .ssh/authorized_keys"

dina@nabilla-VirtualBox:~$ ls .ssh
authorized_keys known_hosts
```

#### 6. Konfigurasi NFS

Konfigurasi NFS (Network File System) merupakan proses mengatur dan mengkonfigurasi sistem berkas yang memungkinkan berbagi sistem berkas antara komputer dalam jaringan.

#### > Shared folder

Membuat folder bersama menggunakan command 'mkdir <nama folder>'

```
dina@nabilla-VirtualBox:~$ mkdir pempar dina@nabilla-VirtualBox:~$
```

#### > Install NFS Server

Menginstall NFS pada master dengan command 'sudo apt install nfs-kernel-server'

```
dina@khairunnisa-VirtualBox:~$ sudo apt install nfs-kernel-server
[sudo] password for dina:
Reading package lists... Done
Building dependency tree
Reading state information... Done
The following packages were automatically installed and are no longer required:
gir1.2-goa-1.0 gir1.2-snapd-1
Use 'sudo apt autoremove' to remove them.
The following additional packages will be installed:
keyutils libnfsidmap2 libtirpc1 nfs-common rpcbind
Suggested packages:
open-iscsi watchdog
The following NEW packages will be installed:
keyutils libnfsidmap2 libtirpc1 nfs-common nfs-kernel-server rpcbind
0 upgraded, 6 newly installed, 0 to remove and 0 not upgraded.
Need to get 492 kB of archives.
After this operation, 1.709 kB of additional disk space will be used.
Do you want to continue? [Y/n] ■
```

#### ➤ Konfigurasi file

Dilakukan di master, buka file /etc/exports dengan command 'sudo nano /etc/exports'

# dina@khairunnisa-VirtualBox:~\$ sudo nano /etc/exports

Dan dilakukan pengeditan pada file, dengan menambahkan < lokasi shared folder> \*(rw,sync,no root squash,no subtree check)

```
Kam 17:33

A M D

dina@khairunnisa-VirtualBox:-

File Edit View Search Terminal Help

GNU nano 2.9.3

/etc/exports

Modified

# /etc/exports: the access control list for filesystems which may be exported

to NFS clients. See exports(5).

# Example for NFSv2 and NFSv3:

# /srv/homes hostname1(rw,sync,no_subtree_check) hostname2(ro,sync,no_subtree_check)

# Example for NFSv4:

# /srv/nfs4

gss/krb5i(rw,sync,fsid=0,crossmnt,no_subtree_check)

# /srv/nfs4/homes gss/krb5i(rw,sync,no_subtree_check)

# /home/pempar *(rw, sync, no_root_squash, no_subtree_check)
```

Lalu, untuk menyimpan ulang daftar direktori setelah mengedit file dapat menggunakan command 'sudo export fs -a' dan untuk memulai ulang layanan pada server dapat menggunakan command 'sudo systemctl restart nfs-kernel-server'

```
dina@khairunnisa-VirtualBox:~$ sudo exportfs -a
dina@khairunnisa-VirtualBox:~$ sudo systemctl restart nfs-kernel-server
```

#### > Install NFS Klient

Melakukan instalasi NFS pada worker dengan command 'sudo apt install nfs-common'

• Worker1

```
dina@ekaratna-VirtualBox:~$ sudo apt install nfs-common
Reading package lists... Done
Building dependency tree
Reading state information... Done
nfs-common is already the newest version (1:1.3.4-2.1ubuntu5.5).
nfs-common set to manually installed.
The following packages were automatically installed and are no longer required:
gir1.2-goa-1.0 gir1.2-snapd-1
Use 'sudo apt autoremove' to remove them.
0 upgraded, 0 newly installed, 0 to remove and 0 not upgraded.
```

• Worker2

```
dina@almirah-VirtualBox:-$ sudo apt install nfs-common
[sudo] password for dina:
Reading package lists... Done
Building dependency tree
Reading state information... Done
The following packages were automatically installed and are no longer required:
gir1.2-goa-1.0 gir1.2-snapd-1
Use 'sudo apt autoremove' to remove them.
The following additional packages will be installed:
keyutils libnfsidmap2 libtirpc1 rpcbind
Suggested packages:
open-iscsi watchdog
The following NEW packages will be installed:
keyutils libnfsidmap2 libtirpc1 nfs-common rpcbind
0 upgraded, 5 newly installed, 0 to remove and 0 not upgraded.
Need to get 399 kB of archives.
After this operation, 1.364 kB of additional disk space will be used.
Do you want to continue? [Yn] y
Get:1 http://id.archive.ubuntu.com/ubuntu bionic-updates/main amd64 keyutils am
d64 1.5.9-9.2ubuntu2.1 [48,1 kB]
Get:2 http://id.archive.ubuntu.com/ubuntu bionic-updates/main amd64 libnfsidmap2 amd64
0.25-5.1 [27,2 kB]
Get:3 http://id.archive.ubuntu.com/ubuntu bionic-updates/main amd64 libtirpc1 a
md64 0.2.5-1.2ubuntu0.1 [75,7 kB]
Get:4 http://id.archive.ubuntu.com/ubuntu bionic-updates/main amd64 rpcbind amd
64 0.2.5-1.2ubuntu0.18.04.4 [42,1 kB]
Get:5 http://id.archive.ubuntu.com/ubuntu bionic-updates/main amd64 nfs-common
Worker3
```

#### Worker3

```
dina@nabilla-VirtualBox:-$ sudo apt install nfs-comm
Reading package lists... Done
Reading package tists... Done
Building dependency tree
Reading state information... Done
nfs-common is already the newest version (1:1.3.4-2.1ubuntu5.5).
nfs-common set to manually installed.
The following packages were automatically installed and are no longer required:
gir1.2-goa-1.0 gir1.2-snapd-1
yes 'ende ast autoremove' to remove them.
```

#### > Mounting

Dilakukan pada worker dengan menggunakan command 'sudo mount <server host>:<lokasi shared folder di server> <lokasi shared folder di client>'

Worker1

```
dina@ekaratna-VirtualBox:~$ sudo mkdir /home/pempar
dina@ekaratna-VirtualBox:~$ sudo mount master:/home/pempar /home/pempar
```

Worker2

```
dina@almirah-VirtualBox:~$ sudo mkdir /home/pempar
dina@almirah-VirtualBox:~$ sudo mount master:/home/pempar /home/pempar
```

Worker3

```
dina@nabilla-VirtualBox:~$ sudo mkdir /home/pempar
dina@nabilla-VirtualBox:~$ sudo mount master:/home/pempar /home/pempar
```

#### **7. MPI**

MPI adalah singkatan dari "Message Passing Interface." Ini adalah standar komunikasi yang digunakan dalam pemrograman paralel, terutama dalam pemrograman terdistribusi untuk sistem berbasis kluster atau superkomputer.

Melakukan instalasi MPI dengan command 'sudo apt install openmpi-bin libopenmpidev'

```
dinagnabilia-VirtualBox:-$ sudo apt install openmpi-bin libopenmpi-dev
Reading package lists... Done
Building dependency tree
Building dependency tree
Gloving packages were automatically installed and are no longer required:
airi.2-pack.-1 & girl.2-sangd-1
Unbinusofnware itoremove' to remove them.
The following packages were automatically installed:
autotools-dev gcc gcc-7 ibverbs-providers libasand libatomici libc-dev-bin libco-dev libcilkrts$ libfabrici libgc-7-dev libhuloc-dev
libhuloc-jugins libhulocs libibverbs-dev libbverbs: libitni liblsand liblidi-dev libnyx2 libni-route-3-200 libnuma-dev libopenmpi2
libpsn-infinipathi libquadnatho librdmacni libtool libtsand libubsand linux-libc-dev vanpages-dev oct-tcd-libopencli openmpi-common
Supgested packages:
gcc-multilb make autoconf automake flex bison gcc-doc gcc-7-multilib gcc-7-doc gcc-7-locales libgcci-dbg libponpi-dbg libtini-dbg
librahamilibrahamilibrahamilibrahamilibrahamilibrahamilibrahamilibrahamilibrahamilibrahamilibrahamilibrahamilibrahamilibrahamilibrahamilibrahamilibrahamilibrahamilibrahamilibrahamilibrahamilibrahamilibrahamilibrahamilibrahamilibrahamilibrahamilibrahamilibrahamilibrahamilibrahamilibrahamilibrahamilibrahamilibrahamilibrahamilibrahamilibrahamilibrahamilibrahamilibrahamilibrahamilibrahamilibrahamilibrahamilibrahamilibrahamilibrahamilibrahamilibrahamilibrahamilibrahamilibrahamilibrahamilibrahamilibrahamilibrahamilibrahamilibrahamilibrahamilibrahamilibrahamilibrahamilibrahamilibrahamilibrahamilibrahamilibrahamilibrahamilibrahamilibrahamilibrahamilibrahamilibrahamilibrahamilibrahamilibrahamilibrahamilibrahamilibrahamilibrahamilibrahamilibrahamilibrahamilibrahamilibrahamilibrahamilibrahamilibrahamilibrahamilibrahamilibrahamilibrahamilibrahamilibrahamilibrahamilibrahamilibrahamilibrahamilibrahamilibrahamilibrahamilibrahamilibrahamilibrahamilibrahamilibrahamilibrahamilibrahamilibrahamilibrahamilibrahamilibrahamilibrahamilibrahamilibrahamilibrahamilibrahamilibrahamilibrahamilibrahamilibrahamilibrahamilibrahamilibrahamilibrahamilibrahamilibra
```

### > Testing

Dilakukan di master, membuat file python di folder sebelumnya, dengan command 'touch < nama file > .py'

```
dina@khairunnisa-VirtualBox:/home/pempar$ sudo chmod -R 777 /home/pempar
dina@khairunnisa-VirtualBox:/home/pempar$ touch test.py
dina@khairunnisa-VirtualBox:/home/pempar$
```

Lalu, dapat melakukan pengeditan dalam file dengan menggunakan command 'nano <nama file>.py'

```
dina@khairunnisa-VirtualBox:/home/pempar$ nano test.py
```

#### 8. Konfigurasi python

#### > Install python

Melakukan instalasi python versi 3 dengan menggunakan command 'sudo apt install python3-pip' dan python versi 2 dengan menggunakan command 'sudo apt install python-pip'

```
dinagkhairunnisa-VirtualBox:/home/pempar$ sudo apt install python3-pip
[sudo] password for dina:
Reading package lists... Done
Building dependency tree
Reading state information... Done
The following packages were automatically installed and are no longer required:
girl.2-goa-1.0 girl.2-snapd-1
Use 'sudo apt autoremove' to remove them.
The following additional packages will be installed:
build-essential dh-python dpkg-dev fakeroot g++ g++7 libalgorthm-diff-perl
libalgorithm-diff-xs-perl libalgorithm-erge-perl libexpati-dev libfakeroot libpython3-dev
libpython3.6-dev libstdc++-7-dev make python-pip-whi python3-dev python3-distutils
python3-libbto3 python3-setuptools python3-wheel python3-6-dev
Suggested packages:
debian-keyring g++-multilib g++-7-multilib gcc-7-doc libstdc++6-7-dbg libstdc++-7-doc make-doc
python-setuptools-doc
The following NEW packages will be installed:
build-essential dh-python dpkg-dev fakeroot g++ g++-7 libalgorithm-diff-perl
libalgorithm-diff-xs-perl libalgorithm-erge-perl libexpati-dev libfakeroot libpython3-dev
libpython3.6-dev libstdc++-7-dev make python-pip-whi python3-dev python3-distutils
python3-libbto3 python3-pip python3-setuptools python3-wheel python3-dev
libpython3.6-dev libstdc++-7-dev make python-pip-whi python3-dev python3-distutils
python3-libbto3 python3-pip python3-setuptools python3-wheel python3-de-v
libpython3-6-dev libstdc++-7-dev nake python-pip-whi python3-dev
libgoraded, 23 newly installed, 0 to remove and 0 not upgraded.

Med to get 60,0 MB of archives.
After this operation, 131 MB of additional disk space will be used.

Do you want to continue? [V/n]

dinagkhairunnisa-VirtualBox:-$ sudo apt install python-pip
Reading package sure automatically installed and are no longer required:
girl.2-goa-1.0 girl.2-snapd-1
Use 'sudo apt autoremove' to remove then.

The following packages were automatically installed and are no longer required:
girl.2-goa-1.0 girl.2-snapd-1
Use 'sudo apt autoremove' to remove then.

The following packages were automatically installed and are
```

#### Install pustaka MPI4

Melakukan instalasi pustaka MPI4 yang menyediakan dukungan untuk komunikasi dan pemrograman paralel menggunakan MPI (Message Passing Interface) dapat dilakukan dengan command 'pip install mpi4py'

#### > Input kunci

Dilakukan oleh master untuk menyalin kunci publik SSH ke mesin worker sehingga master dapat masuk ke mesin worker tanpa diminta kata sandi setiap kali menggunakan command 'ssh-copy-id'

#### Master – worker1

#### Master – worker2

```
dina@master:~$ ssh-copy-id dina@worker2
/usr/bin/ssh-copy-id: INFO: Source of key(s) to be installed: "/home/dina/.ssh/
ines sa.pub"
/usr/bin/ssh-copy-id: INFO: attempting to log in with the new key(s), to filter
out any that are already installed
/usr/bin/ssh-copy-id: INFO: 1 key(s) remain to be installed -- if you are promp
ted now it is to install the new keys
dina@worker2's password:

Number of key(s) added: 1

Now try logging into the machine, with: "ssh 'dina@worker2'"
and check to make sure that only the key(s) you wanted were added.
```

#### • Master – worker3

```
lina@master:~$ ssh-copy-id dina@worker3
/usr/bin/ssh-copy-id: INFO: Source of key(s) to be installed: "/home/dina/.ssh/
.d_rsa.pub"
/usr/bin/ssh-copy-id: INFO: attempting to log in with the new key(s), to filter
out any that are already installed
/usr/bin/ssh-copy-id: INFO: 1 key(s) remain to be installed -- if you are promp
```

#### > Testing

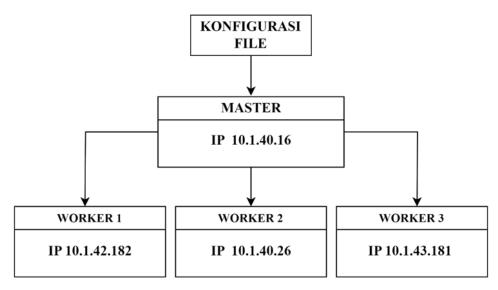
Melakukan uji coba untuk menghasilkan perintah dasar python pada setiap device dengan hasil output "Hello, World!" dengan menggunakan command 'mpirun -np <jumlah prosesor> -host <daftar host> python3 test.py'

```
dina@master:~$ mpirun -n 4 -host master,worker1,worker2,worker3 python3 -m mpi4
py.bench helloworld
Hello, World! I am process 0 of 4 on master.
Hello, World! I am process 1 of 4 on worker1.
Hello, World! I am process 2 of 4 on worker2.
Hello, World! I am process 3 of 4 on worker3.
```

#### 9. Numerik

Numerik mengacu pada bidang matematika yang berkaitan dengan representasi, manipulasi, dan analisis angka (bilangan) serta metode perhitungan yang diterapkan pada masalah matematika atau ilmiah dalam bentuk numerik. Beberapa konsep umum dalam konteks numerik melibatkan representasi angka dalam bentuk biner, operasi aritmetika, analisis numerik, dan pemecahan masalah dengan menggunakan komputasi.





#### > Eliminasi Gaussian

Eliminasi Gaussian, juga dikenal sebagai metode eliminasi Gauss atau eliminasi Gauss-Jordan, adalah suatu metode dalam aljabar linier yang digunakan untuk menyelesaikan sistem persamaan linear dan untuk menemukan invers matriks. Tujuan utama dari metode ini adalah untuk mentransformasikan matriks koefisien dari sistem persamaan linear menjadi bentuk matriks segitiga atas atau bentuk matriks segitiga bawah untuk kemudian melakukan substitusi mundur atau substitusi maju guna mendapatkan solusi sistem persamaan tersebut.

```
bird Mail []
for j in range(kolom):
    matrix.append(0)
A.append(matrix)
                 i in range(baris):
print("Masukkan persamaan ke-%d" % (i + 1))
for j in range(0, kolon):
    A[l][j] = int(input(f"Masukkan angka barts-{i + 1} kolon-{j + 1}: "))
         processes = []
num_processes = 4
rows_per_process = baris // num_processes
       for i in range(num_processes):
    start_row = i * rows_per_process
    end_row = (i + i) * rows_per_process
    if i < num_processes - 1 else barts
    process = nultiprocessing.Process(target=gaussian_elimination_partial, args=(A, start_row, end_row, i))
    processes.append(process)</pre>
         for process in processes:
    process.join()
             d time = time.time()
               t in range(0, barts):
for j in range(0, kolom):
    print("%4.2f" % (A[t][j]), end=" ")
print("\n")
         x3 = A[2][3]
x2 = A[1][3] - A[1][2] * x3
x1 = A[0][3] - A[0][2] * x3 - A[0][1] * x2
print("x1= x4.2f \nx2= x4.2f \nx3= x4.2f" % (x1, x2, x3))
         elapsed_time = end_time - start_time
print("Total execution time for all processes: %f seconds" % elapsed_time)
  dina@master:~$ sudo nano numerik.py
dina@master:~$ mpirun -n 1 -host master,worker1,worker2,worker3 python3 numerik.py
  Masukkan ordo matrix :
Masukkan ordo matrix : 3
Masukkan persamaan ke-1
Masukkan angka baris-1 kolom-1: 1
Masukkan angka baris-1 kolom-2: 2
Masukkan angka baris-1 kolom-4: 4
Masukkan angka baris-1 kolom-4: 4
Masukkan persamaan ke-2
Masukkan angka baris-2 kolom-1: 4
Masukkan angka baris-2 kolom-3: 2
Masukkan angka baris-2 kolom-3: 2
Masukkan angka baris-2 kolom-4: 1
Masukkan angka baris-3 kolom-1: 2
Masukkan persamaan ke-3
Masukkan angka baris-3 kolom-1: 2
Masukkan angka baris-3 kolom-2: 4
Masukkan angka baris-3 kolom-3: 7
Masukkan angka baris-3 kolom-4: 9
Process 0 execution time: 6.67572021484375e-06 seconds
Process 1 execution time: 7.62939453125e-06 seconds
Process 2 execution time: 1.5020370483398438e-05 seconds
Process 3 execution time: 3.743171691894531e-05 seconds
1.00 2.00 3.00 4.00
  4.00 3.00 2.00 1.00
  2.00 4.00 7.00 9.00
  x1= 11.00
x2= -17.00
x3= 9.00
Total execution time for all processes: 0.033666 seconds
```

#### ➤ Newton – Raphson

Metode Newton-Raphson, juga dikenal sebagai metode Newton, adalah metode iteratif untuk menemukan akar dari suatu fungsi matematis. Metode ini menggunakan pendekatan linear untuk mendekati akar fungsi dan memerlukan turunan pertama dari fungsi tersebut. Metode Newton-Raphson dapat digunakan untuk menemukan akar persamaan nonlinier dan memiliki konvergensi cepat jika titik awal yang dipilih cukup dekat dengan akar sejati.

```
GNU nano 2.9.3
                                                                                  numerik2.pv
<mark>lmport</mark> multiprocessing
import time
def f1(x):
return x ** 2 - 20
lef det_f1(x):
    return 2 * x
   newton_raphson(func, d_func, x, tolerence, max_iterations, real_root=None, process_id=θ):
   if d_func(x) == θ:
        print("Newton-Raphson gagal dijalankan pada proses {θ}.".format(process_id))
        return None
else:
UbuntusOftwareions = 1
    start_time = time.time()
    while abs(func(x) / d_func(x)) >= tolerence and iterations <= max_iterations:
        current_iteration_print = "Proses {0}, Iterast : {1}".format(process_id, iterations)
    if func(x) == 0:
        print(current_iteration_print + ", Solusi ditemukan : {0}".format(x))
        return x</pre>
              x = x - func(x) / d_func(x)
if d_func(x) == 0:
    print("Newton-Raphson gagal dijalankan pada proses {0}.".format(process_id))
                    return None
               current_iteration_print += ", {0}".format(x)
              end_time = time.time()
elapsed_time = end_time - start_time
current_iteration_print += ", Waktu per Iterasi: {0} detik".format(elapsed_time)
              print(current_iteration_print)
         print("\nProses {0}, Jumlah iterasi : ".format(process_id), iterations)
print("Proses {0}, Hasil akhir : ".format(process_id), x)
    _name__ == '__main__':
processes = []
inputs = [(f1, det_f1, 1.5, 0.00001, 30, 1, i) for i in range(4)] # 4 proses
    for input_data in inputs:
    p = multiprocessing.Process(target=newton_raphson, args=input_data)
    processes.append(p)
    p.start()
dina@master:~$ mpirun -n 1 -host master,worker1,worker2,worker3 python3 numerik2.py
Proses 1, Iterasi : 1, 7.416666666666667, Waktu per Iterasi: 6.29425048828125e-05 detik
Proses 0, Iterasi : 1, 7.416666666666667, Waktu per Iterasi: 4.57763671875e-05 detik
Proses 3, Iterasi : 1, 7.416666666666667, Waktu per Iterasi: 4.9591064453125e-05 detik
Proses 1, Iterasi : 2, 5.056647940074907, Waktu per Iterasi: 0.003101825714111328 detik
Proses 2, Iterasi : 1, 7.41666666666667, Waktu per Iterasi: 4.9591064453125e-05 detik
Proses 1, Iterasi : 3, 4.505918637197902, Waktu per Iterasi: 0.003255128860473633 detik
Proses 2, Iterasi : 2, 5.056647940074907, Waktu per Iterasi: 0.002245187759399414 detik
Proses 1, Iterasi : 4, 4.472262596169605, Waktu per Iterasi: 0.0034024715423583984 detik
Proses 2, Iterasi : 3, 4.505918637197902, Waktu per Iterasi: 0.002353668212890625 detik
Proses 2, Iterasi : 4, 4.472262596169605, Waktu per Iterasi: 0.0023949146270751953 detik
Proses 1, Iterasi : 5, 4.47213595679263, Waktu per Iterasi: 0.003534555435180664 detik
Proses 2, Iterasi : 5, 4.47213595679263, Waktu per Iterasi: 0.00249481201171875 detik
Proses 1, Jumlah iterasi : 6
Proses 2, Jumlah iterasi : Proses 1, Hasil akhir : 4.47213595679263
 6
Proses 2, Hasil akhir : 4.47213595679263
Proses 0, Iterasi : 2, 5.056647940074907, Waktu per Iterasi: 0.0020194053649902344 detik
Proses 0, Iterasi : 3, 4.505918637197902, Waktu per Iterasi: 0.002707242965698242 detik
Proses 0, Iterasi : 4, 4.472262596169605, Waktu per Iterasi: 0.0027680397033691406 detik
Proses 0, Iterasi : 5, 4.47213595679263, Waktu per Iterasi: 0.002811908721923828 detik
Proses 0, Jumlah iterasi :
Proses 0, Hasil akhir : 4.47213595679263
Proses 3, Iterasi : 2, 5.056647940074907, Waktu per Iterasi: 0.002415895462036133 detik
Proses 3, Iterasi : 3, 4.505918637197902, Waktu per Iterasi: 0.0024902820587158203 detik
Proses 3, Iterasi : 4, 4.472262596169605, Waktu per Iterasi: 0.0025358200073242188 detik
Proses 3, Iterasi : 5, 4.47213595679263, Waktu per Iterasi: 0.0025768280029296875 detik
Proses 3, Jumlah iterasi :
Proses 3, Hasil_akhir : 4.47213595679263
```