



## Antibiotic-induced population fluctuations and stochastic clearance of bacteria

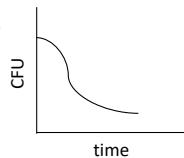
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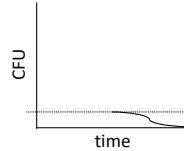
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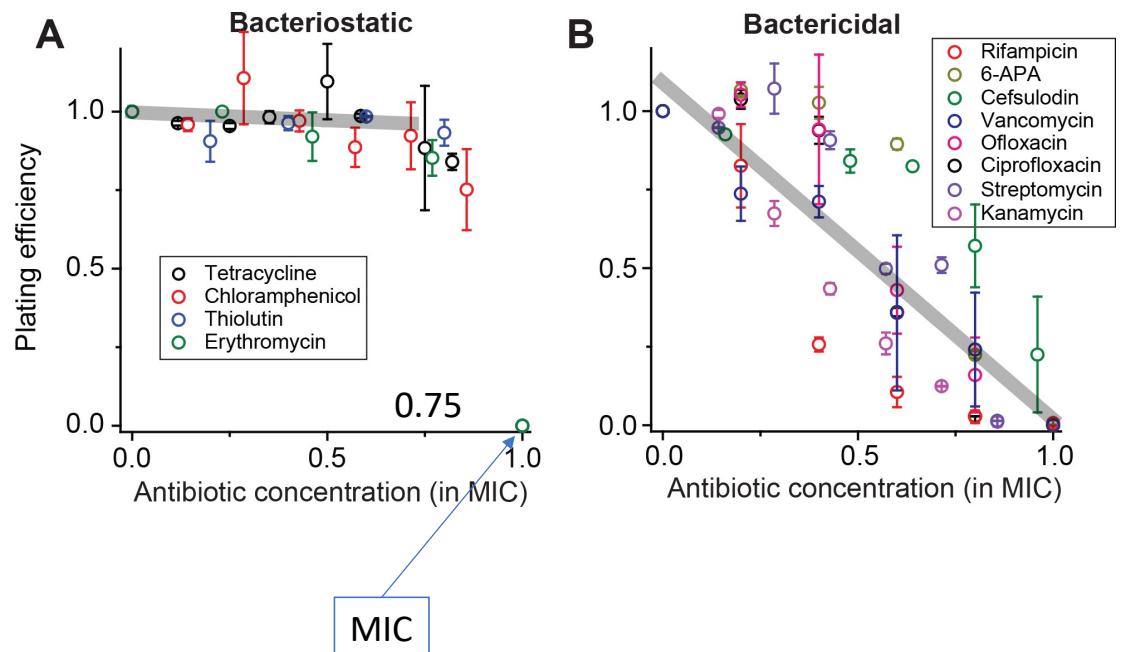
Deterministic models of population dynamics successfully predict **large to small** kill curves under antibiotic treatment.



Due to **experimental detection limits**, these models have never been tested on **small to zero** kill curves.



# Figure 1: Bacteriostatic deterministic, but bactericidal not



*E. coli* dynamics by plating efficiency:  $\frac{\text{CFU}_{\text{abx}}}{\text{CFU}_{\text{nodrug}}}$

# Figure 2: Homogeneous growth with static drugs

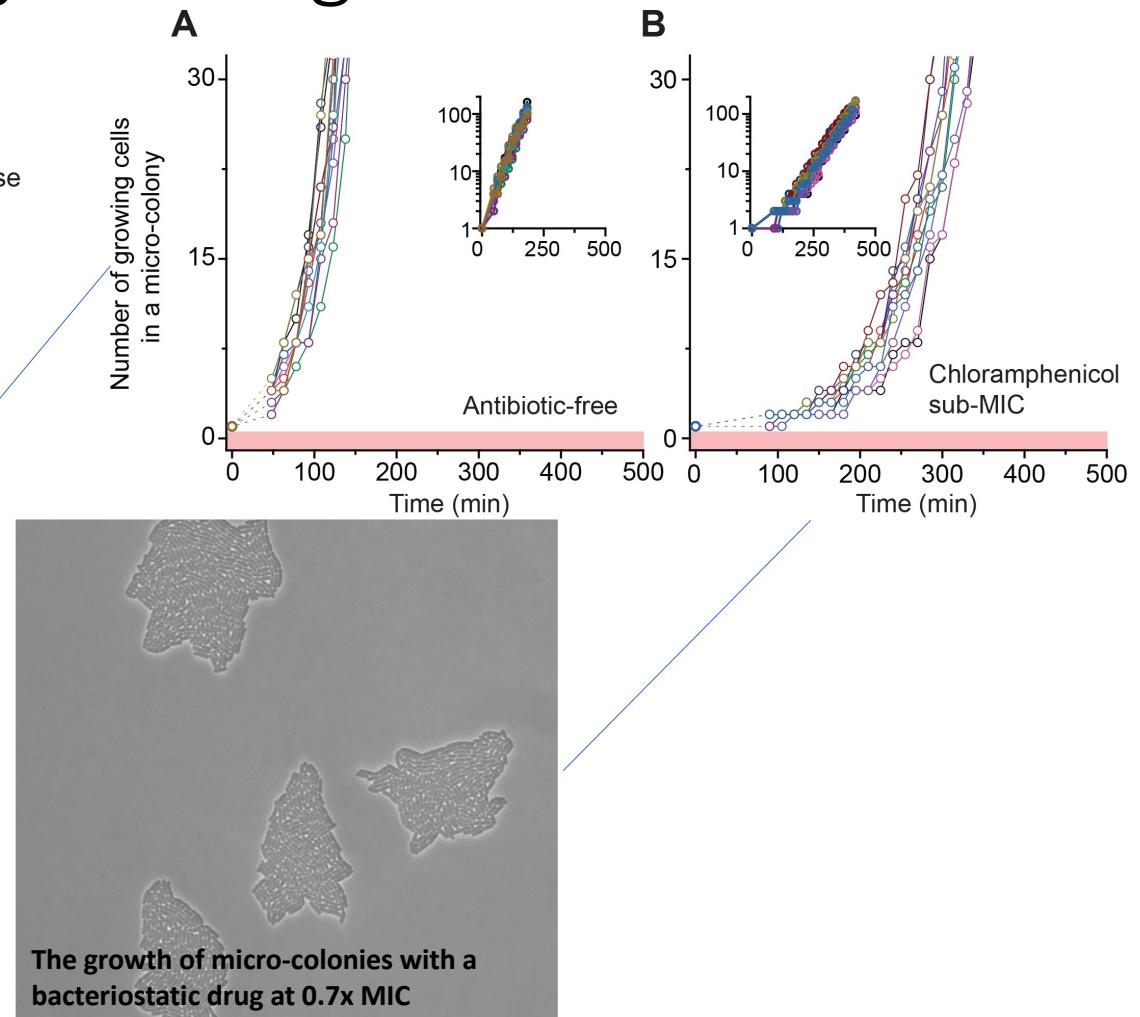
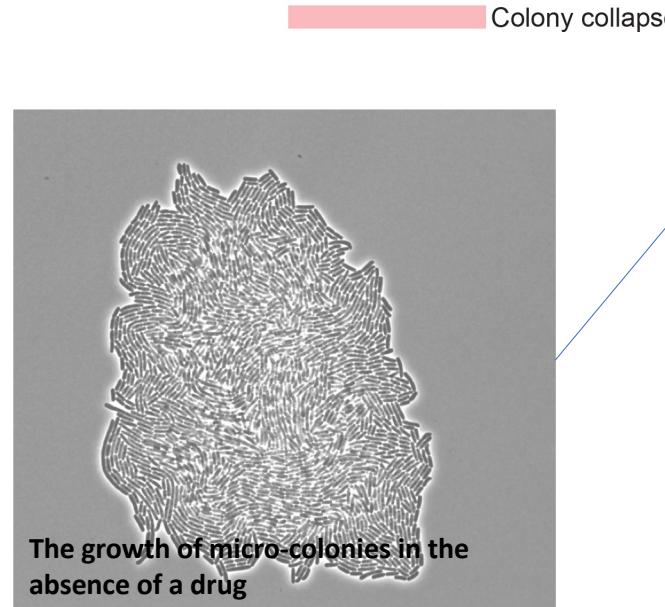
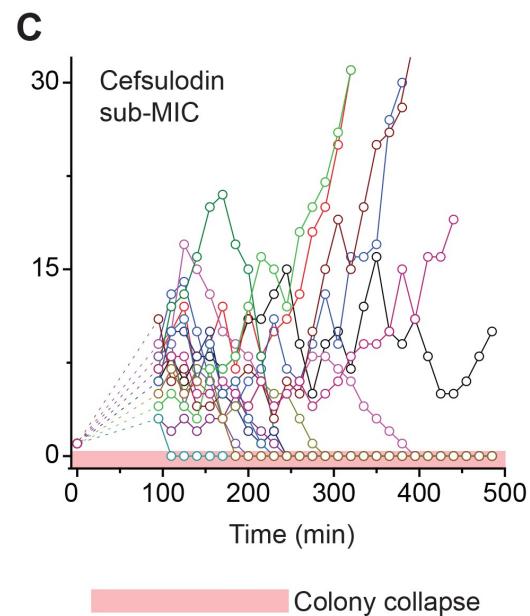
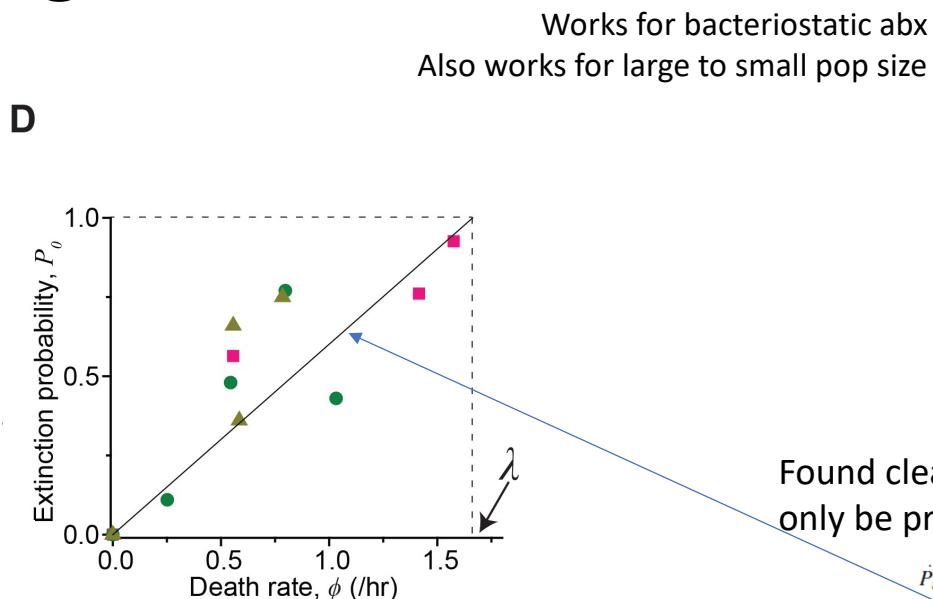


Figure 2: Stochastic fluctuations in population size with cidal drugs



# Figure 2: Probabilistic model and cidal data agree



## A deterministic model of population dynamics

If cells replicate at rate,  $\lambda$ , and die at rate,  $\phi$ , a general deterministic model of population growth can be described by

$$\frac{dn}{dt} = \lambda \cdot n - \phi \cdot n, \quad (\text{A1})$$

where  $n$  is the number of cells in the population. Its solution is

$$n(t) = n(0) \cdot e^{(\lambda-\phi)t}. \quad (\text{A2})$$

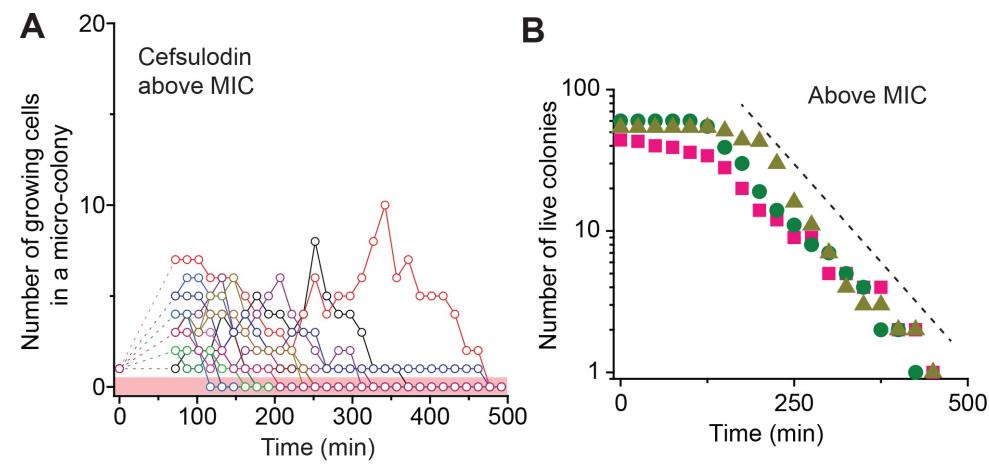
Previous studies modeled the population dynamics of bacteria exposed to antibiotics using this solution; e.g., see (Regoes et al., 2004; Czock et al., 2009). At drug concentrations below the MIC (sub-MIC), growth rate is higher than death rate ( $\lambda > \phi$ ); thus, a bacterial population grows. When the drug concentration reaches the MIC, growth rate and death rate are equal ( $\lambda = \phi$ ); thus, the population size is maintained. At drug concentrations above the MIC, growth rate is lower than death rate ( $\lambda < \phi$ ); thus, a bacterial population declines.

Found clearance of cells (small to zero) within a population can only be predicted probabilistically,

$$\dot{P}_n = \lambda(n-1)P_{n-1} - (\lambda + \phi)nP_n + \phi(n+1)P_{n+1}, \quad (\text{1})$$

The solution,  $P_0 = \Phi/\lambda$ , is shown in black, while experimental data agreement is shown in colored points.

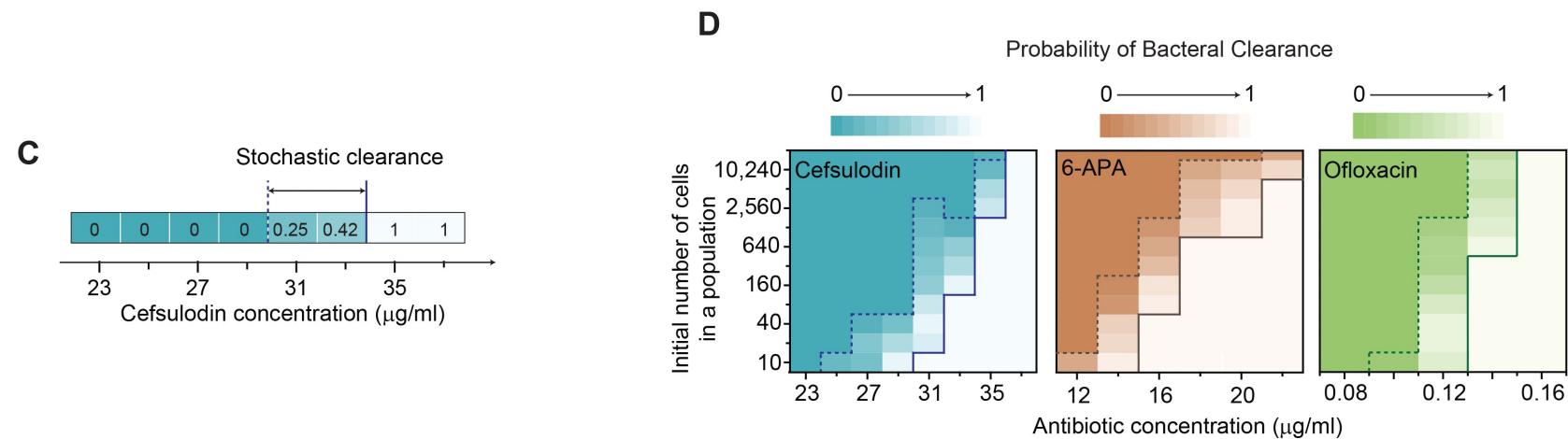
Figure 3: experimental data (above MIC) agree with model



Fluctuating extinction times

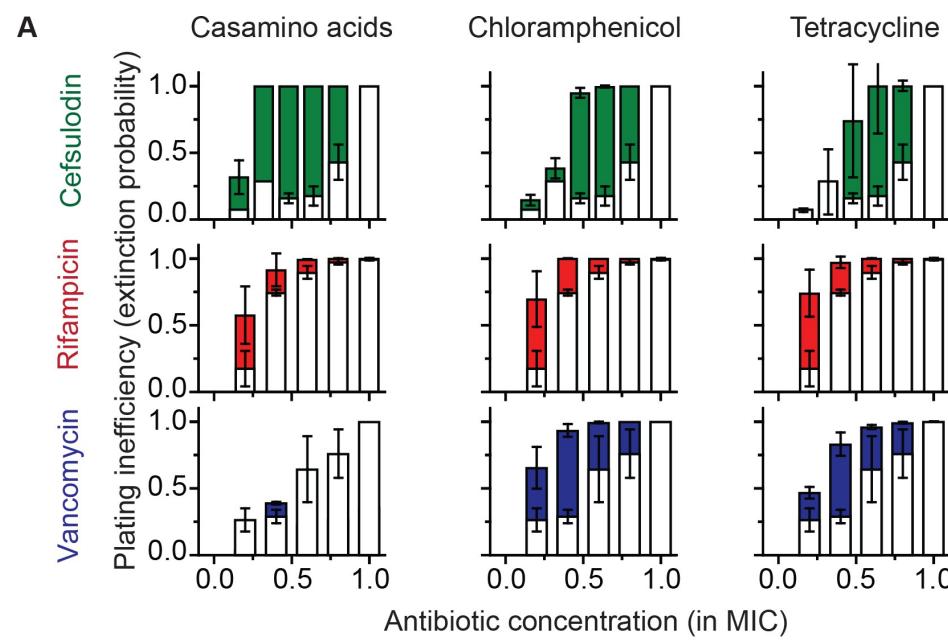
Linear log plot means exponential decay

# Figure 3: sub-MIC cidal drugs can cause stochastic extinction

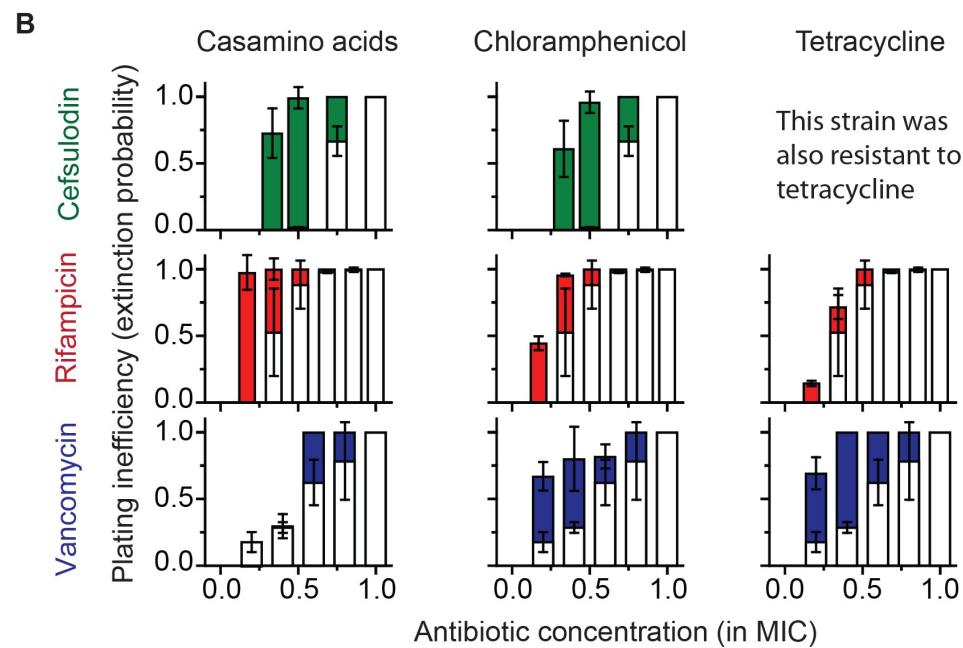


Suggests that as you decrease growth rate,  $\lambda$ , you increase the extinction probability,  $P_0$

Figure 4: used static drugs to decrease  $\lambda$  and increase  $P_0$



# Figure 4: true for RESISTANT strains as well



# Figure 1, S1: not due to heritable resistance

