htnm PYTHON LAST REVIEW

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1 INTRODUCTION TO PROGRAMMING REVIEW

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1.1 PREFACE

Thank you, my teacher, Dr. Dinh Viet Sang, I cannot learn programming in Python that much without you. This notebook uses a huge part your lectures as a guidance.

Dear Data Science & AI - K65,

This is my last notebook in order to prepare for the final exam on Introduction to Programming. If you find this notebook helpful, thanks for reading it. Some might find this one not that helpful, I highly appreciate every line of text you read, including this one.

If you find any mistake, feedback and I will try to fix it as soon as possible.

Thank y'all for supporting me all the time, good luck on all of your exams.

Best wishes,

Hoang Tran Nhat Minh.

1.2 CODES FOR ALL EXERCISES AND SOURCES

SOME OF THE FOLLOWING CONTENTS MIGHT BE ADJUSTED OVER TIME.

Code for all exercises:

https://github.com/htnminh/python-ex-intro-to-prog

Source of this documentation:

https://github.com/htnminh/pdf-python-books-docs/tree/main/PYTHON%20LAST%20REVIEW

Source of this Colab Notebook:

https://colab.research.google.com/drive/1mjtoDbqNHKB2bAb6rTUU8hiJRfUX3Ryt?usp=sharing

2 CHAPTER 1: INTRODUCTION

2.1 CONSTANTS

```
[1]: # CONSTANTS
print('Hello World')
print(12.3)

Hello World
12.3
```

2.2 VARIABLES

```
[2]: # VARIABLES
x = 13.4
y = 4.3
x = 'Hello'
print(x)
print(y)
```

Hello 4.3

2.3 NUMERIC OPERATORS

```
[3]: # NUMERIC OPERATORS

print(5 ** 3.5)

print(19 / 5)

print(19 // 5)

print(19 % 5)

279.5084971874737
```

3.8

2.4 SCIENTIFIC NOTATION

```
[4]: # SCIENTIFIC NOTATION
print(1.234e2)
print(1.234E+2)
print(1.234e-3)
```

123.4 123.4 0.001234

4

2.5 INT AND FLOAT

```
[5]: # INT AND FLOAT
print(1 + 5.3)
print(5 / 5)
print(3 + 5)
6.3
1.0
8
```

2.6 TYPES

```
[6]: # TYPES
    print(3 + 6)
    print('hello' + ' there')

    print(type(3.5))
    print(type('?'))

    print(str(4) + str(5))
    print(int('8'))

9
    hello there
    <class 'float'>
    <class 'str'>
    3.0
    45
    8
```

2.7 (INPUT) TYPE DIFFERENCES

```
[7]: # TYPE DIFFERENCES
a = input('a = ')
print(a * 5)
print(int(a) * 5)

a = 8
88888
40
```

2.8 (INPUT) FILE NAME

```
[8]: # FILE NAME
name = input('Name = ')
#/content/sample_data/README.md
f = open(name, 'r')
```

```
print(f.read())
f.close()
```

Name = /content/sample_data/README.md

This directory includes a few sample datasets to get you started.

* `california_housing_data*.csv` is California housing data from the 1990 US Census; more information is available at:

 ${\tt https://developers.google.com/machine-learning/crash-course/california-housing-data-description}$

- * `mnist_*.csv` is a small sample of the [MNIST database](https://en.wikipedia.org/wiki/MNIST_database), which is described at: http://yann.lecun.com/exdb/mnist/
- * `anscombe.json` contains a copy of [Anscombe's quartet](https://en.wikipedia.org/wiki/Anscombe%27s_quartet); it was originally described in

Anscombe, F. J. (1973). 'Graphs in Statistical Analysis'. American Statistician. 27 (1): 17-21. JSTOR 2682899.

and our copy was prepared by the

[vega_datasets library](https://github.com/altair-viz/vega_datasets/blob/4f6 7bdaad10f45e3549984e17e1b3088c731503d/vega_datasets/_data/anscombe.json).

3 CHAPTER 2: CONTROL FLOW

3.1 COMPARISON OPERATORS

[9]: # COMPARISON OPERATORS print(3 == 4) print(3 != 4) print(3 < 4) print(3 >= 4)

False

True

True

False

3.2 LOGIC OPERATORS

```
[10]: # LOGIC OPERATORS
    print(not False)
    print(True and False)
    print(True or False)
```

True False True

3.3 (INPUT) BRANCHING

```
[11]: # BRANCHING
    a = int(input('a = '))
    b = int(input('b = '))
    if a > b:
        print('larger')
    elif a == b:
        print('equal')
    else:
        print('less')
a = 3
b = 5
less
```

4 CHAPTER 3: FUNCTIONS

4.1 FUNCTION EXAMPLE

```
# FUNCTION EXAMPLE

# name parameter(s)
def two_time(number):
    # docstring
    '''
    2 times a number
    '''
    # body
    doubled = 2 * number
    # returns (if not, it is a void function)
    return doubled
# function call, pass argument(s) to parameter(s)
print(two_time(8))

print(two_time.__doc__)
```

16

2 times a number

4.2 COMMON BUILT-IN PYTHON FUNCTIONS

```
[13]: # COMMON BUILT-IN PYTHON FUNCTIONS
      # previous ones: input(), type(), float(),...
      print(max(6, 8, 5))
      print(min(3, 6, 7))
     8
     3
```

4.3 PASS-BY-OBJECT-REFERENCE

```
[14]: # PASS-BY-OBJECT-REFERENCE
      # Immutable objects: int, float, complex, string, tuple, frozen set, bytes
      # Mutable objects: list, dict, set, byte array
      def change_num(num):
          num += 1
      a = 4
      print(a)
      change_num(a)
      print(a)
      def change_lst(lst):
          lst.append('changed')
      1 = ['original']
      print(1)
      change_lst(1)
      print(1)
     4
     ['original']
```

['original', 'changed']

4.4 SCOPE

```
[15]: # SCOPE
     def f(x):
         x += 1
         print('In f: x = ',x)
     x = 0
     print('First: x =', x)
     f(x)
     print('After f: x =', x)
     First: x = 0
```

In f: x = 1After f: x = 0

4.5 FUNCTIONS AS ARGUMENTS

```
[16]: # FUNCTIONS AS ARGUMENTS
def triple(num):
    return 3 * num
def square(num):
    return num ** 2

def fx_plus_gy(f, x, g, y):
    return f(x) + g(y)

print(fx_plus_gy(triple, 5, square, 8))
print(3 * 5 + 8 ** 2)
79
79
```

4.6 DEFAULT PARAMETER VALUE

```
[17]: # DEFAULT PARAMETER VALUE
def tong(a, b = 2, c = 3):
    return a + b + c

print(tong(1))
# 1 + 2 + 3
print(tong(1, 4))
# 1 + 4 + 3
print(tong(0, 3, 6))
# 0 + 3 + 6
```

4.7 LAMBDA FUNCTION

```
[18]: # LAMBDA FUNCTION
  tong = lambda x, y: x + y
  print(tong(3, 5))
  print((lambda x, y: x * y)(2, 9))
```

8 18

8

4.7.1 LAMBDA EXAMPLE

```
[19]: # LAMBDA EXAMPLE
def multiply_by(n):
    return lambda x: x * n
```

```
double = multiply_by(2)
# multiply_by(2) -> lambda x: x * 2
# -> a doubling function
triple = multiply_by(3)

print(double(16))
print(triple(4))
```

32 12

4.7.2 TEST: WITHOUT LAMBDA

```
[20]: # TEST: WITHOUT LAMBDA
def multiply_by(n):
    def multi(x):
        return x * n
    return multi

double = multiply_by(2)
# multiply_by(2) -> function: multi, where multi return the doubled argument
# -> a doubling function
triple = multiply_by(3)

print(double(16))
print(triple(4))
```

32 12

4.7.3 LAMBDA EXAMPLE

```
[21]: # LAMBDA EXAMPLE

x_plus_fx = lambda x, f: x + f(x)

print(x_plus_fx(3, lambda x: x ** 2))

# x + f(x) = x + x ** 2

# 3 + f(3) = 3 + 3 ** 2
```

12

4.8 RECURSION EXAMPLES

```
[22]: # RECURSION EXAMPLES

def pr(n):
    print(str(n) + '! = ' + str(n - 1) + '! * ' + str(n))

def factorial(n):
```

```
if n == 0:
    print('0! = 1')
    return 1
pr(n)
    return factorial(n - 1) * n
```

```
7! = 6! * 7

6! = 5! * 6

5! = 4! * 5

4! = 3! * 4

3! = 2! * 3

2! = 1! * 2

1! = 0! * 1

0! = 1

5040
```

4.8.1 FACTORIAL RECURSION IN SHORT

```
[23]: # FACTORIAL RECURSION IN SHORT
factorial = lambda n: 1 if n == 0 else factorial(n - 1) * n
print(factorial(7))
```

5040

4.8.2 FIBONACCI RECURSION IN SHORT

```
[24]: # FIBONACCI RECURSION IN SHORT
fib = lambda n: n if n <= 1 else fib(n - 1) + fib(n - 2)
print(*[fib(i) for i in range(15)])</pre>
```

0 1 1 2 3 5 8 13 21 34 55 89 144 233 377

4.8.3 (INPUT) (WARNING: WALL-OF-CODE) TOWER OF HANOI: TRADITIONAL RECURSION PROBLEM

```
[25]: # TOWER OF HANOI: TRADITIONAL RECURSION PROBLEM
    # EXPLICITLY VISUALIZED CODE

def hanoi_tower(n):
    '''run and return number of transfers as text'''
    def transfer(n, start, end, mid):
        if n == 1:
            nonlocal count
            count += 1
            map_ind = ['A', 'B', 'C']
            print(' '*18 + 'Step ' + str(count) + ': ' + map_ind[start] + ' ->___
            →' + map_ind[end])
            move(start, end)
```

```
print_board()
        else:
            transfer(n - 1, start, mid, end)
           transfer(1, start, end, mid)
           transfer(n - 1, mid, end, start)
   count = 0
   transfer(n, 0, 2, 1)
   return count
111
a =
     0 1 2 3
     4 3 2 1
1
      0 0 0 0
     0 0 0 0
printed:
               A \quad B \quad C
               1 . .
                2 . .
                3 . .
                4 . .
111
def print_board():
   '''print current board'''
   print('| A B C |')
   for col in range(n - 1, -1, -1):
       print('| ', end = '')
       for row in range(3):
            character = '.' if a[row][col] == 0 else a[row][col]
            print(str(character) + ' ', end = '')
       print('|')
def move(row_start, row_end):
   '''make a move'''
   def col_lastnonenull(row):
       for col_ind in range(n - 1, -1, -1):
            if a[row] [col_ind] != 0:
                return col_ind
            # return n - 1
   def col_firstnull(row):
        for col_ind in range(n):
            if a[row][col_ind] == 0:
```

```
return col_ind
            # return 0
    a[row_end][col_firstnull(row_end)] =__
 →a[row_start][col_lastnonenull(row_start)]
    a[row_start][col_lastnonenull(row_start)] = 0
# MAIN:
# input n
n = int(input('n = '))
# initialize list of list, n = 4,
a =
      0 1 2 3
      4 3 2 1
1
      0 0 0 0
2
      0 0 0 0
a = [[n - i for i in range(n)]]
for i in range(2):
    a.append([0 for j in range(n)])
# print the initialized board
print()
print_board()
# run, print the board every move and return the result
print('\nNumber of transfers: %i' % hanoi_tower(n))
# n SHOULD BE LESS THAN 5
n = 4
 A B C I
  1 . .
  3 . .
                 Step 1: A -> B
  A B C
  2
                 Step 2: A -> C
| A B C |
```

```
3
                 Step 3: B -> C
  3
        2
                 Step 4: A -> B
     В
        1
                 Step 5: C -> A
                 Step 6: C -> B
  A B
  1 2
                 Step 7: A -> B
     1
     2
                 Step 8: A -> C
     В
     2
                 Step 9: B -> C
     В
        С
                 Step 10: B -> A
I A B C
```

```
3
              Step 11: C -> A
A B C
1
2 3
              Step 12: B -> C
A B C
1
              Step 13: A -> B
A B
              Step 14: A -> C
A B C
     3
              Step 15: B -> C
A B
     2
     3
```

Number of transfers: 15

5 CHAPTER 4: STRINGS

5.1 STRING EXAMPLES

```
[26]: # STRING EXAMPLES
print('abc')
```

abc

5.2 len() OF A STRING

```
[27]: # LEN OF A STRING
print(len('this is a string'))
16
```

5.3 LOOP OVER A STRING

```
[28]: # LOOP OVER A STRING
    for c in 'hi there?':
        print(c)

h
    i

t
    h
    e
    r
    e
    r
    e
    ?
```

5.4 SLICING A STRING

hello

```
[29]: # SLICING A STRING
    print('abcd'[2])
    print('mnpq'[1:])
    print('hello from the other side'[:5])

c
    npq
```

5.5 STRING FORMATTING OPERATOR %

```
[30]: # STRING FORMATTING OPERATOR %
print('%s is a metal' % 'gold')

color = 'yellow'
num = 7
print( '%s is a color of %d main colors in a rainbow!' % (color, num) )

# %s string | %c char | %d decimal | %i integer | %f float
```

```
gold is a metal
yellow is a color of 7 main colors in a rainbow!
```

5.5.1 STRING FORMATTING OPERATOR % EXAMPLE

```
[31]: # STRING FORMATTING OPERATOR % EXAMPLE
# https://docs.python.org/3/library/string.html
print('%.2f' % 3.895)
```

3.90

5.6 in OPERATOR

```
[32]: # in OPERATOR print('e' in 'hello')
```

True

5.7 STRING COMPARISON

```
[33]: # STRING COMPARISON
  print('abc' > 'def')
  print('abc' > 'd')
  print('axyz' < 'bcde')</pre>
```

False False True

5.8 THE DIRECTORY FUNCTION dir()

```
[34]: # THE DIRECTORY FUNCTION dir()
s = '????''
print('...',*dir(s)[30:38], '...\nand a lot more!')
```

```
... __sizeof__ __str__ _subclasshook__ capitalize casefold center count encode
...
and a lot more!
```

5.9 IMPORTANT FUNCTIONS AND METHODS

5.9.1 capitalize(), center()

```
[35]: # capitalize(), center()
    print('hello'.capitalize())
    print('hello'.center(14))
    print('hello'.center(20, '*'))
```

Hello hello

******hello*****

```
5.9.2 endswith(), startswith()
```

```
[36]: # endswith(), startswith()
     print('hello'.endswith('o'))
     print('hello'.endswith('o', 1, 4))
           01234
     # search from 1 to 3 = 'ell'
     print()
     print('hello'.startswith('h'))
     print('hello'.startswith('e', 1, 4))
     # 01234
     # search from 1 to 3 = 'ell'
    True
    False
    True
    True
    5.9.3 find()
[37]: # find()
     print('hello'.find('l'))
     print('hello'.find('l', 3, 5))
     # 01234
    2
    3
    5.9.4 lstrip(), rstrip(), strip()
[38]: # lstrip(), rstrip(), strip()
     def pr(s):
        print('"%s"' % s)
     pr(' hello '.lstrip())
     pr('***_ hello __***** '.lstrip('*'))
     print()
     pr(' hello '.rstrip())
     pr('***_ hello __***** '.rstrip('*'))
     print()
     pr(' hello '.strip())
     print()
    "hello
```

```
hello __**** "
          hello"
              hello __**** "
     "hello"
     "__ hello __**** "
     5.9.5 join()
[39]: # join()
      wrdlst = ['hello', 'from', 'the', 'other', 'side']
      print('_'.join(wrdlst))
      wrdset = {'hello', 'from', 'the', 'other', 'side'}
     print('-'.join(wrdset))
     hello_from_the_other_side
     the-other-from-side-hello
     5.9.6 replace()
[40]: # replace()
      print('hello, long time no see'.replace('l', '*'))
      print('hello, long time no see'.replace('l', '*', 2))
      # only the 2 first ones are replaced
     he**o, *ong time no see
     he**o, long time no see
     5.9.7 lower(), upper()
[41]: # lower(), upper()
      print('hEL10'.lower())
      print('hEL10'.upper())
     hello
     HELLO
```

6 CHAPTER 5: LISTS, SETS, DICTIONARIES AND TUPLES 6.1 LISTS

6.1.1 LIST EXAMPLE

3 4 5 6 7

3 6 8 6 4

```
[42]: # LIST EXAMPLE
     lst = ['a', 8, 'bc', 'd', [15, 6]]
     print(lst)
     ['a', 8, 'bc', 'd', [15, 6]]
     6.1.2 LOOP A LIST
[43]: # LIST LOOPS
     for ele in lst:
         print(ele)
     a
     8
     bc
     d
     [15, 6]
     6.1.3 LISTS ARE MUTABLE
[44]: # LISTS ARE MUTABLE
     lst[0] = '^_^'
     print(lst)
     ['^_^', 8, 'bc', 'd', [15, 6]]
     6.1.4 len() OF A LIST
[45]: # len OF A LIST
     print(len(lst))
     print(lst.__len__())
     5
     5
     6.1.5 THE range() FUNCTION
[46]: # THE range() FUNCTION
     print(*range(8))
     print(*range(3, 8))
     print(*range(3, 8, 3))
     print(*range(8, 3, -2))
     0 1 2 3 4 5 6 7
```

6.1.6 CONCATENATING LISTS USING +

```
[47]: # CONCATENATING LISTS USING +
     print(lst)
     print(lst + [7, 3, 'h'])
     ['^_^', 8, 'bc', 'd', [15, 6]]
     ['^_^', 8, 'bc', 'd', [15, 6], 7, 3, 'h']
     6.1.7 LIST SLICING
[48]: # LIST SLICING
      print(lst)
      print(lst[:3])
     print(lst[-2])
     ['^_^', 8, 'bc', 'd', [15, 6]]
     ['^_^', 8, 'bc']
     6.1.8 LIST METHODS AND FUNCTIONS
[49]: # LIST METHODS AND FUNCTIONS
      for met in dir(lst)[34:]:
          print(met)
     __subclasshook__
     append
     clear
     сору
     count
     extend
     index
     insert
     pop
     remove
     reverse
     sort
     append()
[50]: # append()
     new_lst = lst[:]
      new_lst.append('appended string')
     print(new_lst)
     ['^_^', 8, 'bc', 'd', [15, 6], 'appended string']
```

in OPERATOR

```
[51]: # in OPERATOR
      print(8 in 1st)
      print(9 in lst)
      print('^_^' in lst)
      print('^_^' not in lst)
     True
     False
     True
     False
     max(), min(), sum()
[52]: # max(), min(), sum()
      new_lst = [6, 69, 9]
      print(max(new_lst))
      print(min(new_lst))
     print(sum(new_lst))
     69
     6
     84
     sort(), sorted()
[53]: # sort(), sorted()
      new_lst = [6, 69, 9]
      new_lst = sorted(new_lst)
      print(new_lst)
      new_lst.sort(reverse = True, key = lambda x: x % 8)
      6 % 8 = 6
      69 % 8 = 5
      9 % 8 = 1
      print(new_lst)
     [6, 9, 69]
     [6, 69, 9]
     del, pop(), remove()
[54]: # del, pop(), remove()
      new_lst = lst[:]
      print(new_lst)
      del new_lst[4]
      print(new_lst)
      new_lst.pop()
      print(new_lst)
```

```
new_lst.remove('bc')
     print(new_lst)
     ['^_^', 8, 'bc', 'd', [15, 6]]
     ['^_^', 8, 'bc', 'd']
     ['^_^', 8, 'bc']
     ['^_^', 8]
     reverse()
[55]: # reverse()
     new_lst = lst[:]
     print(new_lst)
     new_lst.reverse()
     print(new_lst)
     ['^_^', 8, 'bc', 'd', [15, 6]]
     [[15, 6], 'd', 'bc', 8, '^_^']
     6.1.9 LISTS AND STRINGS
[56]: # LISTS AND STRINGS
      s = 'this one! is a string'
      print(list(s))
      print(s.split())
     print(s.split('!'))
     new_lst = ['hi', 'there', '?']
     print('-'.join(new_lst))
     ['t', 'h', 'i', 's', ' ', 'o', 'n', 'e', '!', ' ', 'i', 's', ' ', 'a', ' ', 's',
     't', 'r', 'i', 'n', 'g']
     ['this', 'one!', 'is', 'a', 'string']
     ['this one', ' is a string']
     hi-there-?
     6.1.10 ALIASES
[57]: # ALIASES
     lst_a = [1, 3, 4]
      lst_b = lst_a
      lst_b.append('?')
      print(lst_a)
     [1, 3, 4, '?']
```

6.1.11 MUTATION AND ITERATION

```
[58]: # MUTATION AND ITERATION
lst_a = [1, 3, 4]
lst_b = [4, 3, 9]
# trying to remove values in lst_a which are already in lst_b
for num in lst_a:
    if num in lst_b:
        lst_a.remove(num)
print(lst_a)
# avoid mutating the list while iterating over it
```

[1, 4]

6.1.12 LIST ARGUMENTS

```
[59]: # LIST ARGUMENTS

def delete_last(a_lst):
    del a_lst[-1]
    # this function mutates the global list

def wrong_delete_last(a_lst):
    a_lst = a_lst[:-1]
    print('List in wrong one:', a_lst)
    # this one doesn't, a_lst now becomes a local variable

new_lst = [1, 3, 6, 9]
    delete_last(new_lst)
    print(new_lst)

new_lst = [1, 3, 6, 9]
    wrong_delete_last(new_lst)
    print(new_lst)
```

[1, 3, 6] List in wrong one: [1, 3, 6] [1, 3, 6, 9]

6.1.13 MapReduce AND LIST COMPREHENSION

```
map()
[60]: # map()
new_lst = [1, 3, 6, 8, 9, 10]
print(list(map(lambda x: x + 3, new_lst)))
```

[4, 6, 9, 11, 12, 13]

reduce()

```
[61]: # reduce()
  from functools import reduce
  new_lst = [1, 3, 6, 1]
  print(reduce(lambda x, y: x + y, new_lst))
  print(reduce(lambda x, y: x + y, new_lst, 3000))
  # initializer
```

11 3011

MapReduce APPLICATION: COUNT NUMBER OF A WORD

```
[62]: # MapReduce APPLICATION: COUNT NUMBER OF A WORD
      # count the number of the word "the"/"The" in a sentence
      text = 'The word "deep" in "deep learning" refers to the number of layers_{\sqcup}
       →through which the data is transformed. More precisely, deep learning systems ⊔
       \hookrightarrowhave a substantial credit assignment path (CAP) depth. The CAP is the chain\sqcup
       \hookrightarrow of transformations from input to output. CAPs describe potentially causal.
       \hookrightarrowconnections between input and output. For a feedforward neural network, the \sqcup
       \hookrightarrowdepth of the CAPs is that of the network and is the number of hidden layers\sqcup
       \rightarrowplus one (as the output layer is also parameterized). For recurrent neural.
       →networks, in which a signal may propagate through a layer more than once,
       →the CAP depth is potentially unlimited.[2] No universally agreed-upon
       →threshold of depth divides shallow learning from deep learning, but most ⊔
       \hookrightarrowresearchers agree that deep learning involves CAP depth higher than 2. CAP_{\sqcup}
       →of depth 2 has been shown to be a universal approximator in the sense that,
       \hookrightarrowit can emulate any function.[15] Beyond that, more layers do not add to the \sqcup
       \rightarrowfunction approximator ability of the network. Deep models (CAP > 2) are able<sub>\sqcup</sub>
       \hookrightarrowto extract better features than shallow models and hence, extra layers help\sqcup
       →in learning the features effectively.'
      ifThe = lambda word: 1 if word in ['the', 'The'] else 0
      sumof2 = lambda x, y: x + y
      print(list(map(ifThe, text.split())))
      print(reduce(sumof2, list(map(ifThe, text.split()))))
```

LIST COMPREHENSION

```
[63]: # LIST COMPREHENSION
print([c for c in 'hello there'], '\n')
```

```
cnt_lst = [ word for word in text.split() if word in ['the', 'The'] ]
print(cnt_lst)
print(len(cnt_lst))

cnt_lst_2 = [ 1 if word in ['the', 'The'] else 0 for word in text.split() ]
print(cnt_lst_2)

['h', 'e', 'l', 'l', 'o', ' ', 't', 'h', 'e', 'r', 'e']
```

6.2 SETS

 $\{0, 1, 4, 5\}$

6.2.1 SET EXAMPLES

```
[64]: # SET EXAMPLES
print({3, 4, 8})
print(set('hello'))

{8, 3, 4}
{'l', 'e', 'h', 'o'}
```

6.2.2 SET OPERATIONS

```
[65]: # SET OPERATIONS

A = {0, 1, 2, 3}

B = {2, 3, 4, 5}

print(A - B) # in A, not in B

print(A | B) # in any of A or B (bitwise or)

print(A & B) # in both A and B (bitwise and)

print(A ^ B) # in A or B, not both (bitwise xor)

{0, 1}

{0, 1, 2, 3, 4, 5}

{2, 3}
```

6.2.3 SET COMPREHENSION

{8: 'b', '?': 'a'}

```
[66]: # SET COMPREHENSION
      # set of all end-of-sentence words
      print( {word for word in text.split() if word.endswith('.')} )
     {'parameterized).', 'network.', 'transformed.', 'effectively.', '2.', 'output.',
     'depth.'}
     6.3 DICTIONARIES
     6.3.1 DICTIONARY EXAMPLES
[67]: # DICTIONARY EXAMPLES
      d = \{8: 'b', '?': 'a'\}
      print(d)
      print(d[8])
      print(d['?'])
      d['!?'] = 'mnpq'
     print(d)
     {8: 'b', '?': 'a'}
     b
     {8: 'b', '?': 'a', '!?': 'mnpq'}
     6.3.2 in OPERATOR
[68]: # in OPERATOR
      d = \{8: 'b', '?': 'a'\}
      print(d)
      print('?' in d)
     print('b' in d)
     {8: 'b', '?': 'a'}
     True
     False
     6.3.3 get() METHOD
[69]: # get() METHOD
      d = \{8: 'b', '?': 'a'\}
      print(d)
      print(d.get(8))
      print(d.get('a'))
      print(d.get('m', 5)) # not equivalent to d['m'] = 5
     print(d)
```

```
None
5
{8: 'b', '?': 'a'}
```

6.3.4 APPLICATION: COUNTING WORDS

```
[70]: # APPLICATION: COUNTING WORDS
counted = dict()
for word in text.split():
    counted[word] = counted.get(word, 0) + 1
print(counted)

{'The': 2. 'word': 1. '"deep"': 1. 'in': 4. '"deep': 1. 'learning"': 1.
```

{'The': 2, 'word': 1, '"deep"': 1, 'in': 4, '"deep': 1, 'learning"': 1, 'refers': 1, 'to': 5, 'the': 13, 'number': 2, 'of': 8, 'layers': 4, 'through': 2, 'which': 2, 'data': 1, 'is': 6, 'transformed.': 1, 'More': 1, 'precisely,': 1, 'deep': 3, 'learning': 4, 'systems': 1, 'have': 1, 'a': 5, 'substantial': 1, 'credit': 1, 'assignment': 1, 'path': 1, '(CAP)': 1, 'depth.': 1, 'CAP': 4, 'chain': 1, 'transformations': 1, 'from': 2, 'input': 2, 'output.': 2, 'CAPs': 2, 'describe': 1, 'potentially': 2, 'causal': 1, 'connections': 1, 'between': 1, 'and': 3, 'For': 2, 'feedforward': 1, 'neural': 2, 'network,': 1, 'depth': 5, 'that': 3, 'network': 1, 'hidden': 1, 'plus': 1, 'one': 1, '(as': 1, 'output': 1, 'layer': 2, 'also': 1, 'parameterized).': 1, 'recurrent': 1, 'networks,': 1, 'signal': 1, 'may': 1, 'propagate': 1, 'more': 2, 'than': 3, 'once,': 1, 'unlimited.[2]': 1, 'No': 1, 'universally': 1, 'agreed-upon': 1, 'threshold': 1, 'divides': 1, 'shallow': 2, 'learning,': 1, 'but': 1, 'most': 1, 'researchers': 1, 'agree': 1, 'involves': 1, 'higher': 1, '2.': 1, '2': 1, 'has': 1, 'been': 1, 'shown': 1, 'be': 1, 'universal': 1, 'approximator': 2, 'sense': 1, 'it': 1, 'can': 1, 'emulate': 1, 'any': 1, 'function.[15]': 1, 'Beyond': 1, 'that,': 1, 'do': 1, 'not': 1, 'add': 1, 'function': 1, 'ability': 1, 'network.': 1, 'Deep': 1, 'models': 2, '(CAP': 1, '>': 1, '2)': 1, 'are': 1, 'able': 1, 'extract': 1, 'better': 1, 'features': 2, 'hence,': 1, 'extra': 1, 'help': 1, 'effectively.': 1}

6.3.5 LOOP OVER A DICTIONARY

```
[71]: # LOOP OVER A DICTIONARY
d = {8: 'b', '?': 'a', '!': 'b', 10: 15}
for key in d:
    print(key, d[key])
8 b
```

? a ! b 10 15

6.3.6 LISTS OF KEYS AND VALUES

```
[72]: # LISTS OF KEYS AND VALUES
print(list(d.keys()))
print(list(d.values()))
print(list(d.items()))
[8, '?', '!', 10]
```

6.3.7 TWO ITERATION VARIABLES

[(8, 'b'), ('?', 'a'), ('!', 'b'), (10, 15)]

['b', 'a', 'b', 15]

```
[73]: # TWO ITERATION VARIABLES
for key, value in d.items():
    print(key, value)

8 b
? a
! b
```

6.3.8 DICTIONARY COMPREHENSION

```
[74]: # DICTIONARY COMPREHENSION
print({x: x * 8 for x in range(2, 8)})
```

{2: 16, 3: 24, 4: 32, 5: 40, 6: 48, 7: 56}

6.3.9 MEMOIZED RECURSION: FIBONACCI EXAMPLE

```
[75]: # MEMOIZED RECURSION: FIBONACCI EXAMPLE
res = {0: 0, 1: 1}
def fib(n):
    if n in res:
        return res[n]
    res[n] = fib(n - 1) + fib(n - 2)
    return res[n]
print(fib(14))
```

377

10 15

MEMOIZED RECURSION: LONGEST INCREASING SUBSEQUENCE EXAMPLE

```
[76]: # MEMOIZED RECURSION: LONGEST INCREASING SUBSEQUENCE EXAMPLE
from random import randint
num_list = [randint(0, 100) for i in range(15)]

res = {0: 1}
def lis_including(i):
    if i in res:
```

```
return res[i]
max_lis = 1
for j in range(i):
    if num_list[j] < num_list[i]:
        max_lis = max(max_lis, 1 + lis_including(j))
res[i] = max_lis
return max_lis

print(' i num_list[i] lis_including(i)')
for i in range(15):
    print('%3i%13i%20i' % (i, num_list[i], lis_including(i)))
print('Result =', max([lis_including(i) for i in range(15)]))</pre>
```

i	<pre>num_list[i]</pre>	<pre>lis_including(i)</pre>
0	18	1
1	12	1
2	29	2
3	82	3
4	66	3
5	90	4
6	43	3
7	6	1
8	100	5
9	0	1
10	31	3
11	97	5
12	84	4
13	89	5
14	9	2
Result = 5		

6.4 TUPLES

6.4.1 TUPLE EXAMPLES

```
[77]: # TUPLE EXAMPLES
print((3, 5, 7))
print((1, ))
# Warning: Tuple of 1 element must have a comma
print((1))

(3, 5, 7)
(1,)
1
```

6.4.2 TUPLES ARE IMMUTABLE

```
[78]: # TUPLES ARE IMMUTABLE
tup = (3, 4, 7)
# tup[0] = 0
# TypeError: 'tuple' object does not support item assignment
print(tup)
(3, 4, 7)
```

6.4.3 TUPLE DIRECTORIES

```
[79]: # TUPLE DIRECTORIES
print(dir(tuple)[-3:])
```

['__subclasshook__', 'count', 'index']

6.4.4 TUPLES AND ASSIGNMENT

```
[80]: # TUPLES AND ASSIGNMENT
a, b = (3, 5)
print('a = %i\nb = %i' % (a, b))
x, y = 6, 9
print('x = %i\ny = %i' % (x, y))
a = 3
```

b = 5

x = 6

y = 9

6.4.5 TUPLE AS RETURN VALUES

```
[81]: # TUPLE AS RETURN VALUES
print(divmod(100, 32))

def max_and_index(lst):
    index = 0
    for i in range(1, 15):
        if lst[i] > lst[index]:
            index = i
        return lst[index], index

from random import randint
    num_list = [randint(0, 100) for i in range(15)]
    print(num_list)
    print(max_and_index(num_list))
```

```
(3, 4)
[32, 41, 63, 45, 88, 90, 79, 35, 31, 100, 86, 38, 72, 11, 83]
```

(100, 9)

6.4.6 LISTS AND TUPLES

print((3, 6) < (3, 2))

print()

```
[82]: # LISTS AND TUPLES
      z = zip('abcde', [3, 4, 5, 6, 7, 8, 9, 10])
      print(z)
      z = zip('abcde', [3, 4, 5, 6, 7, 8, 9, 10])
      print(list(z))
      z = zip('abcde', [3, 4, 5, 6, 7, 8, 9, 10])
      for pair in z:
          print(pair)
     <zip object at 0x7fb9ea6a24b0>
     [('a', 3), ('b', 4), ('c', 5), ('d', 6), ('e', 7)]
     ('a', 3)
     ('b', 4)
     ('c', 5)
     ('d', 6)
     ('e', 7)
     enumerate()
[83]: # enumerate()
      for ind, c in enumerate('cdef'):
          print(ind, c)
     0 с
     1 d
     2 e
     3 f
     6.4.7 DICTIONARIES AND TUPLES
[84]: # DICTIONARIES AND TUPLES
      d = \{'h': 4, 't': 5, 'n': 6, 'm': 7\}
      print(d.items())
      1 = [(8, 'h'), (7, 't'), (6, 'n'), (5, 'm')]
     print(dict(1))
     dict_items([('h', 4), ('t', 5), ('n', 6), ('m', 7)])
     {8: 'h', 7: 't', 6: 'n', 5: 'm'}
     6.4.8 TUPLE COMPARISON
[85]: # TUPLE COMPARISON
      print((3, ) < (5, ))
      print((3, 6) < (5, 1))
```

```
print(('Alpha', 0) < ('Beta', 8))
print(('Alpha', 0) < ('Alpha', -2))</pre>
```

True True

False

True

False

6.4.9 SORTING EXAMPLE: SORT BY VALUE, NOT KEY

```
[86]: # SORTING EXAMPLE: SORT BY VALUE, NOT KEY
d = {'h': 4, 't': 5, 'n': 6, 'm': 7}
print('Sort by key: ', *sorted(list(d.items())))

print('Sort by value, #1 way:', *sorted(list(d.items()), key = lambda x: x[1]))

value_key_list = sorted([(value, key) for key, value in d.items()])
sorted_value_list = [(key, value) for value, key in value_key_list]
print('Sort by value, #2 way:', *sorted_value_list)
```

```
Sort by key: ('h', 4) ('m', 7) ('n', 6) ('t', 5)
Sort by value, #1 way: ('h', 4) ('t', 5) ('n', 6) ('m', 7)
Sort by value, #2 way: ('h', 4) ('t', 5) ('n', 6) ('m', 7)
```

7 CHAPTER 6: MODULES

7.1 import EXAMPLE

```
[87]: # import EXAMPLE
import math
print(math.sqrt(8))
from math import sqrt
print(sqrt(8))
from random import *
print(randint(3,6))
```

2.8284271247461903

2.8284271247461903

4

7.2 (preparation)

7.2.1 (preparation) mount

```
[88]: # (preparation) mount
from google.colab import drive
drive.mount('/content/gdrive')
```

Mounted at /content/gdrive

7.2.2 (preparation) append path

```
[89]: # (preparation) append path
!ls /content/gdrive/MyDrive/Colab\ Notebooks/hello.py
!cat /content/gdrive/MyDrive/Colab\ Notebooks/hello.py
import sys
sys.path.append('/content/gdrive/MyDrive/Colab Notebooks')

'/content/gdrive/MyDrive/Colab Notebooks/hello.py'
if __name__ == '__main__':
    print('Hello?')
```

7.3 MODULES AS SCRIPTS

```
[90]: # MODULES AS SCRIPTS
hello_path = '/content/gdrive/MyDrive/Colab Notebooks/hello.py'

print('Script in "hello.py":\n-----')
f = open(hello_path, 'r')
print(f.read(), '\n-----')
f.close()

! python '/content/gdrive/MyDrive/Colab Notebooks/hello.py'
```

7.4 __name__

```
[91]: # __name__
print('before import')
import hello
print('after import')
print(hello.__name__)
```

before import
after import

hello

7.5 sys.argv[]

7.6 USEFUL MODULES: BASIC EXAMPLES

```
[93]: # USEFUL MODULES: BASIC EXAMPLES
      # See a lot more in-depth examples in the APPENDIX
      ''' Find out more in: (ctrl + click to open)
      https://docs.python.org/3/library/random.html
      https://docs.python.org/3/library/datetime.html
      https://docs.python.org/3/library/math.html
      https://numpy.org/doc/
      111
      import random
      import datetime
      import math
      import numpy
      print(datetime.datetime.now())
      print(math.factorial(8))
      np_arr = numpy.array([random.uniform(0, 3) for i in range(6)])
      print(np_arr)
      # print values which are > 1.5
      print(np_arr[np_arr > 1.5])
     2021-08-08 15:43:29.936725
```

```
2021-08-08 15:43:29.936725
40320
[1.33882977 2.52062707 2.35784056 0.37683892 2.41519137 2.01498214]
[2.52062707 2.35784056 2.41519137 2.01498214]
```

7.7 pickle MODULE

7.7.1 IMPORT pickle

```
[94]: # IMPORT pickle import pickle as pkl
```

$7.7.2 \quad \text{dump()}$

```
[95]: # dump()
sample_pkl_path = '/content/gdrive/MyDrive/Colab Notebooks/sample_pkl.pkl'
lst = [3, 5, 0, 8]
with open(sample_pkl_path, 'wb') as f:
    # 'wb' = write byte, see more below, in Chapter 7: FILES
    pkl.dump(lst, f)
```

7.7.3 load()

```
[96]: # load()
with open(sample_pkl_path, 'rb') as f:
     # 'rb' = read byte, see more below, in Chapter 7: FILES
     loaded_content = pkl.load(f)
print(loaded_content)
```

[3, 5, 0, 8]

8 CHAPTER 7: FILES

8.1 OPENING A FILE

```
[97]: # OPENING A FILE
f = open(hello_path, 'r')
# 'r' reading | 'w' writing | 'a' appending | 'r+' both reading and writing
```

8.2 LOOP OVER A FILE

print('Hello?')

```
[98]: # LOOP OVER A FILE
for line in f:
    print(line, end = '')
f.close()

if __name__ == '__main__':
```

8.3 READ WHOLE FILE

```
[99]: # READ WHOLE FILE
f = open(hello_path, 'r')
print(f.read())
f.close()

if __name__ == '__main__':
    print('Hello?')
```

8.4 with BLOCK

```
[100]: # with BLOCK
with open(hello_path, 'r') as f:
    print(f.read())
print(f.closed)

if __name__ == '__main__':
    print('Hello?')
True
```

8.5 WRITING FILES

```
[101]: # WRITING FILES
write_path = '/content/gdrive/MyDrive/Colab Notebooks/writeout.txt'
with open(write_path, 'w') as f:
    f.write('Write this line to the file')
with open(write_path, 'r') as f:
    print(f.read())
```

Write this line to the file

8.6 CURRENT POSITION

```
[102]: # CURRENT POSITION
with open(write_path, 'r') as f:
    print(f.tell())
    print(f.read())
    print(f.tell())
```

Write this line to the file 27

8.7 CHANGE POSITION

```
[103]: # CHANGE POSITION

# https://www.tutorialspoint.com/python/file_seek.htm

with open(write_path, 'r') as f:
    print(f.tell())
```

```
f.seek(13)
  print(f.tell())
  print(f.read())
  print(f.tell())

0
13
ne to the file
27
```

9 CHAPTER 8: OBJECT-ORIENTED PROGRAMMING (OOP)

9.1 CREATE A NEW OBJECT EXAMPLE

```
[104]: # CREATE A NEW OBJECT EXAMPLE
             name of class (parent class(es))
       class Complex_number(object):
           # __init__ always run right after calling the class
           def __init__(self, a, b):
               # real and imaginary are attributes
               self.real = a
               self.imaginary = b
           # a method is a function of the class
           def modulus(self):
               from math import sqrt
               return sqrt(self.real ** 2 + self.imaginary ** 2)
           # __str__ is a method which returns (str(an instance))
           def __str__(self):
               return 'Complex number (%s + %si)' % (self.real, self.imaginary)
           # __add__ is a method which returns (an instance + another instance)
           def __add__(self, other):
               return Complex_number(self.real + other.real, self.imaginary + other.
        →imaginary)
           # __sub__ is a method which returns (an instance - another instance)
           def __sub__(self, other):
               return Complex_number(self.real - other.real, self.imaginary - other.
        →imaginary)
           \# __eq__ is a method which returns (an instance == another instance)
           def __eq__(self, other):
               return self.real == other.real and self.imaginary == other.imaginary
```

The most common used methods for a class, in short:

```
__doc__: docstring | __name__: name | __del__: delete
__lt__: "<" | __le__: "<=" | __ne__: "!="
__gt__: ">" | __ge__: ">="
__dir__: dir(an object or an instance)
object.__add__(self, other)
object.__sub__(self, other)
object.__mul__(self, other)
object.__matmul__(self, other)
object.__truediv__(self, other)
object.__floordiv__(self, other)
object.__mod__(self, other)
object.__divmod__(self, other)
object.__pow__(self, other[, modulo])
object.__lshift__(self, other)
object.__rshift__(self, other)
object.\_and\_(self, other)¶
object.__xor__(self, other)
object.__or__(self, other)
```

There are so many more methods for a class that you should find them out yourself, this is the documentation of data model in Python:

https://docs.python.org/3/reference/datamodel.html

I found that the @abstractmethod decorator is not really important for the final exam, since we didn't learn any thing about decorator in Python, so if you are curious enough, this is the documentation of abc:

https://docs.python.org/3/library/abc.html

9.1.1 USING THE OBJECT EXAMPLES

```
[105]: # USING THE OBJECT EXAMPLES
       z1 = Complex_number(6, 9)
       print(z1.real, z1.imaginary)
       print(z1.modulus())
       print(z1)
      6 9
      10.816653826391969
      Complex number (6 + 9i)
[106]: # USING THE OBJECT EXAMPLES
       z2 = Complex_number(2.8, 9.2)
       print(z2.real, z2.imaginary)
       print(z2.modulus())
       print(z2)
      2.8 9.2
```

9.616652224137045

```
Complex number (2.8 + 9.2i)
```

Complex number (8.8 + 18.2i) Complex number (3.2 + -0.19999999999993i)

```
[108]: # USING THE OBJECT EXAMPLES
print(z1 == z2)
z3 = Complex_number(6, 9)
print(z1 == z3)
```

False True

9.2 SUBCLASS

```
[109]: # SUBCLASS
       # You can re-define any method of Complex_number, or
       # add new methods, new attributes in Imaginary_number
       class Imaginary_number(Complex_number):
           def __init__(self, *args):
               if len(args) == 1:
                   self.removed_real_part = None
                   imaginary_part = args[0]
               else: \# len(args) == 2
                   self.removed_real_part = args[0]
                   imaginary_part = args[1]
               # 2 ways to initialize:
               # super().__init__(0, imaginary_part)
               Complex_number.__init__(self, 0, imaginary_part)
           def __str__(self):
               return 'Imaginary number (%si)' % (self.imaginary)
```

9.2.1 USING THE SUBCLASS EXAMPLES

```
[110]: # USING THE SUBCLASS EXAMPLES
img1 = Imaginary_number(3, 8)
print(img1)
print('Removed real part:', img1.removed_real_part)
print('Modulus:', img1.modulus())
```

Imaginary number (8i)

```
Removed real part: 3
Modulus: 8.0

[111]: # USING THE SUBCLASS EXAMPLES
img2 = Imaginary_number(4)
print(img2)
print('Removed real part:', img2.removed_real_part)
print('Modulus:', img2.modulus())

Imaginary number (4i)
Removed real part: None
Modulus: 4.0
```

10 CHAPTER 9: TESTING, DEBUGGING, EXCEPTIONS AND ASSERTIONS

10.1 TESTING AND DEBUGGING

By now, you have done this every time an error occurs in your code, so this is pretty both too easy and too hard to be explained in this notebook. Therefore, I will not explain about it here.

10.2 EXCEPTIONS

10.2.1 COMMON BUILT-IN EXCEPTIONS

```
[112]: # COMMON BUILT-IN EXCEPTIONS
lst = [0, 1, 2]

print(lst[4])
IndexError: list index out of range

print(int(lst))
TypeError: int() argument must be a string, a bytes-like object or a number, not 'list'

print(an_undefined_a_variable)
NameError: name 'an_undefined_a_variable' is not defined

print(a

print(a

print(a

print(st.mnpq)
AttributeError: 'list' object has no attribute 'mnpq'

print(6 / 0)
ZeroDivisionError: division by zero
```

```
print(int('?'))
ValueError: invalid literal for int() with base 10: '?'

f = open('????')
FileNotFoundError: [Errno 2] No such file or directory: '????'
```

10.2.2 (INPUT) HANDLING SPECIFIC EXCEPTIONS

```
[113]: # HANDLING SPECIFIC EXCEPTIONS
try:
    a = float(input('a = '))
    b = float(input('b = '))
    res = a / b

except ValueError: # Handling a specific exception in try clause
    print('Unable to convert to number')
except ZeroDivisionError:
    print('Unable to divide by 0')

except: # Handling any other exception in try clause
    print('Another error')

else: # Only execute if the try clause does not raise any exception
    print(res)

finally: # Always execute
    print('Done')
```

```
a = 4
b = 8
0.5
Done
a = sfgopsgspg
Unable to convert to number
Done
a = 4
b = 0
Unable to divide by 0
Done
a = 4
b = 8
0.5
Done
```

10.2.3 raise AN EXCEPTION

10.2.4 (INPUT) DEFINE AN EXCEPTION

```
[114]: # DEFINE AN EXCEPTION
       class DateFormatError(Exception):
           pass
       # Raise the exception if the string is not of the format '??-??-????'
       # ? is a number, from 0-9
       def num_args_check(date):
           dmy_lst = date.split('-')
           if len(dmy_lst) == 3:
               return True
           return False
       def numeric_check(date):
           dmy_lst = date.split('-')
           for arg in dmy_lst:
               if not arg.isnumeric():
                   return False
           return True
       def args_len_check(date):
           dmy_lst = date.split('-')
           len_lst = [len(dmy_lst[i]) for i in range(3)]
           if tuple(len_lst) == (2, 2, 4):
               return True
           return False
       date = input('Date = ')
       if not num_args_check(date):
           raise DateFormatError(
                   'There must be 3 arguments for day-month-year, respectively')
       if not numeric_check(date):
           raise DateFormatError(
                   'At least one of 3 arguments is not numeric')
```

```
if not args_len_check(date):
    raise DateFormatError(
             'len() of 3 arguments must be 2, 2, 4, respectively')
print('The date is: %s' % date)
Date = 66-99-6969
The date is: 66-99-6969
Date = 41-14-6161-3
DateFormatError: There must be 3 arguments for day-month-year, respectively
Date = 1-12-4251
DateFormatError: len() of 3 arguments must be 2, 2, 4, respectively
Date = 30-12-200x
DateFormatError: At least one of 3 arguments is not numeric
Date = 66-99-6969
The date is: 66-99-6969
10.2.5 unittest MODULE
A module to test your program (in a big project).
(I believe) this one will not appear in the final test, this is the documentation, though:
https://docs.python.org/3/library/unittest.html
```

11 APPENDIX: SOME IMPORTANT MODULES FOR MATH-EMATICS, DATA SCIENCE AND MACHINE LEARNING

11.1 random

```
[115]: # Documentation: https://docs.python.org/3/library/random.html import random
```

11.1.1 INTEGERS

```
[116]: # INTEGERS
print(random.randrange(10))
# a random number in range(10)
print(random.randrange(22, 29, 2))
# a random number in range(22, 29, 2), which are 22, 24, 26 and 28
```

0 24

11.1.2 SEQUENCE

```
[117]: # SEQUENCE
       seq = [3, 5, 0, 8]
       print(random.choice(seq))
       # choose a random element in a sequence
       print(random.choices(seq, k = 2))
       # choose a random element twice in a sequence
      [0, 3]
[118]: # random
       print(random.sample(seq, 2))
       # choose two random elements in a sequence
       print(random.sample(seq, len(seq)))
       # alias of random.shuffle, since it is...
       # Deprecated since version 3.9, will be removed in version 3.11
      [5, 0]
      [3, 0, 5, 8]
      11.1.3 REAL NUMBERS
[119]: # REAL NUMBERS
       print(random.random())
       # a random number in the interval [0.0, 1.0)
       print(random.uniform(3.0, 5.0))
       # a random number between 3.0 and 5.0
       # the end-point might or might not be included,
       # read more in documentation
      0.609703227592042
      3.717343439662672
      11.2 time
[120]: # time
       # Documentation: https://docs.python.org/3/library/time.html
       import time
[121]: # time
       print('before')
       time.sleep(0.5)
       # suspend execution for the given number of seconds
       print('after')
      before
      after
```

```
[122]: # time
print(time.time())
# Return the time in seconds since the epoch as a floating point number
```

1628437430.4016688

```
[123]: # time
    # measure execution time
    time_before = time.time()
    print(time_before)

for i in range(5):
        print(i, end = ' ')
    time_after = time.time()

print('\n%s' % time_after)

print(time_after - time_before)
```

1628437430.4206786 0 1 2 3 4 1628437430.421016 0.00033736228942871094

11.3 math

```
[124]:  # math  # Documentation: https://docs.python.org/3/library/math.html  import math
```

11.3.1 CONSTANTS

```
[125]: # CONSTANTS
    print(math.pi)
    print(math.e)
    print(math.inf)
    print(math.nan)
```

3.141592653589793 2.718281828459045 inf nan

11.3.2 NUMBER-THEORETIC AND REPRESENTATION FUNCTIONS

```
[126]: # NUMBER-THEORETIC AND REPRESENTATION FUNCTIONS
print(math.ceil(3.01))
# the smallest integer greater than or equal to given number
print(math.floor(8.99))
```

```
# the largest integer less than or equal to given number
      4
      8
[127]: # NUMBER-THEORETIC AND REPRESENTATION FUNCTIONS
       print(math.gcd(15, 20))
      5
[128]: # NUMBER-THEORETIC AND REPRESENTATION FUNCTIONS
       print(.1 + .2)
       print(.1 + .2 == .3)
      math.isclose(.1 + .2, .3)
      0.30000000000000004
      False
[128]: True
[129]: # NUMBER-THEORETIC AND REPRESENTATION FUNCTIONS
       print(math.isfinite(9999999999999))
       print(math.isfinite(math.inf))
       print(math.isfinite(math.nan))
       # nan is not finite
       print()
       print(math.isinf(9999999999999))
       print(math.isinf(math.inf))
       print(math.isinf(math.nan))
       # nan is not infinite
       print()
       print(math.isnan(9999999999999))
       print(math.isnan(math.inf))
       print(math.isnan(math.nan))
      True
      False
      False
      False
      True
      False
      False
      False
      True
```

```
[130]: # NUMBER-THEORETIC AND REPRESENTATION FUNCTIONS
      print(math.trunc(3.9))
      print(math.trunc(3.1))
      # truncated to an integral
      3
      11.3.3 POWER AND LOGARITHMIC FUNCTIONS
[131]: # POWER AND LOGARITHMIC FUNCTIONS
      print(math.exp(3)) # e^3
      print(math.e ** 3)
      # more accurate
      20.085536923187668
      20.085536923187664
[132]: # POWER AND LOGARITHMIC FUNCTIONS
      print(math.log(3))
      # natural logarithm of 3
      print()
      print(math.log(5, 2))
      # logarithm of 5 to the base 2
      print(math.log2(5))
      # more accurate
      print()
      print(math.log10(101))
      1.0986122886681098
      2.321928094887362
      2.321928094887362
      2.0043213737826426
[133]: # POWER AND LOGARITHMIC FUNCTIONS
      print(math.pow(2.1, 5.0))
      print(2.1 ** 5.0)
      # more accurate
      print()
      print(math.sqrt(5.6))
      print(5.6 ** 0.5)
      # more accurate
```

40.84101000000001

```
40.84101000000001
```

- 2.3664319132398464
- 2.3664319132398464

11.3.4 TRIGONOMETRIC FUNCTIONS

```
[134]: # TRIGONOMETRIC FUNCTIONS
      # all angle units are radians
      print(math.sin(math.pi / 2))
      print(math.cos(math.pi / 2))
      print(math.tan(math.pi / 2))
      print()
      print(math.acos(1.0))
      # arc cosine
      print(math.asin(1.0))
      print(math.atan(1.0))
      1.0
      6.123233995736766e-17
      1.633123935319537e+16
      0.0
      1.5707963267948966
      0.7853981633974483
      11.3.5 ANGULAR CONVERSION
```

```
[135]: # ANGULAR CONVERSION
    print(math.degrees(math.pi / 2))
    print(math.radians(90))
```

90.0

1.5707963267948966

11.4 numpy

```
[136]: # numpy
# Documentation: https://numpy.org/doc/
import numpy as np
```

11.4.1 ARRAY CREATION

```
[137]: # ARRAY CREATION
    print(np.array( [1, 4, 6, 9] ))
    print(np.array( ((1, 3), (6, 9)) ))
    print(np.array( [(3.2, 2.1), (6.0, 1.3)] ))
    # a list/tuple of lists/tuples of... is allowed
```

```
print()
       print(np.array( [6, 9, 3, 0], dtype = float ))
       print(np.array( [(3.2, 2.1), (6.7, 1.3)], dtype = np.int8 ))
       # there are a lot of data types available,
       # check it out in the documentation
      [1 4 6 9]
      [[1 3]
       [6 9]]
      [[3.2 2.1]
       [6. 1.3]]
      [6. 9. 3. 0.]
      [[3 2]
       [6 1]]
[138]: # ARRAY CREATION
       print(np.arange(10))
       print(np.arange(21.2, 8.1, -2.5))
       # floats can be passed to arange
       print()
       print(np.linspace(2.3, 4.8, 5))
       # arrays with a specified number of elements,
       # and spaced equally between the specified beginning and end values
      [0 1 2 3 4 5 6 7 8 9]
      [21.2 18.7 16.2 13.7 11.2 8.7]
             2.925 3.55 4.175 4.8 ]
      [2.3
[139]: # ARRAY CREATION
       # most types of special two-dimensional matrices in linear algebra
       # can be created using np functions, find out more in the documentation
       print(np.eye(3))
       print(np.diag([3, 4, 5]))
      [[1. 0. 0.]
       [0. 1. 0.]
       [0. 0. 1.]]
      [[3 0 0]
       [0 4 0]
       [0 0 5]]
[140]: # ARRAY CREATION
       print(np.zeros((2, 3)))
       print()
       print(np.ones((3, 2, 4)))
```

```
[0. 0. 0.]]
      [[[1. 1. 1. 1.]
        [1. 1. 1. 1.]]
       [[1. 1. 1. 1.]
        [1. 1. 1. 1.]]
       [[1. 1. 1. 1.]
        [1. 1. 1. 1.]]]
      11.4.2 INDEXING
[141]: # INDEXING
       np_arr = np.arange(3.3, 12, 1.1)
       print(np_arr)
       print(np_arr[-2])
       print(np_arr[-2:])
       # slicing np array is exactly the same as slicing python list
      [ 3.3 4.4 5.5 6.6 7.7 8.8 9.9 11. ]
      9.900000000000000
      [ 9.9 11. ]
[142]: # INDEXING
       print(np_arr.shape)
       np_arr.shape = (2, 4)
       print(np_arr.shape)
      print(np_arr)
      (8,)
      (2, 4)
      [[ 3.3 4.4 5.5 6.6]
       [ 7.7 8.8 9.9 11. ]]
[143]: # INDEXING
       print(np_arr[1])
       print(np_arr[1, 2])
      [7.7 8.8 9.9 11.]
      9.900000000000002
[144]: # INDEXING
       print(np.arange(4))
       np_arr_2 = np.arange(1, 8, 2)
       print(np_arr_2)
       print()
```

[[0. 0. 0.]

```
index_arr = np.array([1, -1, 3])
      print(index_arr)
      print(np_arr_2[index_arr])
      # a np array can be used to select element
      print()
      index_arr_2 = np.array( [[1, 0], [3, 2]] )
      print(index_arr_2)
      print(np_arr_2[index_arr_2])
      print()
      # indexing np arrays which have more dimensions is more complicated,
      # read more in documentation
      [0 1 2 3]
      [1 3 5 7]
      [1 -1 3]
      [3 7 7]
      [[1 \ 0]]
       [3 2]]
      [[3 1]
       [7 5]]
[145]: # INDEXING
      np_arr_3 = np.arange(9)
      print(np_arr_3)
      index_arr_3 = np_arr_3 % 2 == 0
      print(index_arr_3)
      print(np_arr_3[index_arr_3])
      # in data science, filtering data is very important,
      # so this is a must-have tool
      [0 1 2 3 4 5 6 7 8]
      [ True False True False True False True]
      [0 2 4 6 8]
      11.4.3 BROADCASTING
[146]: # BROADCASTING
      # the term broadcasting describes how np treats arrays
      # with different shapes during arithmetic operations
      np_arr_a = np.array([6, 8, 9])
      print(np_arr_a)
      np_arr_b = np.ones(3, dtype = np.int8)
      print(np_arr_b)
      print(np_arr_a + np_arr_b)
```

```
[6 8 9]
[1 1 1]
[7 9 10]

[147]: # BROADCASTING
print(np_arr_a + 1)
# read more about general broadcasting rules for
# more-dimensional-arrays in the documentation
```

[7 9 10]

11.4.4 STRUCTURED ARRAYS

[('Alan', 19, 169.2) ('Paul', 21, 172.3)]

11.5 MOST USED MODULES FOR MATHEMATICS, DATA SCIENCE AND MACHINE LEARNING

```
TensorFlow: https://www.tensorflow.org/
SciPy: https://www.scipy.org/
Matplotlib: https://matplotlib.org/
Pandas: https://pandas.pydata.org/
Keras: https://keras.io/
scikit-learn: https://scikit-learn.org/
statsmodels: https://www.statsmodels.org/
Plotly: https://plotly.com/
Seaborn: https://seaborn.pydata.org/
```

Fun fact: If you know how to use about half of the modules above and understand their mathematical foundations, you can quit college, right now.