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1a)  $\Theta(n)$

1b)  $\Theta(n^2)$

1c)  $\Theta(\log(n))$

2a)

$$3n^4 \leq 3n^4 + 8n^3 - 3n \leq 3n^4 + 8n^4$$

$$3n^4 \leq 3n^4 + 8n^3 - 3n \leq 11n^4$$

2b)  $\sqrt{17n^2 + 4n - 7}$

$$17n \leq \sqrt{17n^2 + 4n - 7} \leq 17n + 4n$$

$$17n \leq \sqrt{17n^2 + 4n - 7} \leq 21n$$

2c)

We say that  $f(n) = O(g(n))$  if there exists positive real constant  $C$  and a positive integer constant  $n(\text{sub}0)$  such that  $f(n) \leq c(g(n))$  for all  $n \geq n(\text{sub}0)$ . and then if  $g(n) = O(h(n))$  then there exists positive real constant  $C$  and a positive integer constant  $n(\text{sub}0)$  such that  $g(n) \leq c(h(n))$  for all  $n \geq n(\text{sub}0)$ . So then at the conclusion you could say that  $f(n) = O(h(n))$  if there exists positive real constant  $C$  and a positive integer constant  $n(\text{sub}0)$  such that  $f(n) \leq c(h(n))$  for all  $n \geq n(\text{sub}0)$ .

3) The running time of this is  $\Theta(\log(n))$ . This is it is proportional to the depth of the recursion tree. At each level, the square root of  $n$  is taken.

4)

1) The worst case run time for `reverse1(lst)` is  $O(n^2)$  because it is going through a for loop  $n$  amount of times and then it is also inserting elements into the list at the 0 index which always pushes the data over one when adding another element.

2) The worst case run time for `reverse2(lst)` is  $O(n)$  because it is going through the list  $n$  amount of times and then it is appending to the end of the list which is a constant amortized

