## Your Paper Title

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#### Abstract

This is the abstract. Summarize the purpose, methods, and main findings of the study.

## 1 Introduction

Introduce the problem, background, and significance of the study.

## 2 Methodology

Describe the datasets and outline each method applied.

#### 2.1 Datasets

Briefly describe Dataset 1 and Dataset 2.

## 2.2 K-Nearest Neighbors (KNN)

Explain the KNN approach applied.

## 2.3 Support Vector Machine (SVM)

Describe the SVM approach.

#### 2.4 Reduction Methods

In this section, we briefly describe reduction techniques employed for instance-based learning. We use a simple 2D dataset for illustrative purposes.

#### 2.4.1 GCNN

#### 2.4.2 EENTH

This subsection outlines the Elimination Editing with Nearest-neighbor Threshold (EENTH) method [1]. This approach uses a modified k-NN rule, integrating probability-based decisions for instance elimination. The main steps are outlined below.

1. **Probability-based Classification**: For each instance x, calculate the probability  $p_i(x)$  of x belonging to each class i based on its k-nearest neighbors. Probabilities are weighted inversely by the distance to each neighbor and normalized:

$$p_i^j = \frac{|\{x_k \in NN_k(x) : y_k = j\}|}{k} \tag{1}$$

$$P_i(x) = \sum_{j=1}^k p_i^j \frac{1}{1 + d(x, x^j)}$$
 (2)

$$p_i(x) = \frac{P_i(x)}{\sum_{j=1}^{M} P_j(x)}$$
 (3)

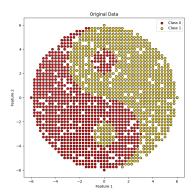
- 2. **Thresholding**: Define a threshold  $\mu$  to refine classification, we will denote as p(x) the highest probability. Instances near decision boundaries, where  $p(x) < \mu$ , are identified as candidates for removal.
- 3. **Elimination**: If an instance x does not match the class with the highest probability, or if its highest class probability falls below  $\mu$ , it is removed from the dataset, resulting in an edited set  $S \subseteq X$ .

The EENTH method thus provides a balance between retaining instances with high classification confidence and discarding uncertain instances near decision boundaries.

#### 2.4.3 DROP3

In this subsection, we describe the basic concepts of the third method in the Decremental Reduction Optimization Procedure (DROP) family, as presented in Section 3 of Wilson et al. [3]. Although we will not delve into every detail, we describe the main ideas of the algorithm and illustrate them on  $D_1$ . See **Figure** 1.

1. **Remove noise**: The first step is to remove noisy instances using Edited Nearest Neighbor (EEN) [2], where any instance misclassified by its k-nearest neighbors is removed. The outcome of applying this technique is shown in **Figure** 2, where noise has been removed. We denote the reduced dataset as  $T \subseteq D_1$ .



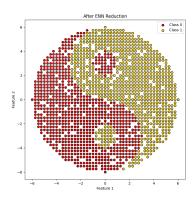


Figure 1: Original Dataset

Figure 2: Effect of EEN

- 2. **Sort points**: The next step is to prioritize removing points that are farthest from the decision boundary. For each point  $x_i \in S$  with class  $y_i$ , we compute the distance to the nearest point with a different class, denoted as  $x_j \in D$  such that  $y_j \neq y_i$  and  $\nexists x_k : |x_k x_i| < |x_j x_i| \land y_i \neq y_k$ .
- 3. **Delete points**: Let S = T. Starting with the points farthest from the boundary, we check if any associated points (points that have  $x_i$  as a neighbor)  $a_j$  receive more votes for their correct class with  $x_i$  as a neighbor (denoted as with) or if they would be classified correctly if  $x_i$  were removed (denoted as without). If without > with, we remove  $x_j$  from S, resulting in  $S' = S \setminus \{x_j\}$ .
- 4. **Selecting neighbors**: A key distinction between DROP1 and DROP2 is that DROP1 removes points that are removed from the dataset from the list of associates while DROP2 doesn't.

## 3 Results

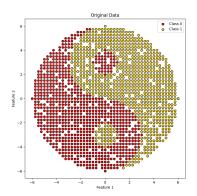
Present the findings for each technique and the statistical analysis.

## 3.1 KNN Results

Discuss the outcomes for KNN.

#### 3.2 SVM Results

Describe the SVM results.



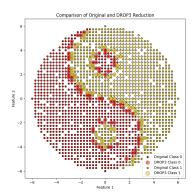


Figure 3: Original Dataset

Figure 4: Effect of DROP3

## 3.3 KNN Reduction Results

Discuss the outcomes for KNN with reduction methods.

#### 3.4 SVM Reduction Results

Describe the SVM results with reduction methods.

## 4 Discussion

Interpret the results, relate to previous work, and discuss implications.

## 5 Conclusion

Conclude the report.

## References

- [1] Fernando Vázquez, Josep Sánchez, and Filiberto Pla. A stochastic approach to wilson's editing algorithm. pages 35–42, 01 2005.
- [2] D. L. Wilson. Asymptotic properties of nearest neighbor rules using edited data. *IEEE Transactions on Systems, Man, and Cybernetics*, 2(3):408–421, 1972.
- [3] Dennis R. Wilson and Tony R. Martinez. Reduction techniques for instance-based learning algorithms. *Machine Learning*, 38(3):257–286, 2000.