

Question 1)

From the textbook, a DFA $M = (Q, \Sigma, \delta, q_0, F)$ exists if a language L is regular where $L = L(M)$

then has a complement $M' = (Q, \Sigma, \delta, q_0, q/F)$ where

the accepting & non-accepting states are switched.

Per Demorgan's laws, $(A \cap B)' = A' \cup B'$ &

according to the textbook, if A & B are regular languages, $A \cup B$ is regular. From the closure to

union proof. Using the closure under complement

& $A' \cup B'$ is regular
proof, $A' \cup B'$ are also regular when $A \cup B$ is

regular. If $A' \cup B'$ is regular, so is $(A \cap B)'$. Under

closure to complement, $A \cap B$ is also regular.

Question 2)

Variable S , Start states for variables
 A & B are $S_A, S_B, Z =$ all rules from A, B .

$$x) \begin{array}{l} S_A \rightarrow wy \\ y \rightarrow a \end{array}$$

$$y) \begin{array}{l} S_B \rightarrow bC \\ C \rightarrow E \end{array}$$

$$z) S \rightarrow S_A S_B$$

Z is ^{that} CFL^{*} accepts
 A & B in this model,
So Z will accept
 $A \cdot B$.

Question 3)

Professor Brany is claiming $S \rightarrow SS$.
If you add S to any context free grammar
you are still not including $S \rightarrow \epsilon$, L^* must
include the empty string. G does not generate
 L^* b/c it is not guaranteed that there is
a terminal pointing to ϵ .

Question 4)

Context free grammar

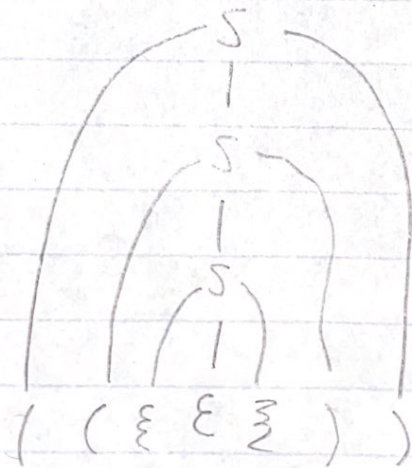
$$S \rightarrow SS$$

$$S \rightarrow (S)$$

$$S \rightarrow \{SS\}$$

$$S \rightarrow \epsilon$$

Parse tree



Question 5)

a) $0^n 1^n$

Alone 1 & 0 are CFL.

From proof in question 2, if A & B are CFL, then $A \cdot B$ are CFL. Same concept here. Since 1 & 0 are context free, $0^n 1^n$ are context free.

b) $1^n 0^n / 0^n 1^n$

$S \rightarrow x$

$x \rightarrow 1x0 \mid \epsilon$

$S \rightarrow y$

$y \rightarrow 0y1 \mid \epsilon$

where S, x, y are variables,
language is $\{0, 1\}^*$

No matter whether the language chooses x or y , it will still create a set of terminals/resulting string representing $0^n 1^n$ or $1^n 0^n$, each having equal 0's & 1's. B/c x & y can infinitely reference itself, there can be $0^n 1^n$ or $1^n 0^n$ # of 1's and 0's. When the # reaches n , the string can simply complete by taking ϵ .

5c)

$S \rightarrow 050/151/\epsilon$

This is essentially a palindrome except S cannot include $S \rightarrow 011$ b/c the string can't have length 1. It needs to be of even length or empty. S is self referential & can loop as many times as needed & needs to start & end in the same string for each loop of S .