

DSO 530 – Bay Area Bike Share Program – Demand Forecasting Model

Project Team:









Chun Yang



Xiaoqiu Yu



Alok Abhishek



Yuzhou Dou





Agenda



- Executive Summary
- Data Description
- Process Overview
- Data Imputation and Outlier handling
- Clustering
- Statistical Models
- Results





Executive Summary





Objective

The Bay Area Bike Share enables quick, easy, and affordable bike trips around the San Francisco Bay Area. We plan to develop insights of bike usage patterns and predict the renting demand to help the company better allocate the bikes and optimize the operations. We hope to make a generic model so that it can then be adapted by bike share program in other cities in countries with final aim of helping companies optimize their operations and improve return on investment. This model can also serve a starting reference for infrastructure planning of autonomous cars.



Data Analysis Methods

Visualization of data to find correlations
Imputing data with average values to make up for missing data
Analyzing test error and validation error rate to find the best fit model



Conclusion

We found some results which were very different from our initial assumptions such as:

- Bike demand is higher on weekdays and during business hours Vs weekend or non business hours
- Bike demand is higher within downtown area Vs areas where educations institutes are

We found three main clusters of bike stations – Stations which were near commercial centers, Tourists spots or educational institutes. Demand was highly correlated to whether the day was holiday or not, and also on the temperature and visibility of the day

Data Description



2 years of bike share program operations including demand and supply provided by Bay are bike share program.

2 GB of data

4 data sets



Stations

Represents a station where users can pickup or return bikes.

7 variables



Status

Represents the number of bikes and docks available for given station and minute.

4 variables



Trip

Represents an individual bike trip.

11 variables



Weather

Represents the weather for a specific day and zip code in the bay area.

24 variables





Process Overview





- Data Discovery and initial analysis
- Went through complete data set to analyze all data and understand every feature
- Finalize imputation methods to cover for missing data

- Data Visualization and understanding
- Used Tableau to visualize relation in between different features and predictors to spot correlation and prediction capabilities
- Data correlation identification, clustering and model ideation

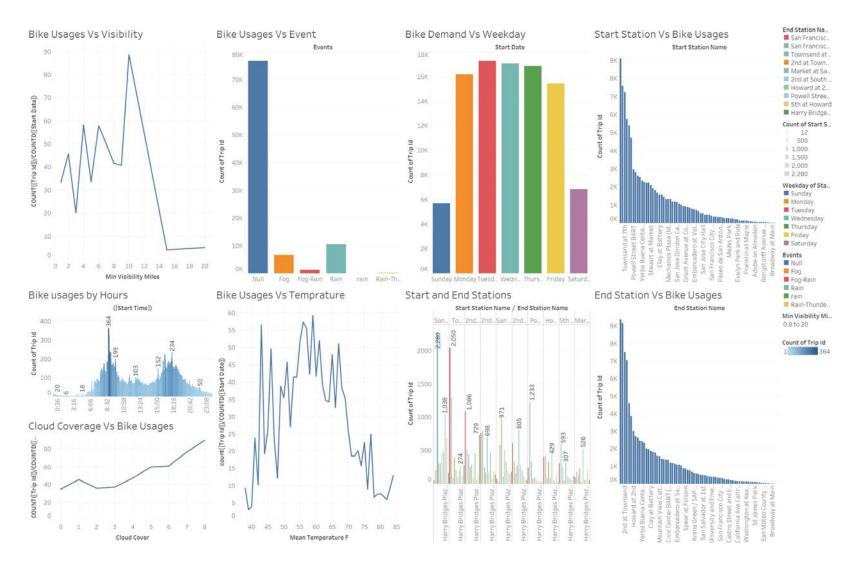
- Data Partition –
 Training, validation

 and Testing
- 70% for training
- 30% for testing

- Predictive Modeling
- Using lineal regression, LASSO, PRC, Random Forest and Decision Tree









Data Imputation & Outlier Treatment



- Some of the weather data like Temperature, Visibility, Cloud Coverage etc. was not available for all zip codes for everyday.
- Since the stations and ZIP codes were geographically close by and weather conditions do not vary too much across the area, we took average across all the zip codes to impute the missing values.
- For all predictors we checked data set for outliers and removed them before modeling.

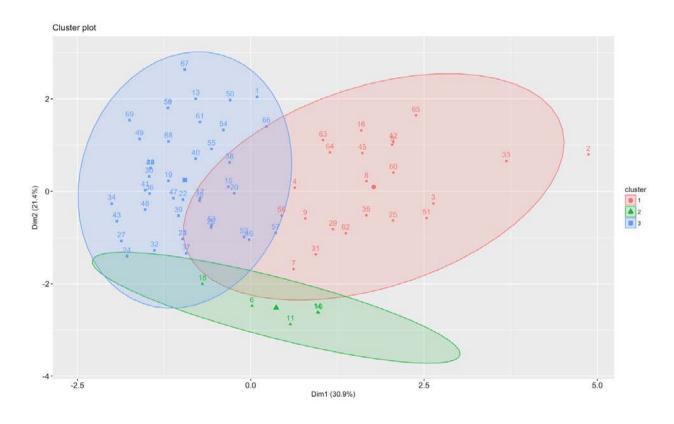
Variables	# of NA	Duration	Duration			
max/mean/min_temperature_f	4	Min.	60			
max/mean/min_dew_point_f	54	1st Qu.	347			
max/mean/min_humidity	54	Median	518			
max/mean/min_sea_level_pressure_inches	1	Mean	1019			
max/mean/min_visibility_miles	22	3rd Qu.	748			
max/mean/min_wind_Speed_mph	1	Max.	17270400			
wind_dir_degrees	1					

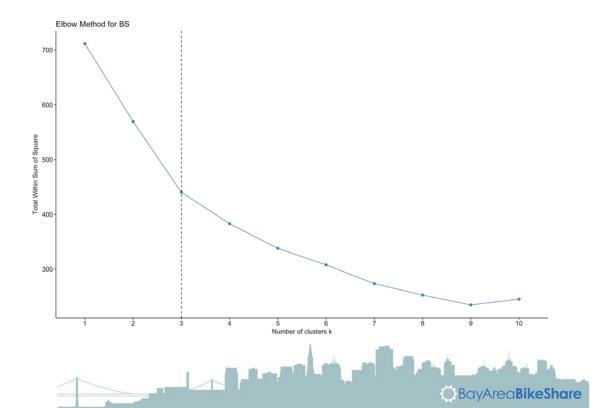
	id ÷	duration*	start date	start_station_name	start station id	end date	end station name
573567	568474	17270400	12/6/2014 21:59	South Van Ness at Market	66	6/24/2015 20:18	2nd at Folsom
382719	825850	2137000	6/28/2015 21:50	Market at Sansome	77	7/23/2015 15:27	Yerba Buena Center of the
440340	750192	1852590	5/2/2015 6:17	San Antonio Shopping Center	31	5/23/2015 16:53	Castro Street and El Camin
371067	841176	1133540	7/10/2015 10:35	University and Emerson	35	7/23/2015 13:27	University and Emerson
80511	111309	722236	11/30/2013 13:29	University and Emerson	35	12/8/2013 22:06	University and Emerson
606064	522337	720454	10/30/2014 8:29	Redwood City Caltrain Station	22	11/7/2014 15:36	Stanford in Redwood City
223017	323594	716480	6/13/2014 16:57	Harry Bridges Plaza (Ferry Building)	50	6/21/2014 23:59	Civic Center BART (7th at N
195380	361321	715339	7/13/2014 5:50	Arena Green / SAP Center	14	7/21/2014 12:32	Adobe on Almaden
421840	774999	688899	5/20/2015 15:27	Palo Alto Caltrain Station	34	5/28/2015 14:49	California Ave Caltrain Stat
524522	635260	655939	2/8/2015 3:05	San Jose Civic Center	3	2/15/2015 17:17	SJSU 4th at San Carlos
287338	237942	644771	4/6/2014 3:37	South Van Ness at Market	66	4/13/2014 14:44	Clay at Battery



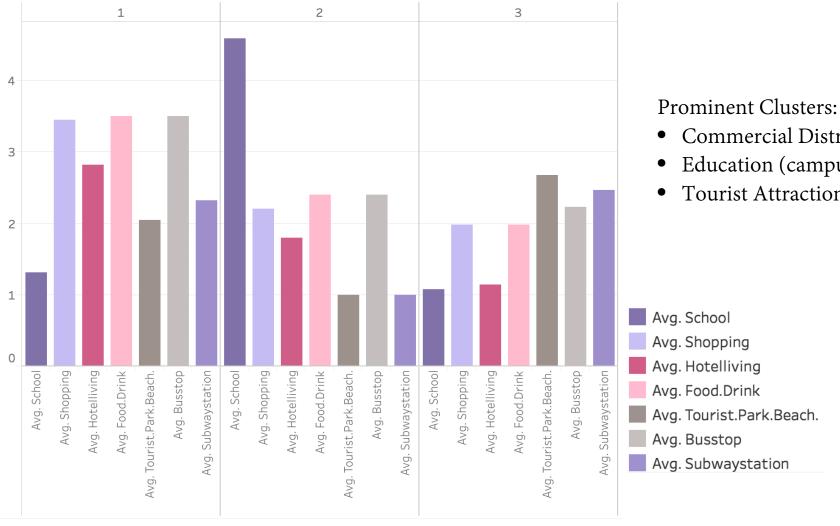
Data Clustering

- Food & Drink Count the restaurants and cafes within 200 meters
- School Calculate the distance to the border of campus and library
- Hotel Count the hotels within 200 meters
- Shopping Count the shopping malls and supermarkets within 200 meters
- Tourist Calculate the distance to the border of parks and beach
- Bus Stops Count the bus stops within 200 meters
- Subway Station -Count the subway stations within 200 meters









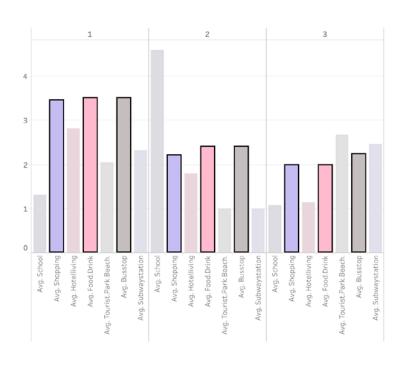
- Commercial Districts (office, shopping, restaurants)
- Education (campus, library)
- Tourist Attraction Spots (pikes, beaches)

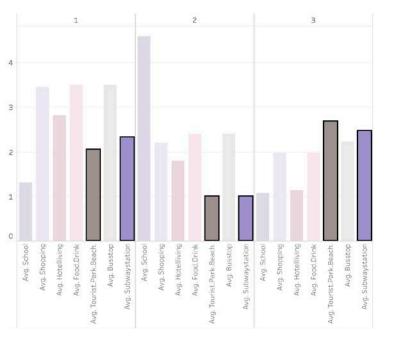
Avg. Tourist.Park.Beach.

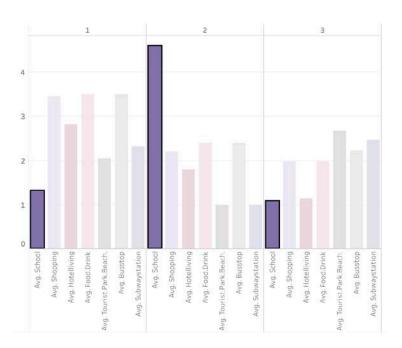


Three Types of Stations





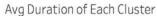


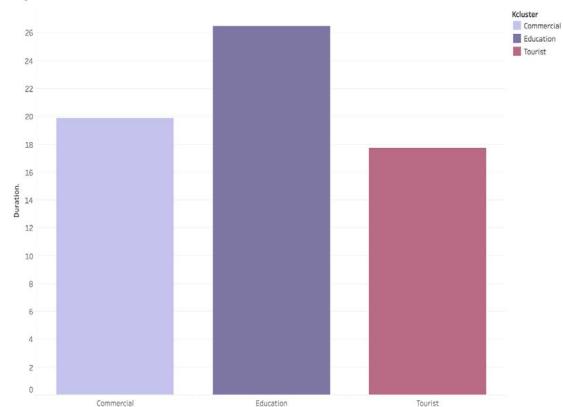


Commercial Stations Tourist Educations



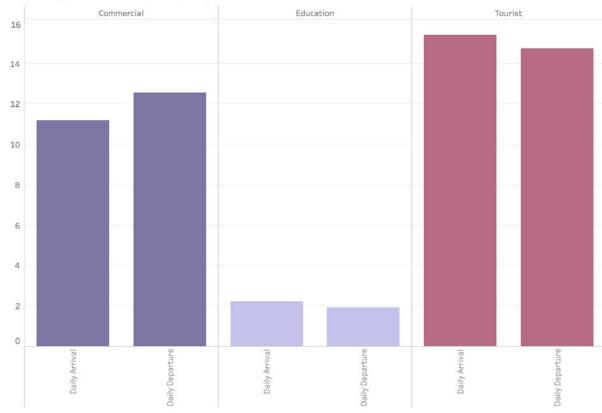






Sum of Duration, for each Kcluster. Color shows details about Kcluster.

Avg Daily Arrival & Avg Daily Departure

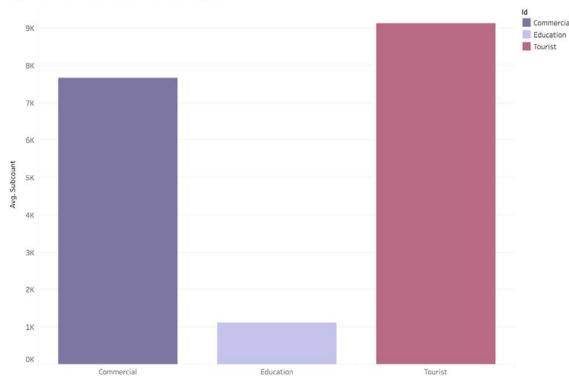


Daily Arrival and Daily Departure for each Id. Color shows details about Id.



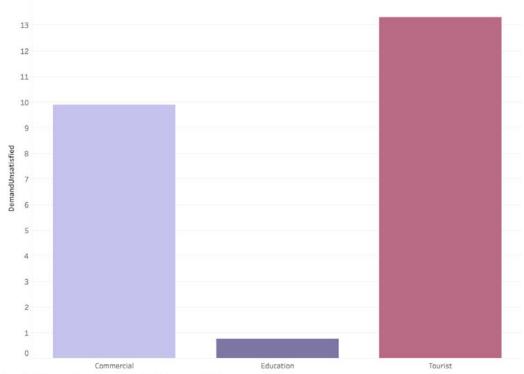






Average of Subcount for each Id. Color shows details about Id.

Avg Demand Unsatisfied Minutes

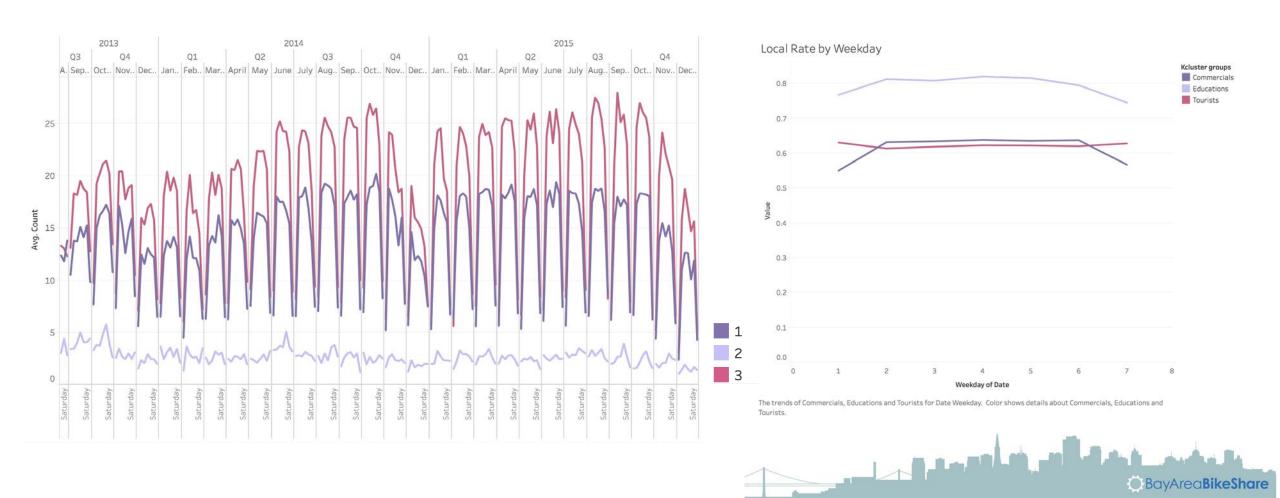


Sum of Daily for each Group. Color shows details about sum of Daily.



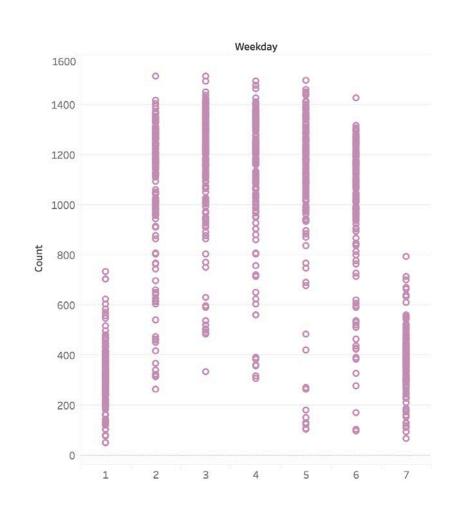


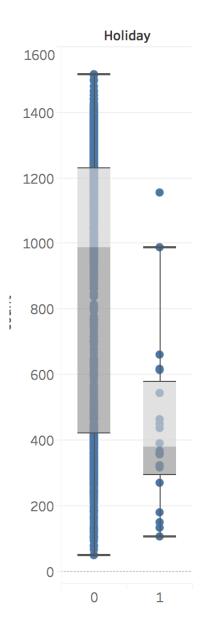
Bike rental pattern for stations around shopping centers and Tourist spots showed similar patterns whereas bike rental pattern in areas close to school showed very low usages probably indicating students saw value in owning their own bikes and using skateboards to travel instead of using bike share program.

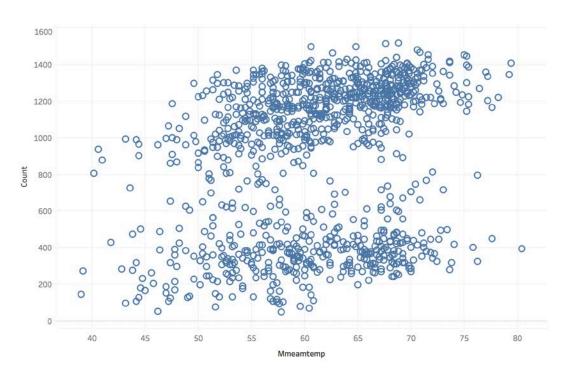


Linear Regression











Linear Regression – Correlation matrix



	count v	weekday	month	day	mmaxtemp m	meamtemp m	mintemp r	nmaxdew m	meandew 1	nmi ndew		mmaxhum	mmeanhum	mmi nhum	mmaxsea	mmeansea	mmi nsea	maxvi s	mmeanvi s	mmi nvi s	mmaxwi nd]	mmeanwind n	maxgust cloud
count		J	- 0. 015	<i>J</i>	0. 262	0. 259	0. 211	0. 167	0. 163	0. 155	count	-0.114	- 0. 133		- 0. 109		- 0. 056		0. 153	0. 164	0. 021	count	0. 017	-0.037 -0.127
weekday	- 0. 001	1. 000	- 0. 009	0. 014	0. 006	0. 007	0. 007	0. 020	0. 022	0. 025	weekday	0. 033	0. 028	0. 020	- 0. 038	- 0. 039	- 0. 039 -	0. 019	- 0. 003	- 0. 025	- 0. 008	weekday	- 0. 022	-0.021 -0.006
month	- 0. 015	- 0. 009	1.000	0. 012	0. 104	0. 111	0. 103	0. 123	0. 093	0. 074	month	0. 015	0. 005	-0.031	- 0. 139	- 0. 140	- 0. 139	0. 011	0. 016	0. 039	- 0. 066	month	- 0. 097	- 0. 001 - 0. 120
day	-0.021	0. 014	0. 012	1.000	0. 022	0. 017	0. 008	0. 013	0. 007	- 0. 005	day	0.006	- 0. 016	-0.033	0. 037	0. 043	0. 047	0. 040	0. 035	0. 020	0. 048	day	0. 030	0. 022 - 0. 058
mmaxtemp	0. 262	0. 006	0. 104	0. 022	1. 000	0. 933	0. 698	0. 658	0. 554	0. 450	mmaxtemp	- 0. 283	- 0. 417	- 0. 464	- 0. 471	- 0. 418	- 0. 376	0. 195	0. 331	0. 387	0. 125	mmaxtemp	0.068	0. 029 - 0. 376
mmeamtemp	0. 259	0.007	0. 111	0. 017	0. 933	1. 000	0. 908	0. 813	0. 759	0. 677	mmeamtemp	- 0. 182	-0. 202	-0.199	- 0. 595	- 0. 542	- 0. 488	0. 244	0. 285	0. 294	0. 264	mmeamtemp	0. 290	0. 155 - 0. 107
mmi ntemp	0. 211	0.007	0. 103	0.008	0. 698	0. 908	1. 000	0. 855	0.868	0. 828	mmi ntemp	- 0. 037	0. 081	0. 143	- 0. 639	- 0. 593	- 0. 536	0. 257	0. 180	0. 135	0. 377	mmi ntemp	0. 490	0. 273 0. 223
mmaxdew	0. 167	0. 020	0. 123	0. 013	0. 658	0. 813	0. 855	1. 000	0.964	0. 882	mmaxdew	0. 340	0. 344	0. 284	- 0. 529	- 0. 498	- 0. 459	0. 195	0. 014	- 0. 061	0. 225	mmaxdew	0. 262	0. 145 0. 236
mmeandew	0. 163	0. 022	0.093	0.007	0. 554	0. 759	0.868	0. 964	1.000	0. 968	mmeandew	0. 392	0. 465	0.430	- 0. 534	- 0. 497	- 0. 450	0. 210	0.002	- 0. 074	0. 232	mmeandew	0. 315	0. 148 0. 325
mmi ndew	0. 155	0. 025	0.074	- 0. 005	0. 450	0. 677	0. 828	0. 882	0. 968	1. 000	mmi ndew	0. 385	0. 526	0. 529	- 0. 506	- 0. 468	- 0. 418	0. 207	0. 003	- 0. 070	0. 213	mmi ndew	0. 328	0. 128 0. 370
mmaxhum	-0.114	0. 033	0.015	0.006	- 0. 283	- 0. 182	- 0. 037	0. 340	0. 392	0. 385	mmaxhum	1.000	0. 861	0.649	0. 061	0. 034	0. 011 -	0.054	- 0. 426	- 0. 548	- 0. 107	mmaxhum	- 0. 116	-0.059 0.412
mmeanhum	-0.133	0. 028	0.005	- 0. 016	- 0. 417	- 0. 202	0. 081	0. 344	0. 465	0. 526	mmeanhum	0.861	1.000	0.935	0.007	- 0. 011	- 0. 017 -	0.045	- 0. 455	- 0. 578	- 0. 034	mmeanhum	0.041	-0.004 0.653
mmi nhum	- 0. 127	0. 020	- 0. 031	- 0. 033	- 0. 464	- 0. 199	0. 143	0. 284	0.430	0. 529	mmi nhum	0.649	0. 935	1.000	- 0. 027	- 0. 039	- 0. 035 -	0.026	- 0. 403	- 0. 519	0.046	mmi nhum	0. 172	0.052 0.736
mmaxsea	- 0. 109	- 0. 038	- 0. 139	0.037	- 0. 471	- 0. 595	- 0. 639	- 0. 529	- 0. 534	- 0. 506	mmaxsea	0.061	0.007	- 0. 027	1.000	0. 982	0. 933 -	0. 203	- 0. 136	- 0. 077	- 0. 378	mmaxsea	- 0. 432	-0.340 -0.104
mmeansea	- 0. 079	- 0. 039	- 0. 140	0.043	- 0. 418	- 0. 542	- 0. 593	- 0. 498	- 0. 497	- 0. 468	mmeansea	0.034	-0.011	-0.039	0. 982	1. 000	0. 980 -	0. 186	- 0. 097	- 0. 023	- 0. 387	mmeansea	- 0. 442	- 0. 362 - 0. 129
mmi nsea	- 0. 056	- 0. 039	- 0. 139	0.047	- 0. 376	- 0. 488	- 0. 536	- 0. 459	- 0. 450	- 0. 418	mmi nsea	0.011	-0.017	-0.035	0. 933	0. 980	1. 000 -	0. 159	- 0. 062	0. 018	- 0. 378	mmi nsea	- 0. 425	- 0. 365 - 0. 133
maxvi s	0.085	- 0. 019	0.011	0.040	0. 195	0. 244	0. 257	0. 195	0. 210	0. 207	maxvi s	- 0. 054	- 0. 045	-0.026	- 0. 203	- 0. 186	- 0. 159	1.000	0. 488	0. 165	0. 135	maxvi s	0. 181	0. 119 - 0. 007
mmeanvi s	0. 153	- 0. 003	0.016	0.035	0. 331	0. 285	0. 180	0. 014	0.002	0. 003	mmeanvi s	- 0. 426	- 0. 455	- 0. 403	- 0. 136	- 0. 097	- 0. 062	0. 488	1. 000	0. 822	0. 150	mmeanvi s	0. 157	0.080 -0.348
mmi nvi s	0. 164	- 0. 025	0.039	0.020	0. 387	0. 294	0. 135	- 0. 061	- 0. 074	- 0. 070	mmi nvi s	- 0. 548	- 0. 578	- 0. 519	- 0. 077	- 0. 023	0. 018	0. 165	0. 822	1. 000	0. 070	mmi nvi s	0.065	-0.023 -0.493
mmaxwi nd	0. 021	- 0. 008	- 0. 066	0.048	0. 125	0. 264	0.377	0. 225	0. 232	0. 213	mmaxwi nd	- 0. 107	- 0. 034	0.046	- 0. 378	- 0. 387	- 0. 378	0. 135	0. 150	0.070	1. 000	mmaxwi nd	0. 778	0. 727 0. 156
mmeanwi nd	0.017	- 0. 022	- 0. 097	0.030	0.068	0. 290	0.490	0. 262	0. 315	0. 328	mmeanwi nd	- 0. 116	0. 041	0. 172	- 0. 432	- 0. 442	- 0. 425	0. 181	0. 157	0.065	0. 778	mmeanwi nd	1. 000	0. 678 0. 308
mmaxgust	- 0. 037	- 0. 021	- 0. 001	0.022	0. 029	0. 155	0. 273	0. 145	0. 148	0. 128	mmaxgust	- 0. 059	- 0. 004	0.052	- 0. 340	- 0. 362	- 0. 365	0. 119	0.080	- 0. 023	0. 727	mmaxgust	0. 678	1.000 0.180
cl oud	- 0. 127	- 0. 006	- 0. 120	- 0. 058	- 0. 376	- 0. 107	0. 223	0. 236	0. 325	0. 370	cl oud	0. 412	0.653	0.736	- 0. 104	- 0. 129	- 0. 133 -	0.007	- 0. 348	- 0. 493	0. 156	cl oud	0. 308	0. 180 1. 000



Linear Regression



Full Model

lm.fit=lm(count~.-date-duration-sub, data=data[train,])

<pre>vif(lm.fit)</pre>						
weekday	month	day	event	weekend	holiday	mmaxtemp
1.026024	1.202142	1.044923	1.846574	1.046579	1.059185	462.925027
mmeamtemp	mmintemp	mmaxdew	mmeandew	mmindew	mmaxhum	mmeanhum
1295.424991	318.323474	47.956358	167.751547	44.492718	17.693517	95.831976
mminhum	mmaxsea	mmeansea	mminsea	maxvis	mmeanvis	mminvis
42.679265	75.021175	218.311572	58.703600	1.827680	5.878593	6.602745
mmaxwind	mmeanwind	mmaxgust	cloud			
2 202522	1 702712	2 622214	2 526/10			

Smaller Model

lm.fit=lm(count~weekday + event + weekend + holiday + mmeamtemp +
mmeandew + mmeanhum + mmeansea + mminvis + mmeanwind + mmaxgust +
cloud, data[train,])

```
vif(lm.fit)

weekday event weekend holiday mmeamtemp mmeandew mmeanhum mmeansea

1.013967 1.699207 1.024605 1.026191 34.534470 44.657349 22.580461 1.682451

mminvis mmeanwind mmaxgust cloud

2.298920 2.493138 2.012138 2.232380
```



Linear Regression

Smaller Model

Final Model

MSE: 185.6062



```
lm.fit=lm(count~ weekday +event + weekend + holiday + mmeamtemp +
mmeanhum + mmeansea + mminvis + mmeanwind + mmaxgust + cloud,
data[train, ])

vif(lm.fit)
weekday event weekend holiday mmeamtemp mmeandew mmeanhum mmeansea
1.013967 1.699207 1.024605 1.026191 34.534470 44.657349 22.580461 1.682451
mminvis mmeanwind mmaxgust cloud
2.298920 2.493138 2.012138 2.232380
```

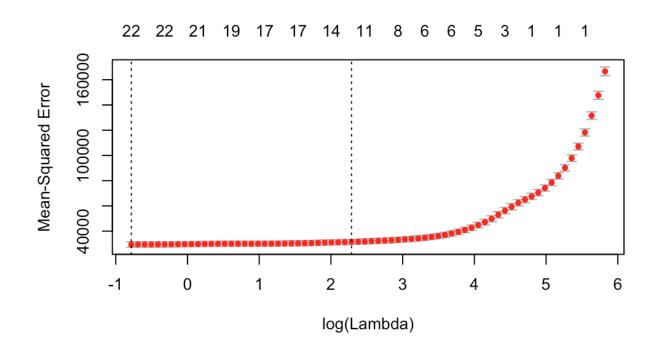
```
lm.fit=lm(count~ event + weekend + holiday + mmeamtemp + mminvis +
mmaxgust + cloud, data[train, ])

Residual standard error: 174.1 on 761 degrees of freedom Multiple R-squared: 0.82, Adjusted R-
squared: 0.8184 F-statistic: 495.4 on 7 and 761 DF, p-value: < 2.2e-16
> vif(lm.fit)
   event weekend holiday mmeamtemp mminvis mmaxgust cloud
1.688162 1.014836 1.023197 1.161850 1.799213 1.071834 1.454505
```



LASSO





bestlam [1] 0.4569004

Variables dropped: Mean temperature Mean sea level pressure

Model Results: MSE: 181.2726



Best Subset



Best subset selection—all 27 variables included

1: weekend

2: weekend mmaxtemp

3: weekend holiday mmaxtemp

4: weekend holiday mmeantemp mminvis....

Based on r^2 , 25 variables are selected

Based on adjusted r², 18 variables are selected

Fit the model again using 18 variables, the test MSE is 182.5887

PCR



Smallest CV happens when the model has 24 components and has explained 100 %

VALIDATION: RMSEP

Cross-validated using 10 random segments.

```
(Intercept) 1 comps 2 comps 3 comps 4 comps 5 comps 6 comps 7 comps 8 comps
CV
             408.7
                      403.2
                               394.6
                                        393.1
                                                 393.5
                                                          360.2
                                                                   363.9
                                                                            339.5
                                                                                     328.3
                      403.2
adjCV
             408.7
                               394.5
                                        393.0
                                                 393.4
                                                          359.2
                                                                   363.7
                                                                            338.6
                                                                                     330.1
      9 comps 10 comps 11 comps 12 comps 13 comps 14 comps 15 comps
                                                                          16 comps 17 comps
         311.9
                  197.3
                             182.3
                                       175.7
                                                 175.3
                                                           175.8
                                                                     176.2
                                                                               176.2
CV
                                                                                         175.8
        311.7
                  191.0
                            181.9
                                       175.4
                                                 175.0
                                                          175.5
                                                                     175.9
                                                                                         175.5
adiCV
                                                                               175.8
     18 comps 19 comps 20 comps 21 comps 22 comps 23 comps 24 comps 25 comps
         175.1
                   175.4
                              175.8
                                        174.0
                                                  173.4
                                                            173.3
                                                                      173.3
                                                                                173.5
CV
adjCV
          174.7
                   175.0
                              175.4
                                        173.5
                                                  173.0
                                                            172.8
                                                                      172.9
                                                                                173.1
```

TRAINING: % variance explained

```
1 comps 2 comps 3 comps 4 comps 5 comps 6 comps 7 comps 8 comps 9 comps 10 comps
       27.878
                47.987
                                                      73.42
Χ
                          57.922
                                   64.323
                                             69.04
                                                               77.54
                                                                        81.43
                                                                                 85.13
                                                                                           88.62
        2.735
                  7.268
                           8.267
                                    8.336
                                             22.69
                                                      23.35
                                                               34.66
                                                                        40.67
                                                                                 48.97
                                                                                           79.88
count
     11 comps 12 comps 13 comps 14 comps 15 comps 16 comps 17 comps 18 comps 19 comps
                              96.21
                                                  98.15
          91.87
                    94.28
                                        97.26
                                                            98.89
                                                                      99.23
                                                                                99.46
                                                                                           99.66
Χ
          81.19
                    82.54
                              82.62
                                        82.63
                                                  82.63
                                                            82.66
                                                                      82.82
                                                                                83.01
                                                                                          83.03
count
     20 comps 21 comps 22 comps 23 comps 24 comps 25 comps
          99.83
                    99.94
                              99.97
                                        99.99
                                                 100.00
                                                           100.00
Χ
          83.03
                    83.41
                              83.58
                                        83.63
                                                  83.63
                                                            83.63
count
```

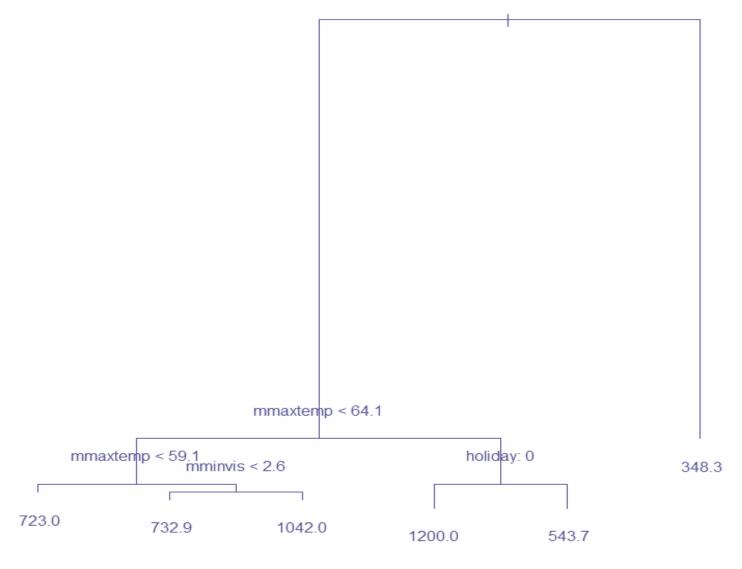
The test error is 182.2452



Decision Tree



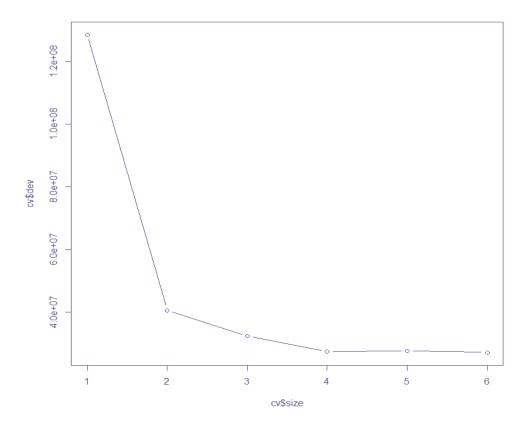




The simple decision tree includes only 6 terminal node. It splits on weekend mmaxtemp holiday and mminvis

Decision Tree

Based on the deviance, there is no need to prune the tree The test error is 189.8095



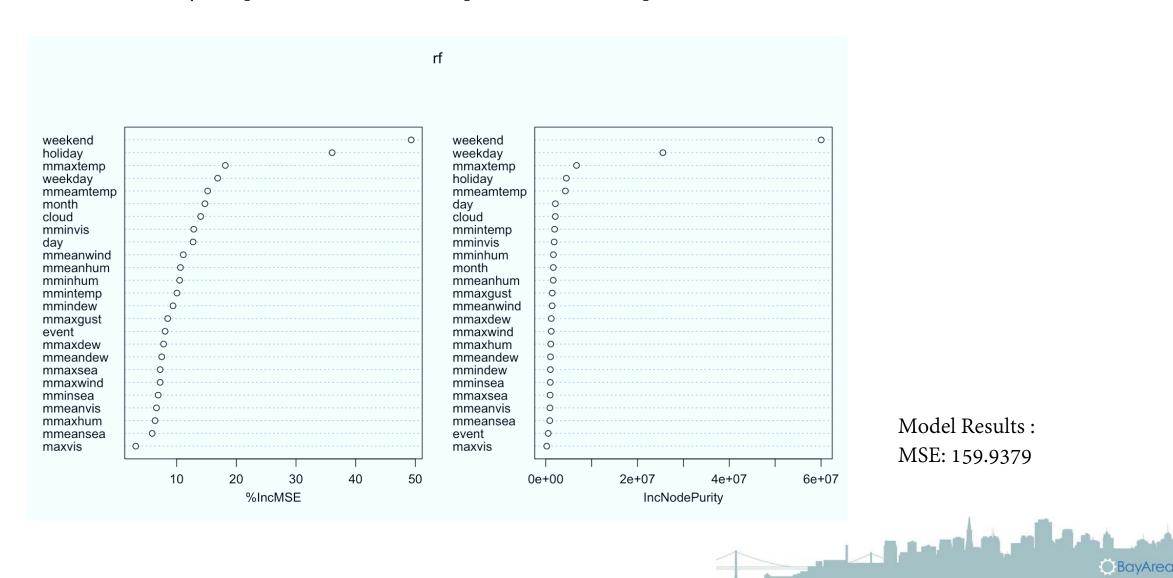




Random Forest



Weekend, holiday, temperature are the most important variables to predict the demand.



Model Results:

MSE: 159.9379

Statistical Models





Linear Regression

MSE - 185.6062



LASSO

MSE - 181.2726 $\lambda - 0.4569004$



Best Selection

MSE – 182.5887 Variables# 18



Random Forest

MSE - 159.9379



Decision Tree

MSE – 189.8095 Terminal Nodes# 6



PCR

MSE – 182.2452 Components# 24



Important Predictors





Weekends

Weekday and Weekends have very different bike demand patterns



Holidays

Bike demand pattern is very different for holidays Vs non Holidays



Temperature

Both extremely high temperature and low temperature negatively impacts bike demands Temperature in between 55° F to 65° F is the sweet spot for high bike usages.



Q&A

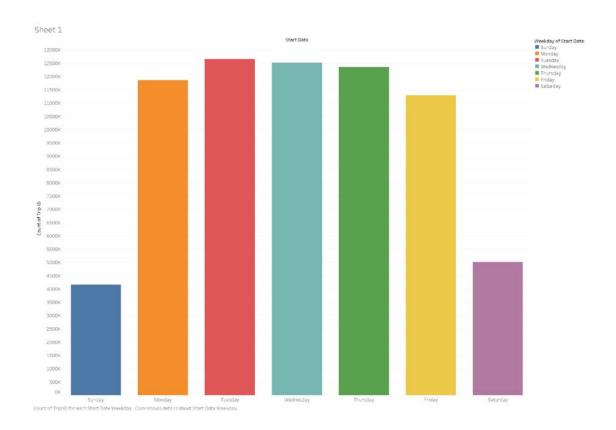




Appendix



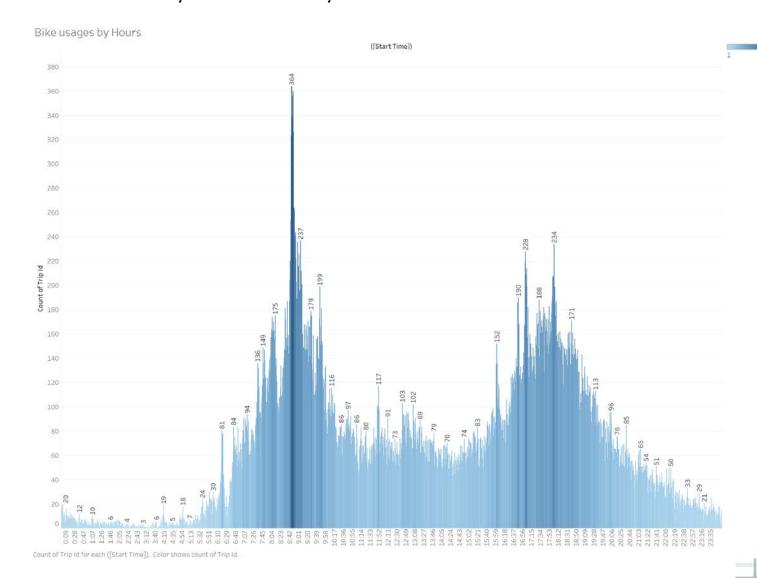
Bike usages pattern on different weekdays



Bike demand on weekends in significantly lower than bike demand on weekdays



Bike demand by hours of the day

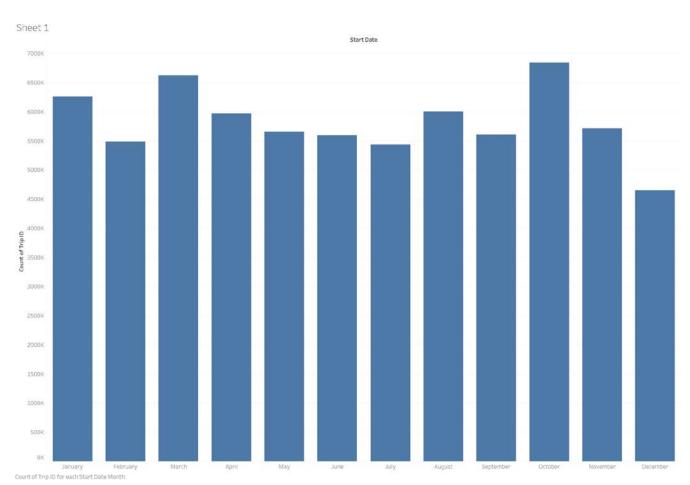


Bi-Model usages pattern with two spikes:

- 1. One at 9 am in the morning and
- 2. Second at 6 pm in the evening



Bike usages pattern for different months

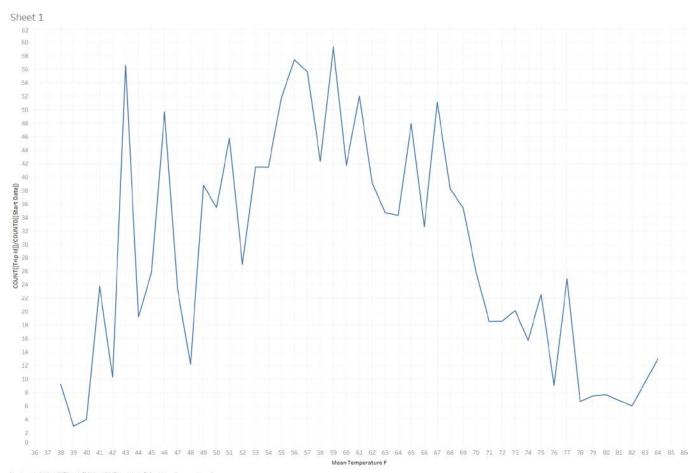


Except for December there is not a lot of variability in demand of bikes across different month.

The drop in December could be contributed to the holiday season.



Effect of temperature on bike demand



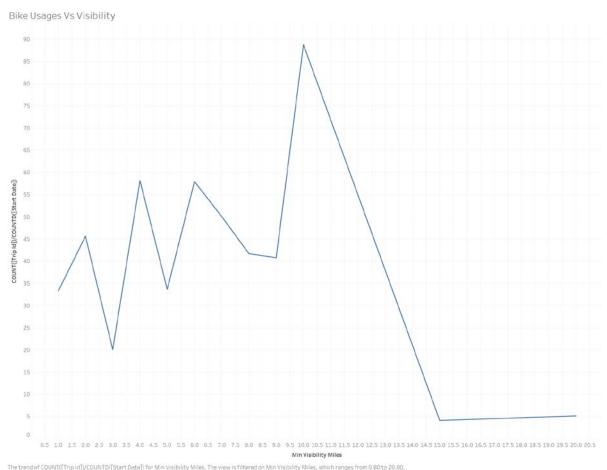
High and Low temperature both negatively impacts the bike demand.

Low temperature has higher variability in the demand

The trend of COUNT([Trip id]]/COUNTD([Start Date]) for Mean Temperature F.



Effect of visibility on bike demand



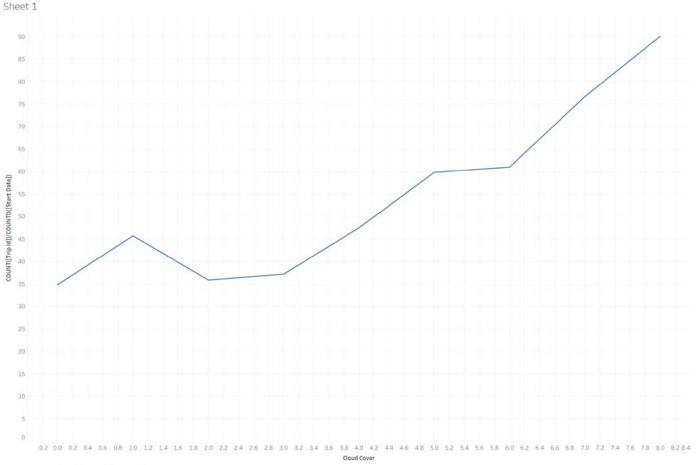
**High visibility correlates to high temperature and therefore bike demand drops off after certain threshold

The trend of COUNT([Trip Id]]/COUNTD[[Start Date]] for Min Visibility Miles. The view is filtered on Min Visibility Miles, which ranges from 0.80 to 20.00.





Bike usages and Cloud Cover – Higher Cloud Cover means lower wind and lower temperature.. Looks like very good indicator for bike usages

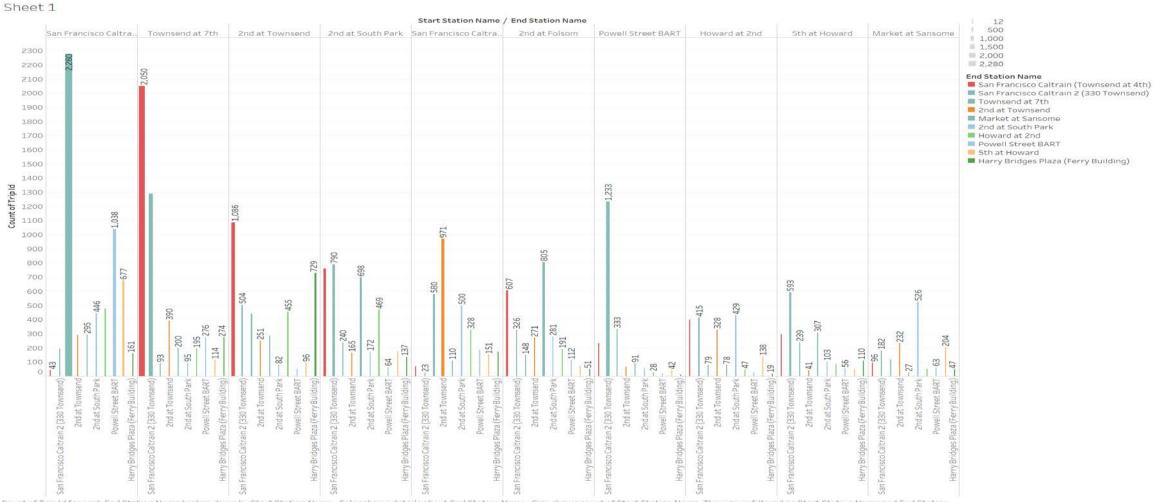


The trend of COUNT([Trip Id])/COUNTD([Start Date]) for Cloud Cover





Bike demand in between top ten stations

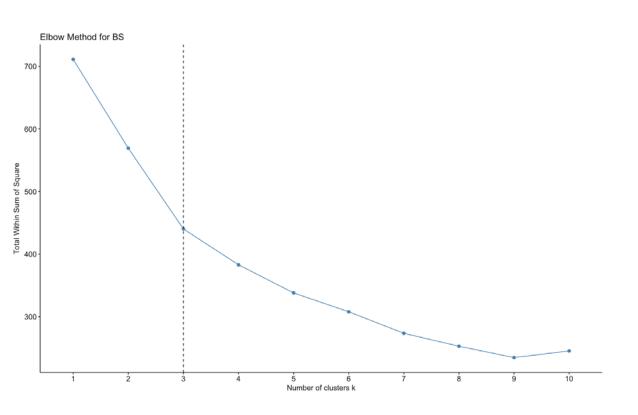


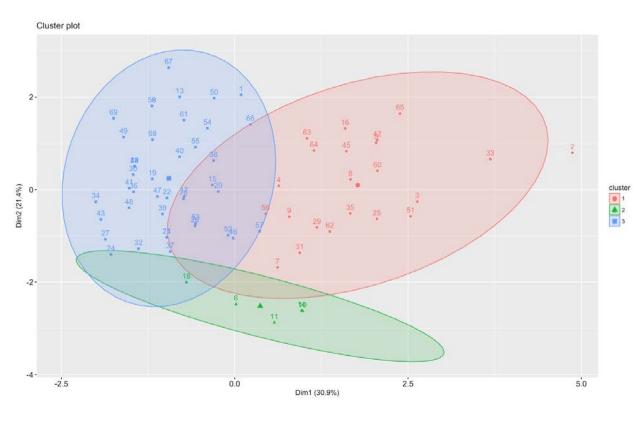
Count of Trip Id for each End Station Name broken down by Start Station Name. Color shows details about End Station Name. Size shows count of Start Station Name. The view is filtered on Start Station Name and End Station Name. The Start Station Name filter keeps 10 of 74 members. The End Station Name filter keeps 10 of 74 members.



Data Clustering



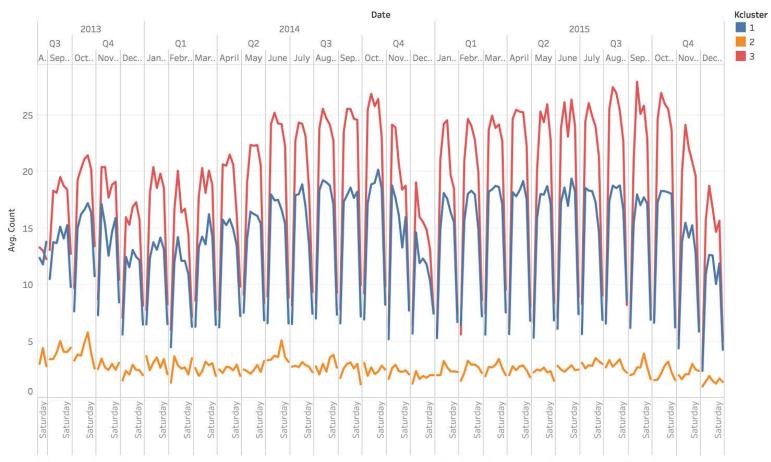








Sheet 4



The trend of average of Count for Date Weekday broken down by Date Year, Date Quarter and Date Month. Color shows details about Kcluster. The view is filtered on Date Year and Kcluster. The Date Year filter keeps 2013, 2014 and 2015. The Kcluster filter keeps 1, 2 and 3.





Building first model with all predictors except date and duration of the rental.

```
lm.fit=lm(count~.-date-duration, data=data[train,])
```

```
## Coefficients:
##
                 Estimate Std. Error t value Pr(>|t|)
## (Intercept)
                578.42707
                           569.28005
                                        1.016 0.309928
## weekday
                  4.34430
                              0.90165
                                        4.818 1.76e-06 ***
## month
                  0.31506
                              0.56375
                                        0.559 0.576418
                  0.21710
## day
                              0.20652
                                        1.051 0.293499
                -10.33674
                              5.99979
                                       -1.723 0.085332
## event1
## weekend1
                 14.42102
                              9.68442
                                        1.489 0.136887
## holiday1
                 37.90535
                             14.38891
                                        2.634 0.008606 **
## sub
                  0.93281
                              0.01032
                                       90.392 < 2e-16 ***
## mmaxtemp
                 14.86021
                              4.55701
                                        3.261 0.001161 **
## mmeamtemp
                -32.70388
                              8.97154
                                       -3.645 0.000286 ***
## mmintemp
                 19.79481
                              4.51608
                                        4.383 1.34e-05 ***
                 -1.55852
                              1.94859
                                       -0.800 0.424071
## mmaxdew
## mmeandew
                  3.00123
                              3.16847
                                        0.947 0.343837
                  0.66477
                              1.37813
## mmindew
                                        0.482 0.629688
                 -0.35587
                              0.97179
                                       -0.366 0.714321
## mmaxhum
## mmeanhum
                  0.28764
                              1.77564
                                        0.162 0.871355
                 -1.50255
                              0.86563
## mminhum
                                       -1.736 0.083015
## mmaxsea
               -509.14426
                            115.92807
                                       -4.392 1.29e-05 ***
## mmeansea
                786.18124
                            201.30784
                                        3.905 0.000103 ***
               -295.99496
## mminsea
                            102.30668
                                       -2.893 0.003925 **
                  8.46994
                              3.07204
                                        2.757 0.005975 **
## maxvis
                 -0.58194
## mmeanvis
                              4.54638
                                       -0.128 0.898183
## mminvis
                  1.80940
                              1.80468
                                        1.003 0.316371
## mmaxwind
                  0.30649
                              0.67761
                                        0.452 0.651174
                 -6.05022
                              1.46041
                                       -4.143 3.83e-05 ***
## mmeanwind
                  1.21832
                              0.49858
                                        2.444 0.014775
## mmaxgust
                 -7.97502
                                       -4.929 1.02e-06 ***
## cloud
                              1.61785
## Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
## Residual standard error: 48.51 on 742 degrees of freedom
## Multiple R-squared: 0.9864, Adjusted R-squared: 0.9859
## F-statistic: 2066 on 26 and 742 DF, p-value: < 2.2e-16
```

```
vif(lm.fit)
       weekday
                                                          weekend
                                                                       holiday
                      month
                                     day
                                                event
      1.027814
                   1.222056
                                1.050529
                                            1.856674
                                                         6.012019
                                                                      1.462918
           sub
                   mmaxtemp
                               mmeamtemp
                                            mmintemp
                                                          mmaxdew
                                                                      mmeandew
      6.447136
                 463.949558 1295.945348
                                          318.503342
                                                        47.973284
                                                                    168.174409
       mmindew
                    mmaxhum
                                mmeanhum
                                              mminhum
                                                          mmaxsea
                                                                      mmeansea
                  17.903077
                                           42.712696
     44.646099
                               97.775558
                                                        75.168141
                                                                    219.318652
       mminsea
                     maxvis
                                              mminvis
                                                                     mmeanwind
                                mmeanvis
                                                         mmaxwind
     59.161199
                   1.830159
                                5.892397
                                            6.651169
                                                         3.302713
                                                                      4.711032
      mmaxgust
                      cloud
      2.641716
                   3.539605
```

High VIF of certain some predictors indicate these predictors have collinearity



Only include one variable for each weather dimension. Select min visibility and max wind, select mean values for all the remaining weather variables. Fit the model again.

```
vif(lm.fit)
                                   holiday
     weekday
                 event
                         weekend
                                                 sub mmeamtemp mmeandew
                        5.693402
                                  1.406270
                                            6.093044 35.096598 46.247453
    1.015807
             1.715371
                                  mmaxwind
    mmeanhum
                         mminvis
                                            mmaxgust
              mmeansea
                                                         cloud mmeanwind
             1.688764 2.312401
                                            2.576081 2.243650
## 23.200081
                                  3.235083
                                                                3.324315
```

Max wind becomes insignificant. Replace it with mean wind, and fit the model.



```
## Residuals:
        Min
                       Median
                                            Max
## -152.939
            -30.438
                       -2.475
                                23.563 286.842
##
## Coefficients:
                Estimate Std. Error t value Pr(>|t|)
## (Intercept) 430.83072
                          565.06479
                                      0.762 0.44603
                 4.58236
## weekday
                            0.93322
                                      4.910 1.12e-06 ***
               -15.45540
                            6.00402
                                     -2.574 0.01024 *
## event1
## weekend1
                10.29027
                            9.81169
                                      1.049
                                            0.29462
                                            0.03642 *
## holiday1
                           14.68745
                30.78426
                                      2.096
                            0.01044
## sub
                 0.92929
                                     88.973
                                             < 2e-16 ***
                            1.53709
                                            0.26846
                1.70224
                                      1.107
## mmeamtemp
                 2.50876
                           1.72985
                                      1.450 0.14740
## mmeandew
                -0.89924
                            0.90049
                                            0.31830
## mmeanhum
                                     -0.999
               -14.85248
                           18.39085
                                     -0.808
## mmeansea
                                            0.41957
                 2.93198
                            1.10784
                                            0.00830 **
## mminvis
                                      2.647
                 0.14922
                            0.69820
                                      0.214 0.83082
## mmaxwind
                1.34533
                            0.51259
## mmaxgust
                                      2.625
                                             0.00885 **
                -6.48441
                            1.34101
                                     -4.835 1.61e-06 ***
## cloud
                            1.27721
                                     -3.713 0.00022 ***
## mmeanwind
                -4.74191
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 50.5 on 754 degrees of freedom
## Multiple R-squared: 0.985, Adjusted R-squared: 0.9847
## F-statistic: 3534 on 14 and 754 DF, p-value: < 2.2e-16
```





```
## Residuals:
##
                                    3Q
        Min
                  1Q
                       Median
                                            Max
## -152.769 -30.532
                       -2.443
                                23.642
                                        286.702
##
## Coefficients:
##
                Estimate Std. Error t value Pr(>|t|)
## (Intercept) 426.74219
                          564.38384
                                      0.756 0.44981
                 4.58283
                            0.93262
## weekday
                                      4.914 1.10e-06 ***
               -15.51768
                            5.99315
                                     -2.589
                                             0.00980 **
## event1
                            9.80281
## weekend1
                10.24132
                                      1.045
                                             0.29648
## holiday1
                30.69521
                           14.67226
                                      2.092
                                             0.03677 *
                 0.92925
                            0.01044
                                             < 2e-16 ***
## sub
                                     89.038
                1.71726
                            1.53452
                                             0.26346
## mmeamtemp
                                      1.119
                 2.49843
                            1.72808
## mmeandew
                                      1.446
                                             0.14865
                -0.89463
                            0.89966
                                     -0.994 0.32034
## mmeanhum
## mmeansea
               -14.71670
                           18.36825
                                     -0.801 0.42327
                 2.92494
                            1.10665
                                      2.643 0.00839 **
## mminvis
                            1.10538
                                     -4.166 3.45e-05 ***
## mmeanwind
                -4.60542
                            0.45574
## mmaxgust
                 1.39536
                                      3.062 0.00228 **
                            1.33689
                                     -4.865 1.39e-06 ***
## cloud
                -6.50445
## ---
## Signif. codes: 0 '*** 0.001 '** 0.01 '* 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 50.47 on 755 degrees of freedom
## Multiple R-squared: 0.985, Adjusted R-squared: 0.9847
## F-statistic: 3811 on 13 and 755 DF, p-value: < 2.2e-16
```



```
## Residuals:
                                   3Q
        Min
                      Median
                                           Max
## -152.994 -31.468
                      -3.113
                               24.972 292.347
##
## Coefficients:
                Estimate Std. Error t value Pr(>|t|)
## (Intercept) -93.163232
                          20.421763 -4.562 5.91e-06 ***
                           0.930578
## weekday
                4.598221
                                      4.941 9.56e-07 ***
                           5.990743 -2.635 0.00859 **
## event1
               -15.783744
## holiday1
                          12.711315
                                     1.791 0.07371 .
                22.764633
## sub
                           0.004411 208.487 < 2e-16 ***
                0.919697
                4.120414
                           0.290933 14.163 < 2e-16 ***
## mmeamtemp
                2.962860
                           0.993616
## mminvis
                                      2.982 0.00296 **
                -4.228595
                           1.072656 -3.942 8.82e-05 ***
## mmeanwind
                           0.450951
                                      2.891 0.00395 **
## mmaxgust
                1.303529
```

9

```
## cloud
               -5.681391
                          1.164088 -4.881 1.29e-06 ***
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 50.54 on 759 degrees of freedom
## Multiple R-squared: 0.9849, Adjusted R-squared: 0.9847
## F-statistic: 5487 on 9 and 759 DF, p-value: < 2.2e-16
```

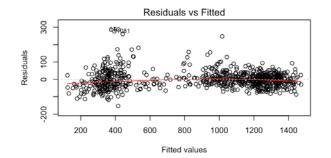


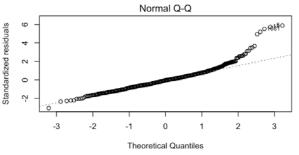
BayAreaBikeShare

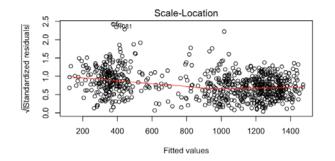
The state of the sales

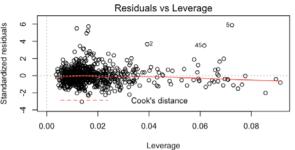
```
vif(lm.fit)
```

```
holiday
                                                  mminvis mmeanwind
weekday
             event
                                  sub mmeamtemp
1.008320
         1.704833
                   1.051485 1.084990 1.255154 1.856926 2.340700
            cloud
mmaxgust
1.990332
         1.687742
```







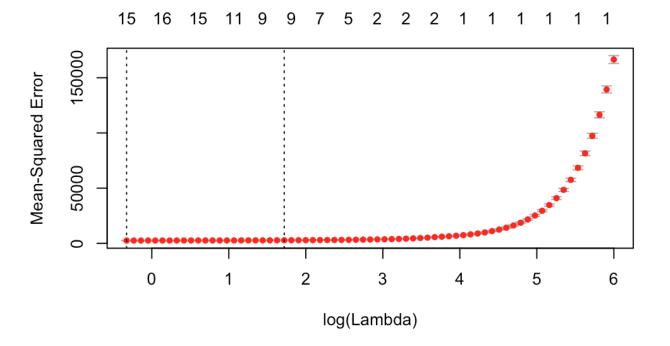




BayAreaBikeShare

```
# test error
pred.count=predict(lm.fit, newdata=data[-train, ])
sqrt(mean((data$count[-train]-pred.count)^2))
## [1] 63.11523
```





```
> bestlam=cv.out$lambda.min
> bestlam
[1] 0.7209649
```

```
> lasso.pred=predict(lasso.mod,s=bestlam ,newx=x[-train,])
> sqrt(mean((lasso.pred-y[-train])^2))
[1] 62.47014
```





	1
(Intercept)	413.84277667
weekday	4.03730568
month	
day	-0.02229262
event1	-16.54263295
weekend1	
holiday1	1.08864565
sub	0.91344106
mmaxtemp	0.16632623
mmeamtemp	
mmintemp	4.18273827
mmaxdew	
mmeandew	
mmindew	0.40188342
mmaxhum	-0.02959267
mmeanhum	
mminhum	-0.31141169
mmaxsea	-16.24131617
mmeansea	
mminsea	
maxvis	5.38296245
mmeanvis	
mminvis	2.15081928
mmaxwind	
mmeanwind	-4.81114118
mmaxgust	0.32461551
cloud	-9.59856436

