

## Assignment-based Subjective Questions

1. From your analysis of the categorical variables from the dataset, what could you infer about their effect on the dependent variable?

Ans: As per the analysis

- More customers tend to hire bike ride during summer and fall
- Weekday doesn't have much impact on bike ride customers.
- The customer count decreases when it snows/rains.
- Working days doesn't have much impact on bike ride customers.
- 2019 attracted more customers.

2. Why is it important to use `drop_first=True` during dummy variable creation?

Ans: `drop_first = True` is important to use, as it helps in reducing the extra column created during dummy variable creation. Hence it reduces the correlations created among dummy variables.

Let's say we have 3 types of values in Categorical column and we want to create dummy variable for that column. If one variable is not A and B, then It is obvious C. So we do not need 3rd variable to identify the C.

3. Looking at the pair-plot among the numerical variables, which one has the highest correlation with the target variable?

Ans: temp and atemp has the highest correlation with the target cnt variable.

4. How did you validate the assumptions of Linear Regression after building the model on the training set?

Ans: we checked following things:

- **Normality of error terms:** errors should be normally distributed.
- **Multicollinearity:** There should not be Multicollinearity among the variables.
- Linear relationship should be existing clearly.
- **Homoscedasticity:** There should be no pattern in residual values
- There should be no correlation among the residuals.

5. Based on the final model, which are the top 3 features contributing significantly towards explaining the demand of the shared bikes?

Ans:

- Temp
- Winter
- Month (sep)

## General Subjective Questions

- Explain the linear regression algorithm in detail.

**Ans:** Linear regression can be defined as the statistical model that analyses the linear relationship between a dependent variable with given set of independent variables.

Linear relationship

between variables means that when the value of one or more independent variables will

change (increase or decrease), the value of dependent variable will also change accordingly

(increase or decrease).

Mathematically the relationship can be represented with the help of following equation

–

$$Y = mX + c$$

Here, Y is the dependent variable we are trying to predict.

X is the independent variable we are using to make predictions.

m is the slope of the regression line which represents the effect X has on Y

c is a constant, known as the Y-intercept. If X = 0, Y would be equal to c.

Furthermore, the linear relationship can be positive or negative in nature as explained below–

- **Positive Linear Relationship:** A linear relationship will be called positive if both independent and dependent variable increases.
- **Negative Linear relationship:** A linear relationship will be called positive if independent increases and dependent variable decreases.

Assumptions -

The following are some assumptions about dataset that is made by Linear Regression model –

✓ Multi-collinearity –

○ Linear regression model assumes that there is very little or no multi-collinearity in the data. Basically, multi-collinearity occurs when the independent variables or features have dependency in them.

✓ Auto-correlation –

○ Another assumption Linear regression model assumes is that there is very little or no auto-correlation in the data. Basically, auto-correlation occurs when there is dependency between residual errors.

✓ Relationship between variables –

○ Linear regression model assumes that the relationship between response and feature variables must be linear.

✓ Normality of error terms –○ Error terms should be normally distributed

✓ Homoscedasticity –

○ There should be no visible pattern in residual values.

• **Explain the Anscombe's quartet in detail.**

**Ans:** Anscombe's quartet tells us about the importance of visualizing data before applying various algorithms to build models. This suggests the data features must be plotted to see the distribution of the samples that can help you identify the various anomalies present in the data (outliers, diversity of the data, linear separability of the data, etc.). Moreover, the linear regression can only be considered a fit for the data with linear relationships and is incapable of handling any other kind of data set.

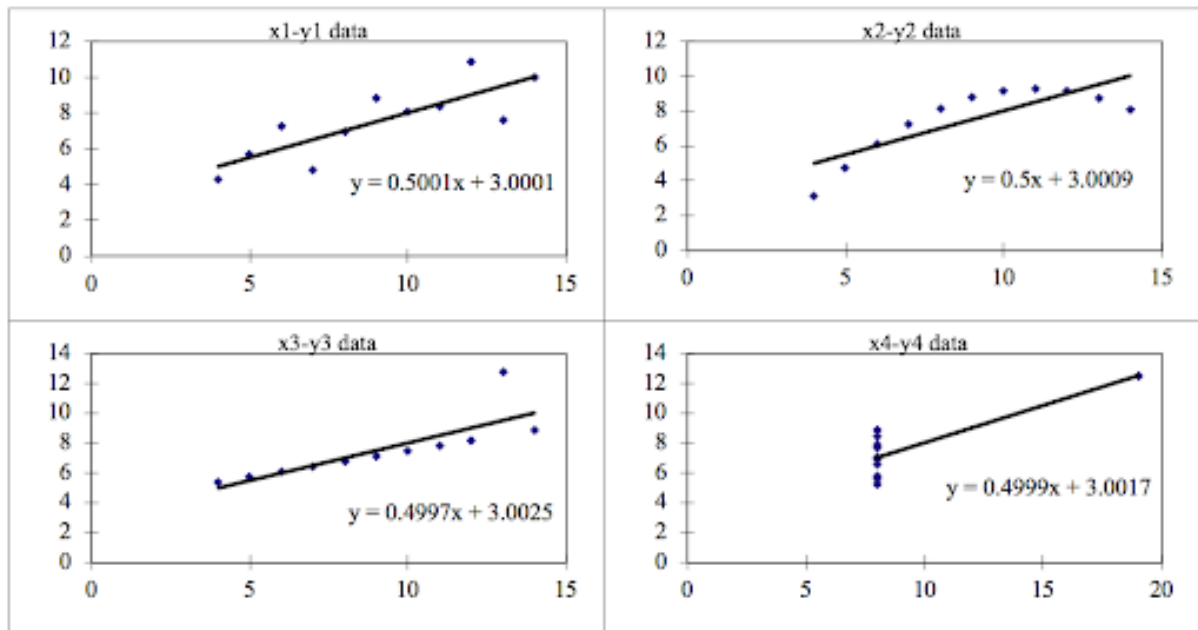
We can define these four plots as follows:

Anscombe's Data											
Observation	x1	y1		x2	y2		x3	y3		x4	y4
1	10	8.04		10	9.14		10	7.46		8	6.58
2	8	6.95		8	8.14		8	6.77		8	5.76
3	13	7.58		13	8.74		13	12.74		8	7.71
4	9	8.81		9	8.77		9	7.11		8	8.84
5	11	8.33		11	9.26		11	7.81		8	8.47
6	14	9.96		14	8.1		14	8.84		8	7.04
7	6	7.24		6	6.13		6	6.08		8	5.25
8	4	4.26		4	3.1		4	5.39		19	12.5
9	12	10.84		12	9.13		12	8.15		8	5.56
10	7	4.82		7	7.26		7	6.42		8	7.91
11	5	5.68		5	4.74		5	5.73		8	6.89

The statistical information for these four data sets are approximately similar. We can compute them as follows:

Anscombe's Data											
Observation	x1	y1		x2	y2		x3	y3		x4	y4
1	10	8.04		10	9.14		10	7.46		8	6.58
2	8	6.95		8	8.14		8	6.77		8	5.76
3	13	7.58		13	8.74		13	12.74		8	7.71
4	9	8.81		9	8.77		9	7.11		8	8.84
5	11	8.33		11	9.26		11	7.81		8	8.47
6	14	9.96		14	8.1		14	8.84		8	7.04
7	6	7.24		6	6.13		6	6.08		8	5.25
8	4	4.26		4	3.1		4	5.39		19	12.5
9	12	10.84		12	9.13		12	8.15		8	5.56
10	7	4.82		7	7.26		7	6.42		8	7.91
11	5	5.68		5	4.74		5	5.73		8	6.89
				Summary Statistics							
N	11	11		11	11		11	11		11	11
mean	9.00	7.50		9.00	7.500909		9.00	7.50		9.00	7.50
SD	3.16	1.94		3.16	1.94		3.16	1.94		3.16	1.94
r	0.82			0.82			0.82			0.82	

However, when these models are plotted on a scatter plot, each data set generates a different kind of plot that isn't interpretable by any regression algorithm, as you can see below:



We can describe the four data sets as:

- **Data Set 1:** fits the linear regression model pretty well.
- **Data Set 2:** cannot fit the linear regression model because the data is non-linear.
- **Data Set 3:** shows the outliers involved in the data set, which cannot be handled by the linear regression model.
- **Data Set 4:** shows the outliers involved in the data set, which also cannot be handled by the linear regression model.

As you can see, Anscombe's quartet helps us to understand the importance of data visualization and how easy it is to fool a regression algorithm. So, before attempting to interpret and model the data or implement any machine learning algorithm, we first need to visualize the data set in order to help build a well-fit model.

- **What is Pearson's R?**

**Ans:** The Pearson correlation coefficient ( $r$ ) is the most common way of measuring a linear correlation. It is a number between  $-1$  and  $1$  that measures the strength and direction of the relationship between two variables.

Pearson correlation coefficient ( $r$ )	Correlation type	Interpretation	Example
Between 0 and 1	Positive correlation	When one variable changes, the other variable changes in the <b>same direction</b> .	Baby length & weight:

Pearson correlation coefficient ( $r$ )	Correlation type	Interpretation	Example
0	No correlation	There is <b>no relationship</b> between the variables.	The longer the baby, the heavier their weight. Car price & width of windshield wipers: The price of a car is not related to the width of its windshield wipers.
Between 0 and $-1$	Negative correlation	When one variable changes, the other variable changes in the <b>opposite direction</b> .	Elevation & air pressure: The higher the elevation, the lower the air pressure.

The Pearson correlation coefficient ( $r$ ) is the most widely used correlation coefficient and is known by many names:

- Pearson's  $r$
- Bivariate correlation
- Pearson product-moment correlation coefficient (PPMCC)
- The correlation coefficient

The Pearson correlation coefficient is a descriptive statistic, meaning that it summarizes the characteristics of a dataset. Specifically, it describes the strength and direction of the linear relationship between two quantitative variables.

Although interpretations of the relationship strength (also known as effect size) vary between disciplines, the table below gives general rules of thumb:

Pearson correlation coefficient ( $r$ ) value	Strength	Direction
Greater than .5	Strong	Positive
Between .3 and .5	Moderate	Positive
Between 0 and .3	Weak	Positive
0	None	None
Between 0 and $-.3$	Weak	Negative
Between $-.3$ and $-.5$	Moderate	Negative

Pearson correlation coefficient ( <i>r</i> ) value	Strength	Direction
Less than $-0.5$	Strong	Negative

The Pearson correlation coefficient is also an inferential statistic, meaning that it can be used to test statistical hypotheses. Specifically, we can test whether there is a significant relationship between two variables.

- **What is scaling? Why is scaling performed? What is the difference between normalized scaling and standardized scaling?**

**Ans:** It is a step of data Pre-Processing which is applied to independent variables to normalize the data within a particular range. It also helps in speeding up the calculations in an algorithm.

Most of the times, collected data set contains features highly varying in magnitudes, units and range. If scaling is not done then algorithm only takes magnitude in account and not units hence incorrect modelling. To solve this issue, we have to do scaling to bring all the variables to the same level of magnitude.

It is important to note that scaling just affects the coefficients and none of the other parameters like t-statistic, F-statistic, p-values, R-squared, etc.

## ***Normalization/Min-Max Scaling:***

- It brings all of the data in the range of 0 and 1

$$\text{MinMax Scaling: } x = \frac{x - \min(x)}{\max(x) - \min(x)}$$

## ***Standardization Scaling:***

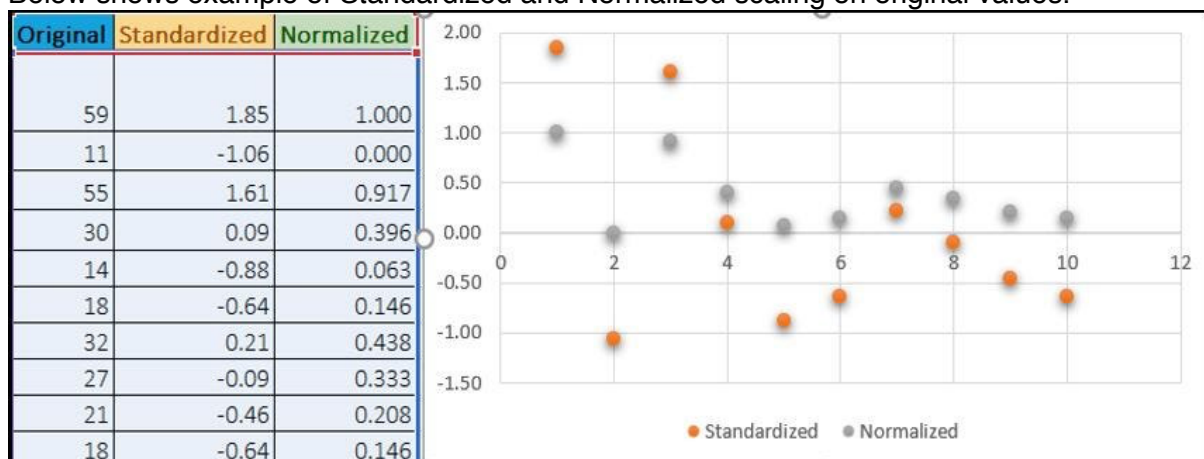
- Standardization replaces the values by their Z scores. It brings all of the data into a standard normal distribution which has mean ( $\mu$ ) zero and standard deviation one ( $\sigma$ ).

$$\text{Standardisation: } x = \frac{x - \text{mean}(x)}{\text{sd}(x)}$$

- One disadvantage of normalization over standardization is that it loses some information in the data, especially about outliers.

### ***Example:***

Below shows example of Standardized and Normalized scaling on original values.



- You might have observed that sometimes the value of VIF is infinite. Why does this happen?

**Ans:**

If there is perfect correlation, then  $VIF = \text{infinity}$ . A large value of VIF indicates that there is a correlation between the variables. If the VIF is 4, this means that the variance of the model coefficient is inflated by a factor of 4 due to the presence of multicollinearity. When the value of VIF is infinite it shows a perfect correlation between two independent variables. In the case of perfect correlation, we get  $R\text{-squared } (R^2) = 1$ , which lead to  $1 / (1 - R^2)$  infinity. To solve this we need to drop one of the variables from the dataset which is causing this perfect multicollinearity.

- What is a Q-Q plot? Explain the use and importance of a Q-Q plot in linear regression.

**Ans:**

Quantile-Quantile (Q-Q) plot, is a graphical tool to help us assess if a set of data plausibly came from some theoretical distribution such as a Normal, exponential or

Uniform distribution. Also, it helps to determine if two data sets come from populations with a common distribution.

This helps in a scenario of linear regression when we have training and test data set received separately and then we can confirm using Q-Q plot that both the data sets are from populations with same distributions.

**Use of Q-Q plot:**

A q-q plot is a plot of the quantiles of the first data set against the quantiles of the second dataset. By a quantile, we mean the fraction (or percent) of points below the given value. That is, the 0.3 (or 30%) quantile is the point at which 30% percent of the data fall below and 70% fall above that value. A 45-degree reference line is also plotted. If the two sets come from a population with the same distribution, the points should fall approximately along this reference line. The greater the departure from this reference line, the greater the evidence for the conclusion that the two data sets have come from populations with different distributions.

**Importance of Q-Q plot:**

When there are two data samples, it is often desirable to know if the assumption of a common distribution is justified. If so, then location and scale estimators can pool both data sets to obtain estimates of the common location and scale. If two samples do differ, it is also useful to gain some understanding of the differences. The q-q plot can provide more insight into the nature of the difference than analytical methods such as the chi-square and Kolmogorov-Smirnov 2-sample tests.