

Agenda

- Data ✓
- Type of Data ✓
- Quantitative vs Qualitative ✓
- Frequency and Cumulative Frequency ✓
- Measure of Frequency ✓
- Measure of Central Tendency ✓
- Measure of Dispersion ✓
- Variance and Standard Deviation ✓

Mean, median, mode

Spread

facts
Pierce of Information

Q. What is Data?

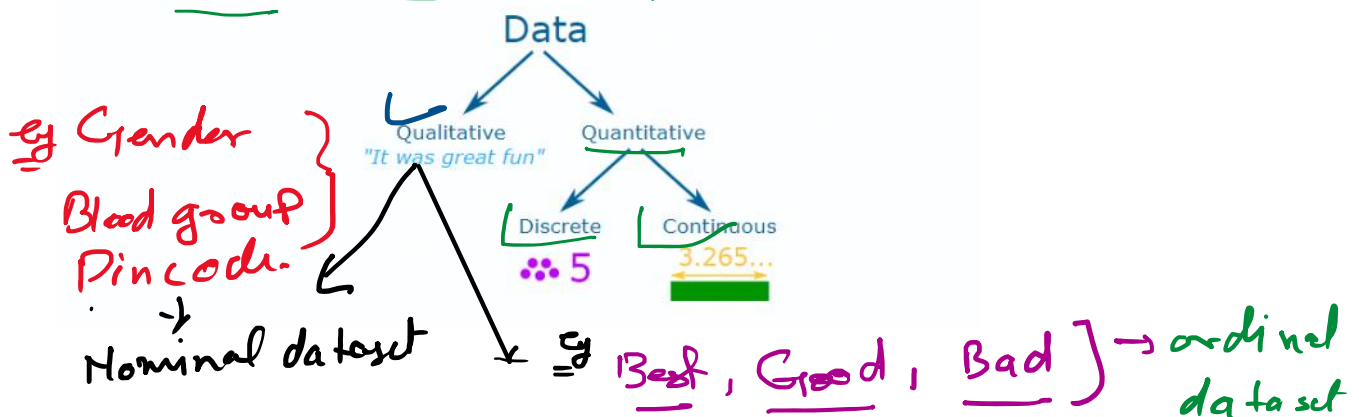
Ans: Data is a collection of facts, such as numbers, words, measurements, observations or just descriptions of things.

Qualitative vs Quantitative

Data can be qualitative or quantitative.

- Qualitative data is descriptive information (it describes something)
- Quantitative data is numerical information (numbers)

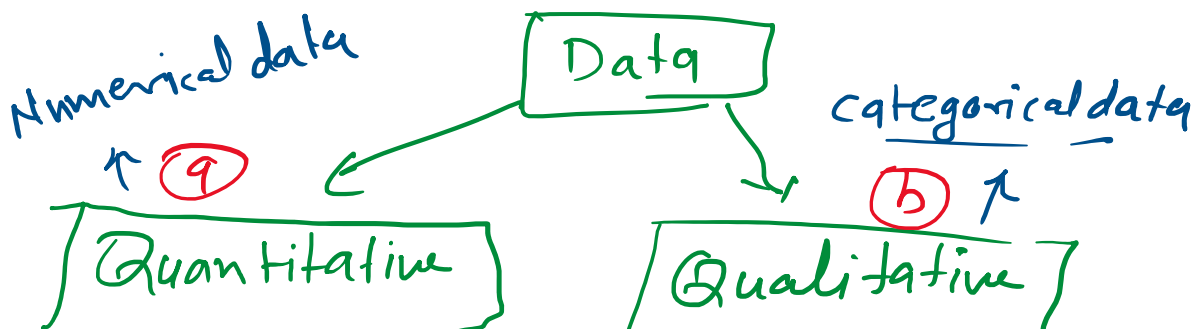
Stringer, category

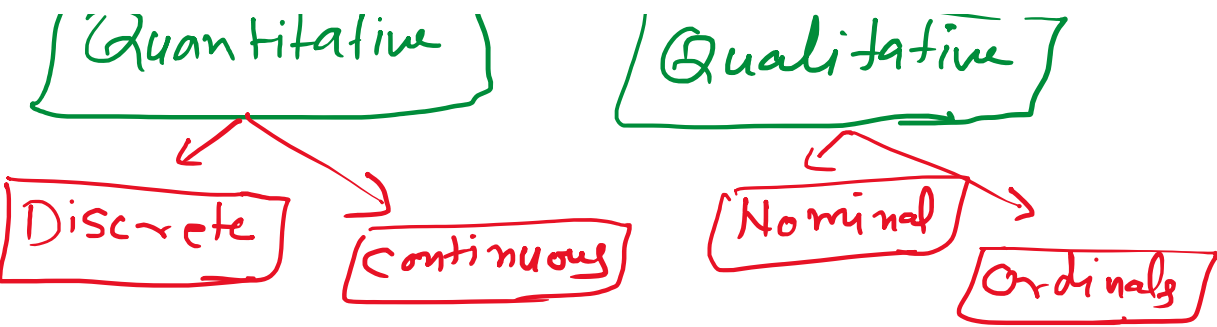


Quantitative data can be Discrete or Continuous:

- Discrete data can only take certain values (like whole numbers)
- Continuous data can take any value (within a range)

Put simply: Discrete data is counted, Continuous data is measured





⑨ Discrete \rightarrow whole No.
 or exact No. } Count

eg (i) Bank A/c No

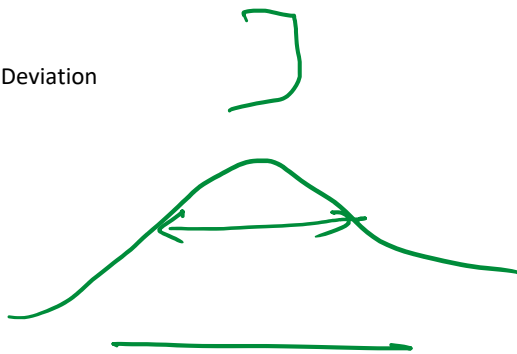
(ii) No. of children in a family

(b) continuous \rightarrow Any value (measure)

$c_f \rightarrow$ weight, height, temperature, speed

Measures of Dispersion (Spread Of Data)

1. Variance
2. Standard Deviation



Variance

The Variance is defined as:

The average of the **squared** differences from the Mean.

To calculate the variance follow these steps:

- Work out the Mean (the simple average of the numbers)
- Then for each number: subtract the Mean and square the result (the *squared difference*).
- Then work out the average of those squared differences. (Why Square?)

- Then work out the average of those squared differences. (Why Square?)

Population Variance

$$\sigma^2 = \sum_{i=1}^N \frac{(x_i - \mu)^2}{N}$$

$x_i \rightarrow$ Data Points

$\mu \rightarrow$ Population mean

$N \rightarrow$ Population Size

Sample Variance

$$s^2 = \sum_{i=1}^n \frac{(x_i - \bar{x})^2}{n-1}$$

$x_i \rightarrow$ Data Point

$\bar{x} \rightarrow$ Sample mean

$n \rightarrow$ Sample Size

Q Why we divide sample variance by $n-1$?

Ans The sample variance is divided by $(n-1)$ so that we can create an unbiased estimator of the population data

Bessel correction

eg $\{1, 2, 3, 4, 5\}$

$$s^2 = \sum_{i=1}^n \frac{(x_i - \bar{x})^2}{n-1}$$



$s^2 \uparrow \propto$ spread graph

x	\bar{x}	$(x_i - \bar{x})^2$
1	3	4
2	3	1
3	3	0
4	3	1
5	3	4
<u>5</u>	<u>3</u>	<u>10</u>
$\bar{x} = 3$		

$$s^2 = \frac{10}{5-1} = \frac{10}{4}$$

$$\boxed{s^2 = 2.5}$$

Standard Deviation

The Standard Deviation is a measure of how spread out numbers are.

Its symbol is σ (the greek letter sigma)

The formula is easy: it is the square root of the Variance. So now you ask, "What is the Variance?"

Population std

$$\sigma = \sqrt{\text{variance}}$$

Sample std

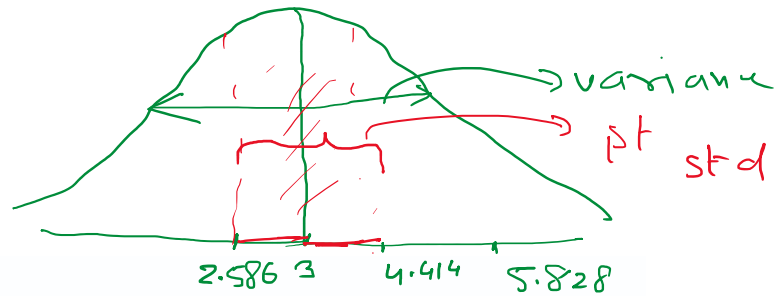
$$\text{std} = \sqrt{s^2}$$

$$\sigma = \sqrt{\text{variance}}$$

$$\text{std} = \sqrt{s^2}$$

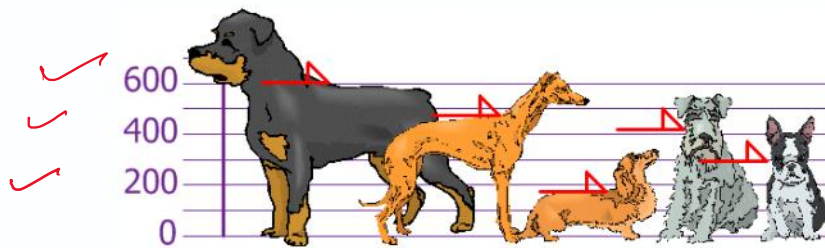
$$\hat{\mu} = 3$$

$$\sigma = 1.414$$



Example

You and your friends have just measured the heights of your dogs (in millimeters):



The heights (at the shoulders) are: 600mm, 470mm, 170mm, 430mm and 300mm.

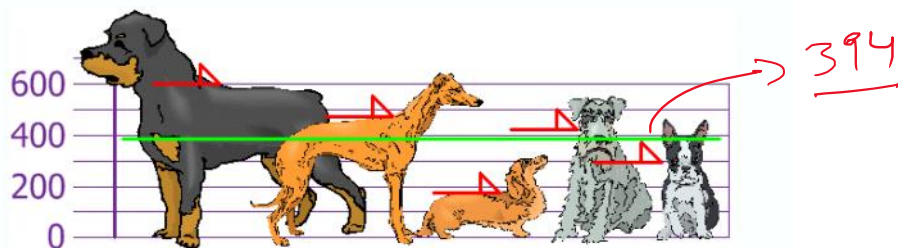
Find out the Mean, the Variance, and the Standard Deviation.

Your first step is to find the Mean:

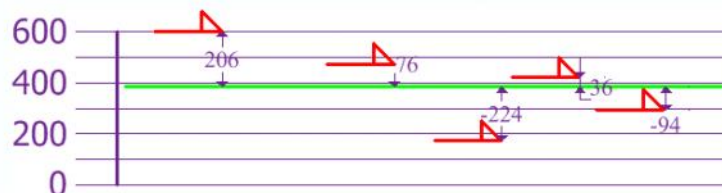
Answer:

$$\begin{aligned} \text{Mean} &= \frac{600 + 470 + 170 + 430 + 300}{5} \\ &= \frac{1970}{5} \\ &= 394 \end{aligned}$$

so the mean (average) height is 394 mm. Let's plot this on the chart:



Now we calculate each dog's difference from the Mean:



To calculate the Variance, take each difference, square it, and then average the result:

Variance

$$\begin{aligned}\sigma^2 &= \frac{206^2 + 76^2 + (-224)^2 + 36^2 + (-94)^2}{5} \\ &= \frac{42436 + 5776 + 50176 + 1296 + 8836}{5} \\ &= \frac{108520}{5} \\ &= 21704\end{aligned}$$

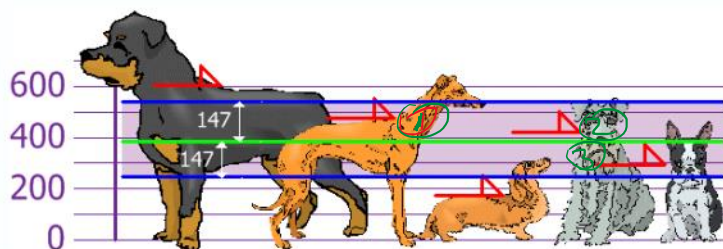
So the Variance is **21,704**

And the Standard Deviation is just the square root of Variance, so:

Standard Deviation

$$\begin{aligned}\sigma &= \sqrt{21704} \\ &= 147.32... \\ &= \underline{147 \text{ (to the nearest mm)}}$$

And the good thing about the Standard Deviation is that it is useful. Now we can show which heights are within one Standard Deviation (147mm) of the Mean:



$\frac{3}{5}$
} 1st std
68%

So, using the Standard Deviation we have a "standard" way of knowing what is normal, and what is extra large or extra small.

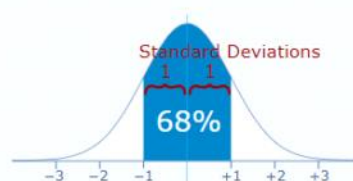
Rottweilers **are** tall dogs. And Dachshunds **are** a bit short, right?

Using

We can expect about 68% of values to be within plus-or-minus 1 standard deviation.

Read [Standard Normal Distribution](#) to learn more.

Also try the [Standard Deviation Calculator](#).



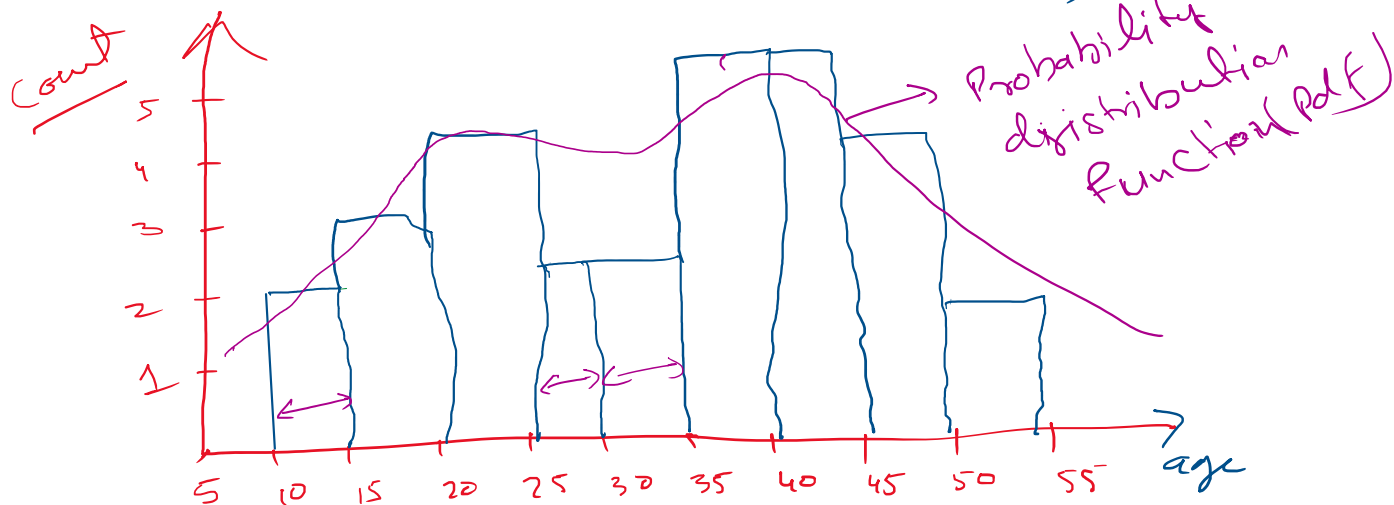
$$\begin{aligned}& \text{394} \\ & \leftarrow 147 \quad \rightarrow 147 \\ & 394 - 147 \quad 394 + 147\end{aligned}$$

Histogram and Skewness

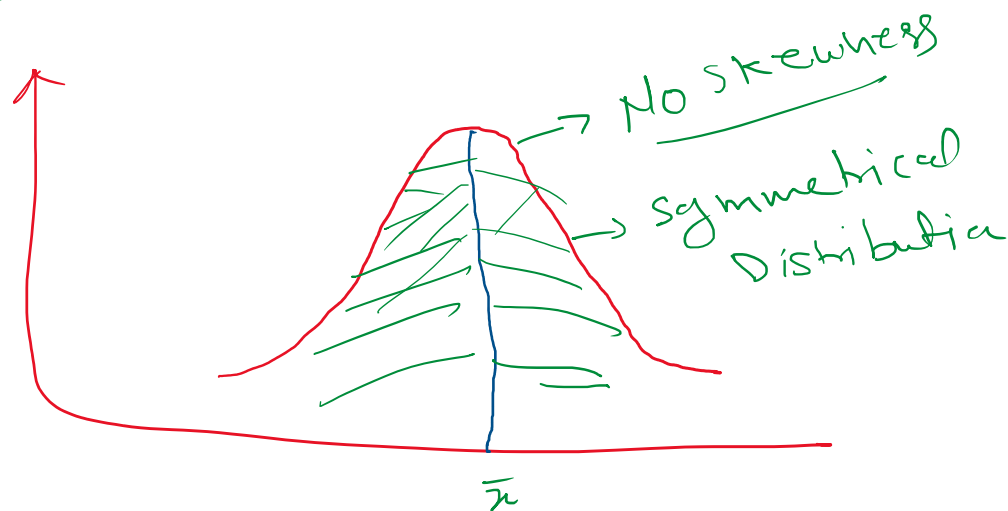
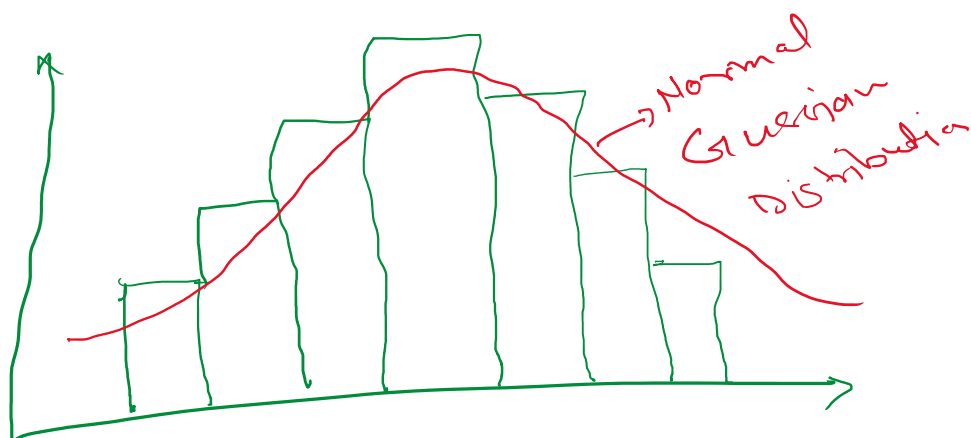
Frequency

$$\frac{50}{10} = 5$$

$$\frac{50}{10} = 5$$



①



① Mean, median & mode all are perfectly at the center.

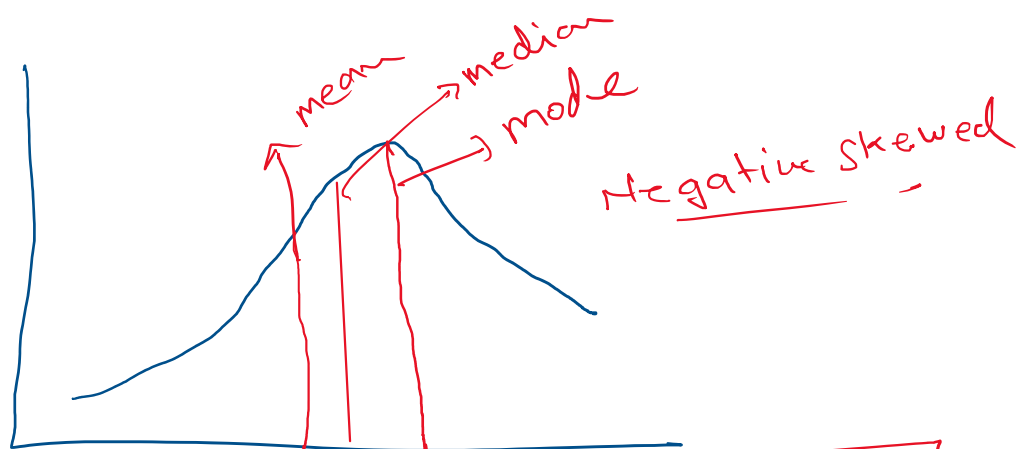
$$\text{Mean} = \text{Median} = \text{mode}$$

⑤ Right Skewed



$$\text{Mean} \geq \text{median} \geq \text{mode}$$

⑥ Left skewed Distribution



$$\text{mean} \leq \text{median} \leq \text{mode}$$