

repeat S until b

→ if c

nos -f gssb noon (a)

$$(x) [\text{repeat}_{\text{nos}}^{\text{tt}}] = \langle S, s \rangle \rightarrow s' \quad \text{iff } B[b]s = \text{tt}$$

$$(x) [\text{repeat}_{\text{nos}}^{\text{ff}}] = \frac{\langle S, s \rangle \rightarrow s', \langle \text{repeat } S \text{ until } b, s' \rangle \rightarrow s''}{\langle \text{repeat } S \text{ until } b, s \rangle \rightarrow s''}$$

if $B[b]s' = \text{ff}$

repeat S until b ~ S; if b then skip else (repeat S until b)

repeat S until b → S; if b then skip else (repeat S until b)

$B[b] = \text{tt}$:k mpm

$$[\text{repeat}_{\text{nos}}^{\text{tt}}] \quad \frac{\langle S, s \rangle \rightarrow s'}{\langle \text{repeat } S \text{ until } b, s \rangle \rightarrow s'}$$

$$:ps) \quad \langle \text{skip}, s' \rangle \rightarrow s' \quad :fap)$$

$$\frac{\langle \text{skip}, s' \rangle \rightarrow s'}{\langle \text{if } b \text{ then skip else (repeat } S \text{ until } b), s' \rangle \rightarrow s'}$$

: [if^{tt}_{ns}] f(a)

$$\langle S, s \rangle \rightarrow s', \langle \text{if } b \text{ then skip else (repeat } S \text{ until } b), s' \rangle \rightarrow s'$$

$$\langle S; \text{if } b \text{ then skip else (repeat } S \text{ until } b), s \rangle \rightarrow s'$$

: (compns)

for

$B[b] = \text{ff}$

:a mpm

$$[\text{repeat}_{\text{ns}}^{\text{ff}}] = \frac{\langle S, s \rangle \rightarrow s', \langle \text{repeat } S \text{ until } b, s' \rangle \rightarrow s''}{\langle \text{repeat } S \text{ until } b, s \rangle \rightarrow s''}$$

:ap)

$$\frac{\langle \text{repeat } S \text{ until } b, s' \rangle \rightarrow s''}{\langle \text{if } b \text{ then skip else (repeat } S \text{ until } b), s' \rangle \rightarrow s''}$$

:ap)

$$\langle \text{if } b \text{ then skip else (repeat } S \text{ until } b), s' \rangle \rightarrow s''$$

∴ [Comp_{nas}] (180) ∴ [if_{nas}^{ff}] (180) ∴ ~~if_{nas}~~ (180)

$$\langle S, s \rangle \rightarrow s', \quad \langle \text{if } b \text{ then skip else (repeat } \dots \text{)}, s' \rangle \rightarrow s''$$

$$\langle S; \text{if } b \text{ then skip else (repeat } \dots \text{)}, s \rangle \rightarrow \underline{s''}$$

∴ sen

∴ sen (180) ∴ sen (180) ∴ sen (180)

$S; \text{if } b \text{ then skip else (repeat } \dots \text{)} \rightarrow \text{repeat } S \text{ until } b$

$$B[b]s' = \text{tt} \quad \text{for } s' \text{ and } s' \text{ and } s' \quad \therefore \text{skip}$$

∴ sen (180) ∴ sen (180) ∴ sen (180)

$$\langle S, s \rangle \rightarrow s', \quad \langle \text{if } b \text{ then skip else (repeat } \dots \text{)}, s' \rangle \rightarrow s''$$

$$\langle S; \text{if } b \text{ then skip else (repeat } \dots \text{)}, s \rangle \rightarrow \underline{s''}$$

∴ skip → sen (180) ∴ skip → sen (180) ∴ skip → sen (180)

$$\langle \text{skip}, s' \rangle \rightarrow s''$$

$$\langle \text{if } b \text{ then skip else (repeat } \dots \text{)}, s' \rangle \rightarrow s''$$

if $B[b]s' = \text{tt}$
↑
! sen

$$\langle \text{skip}, s' \rangle \rightarrow s'$$

$$\therefore \underline{s' = s''}$$

∴ sen (180) ∴ sen (180) ∴ sen (180)

$$\langle S, s \rangle \rightarrow s'$$

$$\langle \text{repeat } S \text{ until } b, s \rangle \rightarrow s' = \underline{s''}$$

$B[b] = \text{tt}$ ↑
∴

if B(b) = ff

if B(b) = ff then s' else s

$\langle S, s \rangle \rightarrow s', \langle \text{if } b \text{ then skip else (repeat } S \dots), s' \rangle \rightarrow s''$

$\langle S; \text{if } b \text{ then skip else (repeat } \dots), s \rangle \rightarrow s''$

[comp ns] %

repeat until b then s'

$\langle \text{repeat } S \text{ until } b, s' \rangle \rightarrow s''$

$\langle \text{if } b \text{ then skip else (repeat } \dots), s' \rangle \rightarrow s''$

if B(b) = ff

if (b)

$\langle S, s \rangle \rightarrow s', \langle \text{repeat } S \text{ until } b, s' \rangle \rightarrow s''$

$\langle \text{repeat } S \text{ until } b, s \rangle \rightarrow s''$

! B(b) = ff then s' else s

sen

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[repeat s] = $\langle \text{repeat } s \text{ until } b, s \rangle \Rightarrow \langle s; \text{ if } b \text{ then skip else (repeat } s \text{ until } b), s \rangle$

. b for ymmie wiger 2000