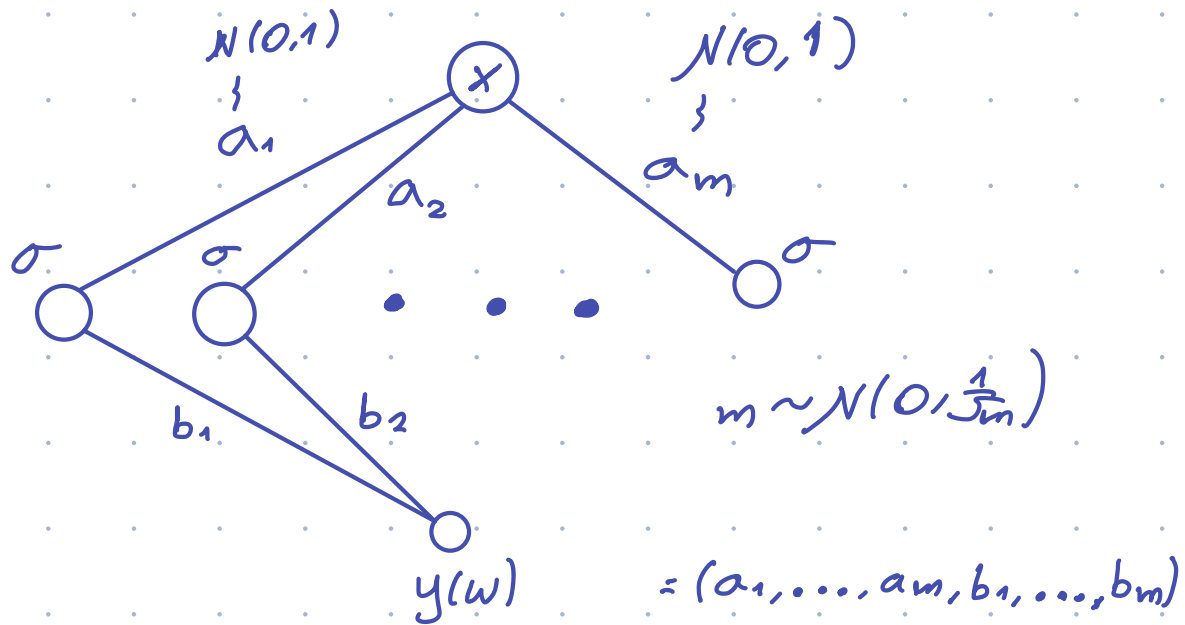


1-dim
 $X = \{x\}$
 $Y = \{y\}$
 \mathbb{R}



$$\hat{y} = y(w) = \sum_{i=1}^m b_i \sigma(a_i x)$$

$$L(w) = \frac{1}{2} \|y - y(w)\|^2 \quad O\left(\frac{1}{m}\right)$$

$$\frac{\partial \hat{y}}{\partial a_i} = b_i \sigma'(a_i x) \cdot x$$

$$\frac{\partial^2 \hat{y}}{\partial a_i \partial a_j} = \begin{cases} b_i x^2 \sigma''(a_i x) & i=j \\ 0 & \text{o.w.} \end{cases}$$

$$\frac{\partial \hat{y}}{\partial b_i} = \sigma(a_i x)$$

$$\frac{\partial^2 \hat{y}}{\partial b_i \partial b_j} = 0$$

$$\frac{\partial^2 \hat{y}}{\partial a_i \partial b_j} = \begin{cases} \sigma'(a_i x) \cdot x & i=j \\ 0 & \text{o.w.} \end{cases} \quad O(1)$$

$$\frac{\partial^2 \hat{y}}{\partial b_i \partial a_j} = \begin{cases} \sigma'(a_j x) \cdot a_j & i=j \\ 0 & \text{o.w.} \end{cases}$$

Hessian =

spectral norm $O(1)$

$$\mathbb{E} \|\nabla_w y(w)\|^2 = m$$

$$\mathbb{E} \| \nabla_w^2 y(w) \| = \mathcal{O}(1)$$

