Cryptanalysis of the RSA-CEGD protocol

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Abstract

Recently, Nenadić et al. (2004) proposed the RSA-CEGD protocol for certified delivery of e-goods. This is a relatively complex scheme based on verifiable and recoverable encrypted signatures (VRES) to guarantee properties such as strong fairness and non-repudiation, among others. In this paper, we demonstrate how this protocol cannot achieve fairness by presenting a severe attack and also pointing out some other weaknesses.

Keywords: Cryptographic protocols; Fair exchange; Non-repudiation;

1 Introduction

Interest in protocols for fair exchange of information with non-repudiation stems from its importance in many applications where disputes among parties can occur. Assurance of these properties enables the deployment of a wide range of applications, such as certified e-mail or business transactions through communication networks. As a result, fair non-repudiation has experienced an explosion of proposals in recent years (see [3] for an excellent survey).

Nevertheless, fairness and non-repudiation have not been so extensively studied as other classic issues, such as confidentiality or authentication. Previous experience in these contexts has shown that designing security protocols is an error-prone task. Consider, as an illustrative example, a non-repudiation protocol proposed in 1996 by Zhou and Gollman [8] that was verified and proved correct using three different methods [1, 6, 9]. Surprisingly, in 2002 Gürgens and Rudolph demonstrated the absence of fair non-repudiation in that protocol under reasonable assumptions [2]. In this case, possible attacks were detected after an analysis performed with a different formalism that considered scenarios not checked before.

The RSA-CEGD protocol [4] was recently proposed for certified delivery of e-goods, i.e. commercial products that can be represented in electronic form

and transmitted over open networks. The scheme is designed to satisfy six major security requirements: non-repudiation of origin; non-repudiation of receipt; strong fairness; e-goods content/quality assurance; e-goods and receipt confidentiality; and transparency of the STTP. In this paper we demonstrate that this protocol suffers from severe security problems, and some of the requirements mentioned above cannot be satisfied. In particular, we present attacks that show how the protocol does not assure fairness.

The rest of this paper is organized as follows. Section 2 introduces the notation and briefly reviews the RSA-CEGD protocol. Section 3 discusses the vulnerabilities and illustrate them through specific attack scenarios. Finally, Section 4 summarizes the paper by presenting some conclusions.

2 Overview of the RSA-CEGD protocol

For readability and completeness, we first provide a brief review of the RSA-CEGD protocol.

2.1 Notation

Throughout this paper, we will use the same notation introduced by the authors in the original paper [4]. The protocol's items and cryptographic symbols are described below.

- P_a , P_b , P_t : different protocol parties, where P_a is the e-goods provider (message sender) and P_b is the purchaser (message receiver). P_t acts as a Semi-Trusted Third Party (STTP).
- D_a : e-goods to be purchased.
- k_a : symmetric key used by P_a to encrypt D_a .
- r_a : random prime generated by P_a .
- $x_a = (r_a \times k_a) \mod n_a$: encryption of key k_a with random number r_a
- $CertD_a = (desc_a, hd_a, h_a, ek_a, sign_{CA})$: certificate for D_a issued by a CA, where:
 - $desc_a = description$ (content summary) of D_a
 - $-hd_a = h(E_{k_a}(D_a))$: hash value of the encryption of D_a with key k_a
 - $-h_a = h(D_a)$: hash value of D_a
 - $-ek_a = E_{pk_a}(k_a)$: encryption of the key k_a with P_a 's public key, pk_a
- $E_{sk_a}(h_a)$: P_a 's RSA signature on D_a serving as a proof of origin of D_a
- $y_a = E_{pk_a}(r_a)$: RSA encryption of number r_a with key pk_a

- r_b : random prime generated by P_b for the generation of the VRES (y_b, x_b, xx_b) .
- $rec_b = (h_a)^{d_b} \mod n_b$: P_b 's receipt for P_a 's e-goods D_a , i.e. P_b 's RSA signature on D_a
- $(y_b, x_b, xx_b) : P_b$'s VRES, where
 - $y_b = r_b^{e_b} \mod (n_b \times n_{bt})$: encryption of r_b with P_b 's public key. Also recoverable by P_t
 - $-x_b = (r_b \times (h_a)^{d_b}) \mod n_b = (r_b \times rec_b) \mod n_b$: encryption of rec_b with r_b
 - $xx_b = (r_b \times E_{sk_{bt}}(h(y_b))) \mod n_{bt}$: control number that confirms the correct use of r_b
- $C_{bt} = (pk_{bt}, w_{bt}, s_{bt}) : P_b$'s RSA public-key certificate issued by P_t
- $pk_{bt} = (e_{bt}, n_{bt})$: public RSA key related to C_{bt} , with $e_{bt} = e_{bt}$
- $sk_{bt} = (d_{bt}, n_{bt})$: private RSA key related to C_{bt}
- $w_{bt} = (h(sk_t, pk_{bt})^{-1} \times d_{bt}) \mod n_{bt}$
- $s_{bt} = E_{sk_t}(h(pk_{bt}, w_{bt}))$: P_t 's signature on $h(pk_{bt}, w_{bt})$
- $s_b = E_{sk_b}(h(C_{bt}, y_b, y_a, P_a))$: P_b 's recovery authorization token.

2.2 Exchange and recovery sub-protocols

The RSA-CEGD is an optimistic fair exchange protocol composed of two sub-protocols, as shown in Fig. 1. As usual, the exchange sub-protocol is used to carry out the exchange between parties without any TTP's involvement. In case the process fails to complete successfully, a recovery protocol can be invoked to handle this situation.

The notion of verifiable and recoverable encrypted signature (VRES) underlies at the core of the RSA-CEGD protocol. A VRES is basically an encrypted signature, which acts as a receipt from the receiver's point of view, with two main properties. First, it can be verified: the receiver is assured that the VRES contains the expected signature without obtaining any valuable information about the signature itself during the verification process. And second, the receiver is assured that the original signature can be recovered with the assistance of a designated TTP in case the original sender refuses to do it.

Due to these two properties, the VRES becomes an interesting cryptographic primitive upon which fairness can be provided. The RSA-CEGD protocol relies on this element within the general scheme we sketch in what follows:

- 1. A ciphers the message with an encryption key and sends it to B.
- 2. B generates the VRES of his signature and sends it back to A.

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The exchange sub-protocol
         P_a \rightarrow P_b: E_{k_a}(D_a), CertD_a, x_a, E_{sk_a}(h_a)
         P_b \rightarrow P_a: (x_b, xx_b, y_b), s_b, C_{bt}
         \mathtt{P_a} 	o \mathtt{P_b}: \quad r_a
E3:
E4:
         P_b 	o P_a:
The recovery sub-protocol
R1:
         P_{\mathtt{a}} 	o P_{\mathtt{t}} :
                          C_{bt}, y_b, s_b, y_a, r_a
R2:
         P_{\text{t}} \to P_{\text{a}}:
                           r_b
R3:
         P_{\text{t}} \to P_{\text{b}}:
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Figure 1: The RSA-CEGD protocol.

- 3. Upon successful verification of the VRES, A is assured that it is secure for her to send the decryption key to B, so he can access the message.
- 4. Finally, B sends his original signature to A as a receipt. In case he refuses, a TTP can recover the signature from the VRES, thus restoring fairness.

The RSA-CEGD protocol makes use of a novel VRES method based on the RSA system, hence its name. The idea stems from the so-called *theory of cross-decryption* [7], which establishes that an RSA encrypted text can be decrypted by using two different keys if both pairs of secret/public keys are appropriately chosen. Party B is enforced to use a key of this kind to encrypt the VRES, while the TTP retains the other. This way, if subsequently B refuses to provide A with his signature, the TTP is able to recover it from the VRES.

3 Protocol vulnerabilities

Before stating specific attack scenarios, note that:

- 1. The VRES received by party P_a in step E2 contains the receipt rec_b , though it is not directly accessible to her. However, party P_a is provided with all the information required by the STTP to assist P_a in the recovery of the receipt, i.e. the authorization token s_b and P_b 's certificate C_{bt} .
- 2. Items $\langle (x_b, xx_b, y_b), s_b, C_{bt} \rangle$ do not contain themselves any link to the current protocol execution. They only refer to the e-goods D_a , the receipt rec_b , an authorization to P_a , P_b 's certificate, and the random numbers r_a and r_b .
- 3. The STTP can restore fairness only upon P_a request. Party P_b has no means to invoke a recovery sub-protocol. This puts P_a in an advantageous position with respect to the other party.

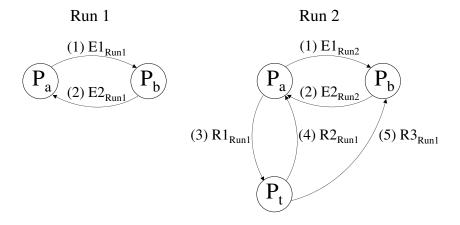


Figure 2: Scheme of the attack.

4. The protocol defines a token for non-repudiation of origin which does not include information to verify who submitted such a token to P_b .

Invocation of the recovery sub-protocol by party P_a will provide P_b with the number r_a , thus being able to recover the encryption key and, hence, access the e-goods D_a . Nevertheless, P_a can appeal to the STTP during a different protocol execution, since the information required to access the receipt does not identify the protocol session. In this scenario, the recovery sub-protocol also sends number r_a to P_b . However, the protocol specification does not require P_b to try the key received on messages of previous exchanges. In other words, is not reasonable to assume that P_b stores all proofs he ever received, especially those related to previous, unsuccessful exchanges.

As a result of the scheme outlined above, party P_a obtains a valid proof (receipt) of P_b having received e-goods D_a . P_b , on the other hand, does not have access to e-goods D_a (or is not aware that he has received the correct decryption key). Thus, non-repudiation is not satisfied and the protocol does not provide fairness for P_b . This situation is described in detail in the attack scenario described in the following section. Furthermore, some other weaknesses are pointed out in Section 3.2.

3.1 A replay attack

The basic scenario is graphically sketched in Fig. 2. The attack is executed through two different protocol runs between the same parties, P_a and P_b . This is not a strong assumption, since it is reasonable to expect that P_b wishes to buy several e-goods from the same seller.

During the first protocol running, P_a carries out step E1 and then waits for the VRES, the authorization token, and P_b 's certificate. We assume that P_a

performs the required verifications on these items, so she is assured they are valid. At this point, P_a aborts the protocol. In fact, there is no abort procedure per se, so she only does not continue with step E3. Note as well that P_b has no means to invoke a recovery sub-protocol in this situation.

Now P_a owns the received items:

$$\langle (x_b, xx_b, y_b), s_b, C_{bt} \rangle$$

and also number r_a and its signature, y_a . From these, P_a constructs and stores the following message:

$$m_1 = < C_{bt}, y_b, s_b, y_a, r_a >$$

Suppose that subsequently P_b contacts P_a to initiate another exchange aimed at buying a different e-good, say D'_a . Again, P_a follows step E1 and, after E2, she receives:

$$<(x'_b, xx'_b, y'_b), s'_b, C_{bt}>$$

from P_b . Then, P_a aborts the exchange sub-protocol and starts an instance of the recovery sub-protocol. According to the protocol semantics, it is expected that P_a sends the following items to the STTP in step R1:

$$m_2 = \langle C_{bt}, y_b', s_b', y_a', r_a' \rangle$$

However, P_a chooses m_1 as the message to send. As this is a valid proof, the STTP will recover numbers r_b and r_a , which will be sent to P_a and P_b , respectively. The key point is that both numbers are not related to the current protocol execution, but with the previous one. This way, P_a can use r_b to obtain the receipt rec_b contained in m_1 . Even though P_b also receives r_a , this number is useless for him to recover the key required to access D'_a . In fact, this r_a might provide P_b with access to the former e-goods he tried to buy. However, in all likelihood he is not aware of this.

As a result, P_a has a valid receipt of P_b having received e-goods D_a , though P_b does not actually own it. Therefore, the protocol does not provide fairness for P_b .

3.2 Indistinguishability of evidences of origin

The protocol establishes the item $E_{sk_a}(h_a)$ as proof of non-repudiation of origin. However, parties' identities are not included in such a token, nor any other information related to the current protocol execution. Even using authenticated channels, evidences obtained do not link together the sender, the originator, the receiver, the current protocol execution, etc. This fact yields to a weakness related to the indistinguishability of evidences exchanged during the protocol, in particular, evidence of origin (EOO).

Suppose P_a and P_b perform a protocol execution, so finally P_b obtains D_a and an EOO = $E_{sk_a}(h_a)$, where $h_a = h(D_a)$. This evidence does not assure itself that P_b is the intended receiver. In other words, if the exchange would

have been carried out between parties P_a and P_c , then the EOO received by P_c would have been identical (assuming that the same symmetric key, k_a is used). This way, once P_b owns D_a and EOO, he might provide another party, P_c , with both items by using a traditional channel. As a result, P_c possesses the e-goods coupled with a valid EOO for her. Party P_a , on the other hand, does not own a receipt issued by P_c . Consequently, the protocol neither provides fairness for P_a .

3.3 On the security of a modified RSA-CEGD

In [5], Nenadić et al. presented a different version of the RSA-CEGD protocol with slight modifications. The structure of this new proposal remains unaltered with respect to the original version. In particular, items sent by P_b during step E2 are the same that appears in the protocol here studied, i.e. the VRES, the authorization token, and P_b 's certificate. Clearly, the attacks described above are still applicable for this version.

4 Conclusions

In this paper, we have demonstrated how the RSA-CEGD protocol suffers from severe vulnerabilities. Our attacks show up that this scheme can lead to an unfair situation for any of the two parties involved in the exchange. To the best of our knowledge, the aforementioned weaknesses have not been pointed out before.

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