

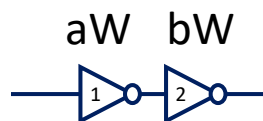
Exercise 1 (60 min, 5 pto).

The diagram in the figure shows the physical scheme of a digital circuit.

- Obtain the transistors scheme from the figure layout.
- Obtain the status of the P and N transistors (On and Off) for the following two combinations $ABCD=\{0101,1011\}$. Do not consider transistors in the inverters. Name the transistors from left to right and from top to bottom (also in the scheme of section a).
- Specify the simplified logic function of OUT based on inputs (A, B, C, and D).
- Get the cross-section view of the XY cut.
- Could you replace some part of the scheme using pass transistors without getting degradation? Specify which transistor could be replaced and why.

Exercise 2 (40 min, 2.5p)

If the delay produced by inverters of minimum size (transistors with dimensions L and W) is, $t_{pi} = \ln 2 \cdot R_{eq} \cdot C_g$, deduce the delay that appears in an inverter (1) of size $W'=aW$, connected to another inverter (2) of size $W'=bW$ (a and b constants).



b) We want to build a chain of inverters of increasing size to minimize the delay caused by a capacity 300 times greater than the capacity of a minimum size inverter ($C_L = 300C_g$). If we want to get the minimum possible delay, calculate:

- Number of stages required
- Size increase factor between stages
- Total delay, based on the delay of the minimum size inverter
- Estimation of total area, based on the area of the minimum size inverter
- Dimensions (L, W) of the transistors of the first three inverters of the chain, assuming that the dimensions of the transistors of the minimum size inverter are:

$$L_n = L_p = 2\lambda \quad W_n = 6\lambda \quad W_p = 15\lambda$$

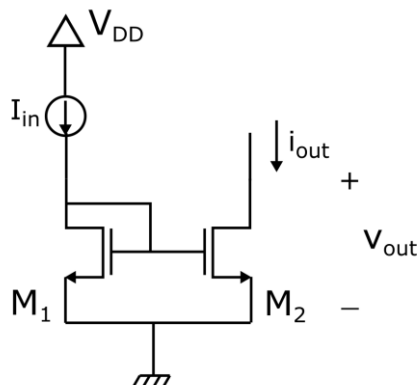
c) We want to design a clock tree for a circuit of 1200 flip-flops. To design this tree:

- only inverters of minimum size must be used
- it needs several stages (forks), and that all stages should have approximately the same *fanout*
- clock input pin must have *fanout* 1 (there must be only one inverter at the input pin)
- the clock reaching the flip-flops must have an even number of inversions

Draw the resulting trees for 3 and 4 stages and calculate their delay.

Exercise 3 (40 min, 2.5p)

The following current mirror has been implemented making use of a 50nm CMOS node. Given the following features and size ratios, answer the questions:



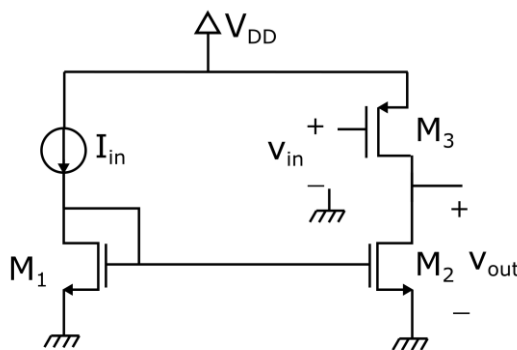
	NMOS	PMOS
$\mu^*C_{ox} (\mu A/V^2)$	100	50
$\lambda (V^{-1})$	0.6	0.6
$V_{th} (V)$	0.28	-0.28

$I_{in} = 20 \mu A$, $V_{DD} = 0.8 V$
 $L = 100 nm$ for all the transistors

	W/L
M₁	10

Assume all the transistors of the exercise are biased in saturation.

- Select proper values for W and L in transistor M₂ to make i_{out} equal to $100 \mu A$.
- Compute the output resistance of the current mirror.
- Justify why the same current mirror but implemented in a bigger CMOS node (such as 800nm) would have a higher output resistance.
- How could you increase the output resistance? With that purpose in mind, redesign and draw a new current mirror by adding one single extra transistor M₃ of size ratio W/L equal to 20. Assume that the gate of M₃ is connected to a voltage V_{bias} , sufficiently high to make it work in saturation. Compute the new output resistance.
- Compute the gain $|A_v| = |V_{out}/V_{in}|$ of the following circuit, where (W/L) M₃ = 20 (this section is totally independent with respect to section d))



NOTE: All the answers must be justified. Answers either with no justification or incorrect justification will not be scored.